## Final-Project

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This project is about digit recognition. let first load the data:

```
rm(list=ls())
library("data.table", lib.loc="~/R/win-library/3.2")

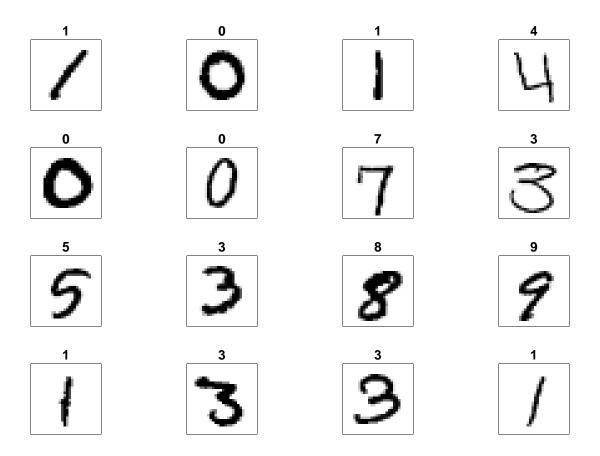
tab5rows <- read.csv("train.csv", header = TRUE, nrows = 5)
classes <- sapply(tab5rows, class)
pixels <- as.matrix(read.csv("train.csv", header = TRUE, colClasses = classes))
rm(classes , tab5rows)

lables <- pixels[,1]
pixels <- pixels[,-1]
N <- nrow(pixels)</pre>
```

Every digit is a 28\*28 pixels and intensity of eac pixels has intensity between (0,256).

Let Plot some of the digits:

```
colors<-c('white','black')
cus_col<-colorRampPalette(colors=colors)
par(mfrow=c(4,4),pty='s',mar=c(1.5,1.5,1.5),xaxt='n',yaxt='n')
for(i in 1:16)
{
    z<-array(pixels[i,],dim=c(28,28))
    z<-z[,28:1] ##right side up
    image(z,main=lables[i],col=cus_col(256))
}</pre>
```



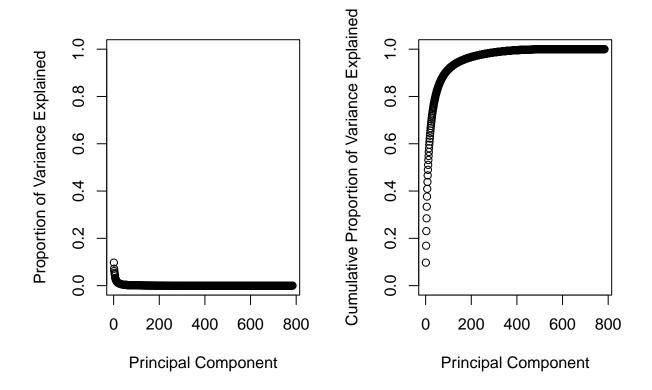
First we split the data to training and test data:

```
set.seed(1)
train <- sample(c(TRUE,FALSE), nrow(pixels),rep=TRUE,prob = c(0.8,0.2))
sum(train)/nrow(pixels)</pre>
```

## [1] 0.7999286

We will find principle components and see which proportion of variance is explained by these components:

```
pr.out <- prcomp(pixels[train, ])
pr.var <- pr.out$sdev^2
pve <- pr.var/sum(pr.var)
resetPar <- function() {
    dev.new()
    op <- par(no.readonly = TRUE)
    dev.off()
    op
}
par(resetPar())
par(mfrow = c(1,2))
plot(pve, xlab="Principal Component", ylab="Proportion of Variance Explained", ylim=c(0,1),type='b')
plot(cumsum(pve), xlab="Principal Component", ylab="Cumulative Proportion of Variance Explained", ylim=</pre>
```



Now we rotate our train and test data to new component space:

```
test.rotated <- pixels[!train, ] %*% pr.out$rotation
train.rotated <- pixels[train, ] %*% pr.out$rotation</pre>
```

Let try to predict the test data by fitting a lda Model to train data:

(Note: we test offline for choosing the best number of components to use and 60 was the best)

```
library(MASS)

rotated.Data <- pixels %*% pr.out$rotation
rotated.Data <- data.frame(cbind("lables" =lables, rotated.Data[,1:60]))

lda.fit=lda(lables ~ . ,data = rotated.Data, subset = train)
lda.pred=predict(lda.fit, rotated.Data[!train,])
table(lda.pred$class ,lables[!train])</pre>
```

```
##
##
           0
                      2
                                     5
                                               7
                                                          9
                1
                           3
                                4
                                          6
                                                     8
##
        769
                0
                      4
                           3
                                0
                                    12
                                          6
                                               3
                                                     8
                                                          4
      0
           0
                    32
                                          6
                                                   51
                                                          4
##
      1
             916
                         19
                               11
                                    11
                                              29
##
      2
           3
                4
                   706
                         28
                                6
                                     4
                                          7
                                               9
                                                     2
                                                          2
                                          2
                                               5
                                                         12
##
      3
           6
                    20 734
                                0
                                    34
                                                   33
##
      4
           2
                0
                           2
                             705
                                    13
                                         11
                                              18
                                                     8
                                                         49
                    15
      5
                                                          7
##
          22
                5
                      8
                         28
                                3 597
                                         33
                                               6
                                                   36
```

```
##
         10
                  19
                                15 732
               1
                        3
                            11
                                      0 710
          0
                  22
                                                   17
##
     7
               1
                       17
                             0
                                 4
                                                1
                                           5 642
##
         11
              21
                  37
                             9
                                35
                                       8
                                                     4
     9
##
               2
                  10
                       20
                            82
                                10
                                       1
                                          53
                                              25 760
```

Finding the test Error:

```
result.lda <- data.table("predict" = lda.pred$class, "lable" = lables[!train])
result.lda[, correct := lable == predict]
print(paste0('Test error is: ', sum(result.lda[, correct])/ nrow(result.lda)))</pre>
```

```
## [1] "Test error is: 0.865286207306914"
```

Let's try to predict the test data by fitting a KNN Model to train data:

(Note: we test offline for choosing the best number of components to use and 50 was the best.)

```
library(FNN)
```

```
## Warning: package 'FNN' was built under R version 3.2.3
```

```
knn.pred <- knn(train.rotated[,1:50], test.rotated[,1:50],lables[train] ,k=10)
table(knn.pred ,lables[!train])</pre>
```

```
##
## knn.pred
                      1
                           2
                                3
                                                               9
                 0
            0 820
                      0
                           3
                                0
                                          0
                                                     0
                                                               2
##
                                     0
                                                          2
##
            1
                 1 948
                           1
                                4
                                     7
                                          2
                                               0
                                                   16
                                                         8
                                                               1
                      1 846
                                3
                                          1
##
            2
                 0
                                     0
                                               1
                                                          2
                                                               1
##
            3
                 0
                      0
                           4 842
                                     0
                                                               3
                           0
                                0 797
                                          0
                                                     3
                                                              10
##
            4
                 0
                      0
                                               3
                                                         0
            5
                      0
                           0
                                6
                                     0 716
##
                 1
                                                2
                                                        13
##
            6
                 3
                      1
                           1
                                1
                                     3
                                          6 796
                                                     0
                                                               1
##
            7
                 0
                      0
                          13
                                8
                                          1
                                               0 813
                                                          3
                                                             15
                                     1
##
            8
                 0
                      0
                           4
                                5
                                     0
                                          1
                                               0
                                                     0 761
                                                               2
##
            9
                 0
                      1
                           1
                                4
                                    19
                                               0
                                                     5
                                                         6 822
                                          1
```

Finding the test Error:

```
result.knn <- data.table("predict.knn" = knn.pred, "lable" = lables[!train])
result.knn[, correct := lable == predict.knn]
print(paste0('Test error is: ', sum(result.knn[, correct])/ nrow(result.knn)))</pre>
```

```
## [1] "Test error is: 0.97120076163275"
```

In final let look at the letter numbers that knn predict uncorrect:

I run it before and attach the result as a pdf with the name 'not\_correct\_test\_letters.pdf'

Note: the numbers that is written above the pictures is the predicted number by knn.

## 2