CIVL

The Concurrency Intermediate Verification Language Reference Manual

v1.5

Matthew B. Dwyer John Edenhofner Ganesh Gopalakrishnan Andre Marianiello Ziqing Luo Zvonimir Rakamaric Michael Rogers Stephen F. Siegel Manchun Zheng Timothy K. Zirkel

November 11, 2015

Contents

Ι	Introduction											
1												
2												
3 Installation and Quick Start												
4	Exa 4.1 4.2 4.3	A Mul	tithreade ing C pro Verifyin Verifyin	phers	11 12 12 12							
II	\mathbf{L}	angua	age		18							
5	Overview of CIVL-C											
5.1 Main Concepts												
	5.2 Example Illustrating Scopes and Processes											
	5.3	Struct	ure of a (CIVL-C program	21							
6	Sequential Elements											
	6.1	Types			23							
		6.1.1		rd types inherited from C								
		6.1.2	The bur	ndle type: \$bundle	23							
		6.1.3	The \$sc	cope type	23							
		6.1.4	The \$ra	ange and \$domain types	24							
	6.2	Expres										
		6.2.1	-	sions inherited from C								
		6.2.2		expressions	25							
			6.2.2.1	Checking if a dyscope is defined: \$scope_defined								
			6.2.2.2	The constant \$here								
			6.2.2.3	The constant \$root								
			6.2.2.4	Scope relational operators								
			6.2.2.5	Scope parent function \$scope_parent								
			6.2.2.6	Lowest Common Ancestor: +	26							

CONTENTS 2

		6	.2.2.7	The \$scop	peof expres	ssion .				 		 		 26
		6.2.3 R	Range a	and domain	expressions	3				 		 		 27
			.2.3.1		ange expres									
		6	.2.3.2	Cartesian	domain ex	pression	s			 		 		 27
	6.3	Statemer	nts							 		 		 27
		6.3.1 C	State	ments						 		 		 27
				and nondete										28
			.3.2.1		commands:									28
			.3.2.2		ninistic sele									29
		_	.3.2.3		ninistic cho									29
		_		n using dom			_							29
	6.4	Function												30
	0.4			t function: S										
		0.4.1 A	DSITAC	t function.	yanstract				• •	 • •	•	 • •	•	 30
7	Cor	ncurrency	v											31
	7.1	v	•	n and mana	gement					 		 		 31
	,,,			cess type: \$	_									
				g if a proces										31
				f process con										31
				l process co										
				ng a new pro	_									
				for process										$\frac{32}{32}$
	7.0			ting a proce		-								
	7.2		•											
				locks: \$atom										32
	7.0			blocks: \$ato										33
	7.3		_	with \$parfo										34
	7.4	_		g										34
				es: \$message										
				nicators: \$g										
		7.4.3 B	Barriers	: \$gbarrieı	r and \$bar	rier .				 		 	•	 35
8	Sno	cification												37
O	8.1													37
	8.2			gnature										37
	0.2	-	-	_										37
				pe qualifier:	_									38
	0.2			type qualifie	_									
	8.3			assumptions										38
				ns: \$assert										38
	0.4			statements:										39
	8.4													39
			-	ion: =>										39
				al quantifier										39
		8.4.3 E	Existent	ial quantifi ϵ	er: \$exist	3				 		 		 39
	8.5	Contract	S							 		 		 40
		8.5.1 P	rocedu	re contracts	3: \$require	es and S	\$ensur	es .		 		 		 40
		8.5.2 L	oop inv	variants: \$i	nvariant					 		 		 40

CONTENTS 3

	8.6	Concurr	ency spe	ecification						 		 				40
		8.6.1 F	Remote 6	expressions	e@x .					 		 				40
		8.6.2	Collectiv	e expression	ns: \$co]	llecti	ve .			 		 				41
9	Poir	nters and	d Heap	S												42
	9.1	Memory	functio	ns: memcpy						 		 				42
	9.2	Heaps, \$	Smalloc	and \$free						 		 				42
10	Libi	raries														43
	10.1	Standard	d CIVL-	C headers						 		 				43
				sics civlc.												43
		1	0.1.1.1	The \$asse	rt and	\$assum	ne fur	actions	s	 		 				43
		1	0.1.1.2	The \$wait												43
		1	0.1.1.3	The \$wait												44
			0.1.1.4													44
		1	0.1.1.5													44
		1	0.1.1.6	The \$scop												44
			0.1.1.7	The \$proc												44
				The heap-												44
				ilities scop												45
				ıtilities poi												45
				The \$equa												45
			0.1.3.2	The \$cont												45
				The \$tran												46
				The \$copy												46
				utilities se												46
			-	The \$seq_	-											47
			0.1.4.2	The \$seq_												47
				The \$seq_												47
				The \$seq_												47
				ency utilitie												48
				The \$gbar												48
			0.1.5.2	The \$gbar												48
				The \$barr		•					•					48
				ype and fur												49
				The \$bund												49
			0.1.6.2													49
			0.1.6.3	The \$bund	-											49
			0.1.6.4	The \$bund	-											49
				icators com	_	_										50
			.0.1.7.1	Messaging												50
				\$gcomm fur												50
			0.1.7.2 $0.1.7.3$													51
	10.9	C librari		фоошш тип	, citoris .					 	•	 	 •	• •	•	51 51

CONTENTS 4

III Semantics	F	53
11 CIVL Model Syntax		54
11.1 Notation and terminology		54
11.2 Definition of Context		54
11.3 Lexical scopes		55
11.4 Functions		57
11.5 Statements		58
11.6 Remarks		59
11.7 Transition system representation of functions		60
12 CIVL Model Semantics	1	61
12.1 State		61
12.2 Jump protocol		62
12.3 Initial State		64
12.4 Transitions		64
12.5 Calls and Spawns		64
12.6 Garbage collection		65
IV Tools	(66
13 Tool Overview	ı	67
13.1 Symbolic execution		67
13.2 Commands		67
13.3 Options		68
13.4 Errors		69
14 Interpreting the Output	i	7 1
14.1 Transitions		71
14.2 States		72
14.3 Property Violations		73
14.4 Statistics		74
15 Emacs mode		76
Bibliography	•	77

Part I Introduction

Acknowledgement

The CIVL project is funded by the U.S. National Science Foundation under awards CCF-1346769 and CCF-1346756.

What is CIVL?

CIVL stands for *Concurrency Intermediate Verification Language*. The *CIVL platform* encompasses:

- 1. the programming language **CIVL-C**, a dialect of C with additional primitives supporting concurrency, specification, and modeling;
- 2. verification and analysis tools, including a symbolic execution-based model checker for checking various properties of, or finding defects in, CIVL-C programs; and
- 3. tools that translate from many commonly used languages/APIs to CIVL-C.

The CIVL-C language is primarily intended to be an intermediate representation for verification. A C program using MPI [2], CUDA [3], OpenMP [4], OpenCL [1], or another API (or even some combination of APIs), will be automatically translated into CIVL-C and then verified. The advantages of such a framework are clear: the developer of a new verification technique could implement it for CIVL-C and then immediately see its impact across a broad range of concurrent programs. Likewise, when a new concurrency API is introduced, one only needs to implement a translator from it to CIVL-C in order to reap the benefits of all the verification tools in the platform. Programmers would have a valuable verification and debugging tool, while API designers could use CIVL as a "sandbox" to investigate possible API modifications, additions, and interactions.

This manual covers all aspects of the CIVL framework, and is organized in parts as follows:

- 1. this introduction, including "quick start" instructions for downloading and installing CIVL and several examples;
- 2. a complete description of the CIVL-C language;
- 3. a formal semantics for the language; and
- 4. a description of the tools in the framework.

Installation and Quick Start

This chapter gives instructions for downloading and installing CIVL, and running the verification tool on an example.

Notes

• The instructions say to install three theorem provers. In reality, each of these is optional. CIVL will still work without any theorem provers, but the results will not be very precise, i.e., it will produce a lot of false warnings. The more provers you install, the more precise the analysis.

Instructions

- 1. Install the automated theorem prover CVC3 (if you have not already). The easiest way to do this is to visit http://www.cs.nyu.edu/acsys/cvc3/download.html and download the latest, optimized build with static library and executable for your OS. Place the executable file cvc3 somewhere in your PATH. You can discard everything else. Alternatively, on some linux systems, CVC3 can be installed using the package manager via "sudo apt-get install cvc3". This will place cvc3 in /usr/bin.
- 2. Install the automated theorem prover CVC4 (if you have not already). The easiest way to do this is to visit http://cvc4.cs.nyu.edu/downloads/ and choose one of the installation approaches. You only need the binary (cvc4), and you must put it in your PATH. Alternatively, on OS X you may install using MacPorts by "sudo port install cvc4".
- 3. Install the automated theorem prover Z3 (if you have not already). Follow instructions at http://z3.codeplex.com/SourceControl/latest#README. Make sure the executable z3 is in your path.
- 4. Install a Java 7 SDK if you have not already. Go to http://www.oracle.com/technetwork/java/javase/downloads/ for the latest from Oracle. On linux, you can instead use the package manager: "sudo apt-get install openjdk-7-jdk".
- 5. Download and unpack the latest stable release of CIVL from http://vsl.cis.udel.edu/civl.
- 6. The resulting directory should be named CIVL-tag for some string tag which identifies the version of CIVL you downloaded. Move this directory wherever you like.

7. The JAR file in the lib directory is all you need to run CIVL. You may move this JAR file wherever you want. You run CIVL by typing a command of the form "java -jar /path/to/civl-TAG.jar ...". For convenience, you may instead use the shell script civl included in the bin directory. This allows you to replace "java -jar /path/to/civl-TAG.jar" with just "civl" on the command line. Simply edit the civl script to reflect the path to the JAR file and place the script somewhere in your PATH. Alternatively, you can define an alias in your .profile, .bash_profile, .bashrc, or equivalent, such as

alias civl='java -jar /path/to/civl-TAG.jar'

In the following, we will assume that you have defined a command civl in one of these ways.

- 8. From the command line, type "civl help". You should see a help message describing the command line syntax.
- 9. From the command line, type "civl config". This should report that cvc3, cvc4, and z3 were found, and it should create a file called .sarl in your home directory.

To test your installation, copy the file examples/concurrency/locksBad.cvl to your working directory. Look at the program: it is a simple 2-process program with two shared variables used as locks. The two processes try to obtain the locks in opposite order, which can lead to a deadlock if both processes obtain their first lock before either obtains the second. Type "civl verify locksBad.cvl". You should see some output culminating in a message

The program MAY NOT be correct. See CIVLREP/locksBad_log.txt

Type "civl replay locksBad.cvl". You should see a step-by-step account of how the program arrived at the deadlock.

Examples

In this section we show a few simple CIVL-C programs which illustrate some of the pertinent features of the language. We also show the results of running some of the tools on them.

4.1 Dining Philosophers

Dijkstra's well-known Dining Philosophers system can be encoded in CIVL-C as shown in Figure 4.1.

In this encoding, an upper bound B is placed on the number of philosophers n. When verifying this program, a concrete value will be specified for B. Hence the result of verification will apply to all n between 2 and B, inclusive.

Both B and n are delcared as *input* variables using the type qualifier \$input. An input variable may be initialized with any valid value of its type. In contrast, non-input variables declared in file scope will be initialized with a special *undefined* value; if such a variable is read before it is defined, an error will be reported. In addition, any input variable may have a concrete initial value specified on the command line. In this case, we will specify a concrete value for B on the command line but leave n unconstrained.

An \$assume statement restricts the set of executions of the program to include only those traces in which the assumptions hold. In contrast with an \$assert statement, CIVL does not check that the assumed expression holds, and will not generate an error message if it fails to hold. Thus an \$assume statement allows the programmer to say to CIVL "assume that this is true," while an \$assert statement allows the programmer to say to CIVL "check that this is true."

A \$when statement encodes a guarded command. The \$when statement includes a boolean expression called the guard and a statement body. The \$when statement is enabled if and only if the guard evaluates to true, in which case the body may be executed. The first atomic statement in the body executes atomically with the evaluation of the guard, so it is guaranteed that the guard will hold when this initial sub-statement executes. Since assignment statements are atomic in CIVL, in this example the body of each \$when statement executes atomically with the guard evaluation.

The \$spawn statement is very similar to a function call. The main difference is that the function called is invoked in a new process which runs concurrently with the existing processes. The \$spawn statement itself returns immediately.

The program may be verified for an upper bound of 5 by typing the following at the command line:

civl verify -inputB=5 diningBad.cvl

```
#include <civlc.h>
$input int B; // upper bound on number of philosophers
$input int n; // number of philosophers
$assume 2<=n && n<=B;</pre>
_Bool forks[n]; // Each fork will be on the table (0) or in a hand (1).
void dine(int id) {
  int left = id;
  int right = (id + 1) \% n;
  while (1) {
    $when (forks[left] == 0) forks[left] = 1;
    $when (forks[right] == 0) forks[right] = 1;
    forks[right] = 0;
    forks[left] = 0;
  }
}
void main() {
  for (int i = 0; i < n; i++) forks[i] = 0;
  for (int i = 0; i < n; i++) $spawn dine(i);
}
```

Figure 4.1: diningBad.cvl: CIVL-C encoding of Dijkstra's Dining Philosophers

The output indicates that a deadlock has been found and a counterexample has been produced and saved. We can examine the counterexample, but it is more helpful to work with a *minimal* counterexample, i.e., a deadlocking trace of minimal length. To find a minimal counterexample, we issue the command

```
civl verify -inputB=5 -min diningBad.cvl
```

The result of this command is shown in Figure 4.2. The output indicates that a minimal counterexample has length 19, i.e., involves 20 states and 19 transitions (the depth of 20 is one more than 19). It was the 26th and shortest trace found. It was deemed equivalent to the earlier traces and hence the earlier ones were discarded and only this one saved. We can replay the trace with the command

```
civl replay diningBad.cvl
```

The result of this command is shown in Figure 4.3. The output indicates that a deadlock has been found involving 2 philosophers. The trace has 15 transitions; after the initialization sequence, each philosopher picks up her left fork.

4.2 A Multithreaded MPI Example

Figure 4.4 is an example of a CIVL-C model of multithreaded MPI program. The program consists of two processes, each of which spawns two threads. All four threads issue message-passing operations.

This example illustrates some of the message-passing primitives provided in CIVL-C. A global communicator object is allocated in the root scope. The constant \$here has type \$scope and refers to the scope in which the expression occurs; in this case it is the root (i.e., file) scope. This global communicator is declared to have NPROCS places; these are points from which messages can be sent or received. The function MPI_Process is used to model an MPI process. Each instance will create its own local communicator object which specifies the global communicator and a place; this is the object that will be used to send or receive messages at that place.

Each process spawns two instances of function Thread. Each thread creates a message object from a buffer, specifying the source and destination places, tag, pointer to the beginning of the buffer, and the size of the buffer. The message is *enqueued* into the communication universe using the local communicator. Similarly, messages are dequeued by specifying the local communicator, source place, and tag.

