# Global irrigation water demands biased by unreliable irrigation efficiencies

## R code

## Arnald Puy

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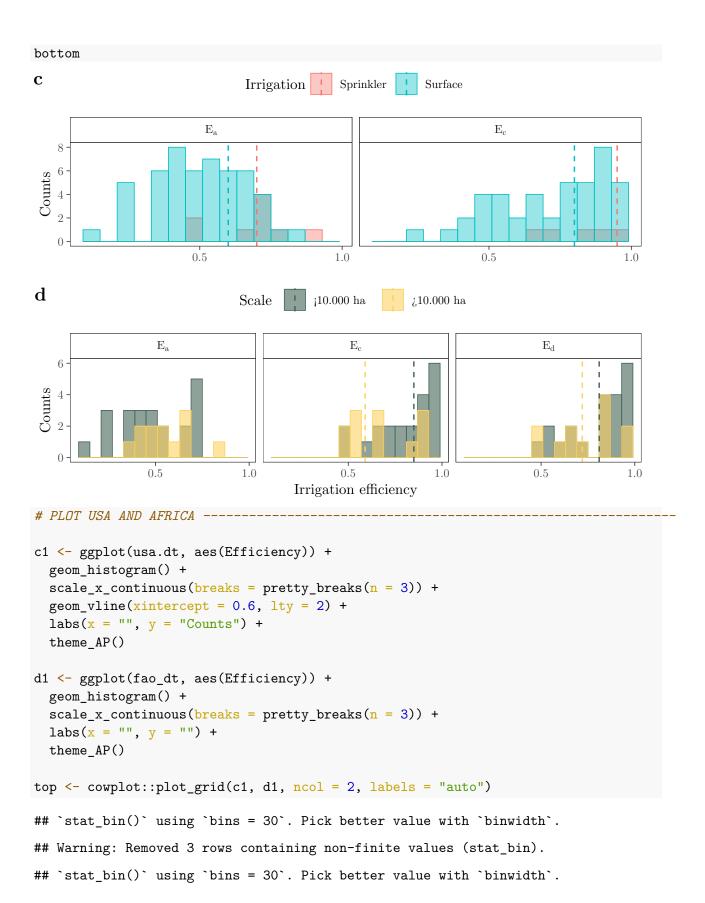
```
# Function to read in all required packages in one go:
loadPackages <- function(x) {</pre>
  for(i in x) {
    if(!require(i, character.only = TRUE)) {
      install.packages(i, dependencies = TRUE)
      library(i, character.only = TRUE)
  }
}
# Load the packages
loadPackages(c("data.table", "tidyverse", "sensobol", "wesanderson",
               "cowplot", "parallel", "foreach", "doParallel",
               "countrycode", "ggridges", "scales", "overlapping",
               "sp", "rworldmap", "ncdf4"))
# Create custom theme
theme_AP <- function() {</pre>
  theme_bw() +
    theme(panel.grid.major = element_blank(),
          panel.grid.minor = element_blank(),
          legend.background = element_rect(fill = "transparent",
                                            color = NA),
          legend.key = element_rect(fill = "transparent",
                                     color = NA),
          legend.position = "top",
          strip.background = element rect(fill = "white"),
          plot.margin = margin(t = 0, r = 0.3, b = 0, l = 0.3, unit ="cm"))
}
# Set checkpoint
dir.create(".checkpoint")
library("checkpoint")
checkpoint("2021-08-02",
           R.version ="4.0.3",
           checkpointLocation = getwd())
```

