# LM Aero Procedures Manual PM4056 Composite Structural Analysis Manual Manual Revision H

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**Revision/Change Summary** 

Revision	Release Date	Description	Affected Sections	Prepared	Approved
H 22-Dec-2016		Added Section 12 Bonded Joints	12	DSN and AS	
	22-Dec-2016	Editorial corrections to Section 19	19	DSN	Morrison
		Update page 4-28 to note that the 6x6 constitutive equation is symmetric	4	DSN	
G	2-Mar-2016	Added Section 13 Composite Design and Analysis Details and Section 18 Structural Certification and Testing	13,18	LKF, AS, DSN	Walsh
F 17-Dec-201		Added Section 15 Durability and Damage Tolerance Analysis	15	RS and LKF	
	17-Dec-2015	Added Export Control Markings to Front Cover, Sections 6, 11, 15 and 19	2, 4, 5, 6, 11,19	LKF	Walsh
		Updated Markings for LM Proprietary Information	1-7,11,19	LKF	
E 18-Dec-14	Updated Design Guidelines Section 2.3.4 to correct that e/D is diameter of the hole not diameter of the fastener.	2 (Rev A)	SN	Walsh	
	18-Dec-14	Updated Design Guidelines Section 11.3, Table 11.3-1 to correct that e/D is diameter of the hole not diameter of the fastener.	11 (Rev A)	SN	Walsh
		Added Section 7 – All New Content: Bending of Laminated Plates and Shells	7	AS	Walsh
		Added Section 19 – All New Content: Effects of Defects and Repair Concepts	19	SN & AS	Walsh
D	28-Mar-2013	Added Section 11 Bolted Composite Joints	11	SN	EPH
С	19-Feb-2013	Added Section 6 Laminated Composite Columns	6	AS	ЕРН
В	31-Jul-11	Added Section 5 Properties of Laminated Composite Beam Cross-Sections	5	MBW	JBD
A	31-Aug-10	Added section 4. Composite Laminates	4	MBW	JBD
-	31-Jul-09	Initial Release	1, 2, 3	MBW, RMT	JBD