Date: 06-05-2025

1. WAP to count digit of a Number.

```
public static int countDigit(int n)
{
    int count=0;
    while(n!=0)
    {
        count++;
        n/=10;
    }
    return count;
}
```

Method Tracing: countDigit(int n)

Purpose

This method counts the number of digits in a given integer $\, n \,$.

Initial Setup

- count is initialized to 0
- Input n is processed in a loop until it becomes 0

Tracing Steps

Example 1: n = 12345

| Iteration | n (before) | Condition (n != 0) | count++ | n /= 10 (after) | count (after) |
|-----------------------|------------|--------------------|---------|-----------------|---------------|
| 1 | 12345 | true | 1 | 1234 | 1 |
| 2 | 1234 | true | 2 | 123 | 2 |
| 3 | 123 | true | 3 | 12 | 3 |
| 4 | 12 | true | 4 | 1 | 4 |
| 5 | 1 | true | 5 | 0 | 5 |
| 6 | 0 | false (loop ends) | - | - | 5 |
| Final Return Value: 5 | | | | | |

Example 2: n = 0

| Iteration | n (before) | Condition (n != 0) | count++ | n /= 10 (after) | count (after) |
|-----------|------------|--------------------|---------|-----------------|---------------|
| 1 | 0 | false (loop ends) | - | - | 0 |

Final Return Value: 0

Example 3: n = -789 (Negative Number)

| Iteration | n (before) | Condition (n != 0) | count++ | n /= 10 (after) | count (after) |
|-----------|------------|--------------------|---------|-----------------|---------------|
| 1 | -789 | true | 1 | -78 | 1 |
| 2 | -78 | true | 2 | -7 | 2 |
| 3 | -7 | true | 3 | 0 | 3 |
| 4 | 0 | false (loop ends) | - | - | 3 |

Final Return Value: 3

Key Observations

- 1. The loop continues until n becomes 0
- 2. Each iteration:
 - o Increments count by 1
 - Divides n by 10 (integer division)
- 3. Works for negative numbers (treats them the same as positives)
- 4. Returns 0 when input is 0 (edge case)
- 5. Time Complexity: $O(log_{10} n)$ (number of digits in n)
 - 2. WAP to find digital sum of a digit.

Method Tracing: digitSum(int n)

Purpose

This method calculates the sum of all digits in a given integer n.

Initial Setup

- sum is initialized to 0
- Input n is processed in a loop until it becomes 0

Tracing Steps

Example 1: n = 12345

| Itoration | n | Condition (n != | n%10 | sum += | n /= 10 | sum |
|-----------|----------|-----------------|---------|--------|---------|---------|
| Iteration | (before) | 0) | (digit) | digit | (after) | (after) |

| 1 | 12345 | true | 5 | 0 + 5 = 5 | 1234 | 5 |
|---|-------|-------------------|---|-------------|------|----|
| 2 | 1234 | true | 4 | 5 + 4 = 9 | 123 | 9 |
| 3 | 123 | true | 3 | 9 + 3 = 12 | 12 | 12 |
| 4 | 12 | true | 2 | 12 + 2 = 14 | 1 | 14 |
| 5 | 1 | true | 1 | 14 + 1 = 15 | 0 | 15 |
| 6 | 0 | false (loop ends) | - | - | - | 15 |

Final Return Value: 15

Example 2: n = 0

| Iteration | n (before) | Condition (n != 0) | n%10 (digit) | sum += digit | n /= 10 (after) | sum (after) |
|-----------|---------------|-----------------------|-----------------|-----------------|--------------------|----------------|
| 1 | 0 | false (loop ends) | - | - | - | 0 |

Final Return Value: 0

Example 3: n = -789 (Negative Number)

| Iteration | n (before) | Condition (n != 0) | n%10 (digit) | sum += digit | n /= 10 (after) | sum (after) |
|-----------|---------------|-----------------------|-----------------|---------------------|--------------------|----------------|
| 1 | -789 | true | -9 | 0 + (-9) = -9 | -78 | -9 |
| 2 | -78 | true | -8 | -9 + (-8) = -17 | -7 | -17 |
| 3 | -7 | true | -7 | -17 + (-7) = -24 | 0 | -24 |
| 4 | 0 | false (loop ends) | - | - | - | -24 |

