

Katholieke Universiteit Leuven

Department of Computer Science

PROJECT

Genetic Algorithms and Evolutionary Computing (B-KUL-H02D1A)

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Introduction

In this report we discuss our solutions and results for the given tasks. For each task, experiments were ran to evaluate our solutions. Unless stated otherwise, the experiments were executed with a certain set of parameters and functions. This was done so that we would have a consistent basis to compare results on. The parameters were also chosen in order to leave enough room for improvement so that the effects of different methods can be compared, while at the same time reducing variation of experiments that are too short or do too little work. The default parameters and functions are as follows:

- number of individuals = 100
- maximum number of generations = 250
- probability of mutation = 0.05
- probability of crossover = 0.95
- percentage of elite population = 0.05
- subpopulations = 1
- loop detection = off
- parent selection function = sus
- crossover function = cross_alternating_edges
- mutation function = mut_inversion
- custom stopping criterion = on
- custom survivor selection function = off

The results shown in tables are the average results of 10 runs. Every experiment is ran 10 times, so that the effects of local optima would be reduced.

The appendix includes tables that contain results of experiments and our code that is relevant to the tasks.

Tasks

1.1 Task 2: Initial experiments

The impact of the following parameters on the results of the existing genetic algorithm was tested by varying them while keeping the rest of the parameters at their default values:

- number of individuals (NIND)
- maximum number of generations (MAXGEN)
- percentage of the elite population (ELITIST)
- probability of crossover (PR_CROSS)
- probability of mutation (PR_MUT)
- local loop removal (LOCALLOOP)

The parameter values were chosen so that evenly spread out options from low to high could be tested. The experiments for this task were executed on a subset of the given datasets to keep the tables readable. The datasets range from ones with a small amount of cities to ones with a large amount of cities. The tables for the results of the experiments can be found in appendix 4.1.1.

1.1.1 Individuals

The minimum path lengths clearly decrease as the number of individuals increases. This is to be expected, as a larger amount of individuals causes a larger amount of mutations and crossover which can positively impact path lengths. Analogously, the maximum path lengths slightly increase as the number of individuals increases. Because of this effect, the mean path lengths remain relatively constant after 100 individuals.

1.1.2 Generations

TODO: COMMENTS

1.1.3 Elitism

TODO: COMMENTS

1.1.4 Crossover

TODO: COMMENTS

1.1.5 Mutation

TODO: COMMENTS

1.1.6 Loop removal

See section 1.4

1.1.7 Mix

After some parameter tuning with the above information in mind, we have come up with a configuration of parameters that performs very well. The results can be seen in table ??. The parameters were:

1.2 Task 3: Stopping criterion

To implement a new stopping criterion, we looked at the commonly used termination conditions outlined by the book. There we see the following suggestions:

- 1. Maximally allowed CPU time elapses.
- 2. Total number of fitness evaluations reaches limit.
- 3. Fitness improvement remains under threshold for a given period of time.
- 4. Population diversity drops under threshold.

The first and second criteria are useful, either to guarantee the evaluations do not go on forever, or when there is some kind of constraint on system resource usage. In the project template, we already have the guarantee of eventual termination because of the limit on the number of generations, and we do not have to account for system resource constraints.

The fourth criterion is also already present in the template and can be adjusted via the GUI. The default value is so strict (95% equal individuals), it practically is never reached.

We decided to implement the third criterion. With this condition, termination occurs when the fitness of the best individual does not improve above a threshold for a given period of time. This period of time is expressed in terms of a certain number of generations. We chose to define this number of generations to be a percentage of the specified maximum number of generations. When testing this termination condition, we see that it does succeed in avoiding computation of useless generations where the fitness does not improve for a long time. Because of the fact that improvements may still happen at a later point in time, the score will be slightly worse with this new condition.

The results of our experiments with this new termination condition are displayed in Table 1.1.

	Default stopping criterion					Custon	n stopping	g criterion	
Dataset	# Generations	Min	Mean	Max		# Generations	Min	Mean	Max
rondrit016.tsp	60.6000	3.8289	3.8405	4.3167		51.9000	3.8598	4.0645	4.9485
rondrit018.tsp	59.9000	3.6123	3.6526	4.3262		62.4000	3.5116	3.7063	4.6899
rondrit023.tsp	92.8000	3.9902	4.2086	5.2684		77.5000	4.3064	4.4586	5.5427
rondrit025.tsp	82.0000	5.3085	5.4600	6.4753		79.2000	5.3707	5.7207	7.3034
rondrit048.tsp	108.7000	7.8736	8.2540	9.5729		109.2000	8.1605	8.9541	10.9159
rondrit050.tsp	101.5000	12.3558	12.9267	14.6198		104.0000	12.0748	12.8018	14.4246
rondrit051.tsp	109.6000	11.8400	12.3779	13.6785		108.9000	11.7734	12.2508	13.6669
rondrit067.tsp	110.0000	11.5868	12.2748	13.8317		107.2000	11.4511	12.4336	14.0862
rondrit070.tsp	110.0000	17.8292	18.6919	20.5209		109.6000	18.3206	18.9595	20.7340
rondrit100.tsp	110.0000	29.6034	31.6596	34.6374		108.7000	29.1263	30.6127	33.1294
rondrit127.tsp	110.0000	19.6930	20.5928	21.9205		110.0000	19.0723	20.0230	21.4847

Table 1.1: Comparison between default and custom stopping criteria.

1.3 Task 4: Other representation

The given project template uses adjacency representation by default for TSP paths. We have chosen to use path representation as the alternative one. Conversion between the two representations was already possible thanks to the 'adj2path' and 'path2adj' functions in the template. To do crossover with path representation, we implemented the Order Crossover method (function 'cross_order') as described in the textbook. Simple Inversion Mutation, which is a mutation operator for path representation, was already provided in the template ('mut_inversion'). We have decided to extend this and have added a function for Inversion Mutation ('mut_inversion2').

Table 1.2 contains the results of experiments with different crossover operators. The 'cross_alternate_edges' function implements Alternating Edge Crossover and is provided in the template. It is clear that Order Crossover performs significantly better than Alternating Edge Crossover; all of the path lengths with Order Crossover are lower for every dataset.

