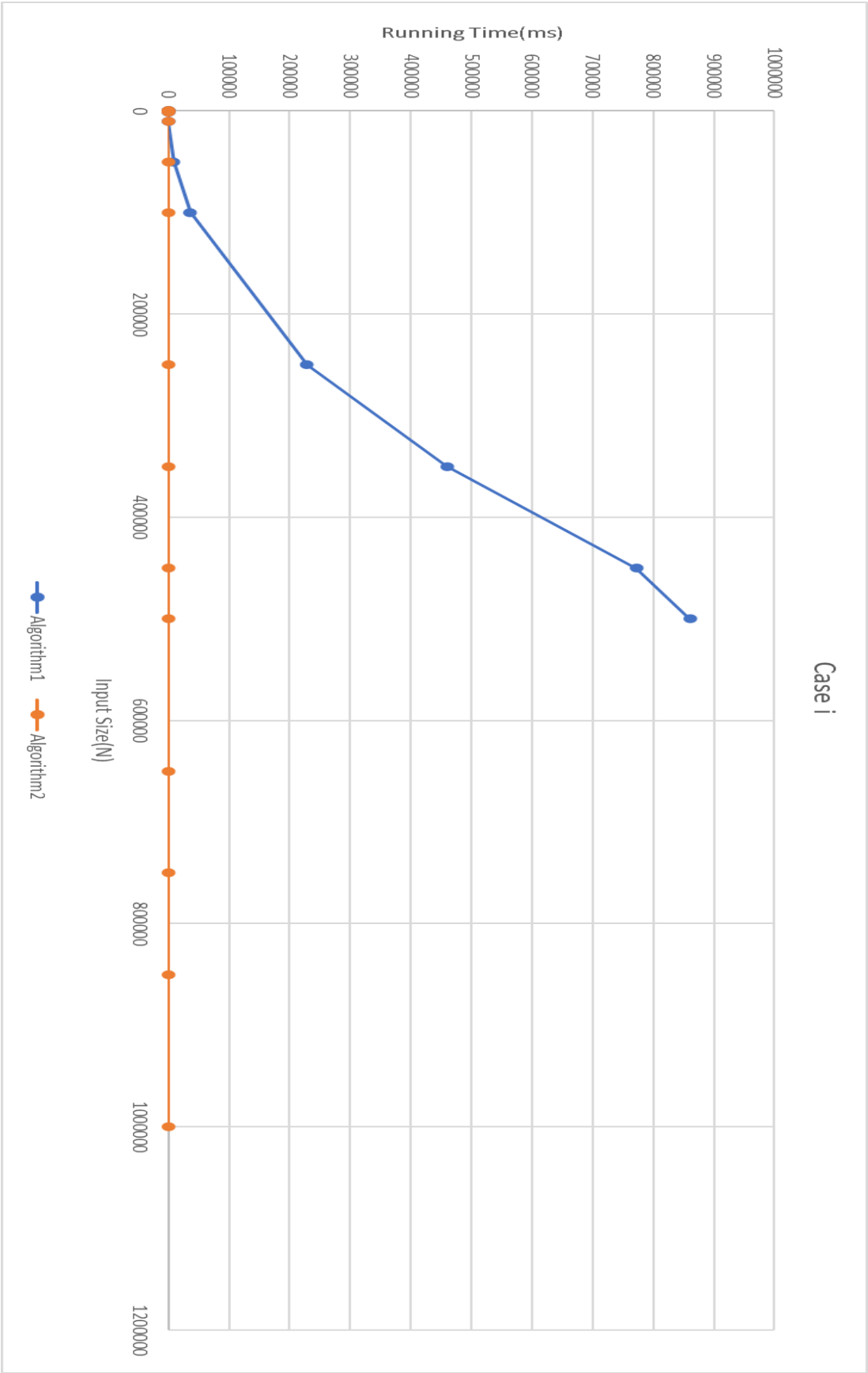