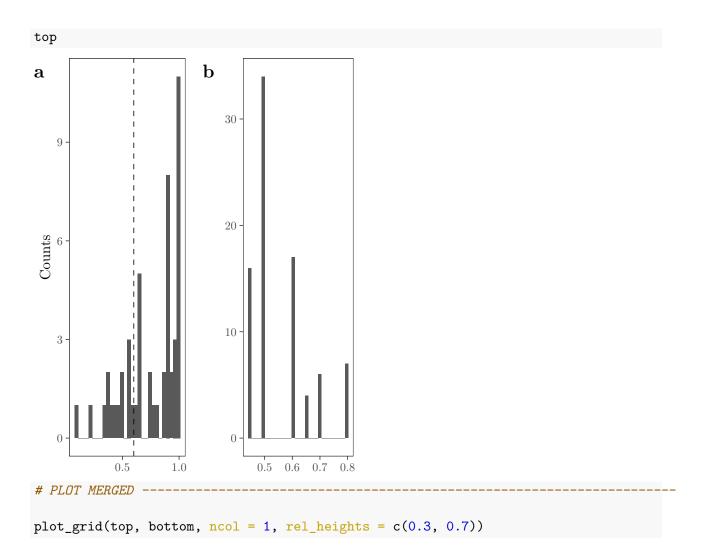
#### 1 Read in data

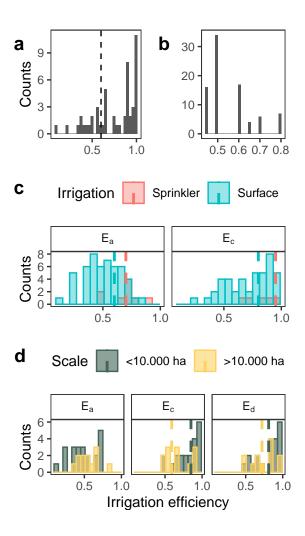
```
# READ IN DATA -----
# Rohwer data
rohwer <- fread("rohwer_data_all.csv")</pre>
rohwer[rohwer == ""] <- NA</pre>
rohwer <- rohwer[, Large_fraction:= Large_fraction / 100]</pre>
# Jager data
jager <- fread("jager_data.csv")</pre>
jager.list <- split(jager, jager$Country)</pre>
# Bos data
bos <- fread("bos_data.csv")</pre>
bos <- bos[, Scale := ifelse(Irrigated_area < 10000, "<10.000 ha", ">10.000 ha")]
# Solley data (USA)
usa.dt <- fread("usa_efficiency.csv")</pre>
usa.dt <- usa.dt[, Efficiency:= consumptive.use / total.withdrawal]
# FAO 1997 data (Irrigation potential in Africa)
fao_dt <- fread("fao_1997.csv")</pre>
fao_dt <- fao_dt[, Efficiency:= Efficiency / 100]</pre>
# Create data set with E_a values as defined by Rohwer
bos.rohwer.ea <- data.table("Irrigation" = c("Surface", "Sprinkler"),</pre>
                              "Value" = c(0.6, 0.7),
                              "variable" = "E[a]")
# Create data set with E_c values as defined by Rohwer
bos.rohwer.ec <- data.table("Irrigation" = c("Surface", "Sprinkler"),</pre>
                              "Value" = c(0.8, 0.95),
                              "variable" = "E[c]")
bos.rohwer.all <- rbind(bos.rohwer.ec, bos.rohwer.ea)</pre>
# As a function of scale
bos.rohwer.mf.ec <- data.table("Scale" = c("<10.000 ha", ">10.000 ha"),
                                 "Value" = c(0.85, 0.59),
                                 "variable" = "E[c]")
bos.rohwer.mf.ed \leftarrow data.table("Scale" = c("<10.000 ha", ">10.000 ha"),
                                 "Value" = c(0.81, 0.72),
                                 "variable" = "E[d]")
bos.rohwer.mf.all <- rbind(bos.rohwer.mf.ec, bos.rohwer.mf.ed)</pre>
```

```
bos2 <- copy(bos)</pre>
bos2 <- setnames(bos2, c("E_a", "E c", "E_d"), c("E[a]", "E[c]", "E[d]"))
# Field and conveyance efficiency -----
a <- bos2 %>%
 melt(., measure.vars = c("E[a]", "E[c]")) %>%
  ggplot(., aes(value, fill = Irrigation, color = Irrigation)) +
  geom_histogram(position = "identity", alpha = 0.4, bins = 15) +
 facet_wrap(~variable, labeller = label_parsed) +
  scale_x_continuous(breaks = pretty_breaks(n = 3)) +
  geom_vline(data = bos.rohwer.all, aes(xintercept = Value,
                                       color = Irrigation,
                                        group = variable),
            lty = 2,
            size = 1) +
  labs(x = "", y = "Counts") +
  theme_AP()
# As a function of scale -----
b <- melt(bos2, measure.vars = c("E[c]", "E[a]", "E[d]")) %>%
 na.omit() %>%
  ggplot(., aes(value, fill = Scale, color = Scale)) +
 geom histogram(bins = 15, position = "identity", alpha = 0.6) +
 labs(x = "Irrigation efficiency", y = "Counts") +
 facet_wrap(~ variable, labeller = label_parsed) +
  geom_vline(data = bos.rohwer.mf.all, aes(xintercept = Value,
                                         color = Scale,
                                         group = variable),
            lty = 2,
             size = 1) +
  scale_x_continuous(breaks = pretty_breaks(n = 3)) +
  scale_color_manual(values = wes_palette(2, name = "Chevalier1"),
                    name = "Scale",
                    labels = c("<10.000 ha", ">10.000 ha")) +
  scale_fill_manual(values = wes_palette(2, name = "Chevalier1"),
                    name = "Scale",
                    labels = c("<10.000 ha", ">10.000 ha")) +
  theme_AP()
bottom <- plot_grid(a, b, ncol = 1, labels = c("c", "d"))
```

