# **Vehicle Vibration Analysis with C++**

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MEC 510, Final Project

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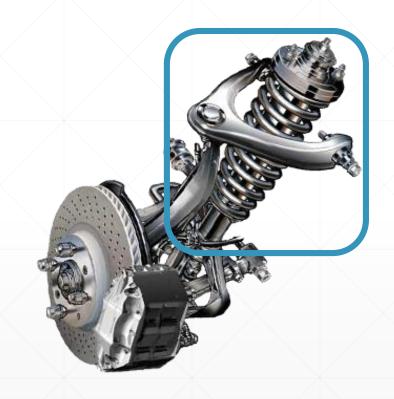
# Problem Background & Description

#### **Motivation**

- MATLAB can be used to successfully analyze a vehicle system
- C++ analysis is much faster than MATLAB
  - MATLAB must run on CPU, C++ can be run using GPU for complex calculations via CUDA
- C++ also allows for direct comparison of multiple vehicle/road object combinations by simply defining more objects

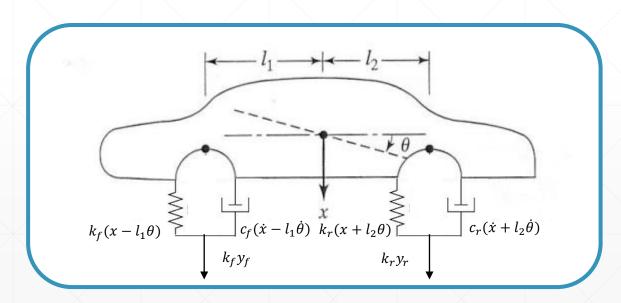
#### **Vehicle Vibrations**

- Suspension systems in vehicles are designed to reduce uncomfortable motions felt by passengers while driving
  - Utilizes springs and shock absorbers to control vibration transmitted through vehicle
- Focused on reducing two kinds of motion
  - Bounce (up and down motion)
  - Pitch (front to back rotation)



#### **Vehicle Model**

- Bounce (x) and pitch (θ) are independent of one another
  - Results in a two degree of freedom system with two coupled differential equations



#### **Vehicle Model**

Mathematical equations governing bounce and pitch response derived from diagram

$$m\ddot{x} + (c_f + c_r)\dot{x} + (k_f + k_r)x + (c_r l_2 - c_f l_1)\dot{\theta} + (k_r l_2 - k_f l_1)\theta = k_f y_f(t) + k_r y_r(t)$$

$$J\ddot{\theta} + (c_f l_1^2 + c_r l_2^2)\dot{\theta} + (k_f l_1^2 + k_r l_2^2)\theta + (c_r l_2 - c_f l_1)\dot{x} + (k_r l_2 - k_f l_1)$$

$$= k_r l_2 y_r(t) - k_f l_1 y_f(t)$$

•  $y_f(t)$  and  $y_r(t)$  are the forcing equations due to bumps on the road and vehicle speed

$$y_f = Asin\left(\frac{2\pi V}{L}t\right)$$
  $y_r = Asin\left(\frac{2\pi V}{L}t - \frac{2\pi(l_1 + l_2)}{L}\right)$ 

### **Project Description**

- Understanding the vibration of the vehicle requires solving the equations of motion to determine x and  $\theta$ 
  - Only x, θ, dx, dθ and t are variable (all other variables in equation are constants)
- Using C++, along with external libraries, the equations can be solved based on user input of parameters

# C++ Code Structure

### **Functionality Overview**

- User inputs car parameters or selects a vehicle class (based on SAE standards)
  - Mass, damping, inertia, etc.
- 2. User inputs road parameters
  - "Wavelength", speed, and amplitude
- 3. User inputs analysis parameters
  - Start time, end time, time step and initial values
- 4. Script outputs natural frequencies, mass and stiffness matrices and writes integration values to a text file

#### **External Libraries**

- Determining the solution for the coupled equations requires the use of linear algebra and differential equations
  - Outside the scope of what MSVS libraries can do natively
- Eigen
  - High level, template library for matrix and vector linear algebra
- Odeint
  - High level, template library for solving differential equations
  - Peer reviewed by Boost for accuracy