The program has a subtle defect, which only manifests on very specific interleavings of the threads. This defect can be found using civl verify.

4.3 Verifying C programs

CIVL can be used to verify C programs, with a number of transformers. One can also insert macros to C programs to tune it for verification, which, most of time, involves defining input variables. This is usually accomplished by the default macro _CIVL.

For example, Figure 4.5 is a simple program that computes the sum of a number of positive numbers. The program can be compiled by any C compiler, as long as no _CIVL macro is defined in the command for compiling. When CIVL runs this program, it will automatically have _CIVL defined and thus N becomes an input variable and sum becomes an output variable and there is an assertion to check the correctness the sum computed by the program.

If one wants to CIVL to treat a program as it is originally, then the command line option -_CIVL can be set to false to disable the _CIVL macro.

4.3.1 Verifying MPI C programs

CIVL generates default input variables for verifying MPI programs:

- _NPROCS: number of MPI processes to be created;
- _NPROCS_LOWER_BOUND/_NPROCS_UPPER_BOUND: lower/upper bound of the number of MPI processes to be created.

CIVL requires at least either _NPROCS or _NPROCS_UPPER_BOUND be specified in the command line in order to verify MPI programs. For example, one can specify civl verify -input_NPROCS=5 ring.c.

4.3.2 Verifying OpenMP C programs

CIVL introduces a default input variables THREAD_MAX for OpenMP programs. Usually, THREAD_MAX needs to be specified in the command line. CIVL will create 1 to THREAD_MAX-1 threads for all OpenMP parallel region during the verification. If THREAD_MAX is not specified, then somewhere in the OpenMP program must be specifying the number of threads explicitly. By default, CIVL applies simplification to OpenMP based on independent loop analysis, and optimally that might

reduce the program to be purely sequential. The option ompNoSimplify can be set to false so as to skip such simplification. Another option, ompLoopDecomp can be used to specify the loop decomposition strategy, which can be ALL, ROUND_ROBIN or RANDOM.

4.3.3 Verifying Pthreads C and CUDA C programs

There are no special option or default input variables for Pthreads or CUDA programs.

```
CIVL v0.15 of 2014-12-23 -- http://vsl.cis.udel.edu/civl
Error 0 encountered at depth 129:
Error 25 encountered at depth 16:
CIVL execution error (kind: DEADLOCK, certainty: PROVEABLE)
A deadlock is possible:
 Path condition: true
 Enabling predicate: false
ProcessState 0: terminated
ProcessState 1: at location 26, f0:21.30-42 "forks[right]"
  Enabling predicate: false
ProcessState 2: at location 26, f0:21.30-42 "forks[right]"
 Enabling predicate: false
at f0:21.30-42 "forks[right]".
State 664
| Path condition
| | true
| Dynamic scopes
| | dyscope 0 (parent=-1, static=0)
| \ | \ | \ | \ reachers = \{1,2\}
| | | variables
| | | | __atomic_lock_var = process<-1>
| | | | B = 5
| | | n = 2
| | | | forks = X_s0v4[0:=1, 1:=1]
| Process states
| | process 2
| | | call stack
| | | | Frame[function=dine, location=25, f0:21.30-42 "forks[right]", scope=3]
: 15327
  validCalls
                    : 17
  proverCalls
  memory (bytes) : 18554880
  time (s)
                    : 2.17
  maxProcs
                    : 6
  statesInstantiated : 9264
                  : 665
  statesSaved
  statesSeen
                    : 1758
  statesMatched : 1177
                    : 2993
  steps
  transitions : 2934
```

The program MAY NOT be correct. See CIVLREP/diningBad_log.txt

Figure 4.2: Output from civ1 verify -inputB=5 -min diningBad.cvl

```
Transition 1: State 0, proc 0:
  0 \rightarrow 1: B = 5 at f0:9.0-12 "$input int B";
  1->2: n = InitialValue(n) at f0:10.0-12 "$input int n";
  2->3: assume ((2<=n)\&\&(n<=B)) at f0:11.0-20 "$assume 2<=n && n ... B";
  3->5: forks = InitialValue(forks) at f0:13.0-12 "int forks[n]";
  5->6: i = 0 at f0:28.7-16 "int i = 0";
--> State 1
Transition 2: State 1, proc 0:
  6->8: LOOP_TRUE_BRANCH at f0:28.18-23 "i < n";
--> State 2
Transition 12: State 12, proc 2:
  18->19: left = id at f0:16.2-15 "int left = id";
  19->20: right = ((id+1)%n) at f0:17.2-26 "int right = (id ... n";
--> State 13
Transition 13: State 13, proc 2:
  20->23: LOOP_TRUE_BRANCH at f0:19.9-10 "1";
--> State 14
Transition 14: State 14, proc 1:
  23->25: forks[left] = 1 at f0:20.29-44 "forks[left] = 1";
--> State 15
Transition 15: State 15, proc 2:
  23->25: forks[left] = 1 at f0:20.29-44 "forks[left] = 1";
--> State 16
Violation of Deadlock found in State 16:
A deadlock is possible:
 Path condition: true
 Enabling predicate: false
ProcessState 0: terminated
ProcessState 1: at location 25, f0:21.30-42 "forks[right]"
  Enabling predicate: false
ProcessState 2: at location 25, f0:21.30-42 "forks[right]"
  Enabling predicate: false
Trace ends after 15 transitions.
Violation(s) found.
. . .
```

Figure 4.3: Output from civl replay diningBad.cvl

```
#include<civlc.h>
#define TAG 0
#define NPROCS 2
#define NTHREADS 2
$gcomm gcomm = $gcomm_create($here, NPROCS);
void MPI_Process (int rank) {
  $comm comm = $comm_create($here, gcomm, rank);
  $proc threads[NTHREADS];
  void Thread(int tid) {
    int x = rank;
    $message in, out = $message_pack(rank, 1-rank, TAG, &x, sizeof(int));
    for (int j=0; j<2; j++) {
      if (rank == 1) {
        for (int i=0; i<2; i++) $comm_enqueue(comm, out);</pre>
        for (int i=0; i<2; i++) in = $comm_dequeue(comm, 1-rank, TAG);</pre>
      } else {
        for (int i=0; i<2; i++) in = $comm_dequeue(comm, 1-rank, TAG);</pre>
        for (int i=0; i<2; i++) $comm_enqueue(comm, out);</pre>
      }
    }
  }
  for (int i=0; i<NTHREADS; i++) threads[i] = $spawn Thread(i);</pre>
  for (int i=0; i<NTHREADS; i++) $wait(threads[i]);</pre>
  $comm_destroy(comm);
}
void main() {
  $proc procs[NPROCS];
  for (int i=0; i<NPROCS; i++) procs[i] = $spawn MPI_Process(i);</pre>
  for (int i=0; i<NPROCS; i++) $wait(procs[i]);</pre>
  $gcomm_destroy(gcomm);
}
```

Figure 4.4: mpi-pthreads.cvl: CIVL-C model of a (defective) multithreaded MPI program.

```
\#ifdef\ \_CIVL
#include<civlc.cvh>
#endif
#ifdef _CIVL
$input int N;
$output int sum;
#else
#define N 100
int sum;
#endif
void main() {
  int localsum = 0;
  for (int i = 1; i <= N; i++) {
  localsum+=i;
  }
  sum = localsum;
#ifdef _CIVL
  acceptain = (N+1)*N/2);
#endif
}
```

Figure 4.5: $_$ CIVL: the default macro

Part II Language

Overview of CIVL-C

5.1 Main Concepts

CIVL-C is an extension of a subset of the C11 dialect of C. It includes the most commonly-used elements of C, including most of the syntax, types, expressions, and statements. Missing are some of the more esoteric type qualifiers, bitwise operations (at least for now), and much of the standard library. Moreover, none of the C11 language elements dealing with concurrency are included, as CIVL-C has its own concurrency primitives.

The keywords in CIVL-C not already in C begin with the symbol \$. This makes them readily identifiable and also prevents any naming conflicts with identifiers in C programs. This means that most legal C programs will also be legal CIVL-C programs.

One of the most important features of CIVL-C not found in standard C is the ability to define functions in any scope. (Standard C allows function definitions only in the file scope.) This feature is also found in GNU C, the GNU extension of C.

Another central CIVL-C feature is the ability to *spawn* functions, i.e., run the function in a new *process* (thread).

Scopes and processes are the two central themes of CIVL-C. Each has a static and a dynamic aspect. The static scopes correspond to the lexical scopes in the program—typically, regions delimited by curly braces {...}. At runtime, these scopes are *instantiated* when control in a process reaches the beginning of the scope. Processes are created dynamically by *spawning* functions; hence the functions are the static representation of processes.

5.2 Example Illustrating Scopes and Processes

To understand the static and dynamic nature of scopes and processes, and the relations between them, we consider the (artificial) example code of Figure 5.1. The static scopes in the scope are numbered from 0 to 6.

The static scopes have a tree structure: one scope is a child of another if the first is immediately contained in the second. Scope 0, which is the file scope (or *root* scope) is the root of this tree. The static scope tree is depicted in Figure 5.2 (left). Each scope is identified by its integer ID. Additionally, if the scope happens to be the scope of a function definition, the name of the function is included in this identifier. A node in this tree also shows the variables and functions declared in the scope. For brevity, we omit the *proc* variables.

We now look at what happens when this program executes. Figure 5.2 (right) illustrates a

```
0
int x;
void f() { 1
  int y;
  void f1() \{ 2 \ldots \}
  if (x>0) { 3
    int z;
    void f2() { 4 int w; ...}
    $proc p2=$spawn f1();
    $proc p3=$spawn f1();
    $proc p4=$spawn f2();
    f2();
void g() \{ 5 \dots \}
void main() { 6
  $proc p1=$spawn f();
  g();
```

Figure 5.1: CIVL-C code skeleton to illustrate scope hierarchy

possible state of the program at one point in an execution. We now explain how this state is arrived at.

First, there is an implicit *root function* placed around the entire code. The body of the *main* function becomes the body of the root function, and the *main* function itself disappears. This minor transformation does not change the structure of the scope tree.

Execution begins by spawning a process p_0 to execute the root function. This causes scope 0 to be instantiated. An instance of a static scope is known as a *dynamic scope*, or *dyscopes* for short. The dynamic scopes are represented by the ovals with double borders on the right side of Figure 5.2. Each dyscope specifies a value for every variable declared in the corresponding static scope. In this case, the value 3 has been assigned to variable \mathbf{x} .

The state of process p_0 is represented by a *call stack* (green). The entries on this stack are *activation frames*. Each frame contains two data: a reference to a dyscope (indicated by blue arrows) and a current location (or programmer counter vaule) in the static scope corresponding to that dyscope (not shown). The dyscope defines the environment in which the process evaluates expressions and executes statements. The currently executing function of a process, corresponding to the top frame in the call stack, can "see" only the variables in its dyscope and those of all the ancestors of its dyscope in the dyscope tree.

Returning to the example, p_0 enters scope 6, instantiating that scope, and then spawns procedure f. This creates process p_1 , with a new stack with a frame pointing to a dyscope corresponding to static scope 1. The new process proceed to run concurrently with p_0 . Meanwhile, p_0 calls procedure g, which pushes a new entry onto its call stack, and instantiates scope 5. Hence p_0 has two entries on its stack: the bottom one pointing to the instance of scope 6, the top one pointing to the instance of scope 5.

Meanwhile, assume x > 0, so that p_1 takes the *true* branch of the if statement, instantiating scope 3 under the instance of scope 1. It then spawns two copies of procedure f1, creating processes p_2 and p_3 and two instances of scope 2. Then p_1 spawns f2, creating process p_4 and an instance of scope 4. Note that the instance of scope 4 is a child of the instance of scope 3, since the (static)

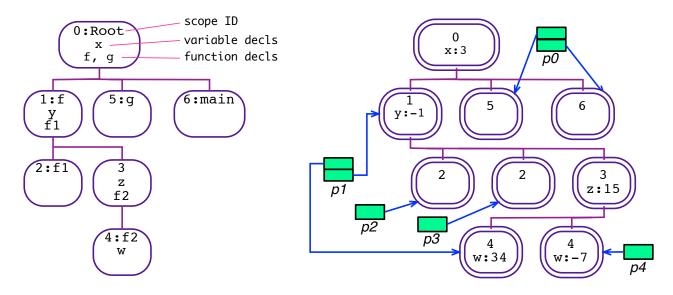


Figure 5.2: Static scope tree and a state for example program

scope 4 is a child of scope 3. Finally, p_1 calls f2, pushing a new entry on its stack and creating another instance of scope 4. The final state arrived at is the one shown.

There are few key points to understand:

- In any state, there is a mapping from the dyscope tree to the static scope tree which maps a dyscope to the static scope of which it is an instance. This mapping is a *tree homomorphism*, i.e., if dyscope u is a child of dyscope v, then the static scope corresponding to u is a child of the static scope corresponding to v.
- A static scope may have any number of instances, including 0.
- Dynamic scopes are created when control enters the corresponding static scope; they disappear from the state when they become unreachable. A dyscope v is "reachable" if some process has a frame pointing to a dyscope u and there is a path from u up to v that follows the parent edges in the dyscope tree.
- Processes are created when functions are spawned; they disappear from the state when their stack becomes empty (either because the process terminates normally or invokes the *exit* system function).

5.3 Structure of a CIVL-C program

A CIVL-C program is structured very much like a standard C program. In particular, a CIVL-C program may use the preprocessor directives specified in the C Standard, and with the same meaning. A source program is preprocessed, then parsed, resulting in a translation unit, just as with standard C. The main differences are the nesting of function definitions and the new primitives beginning with \$, which are described in detail in the remainder of this part of the manual.

A CIVL-C program must begin with the line

#include <civlc.h>

which includes the main CIVL-C header file, which declares all the types and other CIVL primitives. As usual, a translation unit consists of a sequence of variable declarations, function prototypes, and function definitions in file scope. In addition, *assume* statements may occur in the file scope. These are used to state assumptions on the input values to a program.

Sequential Elements

In this chapter we describe the main sequential elements of the language. For the most part these are the same as in C. Primitives dealing with concurrency are introduced in Chapter 7.

6.1 Types

6.1.1 Standard types inherited from C

The civlc.cvh defines standard types inherited from C. The boolean type is denoted _Bool, as in C. Its values are 0 and 1, which are also denoted by \$false and \$true, respectively.

There is one integer type, corresponding to the mathematical integers. Currently, all of the C integer types int, long, unsigned int, short, etc., are mapped to the CIVL integer type.

There is one real type, corresponding to the mathematical real numbers. Currently, all of the C real types double, float, etc., are mapped to the CIVL real type.

Array types, struct and union types, char, and pointer types (including pointers to functions) are all exactly as in C.