## Warning: Removed 74 rows containing non-finite values (stat\_bin).







## 2 The model

#### 2.1 Function to create sample matrix

```
sample_matrix_fun <- function(IFT) {
  params <- params_fun(IFT = IFT)
  mat <- sensobol::sobol_matrices(N = N, params = params)
  out <- list(params, mat)
  names(out) <- c("parameters", "matrix")
  return(out)
}</pre>
```

#### 2.2 Define distributions

```
# DEFINE TRUNCATED DISTRIBUTIONS -
# EA SURFACE -----
Ea.surface <- bos[Irrigation == "Surface"][, .(min = min(E_a, na.rm = TRUE),</pre>
                                                 max = max(E_a, na.rm = TRUE))]
shape <- 3.502469
scale <- 0.5444373
minimum <- Ea.surface$min
maximum <- Ea.surface$max</pre>
weibull_dist <- sapply(c(minimum, maximum), function(x)</pre>
  pweibull(x, shape = shape, scale = scale))
# EC SURFACE -----
Ec.surface <- bos[Irrigation == "Surface"][, .(min = min(E_c, na.rm = TRUE),</pre>
                                                 \max = \max(E_c, na.rm = TRUE))]
shape1 <- 5.759496
shape2 <- 1.403552
minimum.beta <- Ec.surface$min
maximum.beta <- Ec.surface$max</pre>
beta_dist <- sapply(c(minimum.beta, maximum.beta), function(x)</pre>
  pbeta(x, shape1 = shape1, shape2 = shape2))
# EA SPRINKLER -----
Ea.sprinkler <- bos[Irrigation == "Sprinkler"][, .(min = min(E_a, na.rm = TRUE),</pre>
                                                 max = max(E_a, na.rm = TRUE))]
shape.spr <- 6.9913711
scale.spr <- 0.7451178
minimum.spr <- Ea.sprinkler$min
maximum.spr <- Ea.sprinkler$max</pre>
weibull_dist_spr <- sapply(c(minimum.spr, maximum.spr), function(x)</pre>
  pweibull(x, shape = shape.spr, scale = scale.spr))
# MANAGEMENT FACTOR (m) ----
```

```
shape1.m < -5.759496
shape2.m < -1.403552
minimum.m < - 0.65
maximum.m <- 1</pre>
beta_dist.m <- sapply(c(minimum.m, maximum.m), function(x)</pre>
 pbeta(x, shape1 = shape1.m, shape2 = shape2.m))
# FUNCTION TO TRANSFORM TO APPROPRIATE DISTRIBUTIONS -----
distributions_fun <- list(</pre>
  # SURFACE IRRIGATION
  # -----
  "Ea_surf" = function(x) {
   out <- qunif(x, weibull_dist[[1]], weibull_dist[[2]])</pre>
   out <- qweibull(out, shape, scale)</pre>
 },
  "Ec_surf" = function(x) {
   out <- qunif(x, beta_dist[[1]], beta_dist[[2]])</pre>
   out <- qbeta(out, shape1, shape2)</pre>
 },
  # SPRINKLER IRRIGATION
  # -----
  "Ea_sprinkler" = function(x) {
   out <- qunif(x, weibull_dist_spr[[1]], weibull_dist_spr[[2]])</pre>
   out <- qweibull(out, shape.spr, scale.spr)</pre>
 },
  "Ec_sprinkler" = function(x) qunif(x, 0.64, 0.96),
  # MICRO (DRIP) IRRIGATION
  "Ea_micro" = function(x) out <- qunif(x, 0.75, 0.95),
  "Ec_micro" = function(x) out <- qunif(x, 0.9, 0.95),
  # PROPORTION LARGE
  # -----
  "Proportion_large" = function(x) x,
```