	Alternating Edge Crossover			er	Order Crossover
Dataset	# Generations	Min	Mean	Max	# Generations Min Mean Max
rondrit016.tsp	182.4	3.39	3.55	4.32	50.6 3.44 3.46 4.08
rondrit018.tsp	244.5	2.98	4.53	6.46	55.4 3.05 3.06 3.87
rondrit023.tsp	250.0	3.90	6.59	9.43	79.0 3.57 3.59 4.45
rondrit025.tsp	250.0	5.03	8.64	11.94	82.4 4.48 4.51 5.75
rondrit048.tsp	250.0	9.68	14.45	18.81	188.4 5.49 5.54 6.67
rondrit050.tsp	250.0	13.99	19.79	24.57	162.4 8.20 8.23 9.53
rondrit051.tsp	250.0	13.08	18.29	22.54	155.9 8.67 8.69 9.61
rondrit067.tsp	250.0	13.95	18.41	22.28	188.9 7.11 7.14 7.92
rondrit070.tsp	250.0	21.89	28.98	34.40	219.6 10.94 11.06 12.49
rondrit100.tsp	250.0	34.40	43.21	50.05	232.6 17.78 18.22 19.91
rondrit127.tsp	250.0	21.93	26.30	29.49	239.8 12.77 13.03 14.02

Table 1.2: Results of different crossover functions.

Table 1.3 contains the results of experiments with different mutation operators. The 'mut_inversion' function implements Simple Inversion Mutation and is provided in the

template. There is no clear difference between the two methods in these results.

	Simple Inversion Mutation				Invers	ion Mut	ation		
Dataset	# Generations	Min	Mean	Max	-	# Generations	Min	Mean	Max
rondrit016.tsp	168.1	3.39	3.54	4.48		180.5	3.41	3.58	4.57
rondrit018.tsp	237.4	3.06	4.55	6.44		245.2	3.04	4.58	6.36
rondrit023.tsp	250.0	3.91	6.54	9.14		250.0	4.07	6.86	9.53
rondrit025.tsp	250.0	5.05	8.78	12.26		250.0	5.01	8.77	12.53
rondrit048.tsp	250.0	9.34	14.57	19.28		250.0	9.65	14.59	19.29
rondrit050.tsp	250.0	13.98	19.60	24.39		250.0	13.57	19.43	24.01
rondrit051.tsp	250.0	13.49	18.57	22.72		250.0	13.56	18.58	22.65
rondrit067.tsp	250.0	13.95	18.73	22.73		250.0	13.63	18.56	22.24
rondrit070.tsp	250.0	21.58	28.43	34.15		250.0	21.50	28.89	34.42
rondrit 100.tsp	250.0	35.01	43.47	50.80		250.0	34.13	42.89	49.85
rondrit127.tsp	250.0	22.00	26.48	29.43		250.0	21.90	26.30	29.70

Table 1.3: Results of different mutation functions.

Table 1.4 shows results after some parameter tuning with the 'cross_order' and 'mut_inversion2' operators. The parameters used were: a = b, c = d, ... TODO check tuning

Dataset	# Generations	Min	Mean	Max
rondrit016.tsp	43.3	3.42	3.44	4.25
rondrit018.tsp	51.7	3.13	3.16	4.29
rondrit023.tsp	70.2	3.68	3.71	4.65
rondrit025.tsp	72.5	4.43	4.48	6.07
rondrit048.tsp	134.6	6.12	6.15	7.51
rondrit050.tsp	160.2	8.68	8.71	10.28
rondrit051.tsp	144.0	8.92	8.96	10.46
rondrit067.tsp	168.9	7.99	8.01	9.03
rondrit070.tsp	184.4	12.25	12.28	13.56
rondrit100.tsp	230.1	18.31	18.59	20.26
${\rm rondrit} 127. {\rm tsp}$	249.2	12.84	13.23	14.30

Table 1.4: Results with operators for path representation after parameter tuning.

1.4 Task 5: Local optimisation

For this task, we are testing the local optimization already present in the template. This optimization takes a path and tries to remove local loops up to path length 3. With default values for other parameters, this results in major improvements to the score.

The results of our experiments with local optimisation disabled and enabled are displayed in Table 1.5.

	Local	Local optimisation disabled					ptimisatio	n enabled	
Dataset	# Generations	Min	Mean	Max		# Generations	Min	Mean	Max
rondrit016.tsp	108.8	3.9087	5.3409	6.6707		63.4	3.6923	3.7783	4.4343
rondrit018.tsp	109.0	3.8205	5.9391	7.9101		82.7	3.2285	3.8159	4.8886
rondrit023.tsp	109.0	5.2503	8.0243	10.4586		109.0	3.6688	6.0516	8.2630
rondrit025.tsp	109.0	6.8383	10.5710	13.9566		109.0	4.6353	7.9255	11.2084
rondrit048.tsp	109.0	12.9322	17.3083	21.2216		109.0	7.4032	12.2117	15.8290
rondrit050.tsp	109.0	17.5460	23.0187	27.4702		109.0	10.6862	16.3413	19.9854
rondrit051.tsp	109.0	17.0520	21.6487	25.5342		109.0	9.8788	15.0773	19.2524
rondrit067.tsp	109.0	17.2930	21.6320	25.0256		109.0	9.4921	14.8637	18.2992
rondrit070.tsp	109.0	27.0916	33.4376	38.6964		109.0	14.9605	22.7446	27.9257
rondrit100.tsp	109.0	41.7305	49.6807	55.5533		109.0	22.4411	32.7396	38.8860
rondrit127.tsp	109.0	26.5206	30.3975	33.3563		109.0	15.3001	20.8402	24.3830

Table 1.5: Comparison between local optimisation disabled (left) and local optimisation enabled (right).

1.5 Task 7: Optional tasks

1.5.1 7a: Parent selection

Additional parent selection methods we implemented are Fitness Proportional Selection ('sel_fit_prop') and Tournament Selection ('sel_tournament'). Both of them use the same parameters as the existing implementation of Stochastic Universal Sampling so we could easily swap them in.

	Stochastic Universal Sampling								
Dataset	# Generations	Min	Mean	Max					
rondrit016.tsp	109.0	3.9268	5.5816	6.95230040943754					
rondrit018.tsp	109.0	3.8098	5.8874	7.64505139464696					
rondrit023.tsp	109.0	5.2107	8.1510	10.66363338096259					
rondrit025.tsp	109.0	6.9584	10.6573	13.64919455732690					
rondrit048.tsp	109.0	12.5354	17.1587	20.98354804718375					
rondrit050.tsp	109.0	17.6555	23.3466	27.70294938389831					
rondrit051.tsp	109.0	16.8619	21.5905	24.99887566024666					
rondrit067.tsp	109.0	17.3626	21.8921	25.01576819902206					
rondrit070.tsp	109.0	27.3491	33.7980	39.02844367980951					
rondrit100.tsp	109.0	42.5563	50.3468	56.14968388227629					
rondrit127.tsp	109.0	26.3171	30.1653	32.82588637833199					

Table 1.6: Results when using Stochastic Universal Sampling as parent selection method.

		ion		
Dataset	# Generations	Min	Mean	Max
rondrit016.tsp	109.0	3.8584	5.2429	6.65136434345961
rondrit018.tsp	109.0	3.8044	5.8175	7.60837957298278
rondrit023.tsp	109.0	5.0251	7.8150	10.25462477584426
rondrit025.tsp	109.0	6.8520	10.6018	13.97083528139636
rondrit048.tsp	109.0	12.3467	16.3804	20.33995051462599
rondrit050.tsp	109.0	17.7767	23.0010	26.94691760670842
rondrit051.tsp	109.0	16.6423	21.4503	24.88148805771897
rondrit067.tsp	109.0	17.4205	21.8030	24.91090949012749
rondrit070.tsp	109.0	27.0049	33.5066	38.57674586236878
rondrit100.tsp	109.0	42.1082	49.7688	55.34138052048054
rondrit127.tsp	109.0	26.5709	30.3721	33.34923179147698

Table 1.7: Results when using Tournament Selection as parent selection method.