6.1.2 The bundle type: \$bundle

CIVL-C includes a type named \$bundle, declared in the CIVL-C standard header bundle.cvh. A bundle is basically a sequence of data, wrapped into an atomic package. A bundle is created using a function that specifies a region of memory. One can create a bundle from an array of integers, and another bundle from an array of reals. Both bundles have the same type, \$bundle. They can therefore be entered into an array of \$bundle, for example. Hence bundles are useful for mixing objects of different (even statically unknown) types into a single data structure. Later, the contents of a bundle can be extracted with another function that specifies a region of memory into which to unpack the bundle; if that memory does not have the right type to receive the contents of the bundle, a runtime error is generated. The bundle type and its functions are provided by the library bundle.cvh.

The relevant functions for creating and manipulating bundles are given in Section 10.1.6.

6.1.3 The \$scope type

An object of type \$scope is a reference to a dynamic scope. It may be thought of as a "dynamic scope ID," but it is not an integer and cannot be converted to an integer. Operations defined on

scopes are discussed in Section 6.2.2.

6.1.4 The \$range and \$domain types

CIVL-C provides certain abstract datatypes that are useful for representing iteration spaces of loops in an abstract way.

First, there is a built-in type **\$range**. An object of this type represents an ordered set of integers. There are expressions for specifying range values; these are described in Section 6.2.3.1. Ranges are typically used as a step in constructing *domains*, described next.

A domain type is used to represent a set of tuples of integer values. Every tuple in a domain object has the same arity (i.e., number of components). The arity must be at least 1, and is called the *dimension* of the domain object.

For each integer constant expression n, there is a type \$domain(n), representing domains of dimension n. The universal domain type, denoted \$domain, represents domains of all positive dimensions, i.e., it is the union over all $n \ge 1$ of \$domain(n). In particular, each \$domain(n) is a subtype of \$domain.

There are expressions for specifying domain values; these are described in Section 6.2.3.2. There are also certains statements that use domains, such as the "CIVL-for" loop \$for; see Section 6.3.3.

6.2 Expressions

6.2.1 Expressions inherited from C

The following C expressions are included in CIVL:

- constant expressions
- *identifier* expressions (x)
- parenthetical expressions ((e))
- numerical addition (a+b), subtraction (a-b), multiplication (a*b), division (a/b), unary plus (+a), unary minus (-a), integer division (a/b) and modulus (a%b), all with their ideal mathematical interpretations
- array index expressions (a[e]) and struct or union navigation expressions (x.f, p->f)
- address-of (&e), pointer dereference (*p), pointer addition (p+i) and subtraction (p-q) expressions
- relational expressions (a==b, a!=b, a>=b, a<=b, a>b)
- logical not (!p), and (p&&q), and or (p||q)
- sizeof a type (sizeof(t)) or expression (sizeof(e))
- assignment expressions (a=b, a+=b, a-=b, a*=b, a/=b, a%=b, a++, a--)
- function calls f(e1,...,en)
- conditional expressions (b ? e : f).

• cast expressions ((t)e)

Bit-wise operations are not yet supported.

6.2.2 Scope expressions

As mentioned in Section 6.1.3, CIVL-C provides a type \$scope. An object of this type is a reference to a dynamic scope. Several constants, expressions, and functions dealing with the \$scope type are also provided.

The \$scope type is like any other object type. It may be used as the element type of an array, a field in a structure or union, and so on. Expressions of type \$scope may occur on the left or right-hand sides of assignments and as arguments in function calls just like any other expression. Two different variables of type \$scope may be aliased, i.e., they may refer to the same dynamic scope.

A dynamic scope δ is reachable if there exists a path which starts from the dyscope referenced by some frame on the call stack of a process, follows the parent edges in the dyscope tree, and terminates in δ . If a dyscope is not reachable, it can never become reachable, and it cannot have any effect on the subsequent execution of the program.

Normally, a dynamic scope will eventually become unreachable. At some point after it becomes unreachable, it will be collected in a garbage-collection-like sweep, and any existing references to that scope will become *undefined*. An object of type \$scope is also undefined before it is initialized. Any use of an undefined value is reported as an error by CIVL, so it is important to be sure that a scope variable is defined before using it.

6.2.2.1 Checking if a dyscope is defined: \$scope_defined

The header civlc.cvh provides a function \$scope_defined, which checks if a given value of \$scope type is defined, as described in Section 10.1.1.6.

6.2.2.2 The constant \$here

A constant \$here exists in every scope. This constant has type \$scope and refers to the dynamic scope in which it is contained. For example,

```
{ // scope s
  int *p = (int*)$malloc($here, n*sizeof(int));
}
```

allocates an object consisting of n into in the scope s.

6.2.2.3 The constant \$root

There is a global constant \$root of type \$scope which refers to the root dynamic scope.

6.2.2.4 Scope relational operators

Let s_1 and s_2 be expressions of type \$scope. The following are all CIVL-C expressions of boolean type:

• $s_1 == s_2$. This is *true* iff s_1 and s_2 refer to the same dynamic scope.

- $s_1 = s_2$. This is *true* iff s_1 and s_2 refer to different dynamic scopes.
- $s_1 \le s_2$. This is *true* iff s_1 is equal to or a descendant of s_2 , i.e., s_1 is equal to or contained in s_2 .
- $s_1 < s_2$. This is *true* iff s_1 is a strict descendant of s_2 , i.e., s_1 is contained in s_2 and is not equal to s_2 .
- $s_1 > s_2$. This is equivalent to $s_2 < s_1$.
- $s_1 >= s_2$. This is equivalent to $s_2 <= s_1$.

If s_1 or s_2 is undefined in any of these expressions, an error will be reported.

6.2.2.5 Scope parent function \$scope_parent

The CIVL-C header scope.cvh provides the function \$scope_parent that computes the immediate parent of a dynamic scope, as described in Section 10.1.2.

6.2.2.6 Lowest Common Ancestor: +

The expression $s_1 + s_2$, where s_1 and s_2 are expressions of type \$scope, evaluates to the lowest common ancestor of s_1 and s_2 in the dynamic scope tree. This is the smallest dynamic scope containing both s_1 and s_2 .

6.2.2.7 The \$scopeof expression

Given any left-hand-side expression expr, the expression

```
$scopeof(expr)
```

evaluates to the dynamic scope containing the object specified by expr.

The following example illustrates the semantics of the \$scopeof operator. All of the assertions hold:

```
{
    $scope s1 = $here;
    int x;
    double a[10];

{
        $scope s2 = $here;
        int *p = &x;
        double *q = &a[4];

        assert($scopeof(x)==s1);
        assert($scopeof(p)==s2);
        assert($scopeof(*p)==s1);
        assert($scopeof(a)==s1);
        assert($scopeof(a)==s1);
        assert($scopeof(a]==s2);
```

```
assert($scopeof(*q)==s1);
}
```

6.2.3 Range and domain expressions

6.2.3.1 Regular range expressions

An expression of the form

```
lo .. hi
```

where lo and hi are integer expressions, represents the range consisting of the integers lo, lo + 1,..., hi (in that order).

An expression of the form

```
lo .. hi # step
```

where lo, hi, and step are integer expressions is interpreted as follows. If step is positive, it represents the range consisting of lo, lo + step, lo + 2* step, . . ., up to and possibly including hi. To be precise, the infinite sequence is intersected with the set of integers less than or equal to hi.

If step is negative, the expression represents the range consisting of hi, hi + step, hi + 2 * step, ..., down to and possibly including 1o. Precisely, the infinite sequence is intersected with the set of integers greater than or equal to 1o.

6.2.3.2 Cartesian domain expressions

An expression of the form

```
($domain) { r1, ..., rn }
```

where $r1, \ldots, rn$ are n expressions of type \$range, is a Cartesian domain expression. It represents the domain of dimension n which is the Cartesian product of the n ranges, i.e., it consists of all n-tuples (x_1, \ldots, x_n) where $x_1 \in r1, \ldots, x_n \in rn$. The order on the domain is the dictionary order on tuples. The type of this expression is \$domain(n).

When a Cartesian domain expression is used to initialize an object of domain type, the "(\$domain)" may be omitted. For example:

```
dom = \{ 0 ... 3, r2, 10 ... 2 # -2 \};
```

6.3 Statements

6.3.1 C Statements

The usual C statements are supported:

- no-op (;)
- expression statements (e;)
- labeled statements, including case and default labels (1: s)

- for (for (init; cond; inc) s), while (while (cond) s) and do (do s while (cond)) loops
- compound statements ({s1;s2; ...})
- if and if ...else
- goto
- switch
- break
- continue
- return

6.3.2 Guards and nondeterminism

6.3.2.1 Guarded commands: \$when

A guarded command is encoded in CIVL-C using a \$when statement:

```
$when (expr) stmt;
```

All statements have a guard, either implicit or explicit. For most statements, the guard is **\$true**. The **\$when** statement allows one to attach an explicit guard to a statement.

When expr is *true*, the statement is enabled, otherwise it is disabled. A disabled statement is *blocked*—it will not be scheduled for execution. When it is enabled, it may execute by moving control to the stmt and executing the first atomic action in the stmt.

If stmt itself has a non-trivial guard, the guard of the \$when statement is effectively the conjunction of the expr and the guard of stmt.

The evaluation of expr and the first atomic action of stmt effectively occur as a single atomic action. There is no guarantee that execution of stmt will continue atomically if it contains more than one atomic action, i.e., other processes may be scheduled.

Examples:

```
sec subseteq sec
```

This will block until s is positive and then decrement s. The execution of s— is guaranteed to take place in an environment in which s is positive.

```
when (s>0) \{s--; t++\}
```

The execution of s-- must happen when s>0, but between s-- and t++, other processes may execute.

```
shen (s>0) shen (t>0) x=y*t;
```

This blocks until both x and t are positive then executes the assignment in that state. It is equivalent to

```
when (s>0 \&\& t>0) x=y*t;
```

6.3.2.2 Nondeterministic selection statement: \$choose

A \$choose statement has the form

```
$choose {
   stmt1;
   stmt2;
   ...
   default: stmt
}
```

The default clause is optional.

The guards of the statements are evaluated and among those that are *true*, one is chosen nondeterministically and executed. If none are *true* and the default clause is present, it is chosen. The default clause will only be selected if all guards are *false*. If no default clause is present and all guards are *false*, the statement blocks. Hence the implicit guard of the \$choose statement without a default clause is the disjunction of the guards of its sub-statements. The implicit guard of the \$choose statement with a default clause is *true*.

Example: this shows how to encode a "low-level" CIVL guarded transition system:

```
11: $choose {
    $when (x>0) {x--; goto 12;}
    $when (x==0) {y=1; goto 13;}
    default: {z=1; goto 14;}
}
12: $choose {
    ...
}
13: $choose {
    ...
}
```

6.3.2.3 Nondeterministic choice of integer: \$choose_int

The header civlc.cvh provides the function \$choose_int that returns an integer between 0 and the specified value in a nondeterministic way, as described in Section 10.1.1.5.

6.3.3 Iteration using domains with \$for

A CIVL-for statement has the form

```
$for (int i1, ..., in : dom) S
```

where $i1, \ldots, in$ are n identifiers, dom is an expression of type domain(n), and domain(n) is a statement. The identifiers declare n variables of integer type. Control iterates over the values of the domain, assigning the integer variables the components of the current tuple in the domain at the start of each iteration. The scope of the variables extends to the end of domain(n). The iterations takes place in the order specified by the domain, e.g., dictionary order for a Caretesian domain. Note that if a range expression can be used as dom(n) here, which will be automatically converted to one dimensional domain. For example,

```
$for (int i1, ..., in : 0 .. 10) S
```

is equivalent to

```
for (int i1, ..., in : (for int i1, ..., in)) S
```

Note that if a range expression can be used as dom here, which will be automatically converted to one dimensional domain. For example,

```
$for (int i1, ..., in : 0 .. 10) S
is equivalent to
$for (int i1, ..., in : ($domain(1)){0 .. 10}) S
```

There is a also a parallel version of this construct, \$parfor, described in 7.3.

6.4 Functions

6.4.1 Abstract function: \$abstract

An abstract function declares a function without a body, and it has the form

```
$abstract type function(list-of-parameters);
```

It is required that the function should have a non-void return type and take at least one parameter. The return value of the function is evaluated symbolically using the actual arguments of the function call.

Concurrency

7.1 Process creation and management

7.1.1 The process type: \$proc

This is a primitive object type and functions like any other primitive C type (e.g., int). An object of this type refers to a process. It can be thought of as a process ID, but it is not an integer and cannot be cast to one. It is analogous to the \$scope type for dynamic scopes.

Certain expressions take an argument of \$proc type and some return something of \$proc type. The operators == and != may be used with two arguments of type \$proc to determine whether the two arguments refer to the same process.

7.1.2 Checking if a process is defined: \$proc_defined

An object of type \$proc is initially undefined, so a use of that object would result in an error. One can check whether a \$proc object is defined using the function \$proc_defined, declared by the header civlc.cvh, as described in Section 10.1.1.7.

7.1.3 The self process constant: self

This is a constant of type \$proc. It can be used wherever an argument of type \$proc is called for. It refers to the process that is evaluating the expression containing \$self.

7.1.4 The *null* process constant: \$proc_null

This is a constant of type \$proc. It can be used wherever an argument of type \$proc is called for. It simply means that the object doesnt refer to any process.

7.1.5 Spawning a new process: \$spawn

A *spawn* expression is an expression with side-effects. It spawns a new process and returns a reference to the new process, i.e., an object of type **\$proc**. The syntax is the same as a procedure invocation with the keyword **\$spawn** inserted in front:

```
$spawn f(expr1, ..., exprn)
```

Typically the returned value is assigned to a variable, e.g.,

```
$proc p = $spawn f(i);
```

If the invoked function f returns a value, that value is simply ignored.

7.1.6 Waiting for process(es) to terminate: \$wait and \$waitall

Once the system function \$\pmait(\suaitall)\$ provided by the CIVL-C standard header civlc.cvh gets invoked, it will not return until the specified process(es) terminates(terminate), as described in Sections 10.1.1.2 and 10.1.1.2.

7.1.7 Terminating a process immediately: \$exit

Once the function **\$exit** declared in the header civlc.cvh, is called, the calling process terminates immediately, as described in Section 10.1.1.4.

7.2 Atomicity

7.2.1 Atom blocks: \$atom

This defines a number of statements to be executed as a single atomic transition. An \$atom block has the following form:

```
$atom {
    stmt1;
    stmt2;
    ...
}
```

The statements inside an **\$atom** block are to be executed as one transition. It is required that the execution of the statements in an **\$atom** block satisfy all of the following properties:

- 1. deterministic: at each step in the execution of the atom block, there must be at most one enabled statement;
- 2. nonblocking: at each step in the execution, there must be at least one enabled statement, hence, together with (1), there must be exactly one enabled statement;
- 3. finite: the execution of the atom block must terminate after a finite number of steps; and
- 4. *isolated*: there are no jumps from outside the atom block to inside the atom block, or from inside the atom block to outside of it.

Violations of the *deterministic*, *nonblocking*, or *isolated* properties will be reported either statically or dynamically. If the *finite* property is violated, the verification may just run forever.