2.3 Uncertainty in the proportion of large-scale irrigated areas

2.4 Function to create sample matrix and transfrom to appropriate distributions

```
# FULL ALGORITHM TO CREATE SAMPLE MATRIX -----
```

```
full_sample_matrix <- function(IFT, Country) {
   tmp <- sample_matrix_fun(IFT = IFT)
   mat <- tmp[["matrix"]]
   temp <- colnames(mat)
   mat <- sapply(seq_along(temp), function(x) distributions_fun[[temp[x]]](mat[, x]))
   colnames(mat) <- temp
   countries.frac <- countries.list[[Country]]
   out <- list(tmp$parameters, mat)
   names(out) <- c("parameters", "matrix")
   return(out)
}</pre>
```

#### 2.5 Run the model

```
# FULL MODEL -----
full_model <- function(IFT, Country, sample.size, R) {</pre>
  country.differences <- setdiff(rohwer$Country, jager$Country)</pre>
  tmp <- full_sample_matrix(IFT = IFT, Country = Country)</pre>
  mat <- tmp$matrix</pre>
  if(IFT == "Surface" | IFT == "Mixed" | IFT == "Jager") {
    X1 <- mat[, "X1"]</pre>
    X2 <- mat[, "X2"]</pre>
    index <- paste(Country, X1, X2, sep = ".")</pre>
    Proportion_large <- triggers.dt[index][, Proportion_large]</pre>
  }
  if(IFT == "Surface") {
    Mf <- mat[, "m"] - mat[, "r_L"] * Proportion_large</pre>
    y <- mat[, "Ea_surf"] * mat[, "Ec_surf"] * Mf</pre>
  } else if(IFT == "Sprinkler") {
    Mf <- mat[, "m"]</pre>
    y <- mat[, "Ea_sprinkler"] * mat[, "Ec_sprinkler"] * Mf
  } else if(IFT == "Mixed") {
    Mf.surf <- mat[, "m"] - mat[, "r_L"] * Proportion_large</pre>
    y.surf <- mat[, "Ea_surf"] * mat[, "Ec_surf"] * Mf.surf</pre>
    Mf.sprink <- mat[, "m"]</pre>
    y.sprink <- mat[, "Ea_sprinkler"] * mat[, "Ec_sprinkler"] * Mf.sprink</pre>
```

```
y <- 0.5 * y.surf + mat[, "r_L"] * y.sprink</pre>
  } else if(IFT == "Micro") {
    Mf <- mat[, "m"]</pre>
    y <- mat[, "Ea_micro"] * mat[, "Ec_micro"] * Mf
 } else if(IFT == "Jager") {
    if(Country %in% country.differences == TRUE) {
      next
    }
    Mf.surf <- mat[, "m"] - mat[, "r_L"] * Proportion_large</pre>
    y.surf <- mat[, "Ea_surf"] * mat[, "Ec_surf"] * Mf.surf</pre>
    Mf.spr <- mat[, "m"]</pre>
    y.spr <- mat[, "Ea_sprinkler"] * mat[, "Ec_sprinkler"] * Mf.spr</pre>
    Mf.micro <- mat[, "m"]</pre>
    y.micro <- mat[, "Ea_micro"] * mat[, "Ec_micro"] * Mf.micro
    y <- jager.list[[Country]]$Surface_fraction * y.surf +
      jager.list[[Country]]$Sprinkler_fraction * y.spr +
      jager.list[[Country]]$Drip_fraction * y.micro
 }
  ind <- sobol_indices(N = sample.size, Y = y, params = tmp$parameters,
                        boot = TRUE, R = R)
  out <- list(y, ind)</pre>
 names(out) <- c("output", "indices")</pre>
 return(out)
}
```

