

# Compiler Design

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- ▶ Values of this attributes are evaluated by semantic rules associated with the production rules.
- ▶ Evaluation of these semantic rules:
  - ▶ may generate intermediate code.
  - ▶ may put information into the symbol table.
  - ▶ may perform type checking.
- ▶ An attribute may hold almost anything.
  - ▶ a string, a number, a memory location, a complex record

## Syntax Directed Definitions and Translation schemes

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- ▶ Translation schemes.

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- ▶ hide many implementation details such as order of evaluation of semantic actions.
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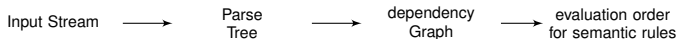
### Translation schemes:

- ▶ indicate the order of evaluation of semantic actions associated with a production rule.

## Syntax Directed Translation

Conceptually with both Syntax Directed Translation and Translation Scheme

- ▶ Parse the input token stream.
- ▶ Build the parse tree.
- ▶ Traverse the tree to evaluate the semantic rules at the parse tree nodes.





## Syntax Directed Definitions

- ▶ A syntax directed definition is a generalization of Context Free Grammar in which:
  - ▶ Each grammar symbol is associated with a set of attribute.
  - ▶ This set of attributes can be classified into two:
    - ▶ Synthesized Attributes.
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  - ▶ Each production rule is associated with a set of semantic rules.
- ▶ The value of an attribute at a parse tree node is defined by the semantic rule associated with a production at that node.
- ▶ The value of a **Synthesized Attribute** at a node is computed from the values of attributes at the children in that node of the parse tree.
- ▶ The value of a **Inherited Attribute** at a node is computed from the values of attributes at the sibling and parents in that node of the parse tree.

## Syntax Directed Definitions

Examples:

- ▶ Synthesized Attributes:

$$E \rightarrow E_1 + E_2 \quad \{E.val = E_1.val + E_2.val\}$$

- ▶ Inherited Attributes:

$$A \rightarrow XYZ \quad \{Y.val = 2 * A.val\}$$

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- ▶ Semantic rules setup and dependencies between attributes which can be represented by a dependency graph.
- ▶ Dependency graph determines the evaluation order of these semantic rules.
- ▶ Evaluation of a semantic rule defines the value of an attribute. A semantic rule may also have some side effects such as printing a value.

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  - ▶ determined by the semantic rules.

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- ▶ Values of attributes in nodes of annotated parse tree are either :
  - ▶ initialized to constant values or by the lexical analyzer.
  - ▶ determined by the semantic rules.
- ▶ The process of computing the attributes values at the nodes is called **annotating** or **decorating** of the parse tree.
- ▶ The order of these computations depends on the **dependency graph** induced by the semantic rules.

## Syntax-Directed Definition

In a Syntax-Directed Definition, each production  $A \rightarrow \alpha$  is associated with a set of semantic rules of the form

$$b = f(c_1, c_2, c_3, \dots, c_k)$$

where  $f$  is a function and  $b$  can be one of the following:

- ▶  $b$  is a **synthesized attribute** of  $A$  and  $c_1, c_2, c_3, \dots, c_k$  are attributes of the grammar symbols in  $\alpha$ , or
- ▶  $b$  is an **inherited attribute** of one of the grammar symbols on the right side of the production  $A \rightarrow \alpha$  and  $c_1, c_2, c_3, \dots, c_k$  are attributes of the grammar symbols in  $\{A, \alpha\}$ .



## Example with Synthesized attributes

- ▶ Grammar Symbols:  $L, E, T, F, n, +, *, (, ), digit$
- ▶ Non-Terminal :  $L, E, T, F$  have an attribute called *val*.
- ▶ Terminal *digit* have an attribute called *lexval*.
- ▶ The value for *lexval* is provided by the lexical analyser.