Once the process enters an \$atom block is said to be executing atomly. The process remains executing atomly until it reaches the terminating right brace of the block. Hence executing atomly is a dynamic, not static condition. For example, the block might contain a function call which takes the process to a point in code which is not statically contained in an atom block; that process is nevertheless still executing atomly and is subject to the rules above. The process only stops

executing atomly when that function call returns and control finally reaches the right curly brace at the end of the atom block (assuming the block is not contained in another atom block).

Note: \$\suait or \$\suaitall calls are not allowed in \$\atom blocks. The rationale for this is that there is never a way to know for certain that another process has terminated (until \$\suait or \$\suaitall has returned) so there is never a way to be certain the \$\suait or \$\suaitall call will not block. If one does occur in an \$\atom block, an error will be reported statically (if it can be detected statically) or dynamically (otherwise). Note that it is not always possible to detect this statically because the \$\atom block may contain a function call, and the function may contain \$\suait or \$\suaitall calls.

7.2.2 Atomic blocks: \$atomic

The statements in an *atomic* block will be executed without other processes interleaving, to the extent possible. It has the form:

```
$atomic {
    stmt1;
    stmt2;
    ...
}
```

It is essentially a weaker form of \$atom. Unlike \$atom, there are no restrictions on the statements that can go inside an \$atomic block. A process executing an \$atomic block will try to execute the statements without interleaving with other processes, unless it becomes blocked. Unlike an \$atom, the statements in an atomic block do not necessarily execute as a single transition; they may be spread out over multiple transitions.

When no statement is enabled, the execution of the **\$atomic** block will be interrupted. At this point, other processes are allowed to execute. Eventually, if the original process becomes enabled due to the actions of other processes, it may be scheduled again, in which case it regains atomicity and continues where it left off. For example, after executing the first loop, the process executing the following code will become blocked at the first **\$wait** or **\$waitall** call:

```
$atomic {
  for (int i = 0; i < 5; i++) p[i] = $spawn foo(i);
  for (int i = 0; i < 5; i++) $wait p[i];
}</pre>
```

Other processes will then execute. Eventually, if the process being waited on terminates, the original process becomes enabled and may be scheduled, in which case it regain atomicity, increments i and proceeds to the next \$wait or \$waitall call. This is in fact a common idiom for spawning and waiting on a set of processes.

A process that enters an **\$atomic** block is said to be *executing atomically*; it remains executing atomically until it reaches the closing curly brace.

Both **\$atom** and **\$atomic** blocks can be nested arbitrarily, but **\$atom** overrides **\$atomic**: a process that is executing atomly will continue executing atomly if it encounters an **\$atomic** statement; but a process executing atomically that encounters an **\$atom** will begin executing atomly.

The atomic semantics are defined more precisely as follows: there is a single global variable called the *atomic lock*. This variable can either be null (meaning the atomic lock is "free"), or it can hold the PID of a process; that process is said to "hold" the atomic lock. Moreover, each

process contains a special integer variable, its *atomic counter*, which is initially 0. Every time a process enters an atomic block, it increments its atomic counter; every time it exits an atomic block, it decrements its counter. In order to increment its counter from 0 to 1, it must first wait for the atomic lock to become free, and then take the lock. When it decrements its counter from 1 to 0, it releases the atomic lock. When a process executing atomically becomes blocked, it releases the lock (without changing the value of its atomic counter).

7.3 Parallel loops with \$parfor

A parallel loop statement has the form

```
$parfor (int i1, ..., in : dom) S
```

The syntax is exactly the same as that for the sequential loop \$for(Section 6.3.3), only with \$parfor replacing \$for.

The semantics are as follows: when control reaches the loop, one process in spawned for each element of the domain. That process has local variables corresponding to the iteration variables, and those local variables are initialized with the components of the tuple for the element of the domain that process is assigned. Each process executes the statement S in this context. Finally, each of these processes is waited on at the end. In particular, there is an effective barrier at the end of the loop, and all the spawned processes disappear after this point.

7.4 Message-Passing

CIVL-C provides a number of additional primitives that can be used to model message-passing systems. This part of the language is built in two layers: the lower layer defines an abstract data type for representing messages; the higher layer defines an abstract data type of *communicators* for managing sets of messages being transferred among some set of processes.

7.4.1 Messages: \$message

Messages are similar to bundles, but with some additional meta-data. The *data* component of the message is the "contents" of the message and is formed and extracted much like a bundle. The meta-data consists of an integer identifier for the *source* place of the message, an integer identifier for the message *destination* place, and an integer *tag* which can be used by a process to discriminate among messages for reception. This is very similar to MPI.

The functions for creating, and extracting information from, messages are given in Section 10.1.7.1.

7.4.2 Communicators: \$gcomm and \$comm

CIVL-C defines a *global communicator* type \$gcomm and a *local communicator* type \$comm. The global communicator is an abstraction for a "communication universe" that stores buffered messages and perhaps other data. The local communicator wraps together a reference to a global communicator and an integer *place*. Most of the message-passing commands take a local communicator as an argument to specify the communication universe used for that operation and the place from which

that operation will be executed. The communication universes are isolated from one another—a message sent on one can never be received using a different communicator, for example.

The global communicator is the shared object that must be declared in a scope containing all scopes in which communication in that universe will take place. It is created by specifying the number of *places* that will comprise the communicator. A place is an address to which messages may be sent or where they may be received. There is not necessarily a one-to-one correspondence between places and processes: many processes can use the same place.

Local communicators are created (typically in some child scope of the scope in which the global communicator is declared) by specifying the gobal communicator to which the local one will be associated and the place ID. The local communicator will be used in most of the message-passing functions; it may be thought of as an ordered pair consisting of a reference to the global communicator and the integer place ID. The place ID must be in $[0, \mathtt{size} - 1]$, where \mathtt{size} is the size of the global communicator. The place ID specifies the place in the global communication universe that will be occupied by the local communicator. The local communicator handle may be used by more than one process, but all of those processes will be viewed as occupying the same place. Only one call to $\mathtt{comm_create}$ may occur for each geomm-place pair.

Both types (\$gcomm and \$comm) are handle types. When declared with a call to the corresponding creation function, they create an object in the specified scope and return a handle to that object. The object can only be accessed through the specified system functions that take this handle as an argument.

The communicator interface is given in Sections 10.1.7.2 and 10.1.7.3.

Certain restrictions are enforced on some relations between the objects involved in a communication universe.

Fix a gcomm object. This object corresponds to a single communication universe with, say, n places. At any time, there can be at most one comm object associated to a given place. If a program attempts to create a comm object with the same gcomm and place as an earlier created comm object, a runtime error will occur. In particular, there can be at most comm objects associated to the comm objects.

The relation between processes and \$comm objects is unconstrained. One process may use any number of \$comm objects. (Of course, the process must have access to handles for those \$comm objects.) Dually, a single \$comm object may be used by any number of processes; this situation arises naturally when modeling a multi-threaded MPI program.

There is no special status given to the process which creates the \$comm object of a given place. Any process which can access a handle for that \$comm object can use it to send or receive messages, regardless of whether that process was the one that created the \$comm object. However, users should be aware that verification is likely to be most efficient when variables are declared as locally as possible, so it is best to declare the \$comm object in the innermost scope possible. Figure 7.1 illustrates an effective way to do this in the context of modeling a multithreaded MPI program. In the code skeleton, each thread can access the local communicator object of its process, but not that of any other process.

7.4.3 Barriers: \$gbarrier and \$barrier

The CIVL-C header concurrency.cvh defines a *global barrier* type \$gbarrier and a *local barrier* type \$barrier. They provide an implementation of a barrier for concurrent programs.

The global barrier is a shared object that must be declared in a scope containing all scopes in which the barrier will be called. It is created by specifying the number of *places* that will comprise

```
$gcomm gcomm = $gcomm_create($here, nprocs);
void Process(int rank) {
    $comm comm = $comm_create($here, gcomm, rank);

    void Thread(int tid) {
        ...$comm_enqueue(comm, msg)...
        ...$comm_dequeue(comm, source, tag)...
}

for (int i=0; i<nthreads; i++) $spawn Thread(i);
    ...
    $comm_destroy(comm);
}

for (int i=0; i<nprocs; i++) $spawn Process(i);
    ...
$gcomm_destroy(gcomm);</pre>
```

Figure 7.1: Code skeleton for model of multithreaded MPI program showing placement of global and local communicator objects

the barrier.

Local barriers are created (typically in some child scope of the scope in which the global barrier is declared) by specifying the gobal barrier to which the local one will be associated and the place ID. The local barrier will be used in the call to the barrier; it may be thought of as an ordered pair consisting of a reference to the global barrier and the integer place ID. The place ID must be in $[0, \mathtt{size} - 1]$, where \mathtt{size} is the size of the global barrier. Only one call to $\mathtt{sbarrier_create}$ may occur for each gbarrier-place pair.

Both types (\$gbarrier and \$barrier) are handle types. When declared with a call to the corresponding creation function, they create an object in the specified scope and return a handle to that object. The object can only be accessed through the specified system functions that take this handle as an argument. The barrier interface is presented in Section 10.1.5.

Specification

8.1 Overview

Specification is the means by which one expresses what a program is supposed to do, i.e., what it means for it to be correct.

There are several specification mechanisms in CIVL-C. First, there are the default properties: these are generic properties which are checked by default in any program, and require no additional specification effort. These properties include absence of deadlocks, division by 0, illegal pointer dereferences, and out of bounds array indexes.

Many more program-specific properties can be specified using assertions. CIVL-C has a rich assertion language which extends the language of boolean-valued C expressions. Assumptions are a specification dual to assertions in that they restrict the set of executions on which the assertions are checked.

Functional equivalence is a power specification mechanism. In this approach, two programs are provided, one playing the role of the specification, the other the role of the implementation. The implementation is correct if, for all inputs x, it produces the same output as that produced by the specification on input x. In other words, the two programs define the same function; this is sometimes known as *input-output equivalence*. In order to take this approach, one must first have a way to specify what the inputs and outputs of a programs are; CIVL-C provides special keywords for this.

Procedure contracts are another powerful specification mechanisms. These typically involve specifying preconditions and postconditions for a function. The function is correct if, whenever it is called in a state satisfying the precondition, when it returns the state will satisfy the postcondition. A program is correct if all its functions satisfy their contract.

8.2 Input-output signature

8.2.1 Input type qualifier: \$input

The declaration of a variable in the root scope may include the type qualifier \$input, e.g.,

\$input int n;

This declares the variable to be an input variable, i.e., one which is considered to be an input to the program. Such a variable is initialized with an arbitrary (unconstrained) value of its type. When

using symbolic execution to verify a program, such a variable will be assigned a unique symbolic constant of its type.

In contrast, variables in the root scope which are not input variables will instead be initialized with the "undefined" value. If an undefined value is used in some way (such as in an argument to an operator), an error occurs.

In addition, input variables may only be read, never written to.

Alternatively, it is also possible to specify a particular concrete initial value for an input variable. This is done using a command line argument when verifying or running the program.

An input variable declaration may contain an initializer. The semantics are as follows: if no command line value is specified for the variable, the initializer is used to initialize the variable. If a command line value is specified, the command line value is used and the initializer is ignored.

Input (and output) variables also play a key role when determining whether two programs are functionally equivalent. Two programs are considered functionally equivalent if, whenever they are given the same inputs (i.e., corresponding **\$input** variables are initialized with the same values) they will produce the same outputs (i.e., corresponding **\$output** variables will end up with the same values at termination).

8.2.2 Output type qualifier: \$output

A variable in the root scope may be declared with this type qualifier to declare it to be an output variable. Output variables are "dual" to input variables. They may only be written to, never read. They are used primarily in functional equivalence checking.

8.3 Assertions and assumptions

8.3.1 Assertions: \$assert

The system function \$assert (provided by the civlc header) has the signature

```
void $assert(_Bool expr, ...);
```

It takes an boolean type expression and a number of optional expressions which are used to construct an error message. Note that CIVL-C boolean expressions have a richer syntax than C expressions, and may include universal or existential quantifiers (see below), and the boolean values \$true and \$false.

During verification, the assertion is checked. If it cannot be proved that it must hold, a violation is reported. If additional arguments are present, then a specific message is printed as well if the assertion is violated. These additional arguments are similar in form to those used in C's printf statement: a format string, followed by some number of arguments which are evaluated and substituted for successive codes in the format string. For example,

```
$assert(x<=B, "x-coordinate %f exceeds bound %f", x, B);</pre>
```

If x=3 and B=2, then the above assertion will be violated and CIVL would print the error message "x-coordinate 3 exceeds bound 2".

8.3.2 Assume statements: \$assume

The system function \$assume (provided by the civic header) has the signature

```
void $assume(_Bool expr);
```

During verification, the given expression is assumed to hold. If this leads to a contradiction on some execution, that execution is simply ignored. It never reports a violation, it only restricts the set of possible executions that will be explored by the verification algorithm.

Like an assertion call, an assume call can be used any place a statement is expected. In addition, an assume call can be used in file scope to place restrictions on the global variables of the programs. For example,

```
$input int B;
$input int N;
$assume(0<=N && N<=B);</pre>
```

declares N and B to be integer inputs and restricts consideration to inputs satisfying $0 \le N \le B$.

8.4 Formulas

A formula is a boolean expression that can be used in an assert statement, assume statement, procedure contract (below), or invariant. Any ordinary C boolean expression is a formula. CIVL-C provides some additional kinds of formulas, described below.

8.4.1 Implication: =>

The binary operation => represents logical implication. The expression p=>q is equivalent to (!p)||q.

8.4.2 Universal quantifier: \$forall

The universally quantified formula has the form

```
$forall { type identifier | restriction} expr
```

where type is a type name (e.g., int or double), identifier is the name of the bound variable, restriction is a boolean expression which expresses some restriction on the values that the bound variable can take, and expr is a formula. The universally quantified formula holds iff for all values assignable to the bound variable for which the restriction holds, the formula expr holds.

A variation on the construct above can be used in the special case where the bound variable is to range over a finite interval of integers. In this case the quantified formula may be written:

```
$forall { type identifier=lower .. upper } expr
```

where lower and upper are integer expressions.

8.4.3 Existential quantifier: \$exists

The syntax for existentially quantified expressions is exactly the same as for universally quantified expressions, with \$exists in place of \$forall.

8.5 Contracts

8.5.1 Procedure contracts: \$requires and \$ensures

The **\$requires** and **\$ensures** primitives are used to encode procedure contracts. There are optional elements that may occur in a procedure declaration or definition, as follows. For a function prototype:

```
T f(...)
    $requires expr;
    $ensures expr;
;

For a function definition:
    T f(...)
    $requires expr;
    $ensures expr;
    {
        ...
}
```

The value \$result may be used in post-conditions to refer to the result returned by a procedure. Status: parsed, but nothing is currently done with this information.

8.5.2 Loop invariants: \$invariant

This indicates a loop invariant. Each C loop construct has an optional invariant clause as follows:

```
while (expr) $invariant (expr) stmt
for (e1; e2; e3) $invariant (expr) stmt
do stmt while (expr) $invariant (expr);
```

The invariant encodes the claim that if expr holds upon entering the loop and the loop condition holds, then it will hold after completion of execution of the loop body. The invariant is used by certain verification techniques.