Final Return Value: -24

(Note: For negative numbers, the sum will also be negative)

Key Observations

- 1. The loop continues until n becomes 0
- 2. Each iteration:
 - Extracts the last digit using n%10
 - Adds the digit to sum
 - Removes the last digit using n /= 10
- 3. Handles negative numbers (digits contribute negatively to the sum)
- 4. Returns 0 when input is 0 (edge case)
- 5. Time Complexity: $O(log_{10} n)$ (number of digits in n)
 - 3. WAP to reverse a Digit of Number.

```
public static int reverseDigit(int n)
{
    int revNum=0;
    while(n!=0)
    {
       revNum=revNum*10+n%10;
       n/=10;
    }
    return revNum;
}
```

Method Tracing: reverseDigit(int n)

Purpose

This method reverses the digits of a given integer n (e.g., 1234 \rightarrow 4321).

Initial Setup

- revNum is initialized to 0
- Input n is processed in a loop until it becomes 0

Tracing Steps

Example 1: n = 1234

| Iteration | n (before) | Condition (n != 0) | n%10 (digit) | revNum = revNum*10 + digit | n /= 10 (after) | revNum (after) |
|-----------|---------------|-----------------------|-----------------|-------------------------------|--------------------|-------------------|
| 1 | 1234 | true | 4 | 0*10 + 4 = 4 | 123 | 4 |
| 2 | 123 | true | 3 | 4*10 + 3 = 43 | 12 | 43 |
| 3 | 12 | true | 2 | 43*10 + 2 = 432 | 1 | 432 |
| 4 | 1 | true | 1 | 432*10 + 1 = 4321 | 0 | 4321 |
| 5 | 0 | false (loop ends) | - | - | - | 4321 |

Final Return Value: 4321

Example 2: n = 100

| Iteration | n (before) | Condition (n != 0) | n%10 (digit) | revNum = revNum*10 + digit | n /= 10 (after) | revNum (after) |
|-----------|---------------|-----------------------|-----------------|-------------------------------|--------------------|-------------------|
| 1 | 100 | true | 0 | 0*10 + 0 = 0 | 10 | 0 |
| 2 | 10 | true | 0 | 0*10 + 0 = 0 | 1 | 0 |
| 3 | 1 | true | 1 | 0*10 + 1 = 1 | 0 | 1 |

| 4 | 0 | false (loop ends) | - | - | - | 1 |
|---|---|----------------------|---|---|---|---|
|---|---|----------------------|---|---|---|---|

Final Return Value: 1

(Note: Leading zeros in the original number are dropped in the reversal)

Example 3: n = -123 (Negative Number)

| Iteration | n (before) | Condition (n != 0) | n%10 (digit) | revNum = revNum*10 + digit | n /= 10 (after) | revNum (after) |
|-----------|---------------|-----------------------|-----------------|-------------------------------|--------------------|-------------------|
| 1 | -123 | true | -3 | 0*10 + (-3) = -3 | -12 | -3 |
| 2 | -12 | true | -2 | -3*10 + (-2) = -32 | -1 | -32 |
| 3 | -1 | true | -1 | -32*10 + (-1) = -321 | 0 | -321 |
| 4 | 0 | false (loop ends) | - | - | - | -321 |

Final Return Value: -321

(Preserves the negative sign while reversing digits)

Key Observations

- 1. **Digit Extraction**: n%10 gets the last digit
- 2. Number Construction: revNum*10 + digit appends the digit
- 3. **Termination**: Loop exits when n becomes 0
- 4. Handling Negatives: Maintains sign while reversing digits
- 5. Leading Zeros: Drops leading zeros from original number
- 6. **Time Complexity**: $O(log_{10} n)$ (number of digits in n)

Special Note

Overflow Risk: For large reversed numbers (e.g., reversing 2147483647 gives 7463847412 which exceeds
 Integer.MAX_VALUE), the result may be incorrect due to integer overflow. This implementation doesn't
 handle overflow cases.

Date: 07-05-2025

4. WAP to find factorial of a number.

```
public static int factorial(int n)
{
    int fact=1;
    for(int i=2;i<=n;i++)
        fact*=i;
    return fact;
}</pre>
```

Method Tracing: factorial(int n)

Purpose

This method calculates the factorial of a non-negative integer n iteratively.

