(d) Difference between $\hat{N}$ and $\hat{S}^z$ operator correlation

(e) Correlation between cumulants of excitations outside reference space