	Fitness Proportional Selection								
Dataset	# Generations	Min	Mean	Max					
rondrit016.tsp	109.0	3.9268	5.5816	6.95230040943754					
rondrit018.tsp	109.0	3.8098	5.8874	7.64505139464696					
rondrit023.tsp	109.0	5.2107	8.1510	10.66363338096259					
rondrit025.tsp	109.0	6.9584	10.6573	13.64919455732690					
rondrit048.tsp	109.0	12.5354	17.1587	20.98354804718375					
rondrit050.tsp	109.0	17.6555	23.3466	27.70294938389831					
rondrit051.tsp	109.0	16.8619	21.5905	24.99887566024666					
rondrit067.tsp	109.0	17.3626	21.8921	25.01576819902206					
rondrit070.tsp	109.0	27.3491	33.7980	39.02844367980951					
rondrit100.tsp	109.0	42.5563	50.3468	56.14968388227629					
rondrit127.tsp	109.0	26.3171	30.1653	32.82588637833199					

Table 1.8: Results when using Fitness Proportional Selection as parent selection method.

1.5.2 7b: Survivor selection

Round robin tournament was chosen as the other strategy for survivor selection. The results for different values of the ELITISM parameter can be found in table 4.17. To evaluate how round robin tournament performs compared to the already implemented elitism, the ELITIST parameter is set to 0 in an experiment. Also, an experiment is done where elitism is combined with round robin tournament. Table 1.9 contains the results of the experiments for this task. TODO: evaluate results after verifying they are correct. The custom stopping criterion needs to be updated first. Last X values should all be equal, instead of just current and current-X.

	Already implemented elitism				Round robin tournament
Dataset	# Generations	Min	Mean	Max	# Generations Min Mean Max
rondrit016.tsp	91.3	3.46	4.66	6.19	0.0 0.00 0.00 0.00
rondrit018.tsp	83.9	3.40	5.20	7.09	0.0 0.00 0.00 0.00
rondrit023.tsp	84.3	4.50	6.91	9.45	0.0 0.00 0.00 0.00
rondrit025.tsp	102.9	5.79	9.11	12.60	0.0 0.00 0.00 0.00
rondrit048.tsp	101.0	10.56	15.16	19.12	0.0 0.00 0.00 0.00
rondrit050.tsp	137.6	14.68	19.80	24.21	0.0 0.00 0.00 0.00
rondrit051.tsp	111.3	14.70	19.24	22.88	0.0 0.00 0.00 0.00
rondrit067.tsp	90.4	15.17	19.11	22.88	0.0 0.00 0.00 0.00
rondrit070.tsp	123.4	23.12	29.61	35.04	0.0 0.00 0.00 0.00
rondrit 100.tsp	106.5	36.29	43.94	50.20	0.0 0.00 0.00 0.00
rondrit127.tsp	113.6	23.02	26.88	30.19	0.0 0.00 0.00 0.00

Table 1.9: Results for the already implemented elitism and our round robin tournament survivor selection.

1.5.3 7c: Diversity preservation

In order to preserve population diversity, we adapted a few of the functions in the template to work with subpopulations, simulating the island model. The results displayed in Table 1.10 through Table ?? show tests performed with 1, 2, 5, 10 and 20 subpopulations or islands.

	# subpopulations = 1									
Dataset	# Generations	Min	Mean	Max						
rondrit016.tsp	99.9	3.7370	5.3014	7.3443						
rondrit018.tsp	120.7	3.4504	5.5736	7.9594						
rondrit023.tsp	124.4	4.6149	7.6039	10.7075						
rondrit025.tsp	134.5	5.8402	9.9015	13.9843						
rondrit048.tsp	129.7	10.9175	16.1203	21.3953						
rondrit050.tsp	194.6	14.7423	21.4762	26.9975						
rondrit051.tsp	169.1	14.7132	20.3833	25.4901						
rondrit067.tsp	139.0	15.3320	20.6747	25.3712						
rondrit070.tsp	187.9	23.1837	31.6961	39.3717						
rondrit100.tsp	174.5	38.1144	48.0221	55.8977						
rondrit127.tsp	195.0	23.8434	29.0456	33.1707						

Table 1.10: Results when using a single subpopulation.

	# subpopulations = 2									
Dataset	# Generations	Min	Mean	Max						
rondrit016.tsp	118.9	4.1112	5.6874	7.9026						
rondrit018.tsp	147.5	3.8393	6.0843	8.5831						
rondrit023.tsp	159.4	5.0312	8.3282	11.8303						
rondrit025.tsp	152.9	6.6344	10.9143	15.5315						
rondrit048.tsp	204.9	11.4129	17.6468	23.8143						
rondrit050.tsp	216.0	16.5176	23.7049	29.4113						
rondrit051.tsp	168.2	16.6110	22.5015	27.8662						
rondrit067.tsp	203.0	16.4217	22.3292	27.4292						
rondrit070.tsp	129.3	27.3049	35.4823	42.9792						
rondrit100.tsp	251.9	40.3992	51.8574	60.8410						
rondrit127.tsp	265.4	25.6029	31.5892	36.3884						

Table 1.11: Results when using two subpopulations.

	# subpopulations = 5					
Dataset	# Generations	Min	Mean	Max		
rondrit016.tsp	126.6	4.1295	5.8593	7.9499		
rondrit018.tsp	121.0	4.0043	6.2663	8.9579		
rondrit023.tsp	138.2	5.1783	8.4623	12.0132		
rondrit025.tsp	166.0	6.4178	11.0127	15.7281		
rondrit048.tsp	117.9	12.4779	18.4335	24.2895		
rondrit050.tsp	164.8	17.1913	24.2682	30.5998		
rondrit051.tsp	166.4	17.3803	23.2727	28.6140		
rondrit067.tsp	225.4	16.5562	22.6888	27.6837		
rondrit070.tsp	183.2	26.8295	35.8003	42.9375		
rondrit100.tsp	199.2	41.8170	53.1547	62.3695		
rondrit127.tsp	218.5	26.4587	32.1475	36.5978		

Table 1.12: Results when using five subpopulations.