Mathematical Definition

$$n! = n \times (n-1) \times (n-2) \times ... \times 2 \times 1$$

 $0! = 1$ (by definition)

Initial Setup

- fact initialized to 1
- Loop runs from i = 2 to i = n

Tracing Steps

Example 1: n = 5

| Iteration | i Value | fact (before) | Operation (fact *= i) | fact (after) |
|-----------|---------|---------------|-----------------------|--------------|
| 1 | 2 | 1 | 1 × 2 = 2 | 2 |
| 2 | 3 | 2 | 2 × 3 = 6 | 6 |
| 3 | 4 | 6 | 6 × 4 = 24 | 24 |
| 4 | 5 | 24 | 24 × 5 = 120 | 120 |

Final Return Value: 120

$$(5! = 5 \times 4 \times 3 \times 2 \times 1 = 120)$$

Example 2: n = 0 (Edge Case)

The loop condition $i \le n$ (2 <= 0) is false immediately.

Final Return Value: 1

(0! = 1 by definition)

Example 3: n = 1 (Edge Case)

The loop condition $i \le n (2 \le 1)$ is false immediately.

Final Return Value: 1

(1! = 1)

Key Characteristics

- 1. **Loop Initialization**: Starts from i = 2 because:
 - 0! and 1! both equal 1 (handled by initialization)
 - Multiplying by 1 is unnecessary
- 2. **Termination Condition**: Loop continues while i <= n
- 3. Efficiency:
 - Time Complexity: O(n)
 - Space Complexity: O(1) (constant space)

5. WAP to calculate Power of a number.

```
public static int power(int n,int pow)
{
    int res=1;
    for(int i=1;i<=pow;i++)
        res*=n;
    return res;
}</pre>
```

Method Tracing: power(int n, int pow)

Purpose

This method calculates n raised to the power pow using iteration.

Mathematical Definition

 $n^pow = n \times n \times ... \times n$ (pow times)

Initial Setup

- res initialized to 1
- Loop runs from i = 1 to i = pow

Tracing Steps

Example 1: n = 2, pow = 3

| Iteration | i Value | res (before) | Operation (res *= n) | res (after) |
|-----------|---------|--------------|----------------------|-------------|
| 1 | 1 | 1 | 1 × 2 = 2 | 2 |
| 2 | 2 | 2 | 2 × 2 = 4 | 4 |
| 3 | 3 | 4 | 4 × 2 = 8 | 8 |

Final Return Value: 8

$$(2^3 = 2 \times 2 \times 2 = 8)$$

Example 2: n = 5, pow = 0 (Edge Case)

The loop condition $i \le pow (1 \le 0)$ is false immediately.

Final Return Value: 1

(Any number to the power 0 is 1 by definition)

Example 3: n = 3, pow = 1 (Edge Case)

| Iteration | i Value | res (before) | Operation (res *= n) | res (after) |
|-----------|---------|--------------|----------------------|-------------|
| 1 | 1 | 1 | 1 × 3 = 3 | 3 |

Final Return Value: 3

```
(3^1 = 3)
```

Key Characteristics

- 1. **Loop Initialization**: Starts from i = 1 (inclusive) to pow (inclusive)
- 2. Base Case Handling: Returns 1 when pow=0 due to initialization
- 3. Efficiency:
 - Time Complexity: O(pow)
 - Space Complexity: O(1) (constant space)
 - 6. WAP to Check number is a perfect number or not.

```
public static boolean isPerfectNumber(int n)
{
    int sum = 0;
    for(int i=1;i<=n/2;i++){
        if(n%i==0)
            sum+=i;
    }
    return sum==n;
}</pre>
```

Method Tracing: checkPerfectNumber(int n)

Purpose

This method checks if a number is a perfect number (a positive integer that equals the sum of its proper divisors).

Mathematical Definition

A perfect number equals the sum of its proper positive divisors (excluding itself).