Status: parsed, but nothing is currently done with this information.

8.6 Concurrency specification

8.6.1 Remote expressions: e@x

These have the form expr@x and refer to a variable in another process, e.g., procs[i]@x. This special kind of expression is used in collective expressions, which are used to formulate collective assertions and invariants.

The expression expr must have \$proc type. The variable x must be a statically visible variable in the context in which it is occurs. When this expression is evaluated, the evaluation context will be shifted to the process referred to by expr.

Status: not implemented.

8.6.2 Collective expressions: \$collective

. These have the form

```
$collective(proc_expr, int_expr) expr
```

This is a collective expression over a set of processes. The expression proc_expr yields a pointer to the first element of an array of \$proc. The expression int_expr gives the length of that array, i.e., the number of processes. Expression expr is a boolean-valued expression; it may use remote expressions to refer to variables in the processes specified in the array. Example:

```
$proc procs[N];
...
$assert $collective(procs, N) i==procs[(pid+1)%N]@i ;
Status: not implemented.
```

Pointers and Heaps

CIVL-C supports pointers, using the same operators with the same meanings as C (&, *, pointer arithmetic). There is also a heap in every scope, and system functions to allocate and deallocate objects in the specified scope.

9.1 Memory functions: memcpy

The function memcpy is defined in the standard C library string.h and works exactly the same in CIVL: it copies data from the region pointed to by q to that pointed to by p. The signature is

void memcpy(void *p, void *q, size_t size);

9.2 Heaps, \$malloc and \$free

As mentioned above, each dynamic scope has an implicit heap on which objects can be allocated and deallocated dynamically. The CIVL-C header civlc.cvh provides the functions \$malloc and \$free for allocating and dealocating memory, repectively, as described in Section 10.1.1.8.

Libraries

10.1 Standard CIVL-C headers

CIVL-C headers have the suffix .cvh. Here is the list of standard libraries provided by CIVL:

- civlc provides types and functions that are used frequently by CIVL-C programs;
- scope provides utility functions related to dynamic scopes;
- pointer provides utility functions dealing with pointers;
- seq provides utility functions of sequences (realized as incomplete array in CIVL-C);
- concurrency provides concurrency utilities such as the barrier;
- bundle provides bundle types and methods;
- comm provides communicators and methods;

10.1.1 CIVL basics civil c.cvh

The header civlc.cvh declares four types, three macros and several functions. The types declared are size_t, \$proc, \$scope and \$int_iter. The declared macros are \$true, \$false and NULL. The functions provided in this header will be described in the following.

10.1.1.1 The \$assert and \$assume functions

The \$assert and \$assume functions have the following signatures

```
void $assert(_Bool expr, ...);
void $assume(_Bool expr);
```

Information about them could be found in Section 8.3.

10.1.1.2 The \$wait function

The **\$wait** function has signature

```
void $wait($proc p);
```

When invoked, this function will not return until the process referenced by p has terminated. Note that p can be any expression of type proc, not just a variable.

10.1.1.3 The \$waitall function

The \$waitall function has signature

```
void $waitall($proc *procs, int numProcs);
```

When invoked, this function will not return until all the numProcs processes referenced by the memory specified by procs have terminated.

10.1.1.4 The \$exit function

This function takes no arguments. It causes the calling process to terminate immediately, regardless of the state of its call stack:

```
void $exit(void);
```

10.1.1.5 The \$choose_int function

The function \$choose_int has the following signature:

```
int $choose_int(int n);
```

This function takes as input a positive integer n and nondeterministically returns an integer in the range [0, n-1].

10.1.1.6 The \$scope_defined function

The function \$scope_defined has signature

```
_Bool $scope_defined($scope s);
```

It returns true if the dynamic scope specified by **s** is defined, else it returns false.

10.1.1.7 The \$proc_defined function

The function **\$proc_defined** has signature

```
_Bool $proc_defined($proc p);
```

It returns \$trueif and only if the given object of \$proc type is defined.

10.1.1.8 The heap-related functions: \$malloc and \$free

The memory allocation function \$malloc is like C's malloc, but takes an extra scope argument:

```
void * $malloc($scope scope, int size);
```

To allocate an object, one first needs a reference to the dynamic scope to be used.

The function **\$free** is used to deallocate a heap object; it is just like C's **free**:

```
void $free(void *p);
```

An error is generated if the pointer is not one that was returned by \$malloc, or if it was already freed.

10.1.2 Scope utilities scope.cvh

The header scope.cvh declares one function: \$scope_parent, which has signature

```
$scope $scope_parent($scope s);
```

This function returns the parent dynamic scope of the dynamic scope referenced by s. If s is the root dynamic scope, it returns the undefined value of type \$scope.

10.1.3 Pointer utilities pointer.cvh

The header pointer.cvh declares functions taking pointers as the arguments for different purposes, including:

- function \$equals for equality checking;
- function \$contains for membership testing;
- function \$translate_ptr for pointer translation;
- function \$copy for copying data through pointers.

10.1.3.1 The \$equals function

The \$equals function has the signature

```
_Bool $equals(void *x, void *y);
```

This function takes two non-null pointers as input. If the two objects that the pointers refer to have the same value, then the function returns **\$true**. Otherwise, it returns **\$false**.

10.1.3.2 The \$contains function

The function \$contains has the signature

```
_Bool $contains(void *ptr1, void *ptr2);
```

This function takes two non-null pointers as input. If the object that the pointer ptr1 points to contains the object pointed to by ptr2, then the function returns \$true. Otherwise, it returns \$false. For example, given

```
int a[10];
struct foo {int x; double y} f;
struct foo b[10];

// ... initialize a, f and b
```

Here are the results of several invocations of \$contains:

- \$contains(&a, &a[3]) returns \$true, since the array a contains the cell a[3];
- \$contains(&a[2], &a[3]) returns \$false;
- \$contains(&a[2], &a[2]) returns \$true, because the relation is relexive;
- \$contains(&f, &f.y) returns \$true, since the struct f contains its field f.y;
- \$contains(&b, &b[2].x) returns \$true.

10.1.3.3 The \$translate_ptr function

The function \$translate_ptr has the signature

```
void * $translate_ptr(void *ptr, void *obj);
```

This function translates a pointer into one object (ptr) to a pointer into a different object (obj) with similar structure.

For example:

```
typedef struct node{
  int x;
  int y;
} node;
typedef struct point{
  double a;
  double b;
  double c;
}point;
node nodes[3];
point points[5];
... // initialize nodes and points
double *p = $translate_ptr(&(nodes[2].y), &points);
// after the translation, p = &(points[2].b);
```

10.1.3.4 The \$copy function

The \$copy function has the signature

```
void $copy(void *ptr, void *value_ptr);
```

It copies the value pointed to by value_ptr to the memory location specified by ptr. This function is different from memcpy only in the way that it can take pointers to (incomplete) array as the argument and copy the whole array to the other.

10.1.4 Sequence utilities seq.cvh

The header seq.cvh provides utility functions dealing with sequences. A sequence is realized as an incomplete array (i.e., an array with no extent specified) of any type T, which applies for all functions of seq.cvh. Functions declared in this header include:

- function \$seq_init for initializing sequences;
- function \$seq_length for computing the length of a sequence;
- function \$seq_insert for element insertion to a sequence;
- function \$seq_remove for element removal of a sequence.

10.1.4.1 The \$seq_init function

The \$seq_init function has the signature

```
void $seq_init(void *seq, int count, void *value);
```

Given a pointer to a sequence of type T, this function sets that sequence to be an array of length count in which every element has the same value, specified by the given pointer value. The parameter seq has the type pointer-to-incomplete-array-of-T, count has any integer type and must be nonnegative, and value has the type pointer-to-T.

10.1.4.2 The \$seq_length function

The \$seq_length function has the signature

```
int $seq_length(void *seq);
```

This function returns the length of the sequence pointed to by the pointer seq. The contract is that seq must be a pointer of a sequence of type T, i.e., seq should have the type pointer-to-incomplete-array-of-T.

10.1.4.3 The \$seq_insert function

The \$seq_insert function has the signature

```
void $seq_insert(void *seq, int index, void *values, int count);
```

Given a pointer to a sequence of type T, this function inserts **count** elements into the sequence starting at position **index**. The subsequence elements of the original sequence are shifted up, and the final length of the array will be its original length plus **count**. The values to be inserted are taken from the region specified by **values**, which has type pointer-to-T.

It is required that O<=index<=length, where length is the original length of the sequence. If index=length, this function appends the elements to the end of the array. If index=0, this inserts the elements at the beginning of the sequence. If count=0, this function is a no-op and values will never be evaluated (hence may be NULL).

10.1.4.4 The \$seq_remove function

The \$seq_remove function has the signature

```
void $seq_remove(void *seq, int index, void *values, int count);
```

This function removes count elements from the sequence of type T pointed to by seq, starting at position index.

If values is not NULL, the removed elements will be copied to the memory region beginning with values, which should have the type pointer-to-T. It is required that 0<=index<length and 0<=count<=length-index. If count=0, this function is a no-op.

10.1.5 Concurrency utilities concurrency.cvh

The header concurrency.cvh declares two types,, \$gbarrier and \$barrier, and several functions dealing with barriers, including:

- functions \$gbarrier_create and \$barrier_create for creating a new global and local barrier, repectively;
- functions \$gbarrier_destroy and \$barrier_destroy for destroying a global and local barriere, respectively;
- function \$barrier_call for a barrier synchronization request.

10.1.5.1 The \$gbarrier_create and \$barrier_create functions

The \$gbarrier_create function has the signature

```
$gbarrier_create($scope scope, int size);
```

It creates a new global object of the given size, puts it in the heap of the given dynamic scope, and returns a handle to the created \$gbarrier object.

The \$barrier_create function has the signature

```
$barrier $barrier_create($scope scope, $gbarrier gbarrier, int place);
```

It creates a local barrier that joins the specified global barrier gbarrier with the id place. The new local barrier object is stored in the heap of the given dynamic scope, and a handle to that object is returned.

10.1.5.2 The \$gbarrier_destroy and \$barrier_destroy functions

The \$gbarrier_destroy and \$barrier_destroy functions has the signatures

```
void $gbarrier_destroy($gbarrier barrier);
void $barrier_destroy($barrier barrier);
```

These functions deallocated the heap memory regions occupied by the specified **\$gbarrier** or **\$barrier** object. They should be invoked before the corresponding dynamic scope becomes unreachable. Otherwise, a memory leak error will be reported.

10.1.5.3 The \$barrier_call function

The \$barrier_call function has the signature

```
void $barrier_call($barrier barrier);
```

When this function is called, the calling process will be blocked until all other processes associated with the same global barrier referred to by the given barrier have made the barrier call.

10.1.6 Bundle type and functions bundle.cvh

The header bundle.cvh defines the type \$bundle (see Section 6.1.2) and several functions dealing with bundles:

- function \$bundle_size for computing the size of a bundle;
- function \$bundle_pack for composing a bundle from some given data;
- function \$bundle_unpack for extracting the data contained by a given bundle;
- function \$bundle_unpack_apply for extacting the data contained by a given bundle and apply some operation to them.

10.1.6.1 The \$bundle_size function

The \$bundle_size function has the signature

```
int $bundle_size($bundle b);
```

It takes a bundle and returns its size.

10.1.6.2 The \$bundle_pack function

The \$bundle_pack function has the signature

```
$bundle $bundle_pack(void *ptr, int size);
```

This function creates a bundle from the memory region specified by ptr and size, copying the data into the new bundle, and returns the new bundle.

10.1.6.3 The \$bundle_unpack function

The \$bundle_unpack function has the signature

```
void $bundle_unpack($bundle bundle, void *ptr);
```

Opposite to \$bundle_pack, this function copies the data from the given bundle into the memory region specified by ptr.

10.1.6.4 The \$bundle_unpack_apply function

The \$bundle_unpack_apply function has the signature

```
void $bundle_unpack_apply($bundle data, void *buf, int size, $operation op);
```

This function unpacks the bundle and applies the specified operation on the content of the bundle. For every binary operation defined in operation, the content of the bundle will be used as the left operand and buf will be used as the right operand. The result of the operation is stored in buf once is it is done.

10.1.7 Communicators comm.cvh

The header comm.cvh declares three types, two macros and a number of functions for communication. The two maros are \$COMM_ANY_SOURCE and \$COMM_ANY_TAG. The three types declared are \$message, \$gcomm and \$comm.

10.1.7.1 Messaging functions

The function \$message_size returns the size of a given message and has the signature

```
int $message_size($message message);
```

The function \$message_source returns the source of a given message and has the signature

```
int $message_source($message message);
```

The function \$message_dest returns the destination of a given message and has the signature

```
int $message_dest($message message);
```

The function \$message_tag returns the tag of a given message and has the signature

```
int $message_tag($message message);
```

The function \$message_pack has the signature

```
$message $message_pack(int source, int dest, int tag, void *data, int size);
```

This function creates a new message of the specified source, dest and tag, copying data from the memory region specified data and size, and returns the newly created message object.

The function \$message_unpack has the signature

```
void $message_unpack($message message, void *buf, int size);
```

This function transfers data from message the memory region specified by buf and size, reproting an error if the size of the message exceeds the specified size.

10.1.7.2 \$gcomm functions

```
/* Creates a new global communicator object and returns a handle to it.
```

- st The global communicator will have size communication places. The
- * global communicator defines a communication "universe" and encompasses
- * message buffers and all other components of the state associated to
- * message-passing. The new object will be allocated in the given scope. */
 \$gcomm \(\)\$gcomm_create(\(\)\$scope s, int size);

```
void $gcomm_destroy($gcomm gcomm); // Destroys the gcomm
```

```
_Bool $gcomm_defined($gcomm gcomm); // Is the gcomm object defined?
```

10.1.7.3 \$comm functions

```
/* Creates a new local communicator object and returns a handle to it.
* The new communicator will be affiliated with the specified global
* communicator. The new object will be allocated in the given scope. */
$comm $comm_create($scope s, $gcomm gcomm, int place);
void $comm_destroy($comm comm); // Destroys the comm
_Bool $comm_defined($comm comm); // Is the comm object defined?
/* Returns the size (number of places) in the global communicator associated
* to the given comm. */
int $comm_size($comm comm);
/* Returns the place of the local communicator. This is the same as the
* place argument used to create the local communicator. */
int $comm_place($comm comm);
/* Adds the message to the appropriate message queue in the communication
* universe specified by the comm.
                                   The source of the message must equal
* the place of the comm. */
void $comm_enqueue($comm comm, $message message);
/* Returns true iff a matching message exists in the communication universe
* specified by the comm. A message matches the arguments if the destination
 * of the message is the place of the comm, and the sources and tags match. */
_Bool $comm_probe($comm comm, int source, int tag);
/* Finds the first matching message and returns it without modifying
* the communication universe. If no matching message exists, returns a message
* with source, dest, and tag all negative. */
$message $comm_seek($comm comm, int source, int tag);
/* Finds the first matching message, removes it from the communicator,
* and returns the message */
$message $comm_dequeue($comm comm, int source, int tag);
```

10.2 C libraries

Each of the following libraries is at least partially implemented and can be included in a CIVL-C program:

• assert

void assert(_Bool expr);
 This is equivalent to an \$assert statement without error messages.