	# subpopulations = 10				
Dataset	# Generations	Min	Mean	Max	
rondrit016.tsp	97.4	4.1405	5.5019	7.7501	
rondrit018.tsp	140.1	3.8233	5.5875	8.1174	
rondrit023.tsp	180.4	4.7633	7.8333	11.6950	
rondrit025.tsp	186.0	6.1102	10.4032	15.4008	
rondrit048.tsp	276.3	10.6240	17.0398	23.1415	
rondrit050.tsp	245.8	15.9304	22.8300	29.9988	
rondrit051.tsp	190.7	16.0860	21.8967	27.5143	
rondrit067.tsp	254.4	15.8431	21.9523	27.1892	
rondrit070.tsp	272.4	24.4098	33.8360	41.4091	
rondrit100.tsp	250.7	39.4631	51.1833	61.1145	
rondrit 127.tsp	282.1	25.3591	31.1691	36.3321	

Table 1.13: Results when using ten subpopulations.

1.6 Task 6: Benchmark problems

For this task, we have selected a set of parameters and methods based on all of the results above. Our algorithm is evaluated by running it on given benchmark problems and calculating the relative error of the results of the algorithm to the known optimal paths of the benchmark problems. The parameters and methods used were as follows:

\bullet TODO

The results are shown in table 1.14. Judging from the relative errors, we can conclude that our solutions are ${
m TODO}$

Dataset	Optimal length	# Generations	Min	Mean	Max	Error Min	Error Mean	Error Max
bcl380.tsp	1621	250.0	10119.10	14190.44	16270.37	524.25%	775.41%	1003.66%
belgiumtour.tsp	1	250.0	884.34	1425.84	2048.85	88333.65%	142483.67%	204785.29%
rbx711.tsp	3115	250.0	27069.22	34898.93	39431.08	769.00%	1020.35%	1265.81%
xqf131.tsp	564	250.0	1752.34	2528.96	3232.48	210.70%	348.40%	572.96%
xq1662.tsp	2513	250.0	21848.41	29270.98	33471.24	769.42%	1064.78%	1331.88%

Table 1.14: Results for benchmark problems with our final algorithm.

Appendix

4.1 Tables

4.1.1 Task 2

Dataset	# Generations	Min	Mean	Max		
number of individuals $= 50$						
rondrit016.tsp	240.3	3.43	4.79	6.15		
rondrit048.tsp	250.0	10.75	15.48	18.92		
rondrit067.tsp	250.0	14.85	19.37	22.58		
rondrit127.tsp	250.0	22.80	27.03	29.92		
nun	nber of individu	als = 10	0			
rondrit016.tsp	191.7	3.40	3.82	4.70		
rondrit048.tsp	250.0	9.88	14.72	18.82		
rondrit067.tsp	250.0	13.49	18.52	22.12		
rondrit127.tsp	250.0	21.59	26.30	29.80		
nun	nber of individu	als = 25	0			
rondrit016.tsp	250.0	3.37	4.75	6.53		
rondrit048.tsp	250.0	8.94	14.62	19.69		
rondrit067.tsp	250.0	12.50	18.28	22.59		
rondrit127.tsp	250.0	20.64	25.96	30.16		
nun	nber of individu	als = 50	0			
rondrit016.tsp	246.5	3.36	4.60	6.49		
rondrit048.tsp	250.0	7.98	14.06	19.49		
rondrit067.tsp	250.0	11.81	17.95	22.71		
${\rm rondrit} 127. {\rm tsp}$	250.0	19.49	25.47	29.85		
number of individuals = 1000						
rondrit016.tsp	243.1	3.35	4.52	6.55		
rondrit048.tsp	250.0	7.81	14.13	19.84		
rondrit067.tsp	250.0	11.15	17.86	23.32		
${\rm rondrit} 127. {\rm tsp}$	250.0	18.92	25.26	30.12		

Table 4.15: Existing genetic algorithm with varying amount of individuals.

Dataset	# Generations	Min	Mean	Max		
max number of generations $= 100$						
rondrit016.tsp	100.0	3.46	4.74	6.28		
rondrit048.tsp	100.0	10.59	15.11	19.11		
rondrit067.tsp	100.0	15.02	19.27	22.78		
${\rm rondrit} 127. {\rm tsp}$	100.0	22.90	26.87	30.22		
max	number of genera	ations =	250			
rondrit016.tsp	176.6	3.40	3.50	4.23		
rondrit048.tsp	250.0	9.60	14.58	18.97		
rondrit067.tsp	250.0	13.52	18.59	22.90		
${\rm rondrit} 127. {\rm tsp}$	250.0	21.99	26.49	30.43		
max	number of genera	ations =	500			
rondrit016.tsp	184.2	3.38	3.40	4.28		
rondrit048.tsp	500.0	8.41	13.89	18.68		
rondrit067.tsp	500.0	12.46	17.94	22.27		
${\rm rondrit} 127. {\rm tsp}$	500.0	20.26	25.27	28.98		
max number of generations = 1000						
rondrit016.tsp	180.7	3.38	3.40	4.24		
${\rm rondrit} 048. {\rm tsp}$	1000.0	7.63	13.77	18.62		
${\rm rondrit} 067. {\rm tsp}$	1000.0	11.20	17.04	21.68		
rondrit127.tsp	1000.0	18.83	24.86	28.70		

Table 4.16: Existing genetic algorithm with varying amount of maximum generations.