#### 2.6 Define settings

```
# DEFINE SETTINGS -----
N <- 2^14
R <- 10^2
```

#### 2.7 Run model

```
# RUN MODEL -----
new.rohwer <- rohwer[Country %in% jager$Country][, IFT:= "Jager"]</pre>
```

### 2.8 Extract model output

```
# EXTRACT MODEL OUTPUT -----
names(y) <- c("Rohwer et al. 2007", "Jägermeyr et al. 2015")
output <- tmp <- list()</pre>
for(i in names(y)) {
  output[[i]] <- lapply(y[[i]], function(x) x[["output"]][1:(2 * N)])</pre>
  if(i == "Rohwer et al. 2007") {
    names(output[[i]]) <- rohwer$Country</pre>
  } else if(i == "Jägermeyr et al. 2015") {
    names(output[[i]]) <- new.rohwer$Country</pre>
  }
  tmp[[i]] <- lapply(output[[i]], data.table) %>%
    rbindlist(., idcol = "Country")
  if(i == "Rohwer et al. 2007") {
    tmp[[i]] <- merge(tmp[[i]], rohwer[, .(Country, IFT)], all.x = TRUE) %%</pre>
      .[, IFT:= factor(IFT, levels = c("Surface", "Sprinkler", "Micro", "Mixed"))]
  } else if(i == "Jägermeyr et al. 2015") {
    tmp[[i]] <- tmp[[i]][, IFT:= "Jager"]</pre>
 }
 tmp[[i]] <- tmp[[i]][, Continent:= countrycode(tmp[[i]][, Country],</pre>
                                                    origin = "country.name",
```

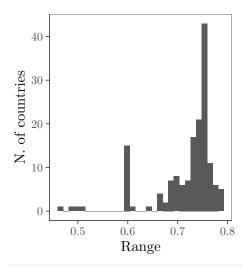
```
destination = "continent")]
}
## Warning in countrycode_convert(sourcevar = sourcevar, origin = origin, destination = dest,
## Warning in countrycode_convert(sourcevar = sourcevar, origin = origin, destination = dest,
uncertainty.dt <- rbindlist(tmp, idcol = "Approach")</pre>
uncertainty.dt <- uncertainty.dt[, Study:= ifelse(IFT == "Jager",
                                                    "The proportion of IFTs is known",
                                                    "The proportion of IFTs is not known")]
# EXPORT UNCERTAINTY IN IRRIGATION EFFICIENCY -----
fwrite(uncertainty.dt, "uncertainty.dt.csv")
# COMPUTE RANGES -----
calc <- uncertainty.dt[, .(min = min(V1), max = max(V1)), .(Continent, Country)] %%</pre>
  .[, .(range = max - min), .(Continent, Country)] %>%
  .[order(range)]
print(calc, n = Inf)
##
        Continent
                                    Country
                                                range
##
     1:
             Asia
                                     Cyprus 0.4679420
     2:
                      United Arab Emirates 0.4900561
##
             Asia
##
     3:
             Asia
                                     Israel 0.4944147
##
     4:
             Asia
                                     Jordan 0.5149145
                                    Austria 0.6014893
##
     5:
           Europe
##
     6:
           Europe
                                    Belgium 0.6014893
             <NA>
                                   Byelarus 0.6014893
##
     7:
           Europe
                                    Denmark 0.6014893
##
     8:
           Europe
                                    Finland 0.6014893
##
     9:
           Europe
                                    Germany 0.6014893
##
    10:
##
    11:
           Europe
                                    Greece 0.6014893
    12:
           Europe
                                    Hungary 0.6014893
##
                                     Latvia 0.6014893
##
    13:
           Europe
    14:
                                  Lithuania 0.6014893
##
           Europe
                                Luxembourg 0.6014893
## 15:
           Europe
##
  16:
           Africa
                                     Malawi 0.6014893
                                   Slovakia 0.6014893
## 17:
           Europe
                                     Sweden 0.6014893
## 18:
           Europe
## 19:
           Europe
                                Switzerland 0.6014893
                                    Ukraine 0.6147176
## 20:
           Europe
## 21:
           Europe
                            Czech Republic 0.6477047
## 22:
           Europe
                                     Russia 0.6622102
## 23:
           Europe
                                    Croatia 0.6645827
                            United Kingdom 0.6680857
## 24:
           Europe
```