Table: Syntax-directed Definition

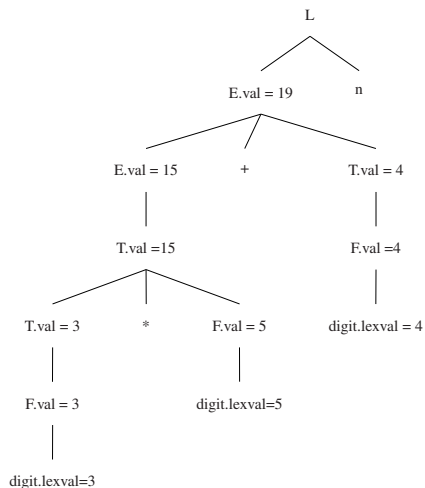
Productions	Semantic Rules
$L \rightarrow En$	<code>print("E.val");</code>
$E \rightarrow E + T$	$E.val = E.val + T.val$
$E \rightarrow T$	$E.val = T.val$
$T \rightarrow T * F$	$T.val = T.val * F.val$
$T \rightarrow F$	$T.val = F.val$
$F \rightarrow (E)$	$F.val = E.val$
$F \rightarrow digit$	$F.val = digit.lexval$

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(Example:  $3 * 5 + 4n$ )

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A declaration generated by the non-terminal  $D$  in the Syntax directed Definition consists of keyword *int* or *real* followed by a list of Identifiers.

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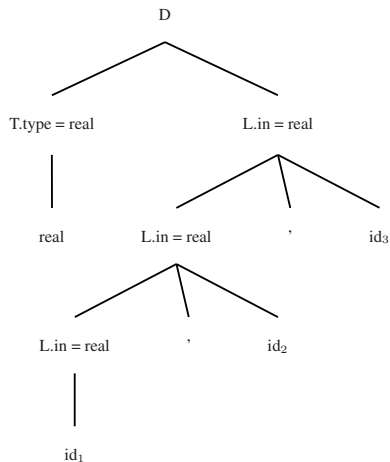
Productions	Semantic Rules
$D \rightarrow TL$	$L.in = T.type$
$T \rightarrow int$	$T.type = integer$
$T \rightarrow real$	$T.type = real$
$L \rightarrow L_1, id$	$L_1.in = L.in$ $addtype(id.entry, L.in)$
$L \rightarrow id$	$addtype(id.entry, L.in)$

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(Example: *real id<sub>1</sub>, id<sub>2</sub>, id<sub>3</sub>*)

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# Dependency Graph

- ▶ Directed Graph.
- ▶ Shows Intermediate dependencies between attributes.
- ▶ Construction
  - ▶ Put each semantic rule into the form  $b = f(c_1, \dots, c_k)$  by introducing dummy synthesized attribute  $b$  for every semantic rule that consists of a **procedure call**.
  - ▶ Eg.

$L \rightarrow En$       `print("E.val")`  
 Becomes:    **dummy** = `print("E.val")`  
 etc.

A dependency graph depicts the flow of information among the attribute instances in a particular parse tree; an edge from one attribute instance to another means that the value of the first is needed to compute the second.

## Dependency Graph Construction

- ▶ **for** each node  $n$  in the parse tree **do**
  - for** each attribute  $a$  of the grammar symbol at node  $a$  **do**
    - ▶ construct a node in the dependency graph for  $a$ ;



## Dependency Graph Construction

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- ▶ **for** each node  $n$  in the parse tree **do**
  - ▶ for each semantic rule  $b = f(c_1, c_2, \dots, c_k)$  associated with the production used at  $n$  **do**
    - ▶ **for**  $i = 1$  to  $k$  **do**  
Construct an edge from the node for  $c_i$  to the node for  $b$ ;

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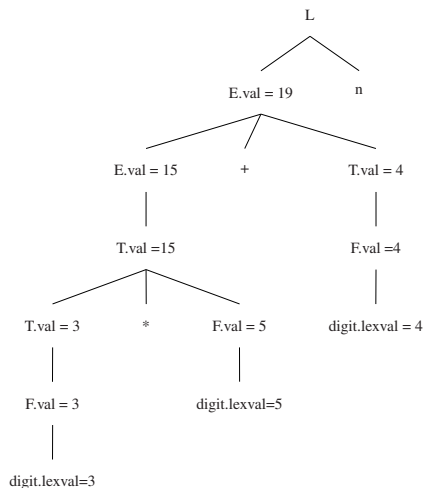
Subscript is E1 is to differentiate it from E in the semantic rules