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Dataset	# Generations	Min	Mean	Max		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	percer	tage of the elite po	pulation	a = 0.00			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit016.tsp	250.0	4.50	5.69	7.18		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit048.tsp	250.0	14.03	17.31	20.50		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit067.tsp	250.0	18.16	21.13	23.96		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit127.tsp	250.0	26.28	28.72	31.22		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	percer	tage of the elite po	pulation	a = 0.05			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit016.tsp	198.6	3.38	3.81	4.80		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit048.tsp	250.0	8.92	14.23	18.51		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit067.tsp	250.0	13.33	18.46	22.14		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit127.tsp	250.0	22.02	26.30	29.37		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	percer	tage of the elite po	pulation	a = 0.10			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit016.tsp	73.2	3.38	3.39	4.01		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit048.tsp	250.0	7.29	9.67	13.38		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit067.tsp	250.0	11.04	14.38	18.90		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit127.tsp	250.0	19.11	22.87	27.30		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	percer	tage of the elite po	pulation	a = 0.30			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit016.tsp	52.8	3.39	3.41	4.08		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit048.tsp	247.7	6.42	7.43	11.04		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit067.tsp	250.0	9.19	10.32	13.71		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit127.tsp	250.0	17.56	18.95	22.25		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	percer	tage of the elite po	pulation	a = 0.50			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit016.tsp	68.3	3.40	3.41	4.12		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit048.tsp	250.0	7.03	7.61	10.62		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit067.tsp	250.0	10.36	11.28	14.48		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit127.tsp	250.0	18.36	19.33	22.32		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	percer	tage of the elite po	pulation	a = 0.70			
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit016.tsp	112.3	3.37	3.38	3.97		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit048.tsp	250.0	8.15	8.87	11.99		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	rondrit067.tsp	250.0	11.75	12.51	15.15		
rondrit016.tsp 250.0 3.57 3.89 4.71 rondrit048.tsp 250.0 11.56 12.56 15.06 rondrit067.tsp 250.0 15.43 16.75 18.79	rondrit127.tsp	250.0	19.56	20.56	23.64		
rondrit048.tsp 250.0 11.56 12.56 15.06 rondrit067.tsp 250.0 15.43 16.75 18.79	percentage of the elite population $= 0.95$						
rondrit067.tsp 250.0 15.43 16.75 18.79	rondrit016.tsp	250.0	3.57	3.89	4.71		
1	rondrit048.tsp	250.0	11.56	12.56	15.06		
rondrit127.tsp 250.0 23.75 24.80 26.80	rondrit067.tsp	250.0	15.43	16.75	18.79		
	rondrit127.tsp	250.0	23.75	24.80	26.80		

Table 4.17: Existing genetic algorithm with varying percentage of the elite population.

Dataset	# Generations	Min	Mean	Max		
pro	probability of crossover $= 0.00$					
rondrit016.tsp	33.0	4.17	4.18	4.64		
rondrit048.tsp	159.7	8.31	8.33	9.39		
rondrit067.tsp	177.2	11.80	11.81	12.50		
rondrit127.tsp	197.7	20.77	20.82	21.12		
pro	obability of crosso	ver = 0.	.10			
rondrit016.tsp	42.3	3.63	3.65	4.38		
rondrit048.tsp	163.1	7.21	7.23	8.04		
rondrit067.tsp	192.5	9.84	9.90	10.85		
rondrit 127.tsp	250.0	16.72	16.88	18.18		
pro	obability of crosso	ver = 0.	.30			
rondrit016.tsp	36.9	3.57	3.58	4.29		
rondrit048.tsp	196.8	6.14	6.17	7.44		
rondrit067.tsp	245.8	7.79	7.95	9.63		
${\rm rondrit} 127. {\rm tsp}$	220.5	15.97	16.14	17.26		
pro	obability of crosso	ver = 0.	.50			
rondrit016.tsp	39.9	3.55	3.57	4.33		
rondrit048.tsp	199.1	6.09	6.31	8.08		
rondrit067.tsp	217.4	8.57	8.91	10.84		
${\rm rondrit} 127. {\rm tsp}$	250.0	15.25	15.81	18.10		
pro	obability of crosso	ver = 0.	.70			
rondrit016.tsp	58.6	3.42	3.44	4.27		
rondrit048.tsp	221.3	6.43	6.90	9.16		
rondrit067.tsp	243.0	9.16	10.09	13.20		
${\rm rondrit} 127. {\rm tsp}$	250.0	16.82	19.07	23.18		
probability of crossover $= 0.95$						
rondrit016.tsp	159.1	3.39	3.42	4.18		
rondrit048.tsp	250.0	9.67	14.65	18.68		
${\rm rondrit} 067. {\rm tsp}$	250.0	13.77	18.74	22.76		
rondrit127.tsp	250.0	21.76	26.14	29.46		

Table 4.18: Existing genetic algorithm with varying probability of crossover.

Dataset	# Generations	Min	Mean	Max			
pro	probability of mutation $= 0.00$						
rondrit016.tsp	122.1	3.38	3.39	3.66			
rondrit048.tsp	250.0	9.95	14.56	18.82			
rondrit067.tsp	250.0	14.24	18.42	22.35			
rondrit127.tsp	250.0	22.66	26.70	30.03			
pro	bability of mutat	ion = 0	.05				
rondrit016.tsp	167.0	3.39	3.41	4.09			
rondrit048.tsp	250.0	9.72	14.68	18.93			
rondrit067.tsp	250.0	13.91	18.67	22.32			
rondrit127.tsp	250.0	21.63	26.11	29.80			
pro	bability of mutat	ion = 0	.10				
rondrit016.tsp	241.0	3.39	4.19	5.40			
rondrit048.tsp	250.0	9.09	14.32	18.58			
rondrit067.tsp	250.0	13.58	18.66	22.57			
rondrit127.tsp	250.0	21.53	26.12	29.56			
pro	bability of mutat	ion = 0	.30				
rondrit016.tsp	250.0	3.45	4.99	6.64			
rondrit048.tsp	250.0	8.88	14.69	19.14			
rondrit067.tsp	250.0	12.81	18.22	22.51			
rondrit 127.tsp	250.0	21.28	26.02	29.34			
pro	bability of mutat	ion = 0	.50				
rondrit016.tsp	250.0	3.41	5.14	6.70			
rondrit048.tsp	250.0	8.98	14.70	19.21			
rondrit067.tsp	250.0	12.50	18.55	22.42			
rondrit127.tsp	250.0	20.78	25.97	29.68			
pro	bability of mutat	ion = 0	.70				
rondrit016.tsp	250.0	3.41	5.30	6.86			
rondrit048.tsp	250.0	9.17	15.13	19.73			
rondrit067.tsp	250.0	12.63	18.44	22.64			
${\rm rondrit} 127. {\rm tsp}$	250.0	20.91	26.20	29.78			
pro	probability of mutation $= 0.95$						
rondrit016.tsp	250.0	3.45	5.46	7.07			
rondrit048.tsp	250.0	9.24	15.34	19.50			
rondrit067.tsp	250.0	13.06	18.83	22.93			
${\rm rondrit} 127. {\rm tsp}$	250.0	20.91	26.24	29.66			

Table 4.19: Existing genetic algorithm with varying probability of mutation.