• math - double sqrt(double x); - double ceil(double x); - double exp(double x); • stdlib - size_t - void * malloc(size_t size); This is equivalent to \$malloc(\$root, size). - void free(void * ptr); This is identical to \$free(ptr). • stdbool - true This is equivalent to \$true. - false This is equivalent to \$false. • stddef - size_t - NULL • stdio - int printf(const char * restrict format, ...); • string - size_t - NULL

- void memcpy(void * restrict dst, const void * restrict src, size_t n);

Part III Semantics

CIVL Model Syntax

11.1 Notation and terminology

Let $\mathbb{B} = \{true, false\}$ (the set of boolean values). Let $\mathbb{N} = \{0, 1, 2, ...\}$ (the set of natural numbers). Given a node u in a tree, we let ancestors(u) denote the set of all ancestors of u, including u. We let ancestors(u) denote the set of all descendants of u, including u.

For any set S, let S^* denote the set of all finite sequences of elements of S. The length of a sequence $\xi \in S^*$ is denoted length(ξ).

11.2 Definition of Context

Definition 11.2.0.1. A CIVL type system is a tuple comprising the following components:

- 1. a set Type (the set of types),
- 2. a type bool \in Type (the boolean type),
- 3. a type proc \in Type (the process-reference type),
- 4. a set Var (the set of all typed variables),
- 5. a function vtype: $Var \rightarrow Type$ (which gives the type of each variable),
- 6. a set Val (the set of all values),
- 7. a function which assigns to each $t \in \mathsf{Type}$ a subset $\mathsf{Val}_t \subseteq \mathsf{Val}$ (the set of values of type t) and which satisfies $\mathsf{Val}_{\mathsf{bool}} = \mathbb{B}$ and $\mathsf{Val}_{\mathsf{proc}} = \mathbb{N}$,
- 8. a function which assigns to each $t \in \mathsf{Type}$ a value $\mathsf{default}_t \in \mathsf{Val}_t$.

The default value will be used to give an initial value to any variable. It could represent something like "an undefined value of type t" or a reasonable initial value (0 for integers, etc.), depending on the language one is modeling.

Definition 11.2.0.2. Given a CIVL type system, a *valuation* in that system is a function $\eta: \mathsf{Var} \to \mathsf{Val}$ with the property that for any $v \in \mathsf{Var}$, $\eta(v) \in \mathsf{Val}_{\mathsf{vtype}(v)}$.

Given a CIVL type system, we let Eval denote the set of all valuations in that system.

Definition 11.2.0.3. Given a CIVL type system, A CIVL expression system for that type system is a tuple comprising the following components:

- 1. a set Expr (the set of all typed expressions over Var),
- 2. a function etype: Expr \rightarrow Type (giving the type of each expression),
- 3. a function eval: Expr \times Eval \rightarrow Val (the evaluation function), satisfying
 - for any $e \in \mathsf{Expr}$ and $\eta \in \mathsf{Eval}$, $\mathsf{eval}(e, \eta) \in \mathsf{Val}_{\mathsf{etype}(e)}$,
- 4. a function which associates to any $V \subseteq \mathsf{Var}$, a subset $\mathsf{Expr}(V) \subseteq \mathsf{Expr}$ (the set of expressions which involve only variables in V) satisfying the following:
 - for any $V \subseteq \mathsf{Var}$ and $\eta, \eta' \in \mathsf{Eval}$, if $\eta(v) = \eta'(v)$ for all $v \in V$, then for any $e \in \mathsf{Expr}(V)$, $\mathsf{eval}(e, \eta) = \mathsf{eval}(e, \eta')$

Definition 11.2.0.4. A CIVL context is a CIVL type system together with a CIVL expression system for that type system.

11.3 Lexical scopes

Definition 11.3.0.5. Given a CIVL context C, a lexical scope system over C is a tuple

$$(\Sigma, root, sparent, vars)$$

consisting of

- 1. a set Σ (the set of static scopes),
- 2. a scope root $\in \Sigma$ (the root scope),
- 3. a function sparent: $\Sigma \setminus \{\text{root}\} \to \Sigma$ such that

$$\{(\mathsf{sparent}(\sigma), \sigma) \mid \sigma \in \Sigma \setminus \{\mathsf{root}\}\}$$

gives Σ the structure of a rooted tree with root root,

- 4. a function vars: $\Sigma \to 2^{\text{Var}}$ (specifying the variables declared in each scope) satisfying
 - $\sigma \neq \tau \Rightarrow \operatorname{vars}(\sigma) \cap \operatorname{vars}(\tau) = \emptyset$.

Definition 11.3.0.6. Given a CIVL context and scope $\sigma \in \Sigma$, the set of *visible variables* in σ is $\bigcup_{\sigma' \in \mathsf{ancestors}(\sigma)} \mathsf{vars}(\sigma')$.

One way this notion will be used: expressions used in a scope σ can only involve variables visible in σ .

Symbol	Section	Meaning
\blacksquare	§11.1	$\{true, false\}$
\mathbb{N}	§11.1	$\{0,1,2,\dots\}$
ancestors	§11.1	set of ancestors of node in a tree (inclusive)
descendants	$\S 11.1$	set of descendants of node in a tree (inclusive)
length	§11.1	length of a sequence
Var	$\S 11.2$	the set of all variables
bool	$\S 11.2$	the boolean type
proc	$\S 11.2$	the process reference type
Val	$\S 11.2$	the set of all values
Val_t	$\S 11.2$	values of type t
$default_t$	§11.2	default value of type t
vtype	$\S 11.2$	function $Var \rightarrow Type$ giving type of each variable
Eval	§11.2	set of all valuations on Var
Eval(V)	§12.1	set of all valuations on variables in $V \subseteq Var$
Expr	§11.2	set of typed expressions over Var
etype	§11.2	$Expr \to Type$, gives type of each expression
eval	§11.2	$Expr \times Eval \to Val$, the evaluation function
\mathcal{C}	$\S 11.2$	a CIVL context
\sum	$\S 11.3$	set of all static scopes
root	$\S 11.3$	the root scope (member of Σ)
sparent	$\S 11.3$	$\Sigma \setminus \{root\} \to \Sigma$, parent function in static scope tree
vars	$\S 11.3$	$\Sigma \to 2^{Var}$, specifies variables declared in scope
Λ	$\S 11.3$	a lexical scope system
void	§11.4	type used for function that does not return a value
Type [′]	§11.4	$Type \cup \{void\}$
${\cal F}$	§11.4	set of function symbols
fscope	§11.4	$\mathcal{F} \to \Sigma \setminus \{\text{root}\}$, gives function scope of each function
returnType	§11.4	$\mathcal{F} \to Type'$, gives return type of each function
params	$\S 11.4$	$\mathcal{F} \to Var^*$, formal parameter sequence for $f \in \mathcal{F}$
f_0	§11.4	the root function (member of \mathcal{F})
func	§11.4	$\Sigma \to \mathcal{F}$, function to which scope belongs
Loc_f	$\S 11.7$	set of locations for $f \in \mathcal{F}$
$lscope_f$	$\S 11.7$	$Loc_f \to \Sigma$, gives scope of each location for $f \in \mathcal{F}$
$start_f$	$\S 11.7$	start location for $f \in \mathcal{F}$ (member of Loc_f)
T_f	$\S 11.7$	set of guarded transitions for $f \in \mathcal{F}$

Figure 11.1: Table of Notation Used to Define CIVL Model Syntax $\,$

11.4 Functions

Fix a CIVL context \mathcal{C} and lexical scope system

$$\Lambda = (\Sigma, \mathsf{root}, \mathsf{sparent}, \mathsf{vars})$$

over \mathcal{C} .

We introduce a new type symbol void, as in C, to use as the return type for a function that does not return a value. Let $\mathsf{Type'} = \mathsf{Type} \cup \{\mathsf{void}\}.$

Definition 11.4.0.7. A function prototype for Λ is a tuple (σ, t, ξ) consisting of

- 1. a scope $\sigma \in \Sigma \setminus \{\text{root}\}\$ (the function scope),
- 2. a type $t \in \mathsf{Type}'$ (the return type),
- 3. a finite sequence $\xi = v_1 v_2 \cdots v_n \in \mathsf{vars}(\sigma)^*$ consisting of variables declared in the function scope (the *formal parameters*).

Definition 11.4.0.8. A CIVL function prototype system consists of

- 1. a set \mathcal{F} (the function symbols),
- 2. a function which assigns to each $f \in \mathcal{F}$ a function prototype, denoted

$$(fscope(f), returnType(f), params(f)),$$

and satisfying

- for any $\sigma \in \Sigma$, there is at most one $f \in \mathcal{F}$ such that $\sigma = \mathsf{fscope}(f)$, and
- 3. a root function f_0 with $\mathsf{fscope}(f_0) = \mathsf{root}$ and which is the only function with root scope.

Definition 11.4.0.9. Given a CIVL function prototype system, and function symbol $f \in \mathcal{F} \setminus \{f_0\}$, the declaration scope of f is the scope $\sigma = \mathsf{sparent}(\mathsf{fscope}(f))$. We also write f is declared in σ .

Note the root function f_0 has no declaration scope.

Just as every scope has a set of visible variables, there is also a set of visible functions:

Definition 11.4.0.10. The functions visible at scope σ are those declared in σ or an ancestor of σ .

We will see that the variables and functions visible at σ are the only variables and functions that can be referred to by statements and expressions used within σ .

Note that only certain scopes are function scopes. There can be additional scopes (intuitively corresponding to block scopes in a source program). Every scope, however, must "belong to" exactly one function. The precise definition is as follows:

Definition 11.4.0.11. Given a CIVL function prototype system, define

func:
$$\Sigma \to \mathcal{F}$$

by

$$\mathsf{func}(\sigma) = \begin{cases} f & \text{if } \sigma = \mathsf{fscope}(f) \text{ for some } f \in \mathcal{F} \\ \mathsf{func}(\mathsf{sparent}(\sigma)) & \text{otherwise.} \end{cases}$$

We say σ belongs to f when $func(\sigma) = f$.

Note that the recursion in Definition 11.4.0.11 must stop as the root scope belongs to the root function and the scopes form a tree.

11.5 Statements

Fix a CIVL function prototype system. A CIVL statement is defined to be a tuple of one of the forms described below. In each case, we give any restritions on the components of the tuple and a brief intuition on the statement's semantics. The precise semantics will be described in §12.

- 1. $\langle parassign, V_1, V_2, \psi \rangle$
 - $V_1, V_2 \subseteq \mathsf{Var}$
 - $\psi \colon V_2 \to \mathsf{Expr}(V_1)$ satisfying $\mathsf{etype}(\psi(v)) = \mathsf{vtype}(v)$ for all $v \in V_2$
 - meaning: parallel assignment, i.e., the assignment of new values to any or all of the variables in V_2 . For each variable in V_2 an expression is given which will be evaluated in the old state to compute the new value for that variable. V_1 contains all the variables that may be used in those expressions. Hence V_1 is the "read set" and V_2 is the "write set" for the parallel assignment.
- 2. $\langle assign, v, e \rangle$
 - $v \in \mathsf{Var}, \ e \in \mathsf{Expr}, \ \mathsf{etype}(e) = \mathsf{vtype}(v)$
 - meaning: simple assignment: evaluate an expression e and assign result to variable v. It is a special case of parassign but is provided for convenience.
- 3. $\langle \mathtt{call}, y, f, e_1, \dots, e_n \rangle$
 - $y \in \mathsf{Var}, f \in \mathcal{F}, e_1, \dots, e_n \in \mathsf{Expr}$
 - n = numParams(f)
 - $etype(e_i) = vtype(v_i)$, where $params(f) = v_1 \cdots v_n$
 - returnType(f) = vtype(y)
 - meaning: evaluate expressions e_1, \ldots, e_n ; push frame on call stack and move control to guarded transition system (see §11.7) for function f; when f returns, pop stack and store returned result in g
- 4. $\langle \mathtt{call}, f, e_1, \dots, e_n \rangle$
 - $f \in \mathcal{F}, e_1, \dots, e_n \in \mathsf{Expr}$
 - n = numParams(f)
 - $etype(e_i) = vtype(v_i)$, where $params(f) = v_1 \cdots v_n$
 - meaning: like above, but return type may be void or returned value could just be ignored
- 5. $\langle \mathbf{fork}, p, f, e_1, \dots, e_n \rangle$
 - $p \in \mathsf{Var}, f \in \mathcal{F}, e_1, \dots, e_n \in \mathsf{Expr}$
 - n = numParams(f)
 - $etype(e_i) = vtype(v_i)$, where $params(f) = v_1 \cdots v_n$
 - $\bullet \ \ \mathsf{returnType}(f) = \mathsf{void}$
 - $\mathsf{vtype}(p) = \mathsf{proc}$

• meaning: evaluate expressions e_1, \ldots, e_n ; create new process and invoke function f in it; return, immediately, a reference to the new process and store that reference in p

```
6. \langle \mathtt{join}, e \rangle
```

- $e \in \mathsf{Expr}$
- etype(e) = proc
- meaning: evaluate e and wait for the referenced process to terminate
- 7. $\langle \mathtt{return}, e \rangle$
 - $e \in \mathsf{Expr}$
 - meaning: evaluate e, pop the call stack and return control, along with the value, to caller
- 8. (return)
 - meaning: pop the call stack and return control to caller; only to be used in functions returning void
- 9. $\langle \mathtt{write}, e \rangle$
 - $e \in \mathsf{Expr}$
 - meaning: evaluate e and send result to output
- 10. $\langle noop \rangle$
 - meaning: does nothing
- 11. $\langle assert, e \rangle$
 - $e \in \mathsf{Expr}$, $\mathsf{vtype}(e) = \mathsf{bool}$
 - meaning: evaluate e; if result is false, stop execution and report error
- 12. $\langle assume, e \rangle$
 - $e \in \mathsf{Expr}$, $\mathsf{vtype}(e) = \mathsf{bool}$
 - meaning: assume e holds (i.e., if e does not hold, the execution sequence is not a real execution)

11.6 Remarks

The system described is sufficiently general to model pointers. There can be (one or more) pointer types and corresponding values. The parallel assignment statement can be used to model statements like C's *p=e;. In the worst case (if no information is known about where p could point), one can let $V_2 = \text{Var}$. Similarly, expressions that involve *p as a right-hand side subexpression can always take $V_1 = \text{Var}$.

Heaps can also be modeled. A heap type may be defined and a variable of that type declared. Expressions to modify and read from the heap can be defined, as can pointers into the heap.