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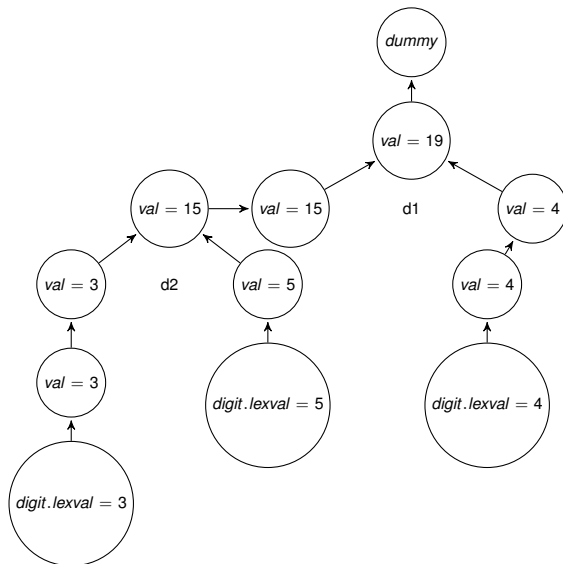
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# Example: Dependency Graph



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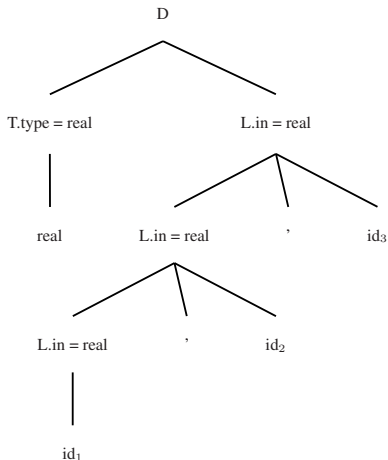
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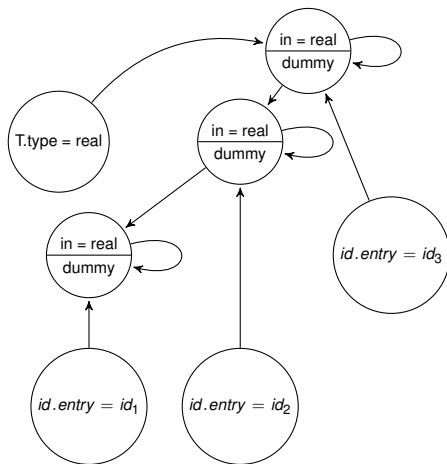
$L.in \rightarrow L.inh$  (inherited)

# Annotated parse Tree

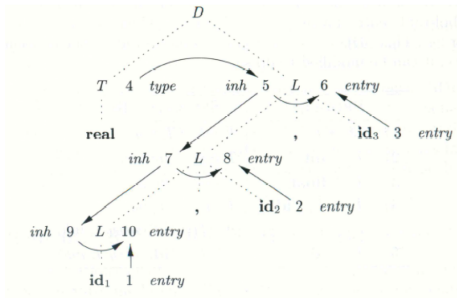
(Example: *real id<sub>1</sub>, id<sub>2</sub>, id<sub>3</sub>*)



## Example: Dependency Graph



## Example: Evaluation Order



- ▶  $a_4 = \text{real}$
- ▶  $a_5 = a_4$
- ▶  $\text{addtype}(\text{id}_3.\text{entry}, a_5)$
- ▶  $a_7 = a_5$
- ▶  $\text{addtype}(\text{id}_2.\text{entry}, a_7)$
- ▶  $a_9 = a_7$
- ▶  $\text{addtype}(\text{id}_1.\text{entry}, a_9)$



## Evaluation Order of Semantic Rules

Several methods have been proposed for the evaluation of semantic rules.

- ▶ **Parse Tree Method:**

- ▶ At compile time evaluation order obtained from dependency graph constructed from the parse tree.
- ▶ Fails if dependency graph contains a cycle.

- ▶ **Rule Based methods:**

- ▶ Semantic rules analyzed by hand or specialized tools at compiler construction time.
- ▶ Order of evaluation of attributes associated with a production is pre-determined at compiler construction time.