4.2 Code

Listing 4.1: The main algorithm - $src/run_ga.m$

```
% run_ga.m (RUN GENETIC ALGORITHM)
%
%
Input parameters:
4 % x, y - coordinates of the cities
```

```
5 | % NIND - number of individuals
6 % MAXGEN - maximal number of generations
7 % ELITIST - percentage of elite population
   % STOP_PERCENTAGE - percentage of equal fitness (stop criterium)
  % PR_CROSS - probability for crossover
10 | PR_MUT - probability for mutation
11 % CROSSOVER - the crossover operator
12 | % MUTATION - the mutation operator
  % LOCALLOOP - local loop removal on/off
   % CUSTOMSTOP - custom stopping criterion on/off
   % CUSTOMSS - custom survivor selection on/off
   % SELECTION - the parent selection function (sus, sel_tournament,
  |% sel_fit_prop, ...)
18 % ah1, ah2, ah3 - axes handles to visualise tsp
   % Output parameters:
20
  % best - vector of the best result of every iteration
   % mean_fits - vector of the mean result of every iteration
   % worst - vector of the worst result of every iteration
   function [best, mean_fits, worst] = run_ga(x, y, NIND, MAXGEN, NVAR,
       ELITIST, STOP_PERCENTAGE, PR_CROSS, PR_MUT, CROSSOVER, MUTATION,
       LOCALLOOP, CUSTOMSTOP, CUSTOMSS, SELECTION, SUBPOP, ah1, ah2, ah3)
26
      GGAP = 1 - ELITIST;
27
      best = zeros(1, MAXGEN);
29
      mean_fits = zeros(1,MAXGEN+1);
      worst = zeros(1,MAXGEN+1);
31
      Dist = zeros(NVAR, NVAR);
33
      for i = 1:size(x,1)
          for j = 1:size(y,1)
              Dist(i,j) = sqrt((x(i)-x(j))^2+(y(i)-y(j))^2);
          end
37
      end
      % initialize population
      Chrom = zeros(NIND, NVAR);
41
      for row = 1:NIND
42
          Chrom(row,:) = path2adj(randperm(NVAR));
44
      % evaluate initial population
      ObjV = tspfun(Chrom, Dist);
46
      % number of individuals of equal fitness needed to stop
48
      stopN = ceil(STOP_PERCENTAGE*NIND);
50
      gen = 0;
      % generational loop
52
      while gen < MAXGEN
          s0bjV = sort(ObjV);
54
          best(gen+1) = min(ObjV);
```

```
minimum = best(gen+1);
56
           mean_fits(gen+1) = mean(ObjV);
57
           worst(gen+1) = max(ObjV);
58
           for t = 1:size(ObjV,1)
59
               if (ObjV(t) == minimum)
60
                   break;
61
               end
           end
63
           if nargin == 19
65
               visualizeTSP(x, y, adj2path(Chrom(t,:)), minimum, ah1, gen,
                   best, mean_fits, worst, ah2, ObjV, NIND, ah3);
           end
68
           \mbox{\ensuremath{\%}} stopping criterion: stop when the minimum of the last stopN
           % generations has not improved
70
           if CUSTOMSTOP == 1
               if (gen-0.1*MAXGEN > 1) && ((best(floor(gen-0.1*MAXGEN)) -
72
                   minimum) <= 1e-15)
                   break;
73
               end
74
           else
               if (sObjV(stopN)-sObjV(1) <= 1e-15)</pre>
76
                   break;
77
               end
           end
80
           % assign fitness values to entire population
           FitnV = ranking(ObjV);
82
           % select individuals for breeding
84
           SelCh = select(SELECTION, Chrom, FitnV, GGAP);
86
           %recombine individuals (crossover)
87
           SelCh = crossover_tsp(CROSSOVER, SelCh, PR_CROSS, SUBPOP);
88
           SelCh = mutate_tsp(MUTATION, SelCh, PR_MUT, SUBPOP);
90
           %evaluate offspring, call objective function
91
           ObjVSel = tspfun(SelCh, Dist);
92
93
           %reinsert offspring into population
94
           if CUSTOMSS == 0
95
                [Chrom, ObjV] = reins(Chrom, SelCh, SUBPOP, 1, ObjV, ObjVSel);
           else
97
                [Chrom, ObjV] = sur_sel_rr_tournament(Chrom, SelCh, ObjV,
                   ObjVSel, 10);
           end
100
           Chrom = tsp_improve_population(NIND, NVAR, Chrom, LOCALLOOP, Dist)
           gen = gen+1;
103
       end
104
```

Listing 4.2: Order crossover for task 4- src/cross_order.m

```
% CROSS_ORDER.M (ORDER CROSSOVER)
   % Order crossover for TSP.
   % Input parameters:
   % ParentOne, ParentTwo - The TSP individuals to apply crossover on in a
   % certain representation.
   % Representation - The representation the given parents are in.
   % If omitted, 2 (path) is assumed.
10
   % Output parameters:
   % ChildOne, ChildTwo - Chromosomes created by mating, ready to be
   \% mutated and/or evaluated, in the same format
   % as OldChrom.
14
   function [ChildOne, ChildTwo] = cross_order(ParentOne, ParentTwo)
16
17
   ParentOne = adj2path(ParentOne);
18
   ParentTwo = adj2path(ParentTwo);
20
   [~, cols] = size(ParentOne);
   ChildOne = zeros(1, cols);
22
   ChildTwo = zeros(1, cols);
24
   rnd = sort(randi(cols, [1, 2]));
25
   a = rnd(1);
   b = rnd(2);
28
   ChildOne(a:b) = ParentOne(a:b);
29
   ChildTwo(a:b) = ParentTwo(a:b);
31
   childOneIdx = rem(b, cols) + 1;
   childTwoIdx = rem(b, cols) + 1;
33
   for i = 1:cols
       current = rem(b + i-1, cols) + 1;
35
       if (all(ChildTwo ~= ParentOne(current)))
37
          ChildTwo(childTwoIdx) = ParentOne(current);
          childTwoIdx = rem(childTwoIdx, cols) + 1;
39
       end
41
       if (all(ChildOne ~= ParentTwo(current)))
42
          ChildOne(childOneIdx) = ParentTwo(current);
43
          childOneIdx = rem(childOneIdx, cols) + 1;
44
       end
45
   end
46
47
   ChildOne = path2adj(ChildOne);
48
   ChildTwo = path2adj(ChildTwo);
50
```