#### **Vehicle Class**

- Stores all required constants for left hand side of motion equation (physical parameters of car)
- Includes the functions required to determine:
  - Natural frequency (Eigen)
- Also includes functions to allow user to either define the vehicle parameters or pick pre-set parameters (SAE vehicle class)

#### **Road Class**

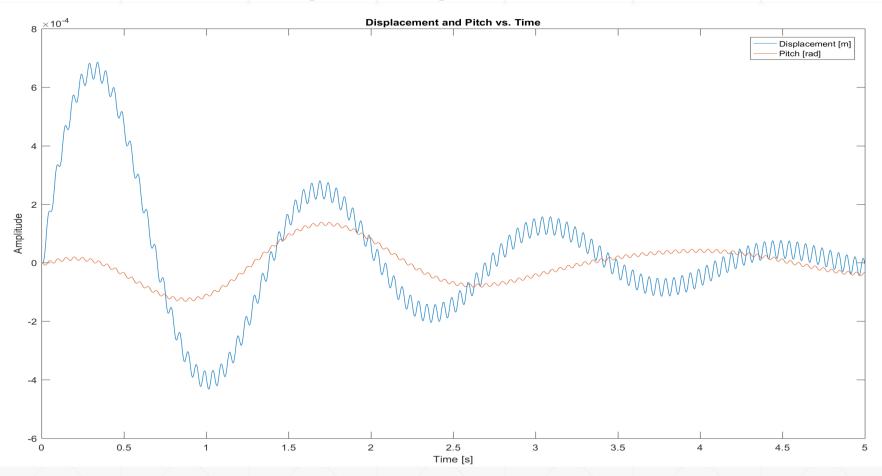
Stores all required constants for forcing functions

# Verification

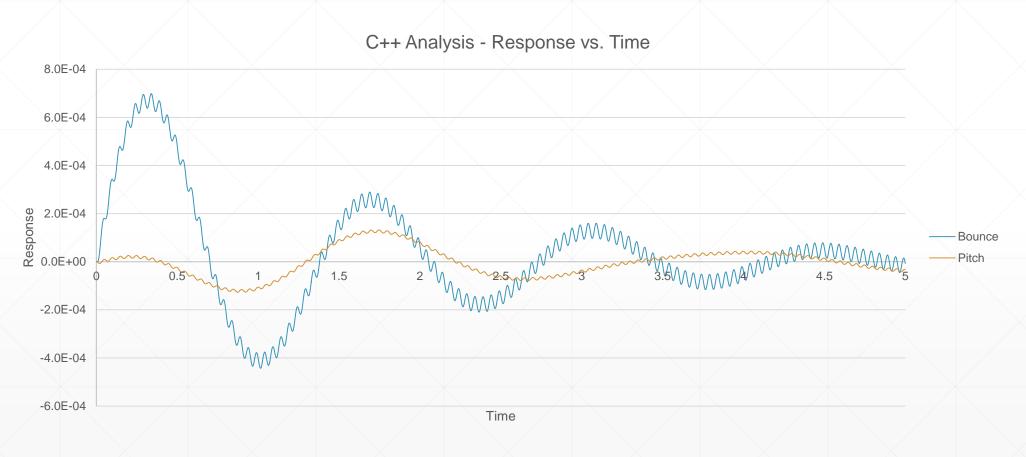
### **Verification Setup**

- Vehicle Parameters
  - Class 4 SAE Vehicle (Luxury vehicle, Jaguar XJ)
- Road Parameters (moderately bumpy road)
  - 10 m/s velocity (approx. 22.4 mph)
  - 0.025 m peak amplitude (approx. 1")
  - 0.5 m wavelength (approx. 20")
- Time period
  - 0-5 seconds

## **MATLAB Results (ode45)**



### C++ Results (Bulirsch-Stoer algorithm)



### **Numerical Comparison**

Maximum Response Values		
	Bounce (m)	Pitch (rad)
C++ Analysis	6.99x10 <sup>-4</sup>	1.32x10 <sup>-4</sup>
MATLAB Analysis	6.86x10 <sup>-4</sup>	1.39x10 <sup>-4</sup>

Percent Error 
$$\begin{cases} Bounce - 0.18\% \\ Pitch - 0.54\% \end{cases}$$

Error is within acceptable range, verification is successful!

# Questions?