- ▶ **Oblivious methods:**

- ▶ Evaluation order is chosen without considering the semantic rules.
- ▶ Restricts the class of syntax directed definitions that can be implemented.
- ▶ Order of evaluation is forced by parsing method.

## Construction of Syntax tree

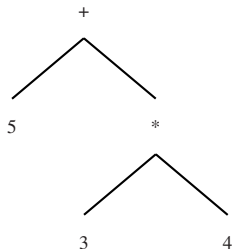
# Syntax - Tree

- ▶ an intermediate representation of the **compiler's input**.
- ▶ A condensed form of parse tree.
- ▶ Syntax tree shows the syntactic structure of the programme while omitting the irrelevant details.
- ▶ Operators or keywords are associated with the interior nodes.
- ▶ Chains of simple productions are collapsed.

**Syntax directed translation can be based on syntax tree as well as parse tree.**

## Syntax - Tree Example

5 + 3 \* 4



- ▶ Leaves: identifiers or constants.
- ▶ Internal nodes: Labelled with operations.
- ▶ Children of a node are its operands.

## Constructing Syntax trees for an Expression:

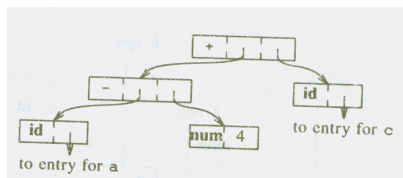
- ▶ Each node can be implemented as a record with several fields.
- ▶ Operator node: one field identifies the operator (called label of the node) and remaining fields contain pointers to operands.
- ▶ The nodes may also contain fields to hold the values (pointers to values) of attributes attached to the nodes.
- ▶ Functions used to create nodes of syntax tree for expressions with binary operator are given below
  - ▶ **mknode**(op, left, right)
  - ▶ **mkleaf**(id, entry)
  - ▶ **makeleaf** (num, val)

**Each function returns a pointer to a newly created node.**

## Example

$a - 4 + c$

1.  $p_1 = \text{mkleaf}(\text{id}, \text{entry}_a);$
2.  $p_2 = \text{mkleaf}(\text{num}, 4);$
3.  $p_3 = \text{mknnode}('-', p_1, p_2);$
4.  $p_4 = \text{mkleaf}(\text{id}, \text{entry}_c);$
5.  $p_5 = \text{mknnode}('+', p_3, p_4);$

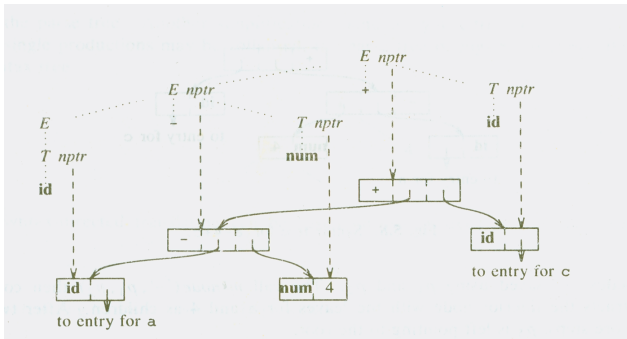


## Syntax-Directed definition for Constructing Syntax Trees

**Table:** Syntax-directed definition for constructing a syntax tree.

Production	Semantic Rules
$E \rightarrow E_1 + T$	$E.nptr = mknode('+', E_1.nptr, T.nptr)$
$E \rightarrow E_1 - T$	$E.nptr = mknode('-', E_1.nptr, T.nptr)$
$E \rightarrow T$	$E.nptr = T.nptr$
$T \rightarrow (E)$	$T.nptr = E.nptr$
$T \rightarrow id$	$T.nptr = mkleaf(id, id.entry)$
$T \rightarrow num$	$T.nptr = mkleaf(num, num.val)$