Initial Setup

- sum initialized to 0
- Loop runs from i = 1 to i = n/2

Tracing Steps

Example 1: n = 6 (Perfect Number)

| Iteration | i Value | n%i | Condition (n%i==0) | sum (before) | sum (after) |
|-----------|---------|-----|--------------------|--------------|-------------|
| 1 | 1 | 0 | true | 0 | 0+1=1 |
| 2 | 2 | 0 | true | 1 | 1+2=3 |
| 3 | 3 | 0 | true | 3 | 3+3=6 |

Final Comparison: 6 == 6

Return Value: true

Example 2: n = 28 (Perfect Number)

| It | teration | i Value | n%i | Condition | sum (before) | sum (after) |
|----|----------|---------|-----|-----------|--------------|-------------|
|----|----------|---------|-----|-----------|--------------|-------------|

| 1 | 1 | 0 | true | 0 | 1 |
|---|----|---|------|----|----|
| 2 | 2 | 0 | true | 1 | 3 |
| 3 | 4 | 0 | true | 3 | 7 |
| 4 | 7 | 0 | true | 7 | 14 |
| 5 | 14 | 0 | true | 14 | 28 |

Final Comparison: 28 == 28

Return Value: true

Example 3: n = 12 (Not Perfect)

| Iteration | i Value | n%i | Condition | sum (before) | sum (after) |
|-----------|---------|-----|-----------|--------------|-------------|
| 1 | 1 | 0 | true | 0 | 1 |
| 2 | 2 | 0 | true | 1 | 3 |
| 3 | 3 | 0 | true | 3 | 6 |
| 4 | 4 | 0 | true | 6 | 10 |
| 5 | 5 | 2 | false | 10 | 10 |
| 6 | 6 | 0 | true | 10 | 16 |

Final Comparison: 16 != 12

Return Value: false

Key Characteristics

- 1. **Loop Optimization**: Only checks up to n/2 since no divisor > n/2 exists
- 2. **Proper Divisors**: Only sums divisors less than n (excludes n itself)
- 3. **Efficiency**:
 - Time Complexity: O(n)
 - Space Complexity: O(1)
 - 7. WAP to check weather a number is prime or not.

```
public static boolean isPrimeNumber(int n)
{
    if (n <= 1)
        return false;
    if (n == 2)
        return true;
    if (n % 2 == 0)
        return false;
    for (int i = 3; i <= Math.sqrt(n); i += 2)
    {
        if (n % i == 0)
            return false;
    }
}</pre>
```

```
}
return true;
}
```

Method Tracing: checkPrimeNumber(int n)

Purpose

This method checks if a number is prime (has exactly two distinct positive divisors: 1 and itself).

Mathematical Definition

A prime number is a natural number greater than 1 that cannot be formed by multiplying two smaller natural numbers.

Initial Checks

```
1. Numbers \leq 1 \rightarrow \text{Not prime}
```

- 2. 2 \rightarrow Only even prime
- 3. Even numbers $> 2 \rightarrow Not prime$

Tracing Steps

```
Example 1: n = 7 (Prime)
```

```
1. 7 > 1 \rightarrow Continue
```

2. $7 != 2 \rightarrow Continue$

3. 7 % 2 != 0 \rightarrow Continue

4. Loop: i from 3 to $\sqrt{7}$ (≈2.645)

o $i=3:3>2.645 \rightarrow Loop exits$

5. No divisors found → **Returns** true

Example 2: n = 9 (Not Prime)

```
1. 9 > 1 \rightarrow Continue
```

2. 9 != 2 \rightarrow Continue

3. 9 % 2 != 0 \rightarrow Continue

4. Loop: i from 3 to $\sqrt{9}$ (3)

o i=3:9%3 == 0 \rightarrow Returns false

Example 3: n = 2 (Edge Case)

```
1. 2 > 1 \rightarrow Continue
```

2. $2 == 2 \rightarrow Returns true$

Example 4: n = 1 (Edge Case)

1. 1 <= 1 \rightarrow Returns false

Key Characteristics

1. Early Eliminations:

- All numbers ≤ 1: Not prime
- Even numbers > 2: Not prime
- 2. Loop Optimization:

- Only checks odd divisors (i += 2)
- Only checks up to √n (largest possible factor)

3. Efficiency:

- o Time Complexity: O(√n)
- Space Complexity: O(1)
- 8. WAP to check a year is leap year.

```
public static boolean isLeapYear(int year)
{
    return year%4==0 && (year%400==0 || year%100!=0);
}
```

Method Tracing: checkLeapYear(int year)

Purpose

This method determines if a given year is a leap year according to the Gregorian calendar rules.