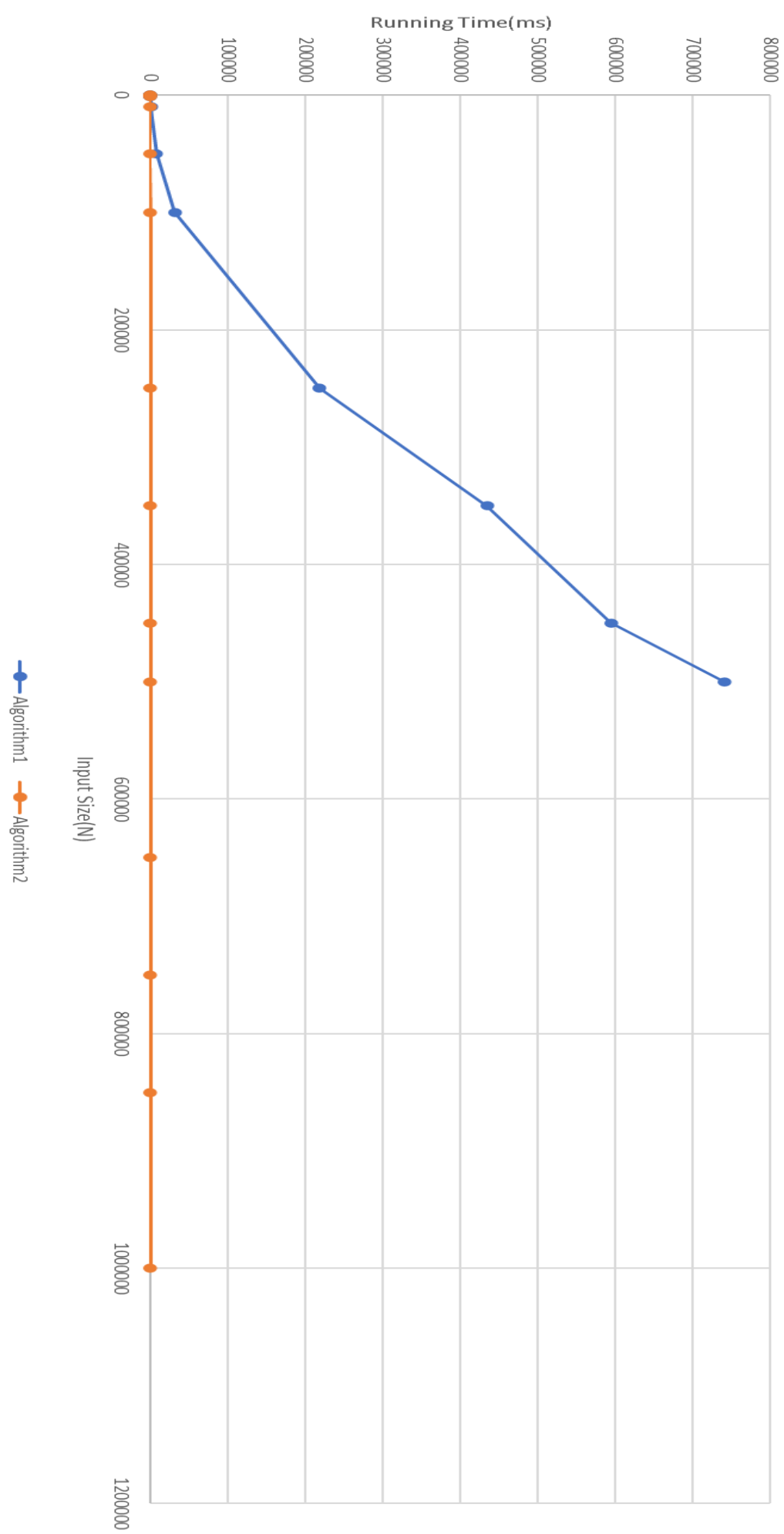