##	OF.	Eumana	Domonio	0 6604020
##	25:	Europe		0.6684038
##	26:	Africa		0.6796764
##	27:	Americas		0.6796800
##	28:	Africa		0.6838233
##	29:	Americas	United States	
##	30:	Asia		0.6879111
##	31:	Asia		0.6892404
##	32:	Europe	Netherlands	
##	33:	Asia	Saudi Arabia	
##	34:	Asia	Kazakhstan	
##	35:	Africa	Mozambique	
##	36:	Americas		0.6959479
##	37:	Europe		0.6976147
##	38:	Africa		0.6985666
##	39:	Africa		0.6985699
##	40:	Africa		0.7002246
##	41:	Africa	South Africa	
##	42:	Africa		0.7025813
##	43:	Asia	•	0.7036842
##	44:	Asia	Kuwait	0.7046397
##	45:	Americas	Canada	0.7077460
##	46:	Africa	Ivory Coast	0.7091386
##	47:	Europe	•	0.7108935
##	48:	Africa	Burkina Faso	0.7115694
##	49:	Europe	Bulgaria	0.7147026
##	50:	Africa	Algeria	0.7182193
##	51:	Europe	Spain	0.7190056
##	52:	Americas	French Guiana	0.7191150
##	53:	Oceania	Australia	0.7218235
##	54:	Africa	Lesotho	0.7226186
##	55:	Asia	Japan	0.7247774
##	56:	Americas	Uruguay	0.7264713
##	57:	Asia	Iraq	0.7277116
##	58:	Asia	Azerbaijan	0.7284226
##	59:	Africa	•	0.7299519
##	60:	Africa	Zaire	0.7306228
##	61:	Africa	Botswana	0.7322712
##	62:	Africa	Gabon	0.7325094
##	63:	Americas	Paraguay	0.7327599
##	64:	Asia	Turkey	0.7330840
##	65:	Africa	Uganda	0.7335162
##	66:	Americas		0.7340006
##	67:	Asia	Burma	0.7344695
##	68:	Americas	Guatemala	0.7352743
##	69:	Africa	Tanzania	0.7353794
##	70:	Oceania	Papua New Guinea	0.7357704
##	71:	Asia		0.7364300
##	72:	Africa	<del>-</del>	0.7364368
			•	

```
73:
                                     Ecuador 0.7379232
##
         Americas
    74:
##
           Africa
                                        Kenya 0.7381012
##
    75:
         Americas
                                        Haiti 0.7389654
    76:
##
           Africa
                                         Chad 0.7398257
##
    77:
           Africa Central African Republic 0.7406275
    78:
                                    Colombia 0.7406412
##
         Americas
##
    79:
           Africa
                                       Gambia 0.7410900
##
    80:
         Americas
                                 Puerto Rico 0.7411452
##
    81:
           Africa
                              Western Sahara 0.7412732
           Europe
##
    82:
                                    Portugal 0.7424699
    83:
##
                                 El Salvador 0.7424882
         Americas
##
    84:
              Asia
                                        India 0.7430188
    85:
                                    Cameroon 0.7430382
##
           Africa
##
    86:
              Asia
                                Turkmenistan 0.7431978
##
    87:
           Africa
                                        Egypt 0.7434191
##
    88:
              Asia
                                        Syria 0.7437367
##
    89:
           Africa
                                  Madagascar 0.7453378
##
    90:
         Americas
                                  Costa Rica 0.7460634
    91:
                                        Yemen 0.7464134
##
              Asia
    92:
           Africa
                          Equatorial Guinea 0.7472551
##
##
    93:
           Europe
                                       Serbia 0.7476467
##
    94:
           Africa
                                     Liberia 0.7479554
##
    95:
         Americas
                                     Bolivia 0.7480052
    96:
           Africa
                                     Somalia 0.7480674
##
##
    97:
             Asia
                                        Laos 0.7481253
    98:
                                    Ethiopia 0.7482251
##
           Africa
##
    99:
           Africa
                                       Rwanda 0.7482431
## 100:
             Asia
                                  Kyrgyzstan 0.7484823
## 101:
              Asia
                                       Bhutan 0.7487014
## 102:
           Europe
                                      Norway 0.7488203
           Europe
## 103:
                                      Poland 0.7495878
## 104:
           Africa
                                         Mali 0.7501681
## 105:
              Asia
                                   Sri Lanka 0.7502131
## 106:
                                    Mongolia 0.7502820
              Asia
## 107:
         Americas
                                    Trinidad 0.7505246
## 108:
           Africa
                               Guinea-Bissau 0.7507230
## 109:
           Africa
                                      Guinea 0.7508012
## 110:
              Asia
                                        China 0.7508179
## 111:
                                  Mauritania 0.7508221
           Africa
## 112:
              Asia
                                   Indonesia 0.7509219
## 113:
             Asia
                                     Armenia 0.7511245
## 114:
           Europe
                     Bosnia and Herzegovina 0.7513991
## 115:
           Africa
                                     Morocco 0.7514743
## 116:
              Asia
                                         Iran 0.7514788
## 117:
         Americas
                                    Suriname 0.7515058
## 118:
         Americas
                                         Peru 0.7516554
## 119:
         Americas
                                   Argentina 0.7521091
## 120:
                                        Chile 0.7522434
         Americas
```