Leap Year Rules

- 1. Divisible by 4: Potential leap year
- 2. **Exception**: If divisible by 100 → Not leap year unless...
- 3. **Exception to Exception**: Also divisible by 400 → Leap year

Method Logic

```
return year%4==0 && (year%400==0 || year%100!=0);
```

Tracing Steps

```
Example 4: year = 2023 (Not Leap Year)
```

- 1. 2023 % 4 == 0 \rightarrow false
 - Short-circuit: skips remaining checks
- 2. Returns false

Key Characteristics

- 1. Logical Structure:
 - year%4==0 : First gate (most common case)
 - year%400==0 : Exception handler (centuries)
 - year%100!=0 : Regular leap year confirmation
- 2. Short-Circuit Evaluation:
 - Stops evaluating if first condition (%4) fails
 - Within parentheses, stops if %400 succeeds
- 3. Efficiency:
 - Time Complexity: O(1) (constant time)
 - Space Complexity: O(1)

Date: 08-05-2025

9. WAP to check a number is Strong Number or Not.

```
public static boolean isStrong(int n)
{
    int sum=0;
    int temp=n;
    while(n!=0){
        int rem = n%10;
        sum+=factorial(rem);
        n/=10;
    }
    return sum==temp;
}
```

Method Tracing: checkStrong(int n)

Purpose

This method checks if a number is a "Strong number" - a special number where the sum of factorials of its digits equals the number itself.

Mathematical Definition

A number is strong if: sum of factorials of each digit = original number

Components

1. Extracts each digit

- 2. Calculates factorial of each digit
- 3. Sums the factorials
- 4. Compares sum to original number

Tracing Steps

Example 1: n = 145 (Strong Number)

| Step | Variable | Value/Operation |
|------------|---------------------|-----------------|
| Init | sum | 0 |
| Init | temp | 145 |
| Loop 1 | rem = 145%10 | 5 |
| | sum += factorial(5) | 0 + 120 = 120 |
| | n /= 10 | 14 |
| Loop 2 | rem = 14%10 | 4 |
| | sum += factorial(4) | 120 + 24 = 144 |
| | n /= 10 | 1 |
| Loop 3 | rem = 1%10 | 1 |
| | sum += factorial(1) | 144 + 1 = 145 |
| | n /= 10 | 0 |
| Comparison | sum == temp | 145 == 145 |
| Result | | true |

Example 2: n = 40585 (Strong Number)

| Step | Variable | Value/Operation |
|--------|---------------------|---------------------|
| Init | sum | 0 |
| Init | temp | 40585 |
| Loop 1 | rem = 40585%10 | 5 |
| | sum += factorial(5) | 0 + 120 = 120 |
| | n /= 10 | 4058 |
| Loop 2 | rem = 4058%10 | 8 |
| | sum += factorial(8) | 120 + 40320 = 40440 |
| | n /= 10 | 405 |
| Loop 3 | rem = 405%10 | 5 |
| | sum += factorial(5) | 40440 + 120 = 40560 |

| | n /= 10 | 40 |
|------------|---------------------|--------------------|
| Loop 4 | rem = 40%10 | 0 |
| | sum += factorial(0) | 40560 + 1 = 40561 |
| | n /= 10 | 4 |
| Loop 5 | rem = 4%10 | 4 |
| | sum += factorial(4) | 40561 + 24 = 40585 |
| | n /= 10 | 0 |
| Comparison | sum == temp | 40585 == 40585 |
| Result | | true |

Example 3: n = 123 (Not Strong)

| Step | Variable | Value/Operation |
|------------|---------------------|-----------------|
| Init | sum | 0 |
| Init | temp | 123 |
| Loop 1 | rem = 123%10 | 3 |
| | sum += factorial(3) | 0 + 6 = 6 |
| | n /= 10 | 12 |
| Loop 2 | rem = 12%10 | 2 |
| | sum += factorial(2) | 6 + 2 = 8 |
| | n /= 10 | 1 |
| Loop 3 | rem = 1%10 | 1 |
| | sum += factorial(1) | 8 + 1 = 9 |
| | n /= 10 | 0 |
| Comparison | sum == temp | 9 == 123 |
| Result | | false |