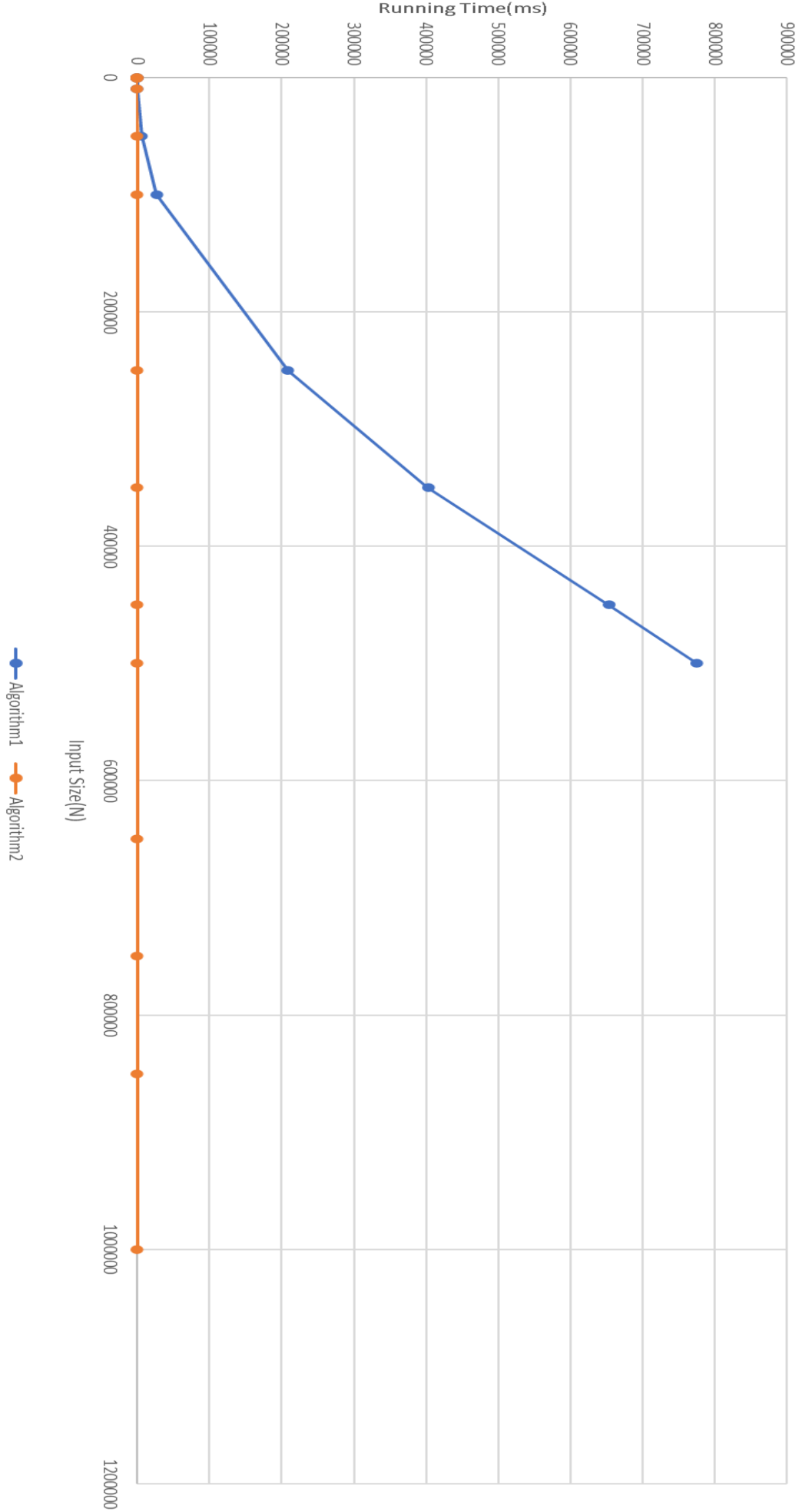
PLOTS:



Case ii



Case iii



## WORST-CASE, BEST-CASE, AND AVERAGE-CASE ANALYSES

Algorithm1:

- Worst-Case: When the second array's all items are same and they are all bigger than first array's all items except the last item in the first array.  
 $f(N) = O(N) + O(N^3) = O(N^3)$
- Average-Case:  $f(N) = O(N^2)$
- Best-Case: When the second array has 1 item and it is bigger than first array's all items.  
 $F(N) = O(N) + O(N) = O(N)$

Algorithm2:

- Worst-Case: When first array's all items are bigger than second array, algorithm has to check 2 more if statements.  
 $f(N) = O(N)$
- Average-Case:  $f(N) = O(N)$
- Best-Case: When second array's all items are bigger than first array's all items.  
 $f(N) = O(N)$
- Worst-Case, Average-Case, Best-Case all of them have  $O(N)$  time complexity because in every condition algorithm has to complete the while statement (because there is no break or return in the statement, every condition are same)

## COMPUTER SPECIFICATIONS

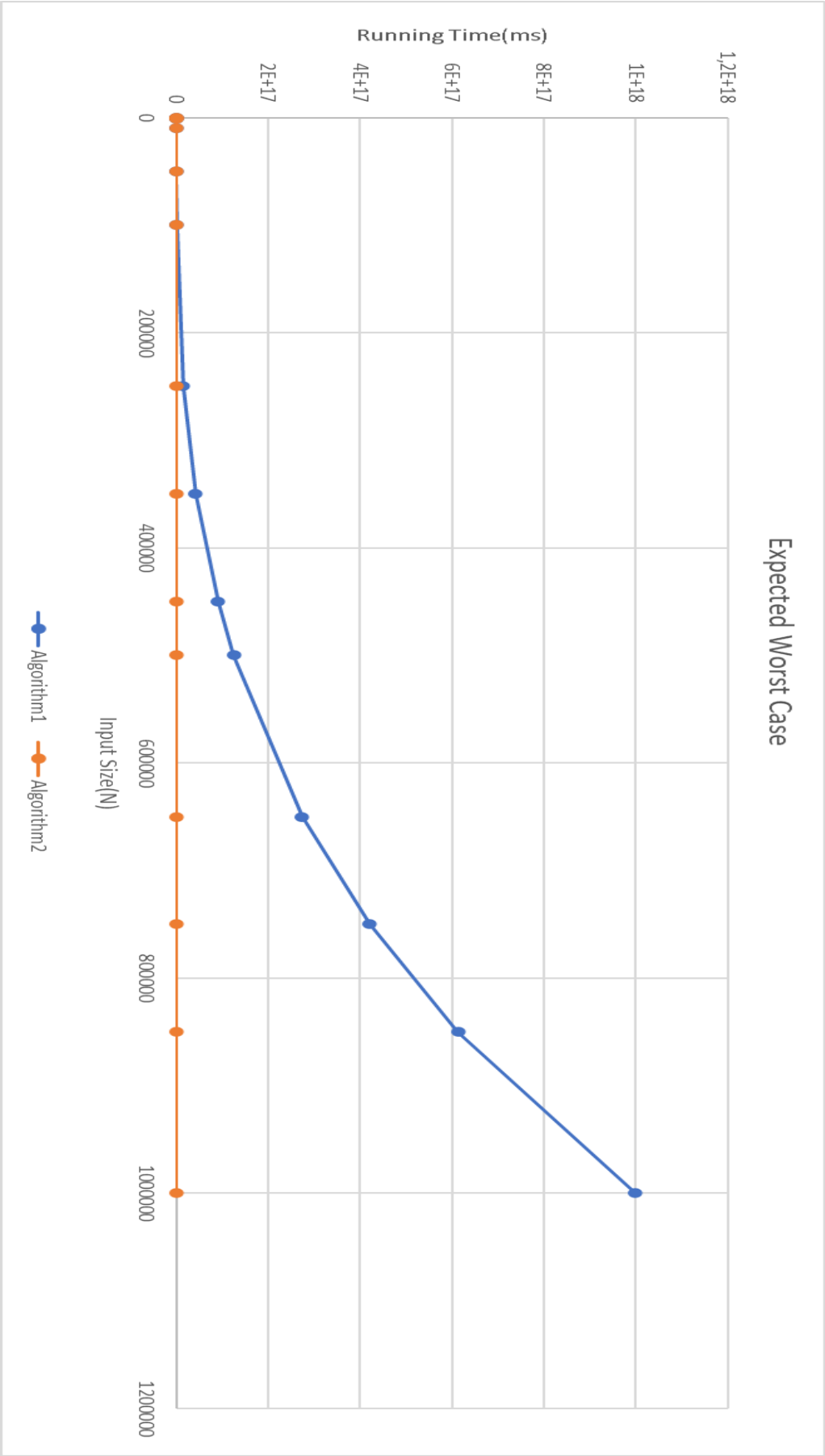
CPU: Intel® Core™ i7-7700HQ CPU @ 2.80GHz