end

Listing 4.3: High level crossover function- src/crossover_tsp.m

```
% CROSSOVER_TSP.M (Crossover for TSP high-level function)
  % This function performs recombination (crossover) between pairs of
  % individuals and returns the new individuals after mating.
  % The function handles multiple populations and calls a given low-level
  % function for the actual recombination process.
  % Input parameters:
  % CROSS_F - String containing the name of the crossover function
   % OldChrom - Matrix containing the chromosomes of the old
  % population. Each line corresponds to one individual
  % PR_CROSS - (optional) Scalar containing the probability of
  % recombination/crossover occurring between pairs
  % of individuals. If omitted or NaN, 0.95 is assumed.
  % SUBPOP - (optional) Number of subpopulations.
  % If omitted or NaN, 1 subpopulation is assumed.
   % Output parameter:
  % NewChrom - Matrix containing the chromosomes of the population
  % after recombination in the same format as OldChrom.
  function NewChrom = crossover_tsp(CROSS_F, OldChrom, PR_CROSS, SUBPOP)
22
   % Check parameter consistency
   if nargin < 2; error('Not enough input parameter'); end</pre>
25
26
   % Probability of crossover
  if nargin < 3; PR_CROSS = 0.95;</pre>
   elseif nargin > 2
29
    if isempty(PR_CROSS), PR_CROSS = 0.7;
     elseif isnan(PR_CROSS), PR_CROSS = 0.7;
31
     elseif length(PR_CROSS) ~= 1, error('PR_CROSS must be a scalar');
    elseif (PR_CROSS < 0 | PR_CROSS > 1), error('PR_CROSS must be a scalar
33
         in [0, 1]');
    end
34
   end
36
   % Population size
   [rows, cols] = size(OldChrom);
  NewChrom = zeros(rows, cols);
   if nargin < 4; SUBPOP = 1;</pre>
41
  elseif nargin > 3
42
    if isempty(SUBPOP), SUBPOP = 1;
43
    elseif isnan(SUBPOP), SUBPOP = 1;
     elseif length(SUBPOP) ~= 1, error('SUBPOP must be a scalar');
45
    end
   end
47
48
  if (rows/SUBPOP) ~= floor(rows/SUBPOP)
```

```
error('OldChrom and SUBPOP disagree');
50
   end
51
  rows = rows/SUBPOP; % Compute number of individuals per subpopulation
52
53
   % Select individuals of subpopulations and call low level function
54
   for subpop = 1:SUBPOP
55
      SubChrom = OldChrom((subpop-1)*rows+1:subpop*rows, :);
56
57
      for row = 1:2:rows
          if row == rows
59
              NewChrom((subpop-1)*rows + row, :) = SubChrom(rows, :);
          elseif rand < PR_CROSS</pre>
61
              % TODO: adapt crossover functions so that feval can be used
                  with all of them
              if strcmp(CROSS_F, 'cross_alternating_edges')
                  NewChrom((subpop-1)*rows + row,:) = cross_alternating_edges
64
                      ([ SubChrom(row,:) ; SubChrom(row+1,:) ]);
                  NewChrom((subpop-1)*rows + row + 1,:) =
65
                      cross_alternating_edges([ SubChrom(row+1,:) ; SubChrom(
                      row,:) ]);
              else
66
                  [ChildOne, ChildTwo] = feval(CROSS_F, SubChrom(row, :),
67
                      SubChrom(row+1, :));
                  NewChrom((subpop-1)*rows + row, :) = ChildOne;
                  NewChrom((subpop-1)*rows + row + 1, :) = ChildTwo;
69
              end
          else
71
              NewChrom((subpop-1)*rows + row, :) = SubChrom(row, :);
              NewChrom((subpop-1)*rows + row + 1, :) = SubChrom(row+1, :);
73
          end
       end
75
   end
77
   end
```

Listing 4.4: Inversion mutation for task 4 - src/mut_inversion2.m

```
% low level function for TSP mutation
2
   function NewChrom = mut_inversion2(OldChrom)
   NewChrom = adj2path(OldChrom);
   % select two positions in the tour
   rndi = zeros(1,2);
   while rndi(1) == rndi(2)
           rndi = randi(size(NewChrom, 2), [1, 2]);
10
   end
11
   rndi = sort(rndi);
12
13
   \mbox{\ensuremath{\mbox{\%}}} reverse a subpath in the chrom
14
   reversed_subpath = NewChrom(rndi(2) : -1 : rndi(1));
15
16
  tmp = [ NewChrom(1:rndi(1)-1) NewChrom(rndi(2)+1:size(NewChrom, 2)) ];
```

```
if (isempty(tmp))
       NewChrom = reversed_subpath;
19
   else
20
       idx = randi(size(tmp, 2));
^{21}
       NewChrom = [ tmp(1:idx) reversed_subpath tmp(idx+1:size(tmp, 2)) ];
22
   end
23
24
   NewChrom = path2adj(NewChrom);
25
   end
27
```

Listing 4.5: High level mutation function - src/mutate_tsp.m

```
% MUTATE_TSP.M (Mutation for TSP high-level function)
  % This function takes a matrix OldChrom containing the
  % representation of the individuals in the current population,
  % mutates the individuals and returns the resulting population.
  % Input parameters:
  % MUT_F - String containing the name of the mutation function
  % OldChrom - Matrix containing the chromosomes of the old
  % population. Each line corresponds to one individual.
  % Representation - The TSP representation the given population is in.
  % PR_MUT - (optional) Scalar containing the probability of
  % mutation. If omitted, 0.05 is assumed.
  % SUBPOP - (optional) Number of subpopulations.
  % if omitted or NaN, 1 subpopulation is assumed
  % Output parameter:
  % NewChrom - Matrix containing the chromosomes of the population
  % after mutation in the same format as OldChrom.
20
^{21}
  function NewChrom = mutate_tsp(MUT_F, OldChrom, PR_MUT, SUBPOP)
22
   % Check parameter consistency
^{24}
  if nargin < 2; error('Not enough input parameters'); end</pre>
  % Probability of mutation
  if nargin < 3; PR_MUT = 0.05; end</pre>
28
   % Population size
30
   [rows, cols] = size(OldChrom);
  NewChrom = zeros(rows, cols);
  if nargin < 4; SUBPOP = 1;</pre>
34
  elseif nargin > 3
35
    if isempty(SUBPOP), SUBPOP = 1;
36
    elseif isnan(SUBPOP), SUBPOP = 1;
37
    elseif length(SUBPOP) ~= 1, error('SUBPOP must be a scalar');
38
     end
39
   end
40
41
```

```
if (rows/SUBPOP) ~= fix(rows/SUBPOP)
       error('OldChrom and SUBPOP disagree');
   end
44
45
   rows = rows/SUBPOP; % Compute number of individuals per subpopulation
46
47
   % Select individuals of subpopulations and call low level function
   for subpop = 1:SUBPOP
49
       SubChrom = OldChrom((subpop-1)*rows+1:subpop*rows,:);
51
       for row = 1:rows
          if rand < PR_MUT</pre>
53
              NewChrom((subpop-1)*rows + row, :) = feval(MUT_F, SubChrom(row
           else
              NewChrom((subpop-1)*rows + row, :) = SubChrom(row, :);
56
           end
       end
58
   end
59
60
   end
61
```