Key Characteristics

1. Digit Extraction:

- Uses n%10 to get last digit
- Uses n/10 to remove last digit

2. Factorial Calculation:

• Assumes existence of factorial() method

• Pre-calculated factorials (0-9):

```
0! = 1, 1! = 1, 2! = 2, 3! = 6

4! = 24, 5! = 120, 6! = 720

7! = 5040, 8! = 40320, 9! = 362880
```

3. Termination:

- Loop continues until n becomes 0
- Preserves original number in temp

10. WAP to check number is neon number or not.

```
public static boolean isNeon(int n)
{
    int squre=n*n;
    int sum =0;
    while(squre!=0){
        sum+=squre%10;
        squre/=10;
    }
    return sum==n;
}
```

Method Tracing: checkNeon(int n)

Purpose

This method checks if a number is a "Neon number" - a number where the sum of digits of its square equals the number itself.

Mathematical Definition

A number is neon if: sum of digits of $(n^2) = n$

Components

- 1. Calculates square of the number
- 2. Sums digits of the square
- 3. Compares sum to original number

Tracing Steps

Example 1: n = 9 (Neon Number)

| Step | Variable | Value/Operation |
|--------|-----------|-----------------|
| Init | square | 9*9 = 81 |
| Init | sum | 0 |
| Loop 1 | square%10 | 81%10 = 1 |

| Result | | true |
|------------|--------------|-----------|
| Comparison | sum == n | 9 == 9 |
| | square /= 10 | 8/10 = 0 |
| | sum += 8 | 1 + 8 = 9 |
| Loop 2 | 8%10 | 8 |
| | square /= 10 | 81/10 = 8 |
| | sum += 1 | 0 + 1 = 1 |

Example 2: n = 1 (Neon Number)

| Step | Variable | Value/Operation |
|------------|--------------|-----------------|
| Init | square | 1*1 = 1 |
| Init | sum | 0 |
| Loop 1 | 1%10 | 1 |
| | sum += 1 | 0 + 1 = 1 |
| | square /= 10 | 1/10 = 0 |
| Comparison | sum == n | 1 == 1 |
| Result | | true |

Example 3: n = 3 (Not Neon)

| Step | Variable | Value/Operation |
|------------|--------------|-----------------|
| Init | square | 3*3 = 9 |
| Init | sum | 0 |
| Loop 1 | 9%10 | 9 |
| | sum += 9 | 0 + 9 = 9 |
| | square /= 10 | 9/10 = 0 |
| Comparison | sum == n | 9 == 3 |
| Result | | false |

Key Characteristics

1. Square Calculation:

- Computes n*n upfront
- Works for both positive and negative (though negatives would fail comparison)

2. **Digit Summation**:

- Uses modulo 10 to extract last digit
- Uses integer division by 10 to remove last digit

3. Termination:

- Loop continues until square becomes 0
- Final comparison is exact equality check
- 11. WAP to check a number is happy number or not.

Method Tracing: happyNumber(int n)

Purpose

This method determines if a number is a "Happy Number" - a number that eventually reaches 1 when replaced by the sum of the squares of its digits repeatedly.

Mathematical Definition

A happy number is defined by the process:

- 1. Start with any positive integer
- 2. Replace the number by the sum of the squares of its digits
- 3. Repeat until the number equals 1 (happy) or loops endlessly in a cycle (unhappy)

Key Insight

Unhappy numbers will eventually reach the cycle 4 \rightarrow 16 \rightarrow 37 \rightarrow 58 \rightarrow 89 \rightarrow 145 \rightarrow 42 \rightarrow 20 \rightarrow 4

Tracing Steps

Example 1: n = 19 (Happy Number)

| Outer Loop | n Value | Inner Loop Operations | sum | New n |
|------------|---------|-----------------------|-----|-------|
| 1 | 19 | $9^2 + 1^2 = 81 + 1$ | 82 | 82 |
| 2 | 82 | $2^2 + 8^2 = 4 + 64$ | 68 | 68 |
| 3 | 68 | $8^2 + 6^2 = 64 + 36$ | 100 | 100 |

| 4 | 100 | $0^2 + 0^2 + 1^2 = 0 + 0 + 1$ | 1 | 1 |
|-------------|--------------------|-------------------------------|---|---|
| Termination | n=1 → Happy Number | | | |

Example 2: n = 4 (Unhappy Number)

