

$$1) L_1 = \{0^i 1^j 0^k : i, j, k \geq 0 \text{ and } (i=j \text{ or } j=k)\}$$

$$S \rightarrow AB|BC$$

$$A \rightarrow 0A1|\epsilon$$

$$B \rightarrow 0B1|\epsilon$$

$$C \rightarrow 1C0|\epsilon$$

yes this can create multiple strings with
 2 different derivations. An example is 010
 which has the two strings 0, 10

2)

$$A \rightarrow BAB|B|\epsilon$$

$$B \rightarrow 00|\epsilon$$

eliminate ϵ

$$A \rightarrow BAB|B|AB|BA|A|B$$

$$B \rightarrow 00$$

New start state

$$S \rightarrow A|\epsilon$$

$$A \rightarrow BAB|B|AB|BA|A|B$$

$$B \rightarrow 00$$

Remove unit productions

$$S \rightarrow A|\epsilon$$

$$A \rightarrow BAB|00|AB|BA|A$$

$$B \rightarrow 00$$

$$V_0 \rightarrow \emptyset$$

$$x \rightarrow AD$$

$$S \rightarrow \epsilon \mid BZ \mid BB \mid BA \mid AD \mid V_0V_0$$

$$A \rightarrow BZ \mid BB \mid BA \mid AD \mid V_0V_0$$

$$x \rightarrow AB$$

$$B \rightarrow V_0V_0$$

$$V_0 \rightarrow \emptyset$$

3)