2.80GHz

RAM: 16.0GB

OPERATING SYSTEM: Windows 10 Pro

EXPECTED WORST-CASE CHARTS



## DISCUSSION:

To make it clear, Algorithm1 slower than Algorithm2.

The worst-case growth rate from the above plot and theoretical data from step 3 are coherent. From the above plot, it can be seen that algorithm1 has  $O(N^3)$  growth rate as expected and algorithm2 has  $O(N)$  growth rate. Because operations for  $O(N^3)$  is very high  $O(N)$  looks like a straight line with 0 tangents which should have a tangent bigger than 0.

Algorithm1 is slower in case1 compare to case2. However, my expectation was reverse, because in case2 algorithm1 runs 2 nested for loops however in case 2 it is 3 nested for loop. The underlying reason for this problem is my break statement. Although in case 2 it is 3 for loops when the program finds the wanted case it breaks, however in case 2 break does not work. Therefore, it totally runs 2 nested for loops.

Moreover, in Linux machine running algorithms take more time compare to run them in visual studio

## TABLES

These are the tables to compare the datas clearly.

### *Case i*

Size	Algorithm1(ms)	Algorithm2(ms)
10	0	0
100	0	0
1000	3	0
10000	394	0
50000	9445	1
100000	36649	1
250000	228955	2
350000	459836	3
450000	772609	4
500000	861064	4
650000		5
750000		8
850000		6
1000000		8

### *Case ii*

Size	Algorithm1(ms)	Algorithm2(ms)
10	0	0
100	0	0
1000	3	0
10000	318	0
50000	7372	0
100000	31464	1
250000	218253	4
350000	434657	3

450000	594293	4
500000	740803	6
650000		6
750000		6
850000		8
1000000		10

### *Case iii*

Size	Algorithm1(ms)	Algorithm2(ms)
10	0	0
100	0	0
1000	3	0
10000	300	0
50000	6457	1
100000	26660	2
250000	208860	5
350000	403293	7
450000	653244	9
500000	775596	9
650000		8
750000		10
850000		9
1000000		8

### *WorstCase*

Size	Algorithm1(operations)	Algorithm2(operations)
10	1000	10
100	1000000	100
1000	1000000000	1000
10000	1E+12	10000
50000	1,25E+14	50000
100000	1E+15	100000
250000	1,5625E+16	250000
350000	4,2875E+16	350000
450000	9,1125E+16	450000
500000	1,25E+17	500000
650000	2,74625E+17	650000
750000	4,21875E+17	750000
850000	6,14125E+17	850000
1000000	1E+18	1000000