- Immediately terminates (n=4 is in the unhappy cycle)
- **Result**: Unhappy number

Example 3: n = 2 (Unhappy Number)

| Outer Loop | n Value | Inner Loop Operations | sum | New n |
|-------------|----------------------|-----------------------|-----|-------|
| 1 | 2 | $2^2 = 4$ | 4 | 4 |
| Termination | n=4 → Unhappy Number | | | |

Key Characteristics

1. Termination Conditions:

• Stops when n becomes 1 (happy) or 4 (unhappy cycle starter)

2. Digit Processing:

- Extracts each digit using n%10
- Removes digit using n/10
- Squares each digit and sums them

3. Cycle Detection:

- Uses 4 as proxy for detecting the unhappy cycle
- All unhappy numbers eventually reach 4

12. WAP to check Armstrong Number or not.

```
public static boolean IsArmStrong(int n)
{
    int count = countDigit(n);
    int sum=0;
    int temp=n;
    while (n!=0) {
        sum+=power(n%10, count);
        n/=10;
    }
    return sum==temp;
}
```

Method Tracing: armstrongNumber(int n)

Purpose

This method checks if a number is an Armstrong number (also called narcissistic number) - a number that equals the sum of its own digits each raised to the power of the number of digits.

Mathematical Definition

An n-digit number is Armstrong if: $digit_1^n + digit_2^n + ... + digit_k^n = original number$

Components

- 1. Counts digits (countDigit)
- 2. Calculates power of each digit (power)
- 3. Sums the powered digits
- 4. Compares sum to original number

Tracing Steps

Example 1: n = 153 (Armstrong Number)

| Step | Variable | Value/Operation |
|------------|-------------|---------------------|
| Init | count | countDigit(153) → 3 |
| Init | sum | 0 |
| Init | temp | 153 |
| Loop 1 | n%10 | 153%10 = 3 |
| | power(3,3) | 27 |
| | sum += 27 | 0 + 27 = 27 |
| | n /= 10 | 15 |
| Loop 2 | 15%10 | 5 |
| | power(5,3) | 125 |
| | sum += 125 | 27 + 125 = 152 |
| | n /= 10 | 1 |
| Loop 3 | 1%10 | 1 |
| | power(1,3) | 1 |
| | sum += 1 | 152 + 1 = 153 |
| | n /= 10 | 0 |
| Comparison | sum == temp | 153 == 153 |
| Result | | true |

Example 2: n = 370 (Armstrong Number)

| Step | Variable | Value/Operation |
|------|----------|-----------------|
| Init | count | 3 |
| Init | sum | 0 |

| Init | temp | 370 |
|------------|------------|----------------|
| Loop 1 | 370%10 | 0 |
| | power(0,3) | 0 |
| | sum += 0 | 0 |
| | n /= 10 | 37 |
| Loop 2 | 37%10 | 7 |
| | power(7,3) | 343 |
| | sum += 343 | 0 + 343 = 343 |
| | n /= 10 | 3 |
| Loop 3 | 3%10 | 3 |
| | power(3,3) | 27 |
| | sum += 27 | 343 + 27 = 370 |
| | n /= 10 | 0 |
| Comparison | 370 == 370 | |
| Result | | true |

Example 3: n = 123 (Not Armstrong)

| Step | Variable | Value/Operation |
|--------|------------|-----------------|
| Init | count | 3 |
| Init | sum | 0 |
| Init | temp | 123 |
| Loop 1 | 123%10 | 3 |
| | power(3,3) | 27 |
| | sum += 27 | 0 + 27 = 27 |
| | n /= 10 | 12 |
| Loop 2 | 12%10 | 2 |
| | power(2,3) | 8 |
| | sum += 8 | 27 + 8 = 35 |
| | n /= 10 | 1 |
| Loop 3 | 1%10 | 1 |
| | power(1,3) | 1 |

| | sum += 1 | 35 + 1 = 36 |
|------------|-----------|-------------|
| | n /= 10 | 0 |
| Comparison | 36 == 123 | |
| Result | | false |

Key Characteristics

1. Digit Counting:

- Must count digits before destruction of n
- Uses helper method countDigit

2. Power Calculation:

- Each digit raised to digit count power
- Uses helper method power

3. **Termination**:

- Continues until all digits processed (n=0)
- Preserves original number in temp