## Example: Construction of a Syntax-tree for $a-4+c$





## Directed Acyclic Graphs for Expression

## Bottom up Evaluation of S - Attributed Definitions

- ▶ A translator for an S-attributed definition can often be implemented with the help of an LR parser.
- ▶ From an S-attributed definition the parser generator can construct a translator that evaluates attributes as it parses the input.
- ▶ We put the values of the synthesized attributes of the grammar symbols a stack that has extra fields to hold the values of attributes.
- ▶

**Table:** Implementation of a Calculator with an LR parser

Production	Code Fragment
$L \rightarrow En$	<code>print(val[top]);</code>
$E \rightarrow E_1 + T$	<code>val[ntop] = val[top - 2] + val[top]</code>
$E \rightarrow T$	
$T \rightarrow T_1 * F$	<code>val[ntop] = val[top - 2] * val[top]</code>
$T \rightarrow F$	
$F \rightarrow (E)$	<code>val[ntop] = val[top - 1]</code>
$F \rightarrow digit$	

**Table:** Moves made by translator on Input  $3*5+4n$

Input	State	val	Production Used
3*5+4n	—	—	
*5+4n	3	3	
*5+4n	F	3	$F \rightarrow digit$
*5+4n	T	3	$T \rightarrow F$
5+4n	T *	3 _	
+4n	T * 5	3 _ 5	
+4n	☐ * F	3 _ 5	$F \rightarrow digit$
+4n	T	15	$T \rightarrow T * F$
+4n	E	15	$E \rightarrow T$
4n	E +	15 _	
n	E + 4	15 _ 4	
n	E + F	15 _ 4	$F \rightarrow digit$
n	E + T	15 _ 4	$T \rightarrow F$
n	E	19	$T \rightarrow F$
En	E n	19 _	
	L	19	$L \rightarrow En$

## Bottom-Up Evaluation of Inherited Attributes

# Type Checking

## Type Checking

- ▶ Type checking is the process of verifying that each operation executed in a program respects the type system of the language.
- ▶ This generally means that all operands in any expression are of appropriate types and numbers.
- ▶ Mostly what we do in semantic analysis phase is type checking.

## Designing a Type Checker

When designing a Type Checker for a compiler here's the process:

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- ▶ Identify the semantic rules for the language.
- ▶ If a problem found, e.g. one tries to add a character to a double in C, we encounter a type error.
- ▶ A language is considered ***strongly-typed*** if each and every type error is detected during compilation.
- ▶ Type checking can be done in compile time or in execution time.

## Static Type Checking

- ▶ Static type checking is done at compile time. The information type checker needs is obtained via declarations and stored in a master symbol table.
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- ▶ After this information is collected, the types involved in each operation are checked.
- ▶ For example, if  $a$  and  $b$  are of type `int` and we assign very large values to them,  $a * b$  may not be in the acceptable range of `ints`, or an attempt to compute the ratio between two integers may raise a division by zero. These kind of type errors usually can not be detected at compile time.

## Dynamic Type Checking

- ▶ Dynamic type checking is implemented by including type information for each data location at runtime.
- ▶ For example, a variable of type double would contain both the actual double value and some kind of tag indicating “double type”.
- ▶ The execution of any operation begins by first checking these type tags. The operation is performed only if everything checks out. Otherwise, a type error occurs and usually halts execution.

## Type Expressions

The type of a language construct will be denoted by a “type expression”.

The few basic type expressions are as follows:

- ▶ The basic types are boolean, char, integer, and real. A special basic type, `type_error`, will signal an error during type checking. Finally, a basic type `void` denoting “the absence of a value ” allows statements to be checked.
- ▶ Type expression may be named, a type name is a type expression.



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- ▶ Type expression may be named, a type name is a type expression.
- ▶ A type constructor applied to type expression is a type expression. Constructors include:
  - ▶ Arrays
  - ▶ Products
  - ▶ Records
  - ▶ Pointers
  - ▶ Functions

## Arrays:

If  $T$  is a Type expression, then  $\text{array}(I, T)$  is a type expression denoting the type of an array with elements of type  $T$  and index set  $I$ .  $I$  is often a range of integers. For example

- ▶ `var A: array[1..10] of integer;`

Associates the type expression: **`array(1..10, integer)`** with **`A`**

## Products

If  $T_1$  and  $T_2$  are type expressions, their Cartesian product  $T_1 \times T_2$  is a type expression.