11.7 Transition system representation of functions

Definition 11.7.0.12. Given a CIVL function prototype system and $f \in \mathcal{F}$, a guarded transition system for f is a tuple (Loc, Iscope, start, T), where

- Loc is a set (the set of *locations*),
- Iscope: Loc $\to \Sigma$ is a function which associates to each $l \in \mathsf{Loc}$ a scope Iscope(l) $\in \Sigma$ belonging to f,
- $start \in Loc \text{ (the } start \ location),$
- T is a set of guarded transitions, each of which has the form $\langle l, g, s, l' \rangle$, where
 - $-l, l' \in Loc$ (the source and target locations)
 - $-g \in \mathsf{Expr}(V)$, where V is the set of variables visible at $\mathsf{lscope}(l)$, and $\mathsf{etype}(g) = \mathsf{bool}(g)$ is called the guard,
 - -s is a statment all of whose constituent variables, expressions, and function symbols are visible at $\mathsf{lscope}(l)$.

Furthermore, if the guarded transition system contains a statement of the form $\langle \text{return} \rangle$ then returnType(f) = void. If it contains a statement of the form $\langle \text{return}, e \rangle$ then

$$etype(e) = returnType(f)$$
.

Definition 11.7.0.13. Given a CIVL prototype system, a CIVL model M for that system assigns, to each $f \in \mathcal{F}$, a guarded transition system

$$(\mathsf{Loc}_f, \mathsf{Iscope}_f, \mathsf{start}_f, T_f)$$

for f. Moreover, if $f \neq f'$ then $\mathsf{Loc}_f \cap \mathsf{Loc}_{f'} = \emptyset$.

Definition 11.7.0.14. Given a CIVL model M, let $\mathsf{Loc} = \bigcup_{f \in \mathcal{F}} \mathsf{Loc}_f$.

CIVL Model Semantics

12.1 State

Fix a CIVL model M. Recall that a valuation is a type-respecting function from Var to Val. Given a subset $V \subseteq Var$ of variables, we define a valuation on V to be a type-respecting function from V to Val. Let Eval(V) denote the set of all valuations on V. Note that Eval(Var) = Eval.

Definition 12.1.0.15. A state of a CIVL model M is a tuple

$$s = (\Delta, \mathsf{droot}, \mathsf{dparent}, \mathsf{static}, \mathsf{deval}, P, \mathsf{stack}),$$

where

- 1. Δ is a finite set (the set of *dynamic scopes* in s),
- 2. $droot \in \Delta$ (the root dynamic scope),
- 3. dparent: $\Delta \setminus \{droot\} \to \Delta$ is a function such that the set

$$\{(\mathsf{dparent}(\delta), \delta) \mid \delta \in \Delta \setminus \{\mathsf{droot}\}\}$$

gives Δ the structure of a rooted tree with root droot,

- 4. static: $\Delta \to \Sigma$,
- 5. $\mathsf{static}(\mathsf{droot}) = \mathsf{root}$ and droot is the only $\delta \in \Delta$ satisfying $\mathsf{static}(\delta) = \mathsf{root}$,
- 6. $\mathsf{static}(\mathsf{dparent}(\delta)) = \mathsf{sparent}(\mathsf{static}(\delta)) \text{ for any } \delta \in \Delta,$
- 7. deval is a function that assigns to each $\delta \in \Delta$ a valuation $\operatorname{deval}(\delta) \in \operatorname{Eval}(\operatorname{vars}(\operatorname{static}(\delta)))$,
- 8. P (the set of process IDs in s) is a finite subset of Val_{proc} , and
- 9. stack: $P \rightarrow \mathsf{Frame}^*$, where

$$\mathsf{Frame} = \{(\delta, l) \in \Delta \times \mathsf{Loc} \mid \mathsf{Iscope}(l) = \mathsf{static}(\delta)\}.$$

Let State denote the set of all states of M.

Remarks:

- 1. We will also refer to dynamic scopes as dyscopes.
- 2. The elements of Δ contain no intrinsic information. Instead, all of the information concerning dyscopes is encoded in the functions that take elements of Δ as arguments. Hence we might just as well call the elements of Δ "dynamic scope IDs" (just as we call the elements of P "process IDs"). One could use natural numbers for the dyscopes, just as one does for processes.
- 3. The reason for using some form of ID for dyscopes and processes, rather than just incorporating the data in the appropriate part of the state, is that both kinds of objects may be shared. There can be several components of the state that refer to the same dyscope d: e.g., d could have several children, each of which has a parent reference to d, as well as a reference from a frame. A process can be referred to by any number of variables of type proc.
- 4. If $\sigma = \text{static}(\delta)$, we say that δ is an instance of σ or σ is the static scope associated to δ . In general, a static scope can have any number (including 0) of dynamic instances. The exception is the root scope root, which must have exactly one instance (droot).
- 5. A valuation $deval(\delta)$ assigns a value to each variable in the static scope associated to δ . The function deval thereby encodes the value of all variables "in scope" in state s.
- 6. The sequence $\mathsf{stack}(p)$ encodes the state of the call stack of process p. The elements of the sequence are called *activation frames*. The first frame in the sequence, i.e., the frame in position 0, is the bottom of the stack; the last frame is the top of the stack.
- 7. Each frame refers to a dyscope δ and a location in the static scope associated to δ .

Definition 12.1.0.16. A dyscope $\delta \in \Delta$ is a function node if $\mathsf{static}(\delta)$ is the function scope of some function.

Definition 12.1.0.17. Given any $\delta \in \Delta$, $\mathsf{fnode}(\delta) \in \Delta$ is defined as follows: if δ is a function node, then $\mathsf{fnode}(\delta) = \delta$, else $\mathsf{fnode}(\delta) = \mathsf{fnode}(\mathsf{dparent}(\delta))$. We call $\mathsf{fnode}(\delta)$ the function node associated to δ .

The relation $\{(\delta, \delta') \mid \mathsf{fnode}(\delta) = \mathsf{fnode}(\delta')\}$ is an equivalence relation \sim on Δ . Let $\bar{\Delta} = \Delta / \sim$ and write $[\delta]$ for the equivalence class containing δ .

The set of activation frames in a state s may be identified with the set

$$AF(s) = \bigcup_{p \in P} \{p\} \times \{0, \dots, \mathsf{length}(\mathsf{stack}(p)) - 1\}$$

Namely, (p, i) corresponds to the i^{th} entry in the call stack $\mathsf{stack}(p)$ (where the elements of the stacks are indexed from 0).

Define $\Psi \colon AF(s) \to \bar{\Delta}$ as follows: given (p,i), let (δ,l) be the corresponding frame; set $\Psi(p,i) = [\delta]$.

12.2 Jump protocol

When control moves from one location to another within a function's transition system, dyscopes may be added, because you can jump out of scope nests and into new scope nests. The motivating

```
1 procedure jump(s: State, p: Val_{proc}, l': Loc): State is
           let (\Delta, droot, dparent, static, deval, P, stack) = s;
           let \delta be the dyscope of the last frame on \mathsf{stack}(p);
  3
           let \sigma = \operatorname{static}(\delta);
  4
           let \sigma' = \mathsf{Iscope}(l');
  5
           let \sigma_{\mathsf{lub}} be the least upper bound of \sigma and \sigma' in the tree \Sigma;
  6
           let m be the minimum integer such that sparent<sup>m</sup>(\sigma) = \sigma_{\text{lub}};
  7
           let \delta_{\mathsf{lub}} = \mathsf{dparent}^m(\delta);
  8
           let n be the minimum integer such that sparent<sup>n</sup>(\sigma') = \sigma_{\text{lub}};
  9
           let \delta_0, \ldots, \delta_{n-1} be n distinct objects not in \Delta;
10
           let \Delta' = \Delta \cup \{\delta_0, \dots, \delta_{n-1}\};
11
           define dparent': \Delta' \setminus \{droot\} \rightarrow \Delta' by
12
         \begin{aligned} \operatorname{dparent}'(\delta') &= \begin{cases} \operatorname{dparent}(\delta') & \text{if } \delta' \in \Delta \\ \delta_{i+1} & \text{if } \delta' = \delta_i \text{ for some } 0 \leq i < n-1; \\ \delta_{\text{lub}} & \text{if } n \geq 1 \text{ and } \delta' = \delta_{n-1} \end{cases} \\ \operatorname{define static}' &: \Delta' \to \Sigma \text{ by static}'(\delta') &= \begin{cases} \operatorname{static}(\delta') & \text{if } \delta' \in \Delta \\ \operatorname{sparent}^i(\sigma') & \text{if } \delta' = \delta_i \text{ for some } 0 \leq i < n; \end{cases} \\ \operatorname{for } \delta' \in \Delta' \text{ and } v \in \operatorname{vars}(\operatorname{static}(\delta')), \text{ let } \operatorname{deval}'(\delta')(v) &= \begin{cases} \operatorname{deval}(\delta')(v) & \text{if } \delta' \in \Delta \\ \operatorname{default}_t & \text{otherwise}; \end{cases} \end{aligned}
13
14
           define stack' to be the same as stack except that the last frame on stack'(p) is replaced with
15
           (\delta_0, l') if n \ge 1, or with (\delta_{\mathsf{lub}}, l') if n = 0;
           let s' = (\Delta', droot, dparent', static', deval', P, stack');
16
           return the result of removing all unreachable dyscopes from s';
17
```

Figure 12.1: Jump protocol: how the state changes when control moves to a new location within a function. The procedure may only be called if $\mathsf{func}(\sigma) = \mathsf{func}(\sigma')$, i.e., the jump is contained within one function.

idea is that you have to move up the dyscope tree every time you move past a right curly brace (i.e., leave a scope) and then push on a new scope for each left curly brace you move past. So there is a sequence of upward moves followed by a sequence of pushes to get to the new location. (And either or both sequences could be empty.) At the end, if any dyscopes become unreachable, they are removed from the state.

Note however, that we do not assume that scopes are associated to locations in a nice lexical pattern (or any pattern at all). The protocol described here works for any arbitrary assignment of scopes to locations.

The precise protocol is described in Figure 12.1. The algorithm shown there takes as input a well-formed state, a process ID, and a location l' for the function that p is currently in. Say the current dyscope for p is δ , and l' is in static scope σ' . Let $\sigma = \operatorname{static}(\delta)$. Hence the current static scope is σ and the new static scope will be σ' .

First, you have to find the least upper bound σ_{lub} of σ and σ' in the static scope tree. (Hence σ_{lub} is a common ancestor of σ and σ' , and if σ'' is any common ancestor of σ and σ' then σ'' is an ancestor or equal to σ_{lub} .) Note that the least upper bound must exist since the function scope is a common ancestor of σ and σ' . There is a chain of static scopes from σ up to σ_{lub} and a corresponding chain δ , $\mathsf{dparent}^m(\delta), \ldots, \mathsf{dparent}^m(\delta)$ in the dynamic scope tree. Let $\delta_{\mathsf{lub}} = \mathsf{dparent}^m(\delta)$. This will

become the least upper bound of δ and the new dynamic scope corresponding to σ' that will be added to the state.

Next you add new dyscopes corresponding to the chain of static scopes leading from σ_{lub} down to σ' . The variables in the new scopes are assigned the default values for their respective types. The dparent, static, and deval maps are adjusted accordingly. Finally, the stack is modified by replacing the last activation frame with a frame referring to the (possibly) new dynamic scope and new location l'.

This protocol is executed every time control moves from one location to another.

Note that in CIVL all jumps stay within a function. There is no way to jump from one function to another (without returning).

A small variation is the protocol for moving to the start location of a function when the function is first pushed on the stack. Since the start location is not necessarily in the function scope (it may be a proper descendant of that scope), you have to execute the second half of the protocol to push a sequence of scopes from the function scope to the scope of the start location.

12.3 Initial State

The *initial state* for M is obtained by creating one process (let $P = \{0\}$) and having it call the root function f_0 . Hence start with the state s in which $P = \{0\}, \ldots$ The initial state is $\mathsf{jump}(s, 0, \mathsf{start}_{f_0})$.

12.4 Transitions

The transitions follow the usual "interleaving" semantics. Given a state σ , one defines the set of enabled transitions in σ as follows. Let $p \in P$. Look at the last frame (d, l) of $\mathsf{stack}(p)$ (i.e., the top of the call stack), assuming the stack is nonempty. Look at all guarded transitions emanating from l. For each such transition, evaluate the guard using the valuation formed by taking the union of the valuations of all ancestors of d (including d). In other words, follow the standard "lexical scoping" protocol to determine the value of any variable that could occur at this point. Those transitions whose guard evaluates to true are enabled.

For each enabled transition, a new state is generated by executing the transition's statement. For the most part, the semantics are obvious, but there are a few details that are a bit subtle.

12.5 Calls and Spawns

Both calls and forks of a function f entail the creation of a new frame. First, a new dyscope d corresponding to $\mathsf{fscope}(f)$ is created. To find out where to stick that new scope in the dynamic scope tree, proceed as follows: begin in the dyscope for the process invoking the fork or call and start moving up its parent sequence until you reach the first dyscope d' whose associated static scope is the defining scope of f. (You must reach such a scope, or else f would not be visible, and the model would have a syntax error!) Insert d right under d', i.e., $\mathsf{dparent}(d) = d'$. This preserves the required correspondence between static scopes and dyscopes. Now you move to the start location, using the jump protocol, which may involve the creation of additional dyscopes under d. The new frame references the last dynamic scope you created, and the location is the start location of f. Variables are given their initial values in all the newly created dyscopes (however that is done).

All of that is the same whether the statement is a fork or call. The only difference is what happens next: for a call, the new frame is pushed onto the calling process' call stack. For a fork, a new process is "created", i.e., you pick a natural number not in P and add it to P, and push the frame onto the new stack. To be totally deterministic, you could pick the least natural number not in P.

12.6 Garbage collection

In a state s, a dyscope is unreachable if there is no path from a frame in a call stack to that dyscope (following the **dparent** edges). You can remove all unreachable dyscopes.

If a process has terminated (has empty stack) and there are no references to that process in the state, you can just remove the process from the state.

In any state, you can renumber the processes (and update the references accordingly) however you want, to get rid of gaps, put them in a canonic order, etc.

Part IV Tools

Tool Overview

13.1 Symbolic execution

The tools currently in the CIVL tool kit all use *symbolic execution*. This is a technique in which variables are assigned symbolic rather than concrete values. In particular, input variables are assigned unique *symbolic constants*, which are symbols such as X, Y, and so on. Operations produce symbolic expressions in those symbols, such as (X + Y)/2.

13.2 Commands

Current tools allow one to run a CIVL program using random choice to resolve nondeterministic choices; verify a program using model checking to explore all states of the program; and replay a trace if an error is found. There are also commands to show the results just of preprocessing or parsing a file; as these are basically sub-tasks of the other tasks, they are used mainly for debugging. Each tool is launched from the command line by typing "civl cmd ...", where cmd is one of

- help: print usage information
- run: run the program using random simulation
- verify: verify program
- replay : replay trace for program
- parse : show result of preprocessing and parsing file
- preprocess: show result of preprocessing file only.