Listing 4.6: Fitness proportional selection for task 7a - src/sel_fit_prop.m

```
% SEL_FIT_PROP.m (FITNESS PROPORTIONAL SELECTION)
2
   % This function performs fitness proportional selection.
   % Syntax: NewChrIx = fitpropsel(FitnV, NSel)
6
   % Input parameters:
   % FitnV - Column vector containing the fitness values of the
   % individuals in the population.
   % Nsel - number of individuals to be selected
11
   % Output parameter:
   % NewChrIx - column vector containing the indexes of the selected
   % individuals relative to the original population, shuffled.
   % The new population, ready for mating, can be obtained
   % by calculating OldChrom(NewChrIx,:).
17
   function NewChrIx = sel_fit_prop(FitnV, NSel)
19
   NewChrIx = zeros(NSel, 1);
20
21
   fitSum = sum(FitnV);
   [selProp, I] = sort(FitnV / fitSum);
23
24
   for i = 1:NSel
      s = find(cumsum(selProp) >= rand, 1, 'first');
26
      NewChrIx(i) = I(s);
27
   end
28
30 end
```

Listing 4.7: Tournament selection for task 7a - src/sel_tournament.m

```
% SEL_TOURNAMENT.m (TOURNAMENT SELECTION)
  % This function performs tournament selection.
4
  % Input parameters:
  % FitnV - Column vector containing the fitness values of the
   % individuals in the population.
  % Nsel - number of individuals to be selected
  % Output parameter:
10
  % NewChrIx - column vector containing the indexes of the selected
   % individuals relative to the original population, shuffled.
  % The new population, ready for mating, can be obtained
  % by calculating OldChrom(NewChrIx,:).
15
  function NewChrIx = sel_tournament(FitnV, NSel)
16
17
  NewChrIx = zeros(NSel, 1);
18
19
   [NInd, ~] = size(FitnV);
20
21
  k = max(2, floor(0.05*NInd));
22
23
  for i = 1:NSel
      randIdx = randi(NInd, [k, 1]);
25
       [~, I] = max(FitnV(randIdx));
      NewChrIx(i) = randIdx(I);
27
   end
29
   end
```

Listing 4.8: Round robin tournament survival selection for task 7b - $src/sur_sel_rr_tournament.m$

```
% SUR_SEL_RR_TOURNAMENT.M (ROUND ROBIN TOURNAMENT SURVIVOR SELECTION)
%
% Reinserts offspring in the population by round-robin tournament
% survivor selection.
%
%
% Input parameters:
% Chrom - Matrix containing the individuals (parents) of the current
% population. Each row corresponds to one individual.
% SelCh - Matrix containing the offspring of the current population.
% Each row corresponds to one individual.
% ObjVCh - Column vector containing the objective values of the
individuals (parents - Chrom) in the current population,
% needed for fitness-based insertion saves recalculation of
% objective values for population
% ObjVSel - Column vector containing the objective values of the
% offspring (SelCh) in the current population, needed for
```

```
% partial insertion of offspring, saves recalculation of
  % objective values for population
  % q - The amount of other individuals that each individual is
   % to be evaluated against
21
  % Output parameters:
  % Chrom - Matrix containing the individuals of the current
  % population after reinsertion.
  % ObjVCh - if ObjVCh and ObjVSel are input parameter, than column
  % vector containing the objective values of the individuals
   % of the current generation after reinsertion.
  function [Chrom, ObjVCh] = sur_sel_rr_tournament(Chrom, SelCh, ObjVCh,
       ObjVSel, q)
30
  pop = [Chrom; SelCh];
31
  popFit = [ObjVCh; ObjVSel];
   [Npop, ~] = size(pop);
   [NIND, ~] = size(Chrom);
34
   wins = zeros(Npop, 1);
35
36
  for i = 1:Npop
37
      wins(i) = sum(popFit(i) >= popFit(randi(Npop, [q 1])));
38
   end
39
40
   [~, I] = sort(wins);
41
42
  Chrom = pop(I(1:NIND), :);
   ObjVCh = popFit(I(1:NIND));
44
45
46
```

Listing 4.9: Template function for testing the algorithm. Other testing functions are omitted because they are very similar to this one - src/test_template.m

```
NIND=100; % Number of individuals
  MAXGEN=250; % Maximum no. of generations
  ELITIST=0.05; % percentage of the elite population
  STOP_PERCENTAGE=.95; % percentage of equal fitness individuals for
      stopping
  PR_CROSS=.95; % probability of crossover
  PR_MUT=.05; % probability of mutation
  LOCALLOOP=1; % local loop removal
  CROSSOVER = 'cross_alternating_edges'; % crossover operators
  MUTATION = 'mut_inversion'; % mutation operators
  SELECTION = 'sus'; % parent selection algorithm
  SUBPOP = 1; % Amount of subpopulations
11
  SCALING = 1; % City location scaling on/off
  CUSTOMSTOP = 0; % Custom stopping criterion on/off
  CUSTOMSS = 0; % Custom survivor selection on/off
  RUNS = 1; % Number of ga runs in tests
15
16
17
  datasetslist = dir('datasets/');
```

```
Ndatasets = size(datasetslist, 1) - 2;
20
   results = zeros([Ndatasets 4]);
^{21}
22
   out = fopen('./table.tex', 'w');
23
   fprintf(out, 'A & B & C & D & E\n\\midrule\n');
24
25
   for ds = 1:Ndatasets
26
       datasetslist(ds + 2).name
27
       data = load(['datasets/' datasetslist(ds + 2).name]);
       x = data(:,1);
30
       y = data(:,2);
32
       if SCALING == 1
          x = x / \max([data(:,1); data(:,2)]);
34
          y = y / \max([data(:,1); data(:,2)]);
       end
36
37
       NVAR=size(data,1);
38
39
       for i = 0:RUNS
40
           [best, mean, worst] = run_ga(x, y, NIND, MAXGEN, NVAR, ELITIST,
41
              STOP_PERCENTAGE, PR_CROSS, PR_MUT, CROSSOVER, MUTATION,
              LOCALLOOP, CUSTOMSTOP, CUSTOMSS, SELECTION, SUBPOP);
          Ngen = find(best, 1, 'last');
          B = best(Ngen);
43
          M = mean(Ngen);
          W = worst(Ngen);
45
          results(ds, :) = results(ds, :) + [Ngen B M W];
47
       end
       results(ds, :) = results(ds, :) / RUNS;
50
51
       fprintf(out, '%s & %d & %d & %d & %d \\\\n', datasetslist(ds + 2).
52
           name, results(ds, 1) - 1, results(ds, 2), results(ds, 3), results(
           ds, 4));
53
   end
54
   fclose(out);
56
57
   results
```