## Records

The record type constructor will be applied to a tuple formed from field names and field types.

```

type    row =    record
                    address:          integer;
                    lexeme:           array [1..15] of char
                    end ;
var     table:   array[1..10] of row;
  
```

declares the name *row* representing the type expression  
**record((address × integer) × (lexeme × array(1 .. 15, char)))**

The variable *table* to be an array of records of this type.

## Pointers:

If  $T$  is a type expression, then  $pointer(T)$  is a type expression denoting the type “pointer to an object of type  $T$ ”.

For example,

var  $p$ :  $\uparrow$  row

declares variable  $p$  to have type pointer (row).

## Functions:

Mathematically, a function maps elements of one set, the domain, to another set, the range. We may treat functions in programming languages as mapping a *domain type*  $D$  to a *range type*  $R$ . The type of such a function will be denoted by  $D \rightarrow R$ .

As for example,

**function f(a, b : char):  $\uparrow$  integer;**

The type of f is denoted by the type expression

$char \times char \rightarrow pointer(integer)$

## Specification of a simple Type Checker

The following grammar generate programs, represented by the nonterminal  $P$ , consisting of a sequence of declarations  $D$  followed by a single expression  $E$ .

$$P \rightarrow D; E$$

$$D \rightarrow D; D \mid id : T$$

$$T \rightarrow char \mid integer \mid array[num] of T \mid \uparrow T$$

$$E \rightarrow literal \mid num \mid id \mid E mod E \mid E[E] \mid E \uparrow$$

**Table:** Translation Scheme that saves the type of an identifier

Productions	Associated rules for type
$P \rightarrow D; E$	
$D \rightarrow D; D$	
$D \rightarrow id : T$	{ addtype(id.entry, T.type) }
$T \rightarrow char$	{ T.type = char }
$T \rightarrow integer$	{ T.type = integer }
$T \rightarrow \uparrow T_1$	{ T.type = pointer( $T_1.type$ ) }
$T \rightarrow array[num] \text{ of } T_1$	{ T.type = array( 1 ... num.val, $T_1.type$ ) }



# Type Checking of Expressions

**Table:** Associated rules for Type Checking

Productions	Associated rules for type
$E \rightarrow literal$	$E.type = char$
$E \rightarrow num$	$E.type = integer$
$E \rightarrow id$	$E.type = lookup(id.entry)$
$E \rightarrow E_1 mod E_2$	$E.type = \text{if } E_1.type = integer \text{ and } E_2.type = integer \text{ then } integer \text{ else } type\_error$
$E \rightarrow E_1[E_2]$	$E.type = \text{if } E_2.type = integer \text{ and } E_1.type = array(s, t) \text{ then } t \text{ else } type\_error$
$E \rightarrow E_1 \uparrow$	$E.type = \text{if } E_1.type = pointer(t) \text{ then } t \text{ else } type\_error$

## Type Checking of Statements

The state statements we consider are assignment, conditional, and while statements.

Table: default

Productions	Associated rules for type
$S \rightarrow id = E$	{ S.type = <b>if</b> id.type == E.type <b>then</b> void <b>else</b> type_error }
$S \rightarrow \text{if } E \text{ then } S_1$	{ S.type = <b>if</b> E.type == Boolean <b>then</b> $S_1.type$ <b>else</b> type_error }
$S \rightarrow \text{while } E \text{ do } S_1$	{ S.type = <b>if</b> E.type == Boolean <b>then</b> $S_1.type$ <b>else</b> type_error }
$S \rightarrow S_1; S_2$	{ S.type = <b>if</b> $S_1.type$ == void <b>and</b> $S_2.type$ == void <b>then</b> void <b>else</b> type_error }

## Type Checking of Functions

Productions	Associated actions
$T \rightarrow T_1 ' \rightarrow' T_2$	$\{ T.type = T_1.type \rightarrow T_2.type \}$
$E \rightarrow E_1(E_2)$	$\{ E.type = \text{if } E_2.type == s \text{ and } E_1.type == s \rightarrow t \text{ then } t \text{ else } type\_error \}$