The additional arguments and options are described below and are also shown by the help command. A number of properties are checked when running or verifying a CIVL program. These include the following:

- absence of deadlocks
- absence of assertion violations
- absence of division or modulus with denominator 0

- absence of illegal pointer dereferences
- absence of out-of-bounds array indexes
- absence of invalid casts
- every object is defined (i.e., initialized) before it is used.

13.3 Options

The following command line options are available:

```
-debug or -debug=boolean (default: false)
  debug mode: print very detailed information
-echo or -echo=boolean (default: false)
  print the command line
-enablePrintf or -enablePrintf=boolean (default: true)
  enable printf function
-errorBound=integer (default: 1)
  stop after finding this many errors
-guided or -guided=boolean (default: false)
  user guided simulation; applies only to run, ignored for all other commands
-id=integer (default: 0)
  ID number of trace to replay
-input key=value
  initialize input variable key to value
-maxdepth=integer (default: 2147483647)
  bound on search depth
-min or -min=boolean (default: false)
  search for minimal counterexample
-por=string (default: std)
  partial order reduction (por) choices: std (standard por) or scp (scoped por)
-random or -random=boolean (default: varies)
  select enabled transitions randomly; default for run, ignored for all other commands
-saveStates or -saveStates=boolean (default: true)
  save states during depth-first search
-seed=string (default: none)
  set the random seed; applies only to run
-showAmpleSet or -showAmpleSet=boolean (default: false)
  print the ample set of each state
```

```
-showModel or -showModel=boolean (default: false)
  print the model
-showProverQueries or -showProverQueries=boolean (default: false)
  print theorem prover queries only
-showQueries or -showQueries=boolean (default: false)
  print all queries
-showSavedStates or -showSavedStates=boolean (default: false)
  print saved states only
-showStates or -showStates=boolean (default: false)
  print all states
-showTransitions or -showTransitions=boolean (default: false)
  print transitions
-simplify or -simplify=boolean (default: true)
  simplify states?
-solve or -solve=boolean (default: false)
  try to solve for concrete counterexample
-sysIncludePath=string (default: )
  set the system include path
-trace=string (default: )
  filename of trace to replay
-userIncludePath=string (default: )
  set the user include path
-verbose or -verbose=boolean (default: false)
  verbose mode
```

13.4 Errors

When a property violation occurs, either in *verification* or *run* mode, a brief report is written to the screen. In addition, a report may be *logged* in the directory CIVLREP.

The *error bound* parameter determines how many errors can be encountered before a search terminates. By default, the error bound is 1, meaning a search will stop as soon as the first error is found. The error bound can be set to a higher number on the command line using option *errorBound*.

When the error bound is greater than one, the CIVL verifier continues searching after the first error is discovered. It first attempts to "recover" from the error by adding to the path condition a clause which guarantees that the error cannot happen. For example, if the error was caused by a possible division by zero, x/y, where y is an unconstrained real symbolic constant, CIVL will add to the path condition the predicate $y \neq 0$, and continue the search. In some cases, CIVL determines that the modified path condition is unsatisfiable, in which case the search will back-track in the usual symbolic execution way.

In addition to the printed reports, errors are logged. However, CIVL follows a protocol aimed at limiting the number of reports of errors which are essentially the same. This protocol uses a simple equivalence relation on the set of errors. Two erroneous states are considered equivalent if the errors are of the same *kind* (deadlock, division by zero, illegal pointer dereference, etc.) and every process is at the same location in both states. When an error is encountered, CIVL first checks to see if an earlier equivalent errors exists in the log. If so, the lengths of the traces leading to the two error states are compared. If the new trace is shorter, the old log entry is replaced with the new one. In this way, only the shortest representative error trace for each equivalence class of errors is recorded in the log.

A log entry actually entails two things: first, a plain text entry similar to the one printed to the screen is made in a log file in CIVLREP. The name of this file is usually of the form $root_log.txt$, where root is the root of the original file name, i.e., the substring of the file name that ends just before the first '.'. For example, if the file name is diningBad_cvl, the log file will be named diningBad_log.txt. This is a plain text, human-readable file which summarizes the results of the verification run.

In addition, each saved trace is stored in a separate file in CIVLREP. The names of these files have the form $root_id.trace$, where id is the error ID (reported when the error is printed and logged). This file is not intended to be human-readable. It contains a compressed representation of the trace, including all of the options and parameter values and choices made a nondeterministic points. This file is used by CIVL when replaying an error trace.

As mentioned above, the CIVL replay command is used to play an earlier-saved error trace. When more than one trace has been saved, the -id command line option can be used to specify which one to play. (The default *id* is 0).

Interpreting the Output

14.1 Transitions

Transitions are printed during trace replay, in the course of a run, or during verification if option show Transitions is selected. A typical transition is printed as follows:

```
State 6, proc 0:

44->49: LOOP_FALSE_BRANCH at f0:36.18-23 "i < n";

49->RET: return (init) at f0:37.0-1 "}";

7->8: i = 0 at f0:42.7-16 "int i = 0";

--> State 74
```

This means that the transition begins executing from the state with ID 6, and it is executed by the process with PID 0. The transition is executed in a sequence of atomic steps; in this case there the transition consists of three steps.

Process 0 begins at location 44; this is a static location in the program graph of a function in the CIVL model. Details about the locations can be seen by printing the CIVL model. In executing the first step, control moves from location 44 to location 49. This first step is an edge in the program graph corresponding to the *false* branch of a loop condition, i.e., the branch that exits the loop.

The remainder of the line describing the step specifies the part of the original source code corresponding to this step. The source code fragment can be found in file f0. To save space and avoid constantly repeating long paths, all the source files involved in a program are printed once and assigned keys such as f0, f1, etc. The legend is printed out once at the beginning of the run; in this case it is simply the following:

```
File name list:
f0 : dining.cvl
```

The source code fragment begins on character 18 of line 36 of f0, and extends to character 23 of that line. This range is inclusive on the left and exclusive on the right, so the total number of characters in this range is 23 - 18 = 5. The five characters from the source code are printed next inside double quotes. For longer ranges, this excerpt will be abbreviated using an elipsis.

The second step executes a *return* statement, which results in popping the top activation frame from process 0's call stack. The function returning is init. Since the program counter for that frame disappears with the execution of this step, there is no final value for its new location; this is signified using the pseudo-location RET.

```
State 7
| Path condition
| | 0 <= SIZEOF(dynamicType<146>)+-1
| Dynamic scopes
| | dyscope d0 (id=0, parent=d0, static=0)
| | | variables
| | | | __atomic_lock_var = process<-1>
| | dyscope d1 (id=1, parent=d0, static=4)
| \ | \ | reachers = \{0\}
| | | variables
| \ | \ | \ | \ |_heap = \frac{A[1][]}{H_pos1v0i010[0:=A<(H_pos1v0i010[0].0)[0:=1, 1:=2, 2:=3],2>]>>
| \ | \ | \ | \ a = \&heap0bject < d1,0,0 > [0]
| \ | \ | \ | \ b = \&heapObject < d1,0,0 > [0].a[2]
| Process states
| | process p0 (id=0)
| | | atomicCount=0
| | | call stack
| | | Frame[function=_CIVL_system, location=14, f0:25.2-9 "$assert", dyscope=d1]
```

Figure 14.1: Complete print-out of a state

In the new top frame, control is at location 7, and an assignment statement is executed, moving control to location 8. With this last step, the transition ends at State 74.

Between transitions, processes can be renumbered. Hence a process with PID 0 in one state, may have a different PID in another state. The same is true for dynamic scope IDs. Within a single transition, however, these numbers will not change.

14.2 States

States are printed typically when a property is violated, at the initial or final points of a trace replay, or if the option showStates, showSavedStates, verbose, or debug is selected.

A complete print-out of a state can be seen in Figure 14.1. The state is presented in hierarchical way. At the top-most level of this hierarchy, there are 3 main parts to the state:

- 1. the *path condition*, i.e., the boolean-valued symbolic expression used in symbolic execution to keep track of all conditions on the input symbols which must hold in order for the current path to have been followed;
- 2. the *dynamic scopes*, and
- 3. the process states.

The dynamic scopes are numbered starting from 0. This numbering is arbitrary and is invisible to the program, i.e., there is no way for the program to obtain its dynamic scope ID. This allows the verifier to renumber dynamic scopes at will in order to transform a state into an equivalence canonical form.

The print-out of each dynamic scope specifies the ID of the dyscope's parent in the dyscope tree. (The root dyscope shows -1 for the parent.) This specifies the complete tree structure of the dyscopes. Each dyscope is an instance of some static scope; the representation also shows the ID of this static scope.

The next line in the representation of the dyscope shows a set of *reachers*. These are the PIDs of the processes that can *reach* this dyscope. A process can reach a dyscope if there is path in the dyscope tree that starts from a dyscope referenced by a frame on the process' call stack and follows the parent edges in the tree.

The *variables* section of the dyscope representation consists of one line for each variable in the static scope corresponding to the dyscope. There are also special hidden variables, such as the heap. In each case, the value assigned to the variable is shown. A value of NULL indicates that the variable is currently undefined. The format for the value of a pointer depends on the type of object being referenced, as follows:

- A variable: &variable <dyscope name>
- An element of an array: & array < dyscope name > [index]
- A struct field: &variable <dyscope name>. field
- A heap cell: variable <dyscope name, malloc ID, malloc call number>

The process states section consists of one sub-section for each process currently in the state. Like the dynamic scopes, the processes are numbered in some arbitrary way. For each process, the value of the *atomic count* is given. This is the nesting depth of the atomic blocks in which the process is currently located, i.e., the number of times the process has entered an atomic block without exiting the block.

The call stack of the process lists the activation frames on the stack from top to bottom. The frame at the top correspond to the function currently executing in that process. The name of the function, the value of the program counter (location), and the source code for that location, and the dyscope ID for the frame are shown.

14.3 Property Violations

As described in Section 13.4, an error report is printed whenever CIVL encounters an error. A typical error report appears as follows:

```
Error 0 encountered at depth 21:
CIVL execution error (kind: DEADLOCK, certainty: PROVEABLE)
A deadlock is possible:
Path condition: true
Enabling predicate: false
ProcessState 0: terminated
ProcessState 1: at location 25, f0:21.30-42 "forks[right]"
Enabling predicate: false
ProcessState 2: at location 25, f0:21.30-42 "forks[right]"
Enabling predicate: false
at f0:21.30-42 "forks[right]".
```

The report begins with "Error 0". The errors are numbered in the order they are discovered in this search; this indicates that this is the first (0th) error encountered. The depth refers to the length of the depth-first search stack when the error was encountered. In this case, the depth was 21, meaning that the trace leading to the erroneous state is a sequence of 21 states and 20 transitions.

The errors are categorized by *kind*. The error kinds include *deadlock*, indicating that it is possible no transition is enabled in the state; *assertion violation*, indicating an assertion may fail in the state; *division by zero*; and *out of bounds*, indicating an array index may be out of bounds, among many more.

In addition to the brief report shown above, most error reports also include a complete print-out of the state at which the error occurred. They will also include additional information specific to the kind of error. For example, the deadlock error report shown above includes the following information:

- the value of the path condition;
- the *enabling predicate*, which is the disjunction of the guards associated to all transitions departing from the current state. This is the predicate that CIVL has found to possibly be unsatisfiable under the context of the path condition; and
- for each process, the current location of the process and the enabling predicate for that process, i.e., the disjunction of the guards associated to all transitions departing from the current state in that process (CIVL has found that all of these may be unsatisfiable).

Errors are also categorized as to their *certainty*. CIVL is *conservative*, meaning that if it not sure a property holds in a state, it will report it. This means that it may sometimes raise *false alarms*, i.e., report a possible error even when none exists. The certainty measures how certain CIVL is that the error is real. The certainty levels, from most to least certain, are as follows:

- 1. concrete: this indicates that CIVL has actually found concrete values for all input variables that are guaranteed to drive the execution along the current trace and result in the error;
- 2. proveable: this indicates that a theorem prover (either the external one or CIVL's builtin prover) has determined that the error is feasible, which includes proving that the path condition is satisfiable; however, it has not necessarily found concrete values for the inputs;
- 3. *maybe*: this indicates the prover is not sure whether this is an error; this could be due to the incompleteness of the decision procedure, or it could be a real error;
- 4. none: probably an internal CIVL error: the theorem prover has not said anything.

14.4 Statistics

- validCalls: the number of calls to the CIVL valid method, used to determine if a first-order formula is valid under a given first-order context. Some of these queries are resolved quickly by CIVL; when CIVL cannot resolve the query itself, it calls a separate theorem prover (CVC3)
- proverCalls: the number of calls to the separate theorem prover's valid method
- memory: the total amount of memory, in bytes, consumed by the Java virtual machine at the end of the search/run.

- time: the total time, in seconds, used to perform the CIVL operation
- maxProcs: the maximum process count achieved, over all states encountered in the search/run
- statesInstantiated: the number of state objects instantiated during the course of the verification/run
- statesSaved: the number of states saved in the course of a search
- statesSeen: the number of states pushed onto the depth-first search stack in the course of the search; note that "intermediate states" created in the process of executing a transition are not pushed onto the stack, only the final state resulting from the transition is pushed
- statesMatched: the number of times a state encountered in the depth-first search was found to match a saved state seen earlier in the search
- steps: the total number of primitive steps executed during the verification/run. A step is the smallest, atomic, unit of execution; each transition is composed of one or more steps. This number is a good measure for the total amount of "work" carried out by CIVL
- transitions: the total number of transitions executed during the verification/run. A transition is a coarser unit of execution; each transition consists of one or more steps executed from a single process, resulting in a state which is then pushed onto the DFS stack.

Emacs mode

A CIVL-C mode for the emacs text editor is available in directory emacs in the CIVL distribution. This provides syntax highlighting and automatic indentation for CIVL-C programs.

To install this mode:

- 1. Copy file civl-syntax.el to ~/.emacs.d/lisp or another favorite location
- 2. Include that path in your load path in .emacs:

```
(add-to-list 'load-path "~/.emacs.d/lisp")
```

3. Add the following lines to your ~/.emacs file:

```
(require 'civl-syntax)
(civl-syntax)
```

We are grateful to William Killian of the University of Delaware for writing this emacs module.

Bibliography

- [1] Khronos Group. OpenCL: The open standard for parallel programming of heterogeneous systems. https://www.khronos.org/opencl/.
- [2] MESSAGE PASSING INTERFACE FORUM. MPI: A message-passing interface standard, version 3.0. http://www.mpi-forum.org/docs/docs.html, Sept. 2012.
- [3] NVIDIA. CUDA C Programming Guide Version 5.0. http://docs.nvidia.com/cuda/cuda-c-programming-guide/. accessed March 3, 2014.
- [4] OPENMP ARCHITECTURE REVIEW BOARD. OpenMP API Specification for Parallel Programming. http://openmp.org/wp/. accessed Feb. 8, 2014.