

# Fundamentals of Radar Signal Processing

- ✓ State-of-the-art Fourier analysis techniques
- ✓ Target and interference models
- ✓ Synthetic aperture imaging
- ✓ Adaptive array processing

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