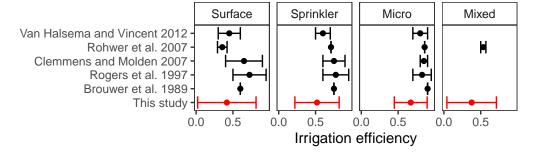
```
## 121:
           Africa
                                Sierra Leone 0.7525826
## 122:
           Africa
                                       Niger 0.7526578
## 123:
           Africa
                                      Angola 0.7530253
## 124:
           Africa
                                     Burundi 0.7531444
## 125:
         Americas
                                      Belize 0.7533846
## 126:
                                 South Korea 0.7544530
             Asia
## 127:
         Americas
                                      Mexico 0.7544977
## 128:
             Asia
                                    Malaysia 0.7545882
## 129:
           Africa
                                    Djibouti 0.7546681
## 130:
         Americas
                                    Honduras 0.7550064
## 131:
           Africa
                                        Togo 0.7550732
## 132:
           Africa
                                     Eritrea 0.7555949
## 133:
                                     Moldova 0.7563886
           Europe
## 134:
             Asia
                                    Cambodia 0.7569788
## 135:
           Africa
                                     Senegal 0.7574388
## 136:
           Europe
                                   Macedonia 0.7578519
## 137:
           Africa
                                     Nigeria 0.7589399
           Africa
## 138:
                                       Sudan 0.7593515
## 139:
                                    Thailand 0.7607690
             Asia
## 140:
             Asia
                                    Pakistan 0.7615949
## 141:
         Americas
                                   Nicaragua 0.7622110
## 142:
                                     Vietnam 0.7641254
             Asia
## 143:
         Americas
                                   Venezuela 0.7645259
## 144:
         Americas
                         Dominican Republic 0.7645690
## 145:
                                     Albania 0.7647019
           Europe
## 146:
                                  Uzbekistan 0.7672137
             Asia
## 147:
             Asia
                                  Tajikistan 0.7680949
## 148:
             Asia
                                     Georgia 0.7709388
## 149:
             Asia
                                  Bangladesh 0.7714909
## 150:
         Americas
                                      Guyana 0.7752999
## 151:
                                 Philippines 0.7759418
             Asia
## 152:
         Americas
                                      Panama 0.7774470
## 153:
           Europe
                                    Slovenia 0.7784899
## 154:
                                 North Korea 0.7820092
             Asia
## 155:
           Africa
                                       Ghana 0.7850875
## 156:
             Asia
                                 Afghanistan 0.7865884
## 157:
             Asia
                                        Oman 0.7878713
## 158:
          Oceania
                                 New Zealand 0.7892427
        Continent
                                     Country
                                                  range
ggplot(calc, aes(range)) +
  geom_histogram() +
  labs(x = "Range", y = "N. of countries") +
  theme_AP()
```

## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



```
# COMPARE RANGES -----
```

```
ranges_empirical <- uncertainty.dt[, .(higher = max(V1), lower = min(V1)), IFT] %>%
  .[, Study:= "This study"]%>%
  .[!IFT == "Jager"]
ranges_efficiencies <- fread("ranges_efficiencies.csv")</pre>
rbind(ranges_empirical, ranges_efficiencies)[, mean.value:= (higher + lower) / 2] %>%
  .[, Study:= factor(Study, levels = c("This study",
                                        "Brouwer et al. 1989",
                                        "Rogers et al. 1997",
                                        "Clemmens and Molden 2007",
                                        "Rohwer et al. 2007",
                                        "Van Halsema and Vincent 2012"))] %>%
 na.omit() %>%
 ggplot(., aes(mean.value, Study, color = ifelse(Study == "This study", "red", "black"))) +
  geom point() +
  scale_x_continuous(breaks = pretty_breaks(n = 3)) +
  geom_errorbar(aes(xmin = lower, xmax = higher)) +
  scale_color_identity() +
  facet_wrap(~IFT, ncol = 4) +
  labs(x = "Irrigation efficiency", y = "") +
  theme_AP()
```



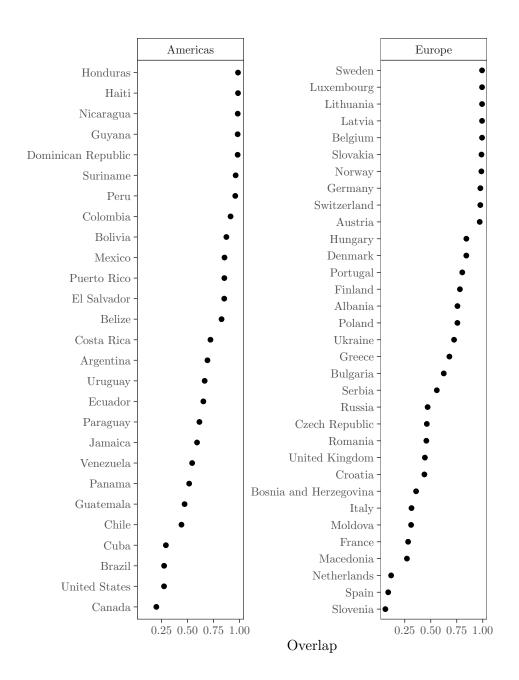
```
# CHECK OVERLAP -----
dd <- uncertainty.dt[!Continent == "Oceania"][Study == "The proportion of IFTs is not known"] '
  split(., .$Continent, drop = TRUE)
overlap.dt <- lapply(dd, function(x) split(x, x$IFT, drop = TRUE)) %%</pre>
  lapply(., function(x) lapply(x, function(y) y[, V1])) %>%
 lapply(., function(x) overlap(x)$0V)
overlap.dt
## $Africa
## Surface-Sprinkler
                        Surface-Mixed
                                         Sprinkler-Mixed
           0.2341197
                                               0.1513037
##
                             0.7482128
##
## $Americas
## Surface-Mixed
##
       0.7622839
##
## $Asia
## Surface-Micro Surface-Mixed Micro-Mixed
##
      0.04502982
                   0.72015229
                                  0.01232303
##
## $Europe
                                         Sprinkler-Mixed
## Surface-Sprinkler
                        Surface-Mixed
          0.2404475
                                               0.1536190
                             0.7435392
ff <- uncertainty.dt[!Continent == "Oceania"] %>%
  .[Country %in% intersect(rohwer[, Country], jager[, Country])] %>%
  split(., .$Country, drop = TRUE) %>%
 lapply(., function(x) split(x, x$Approach, drop = TRUE)) %>%
 lapply(., function(x) lapply(x, function(y) y[, V1])) %>%
 lapply(., function(x) overlap(x)$0V) %>%
 lapply(., data.table) %>%
 rbindlist(., idcol = "Country") %>%
  .[, Continent:= countrycode(.[, Country],
                             origin = "country.name",
                             destination = "continent")]
list_continents <- list(c("Africa", "Asia"), c("Americas", "Europe"))</pre>
# PLOT OVERLAP -----
dd <- list()
for(i in 1:length(list_continents)) {
  dd[[i]] <- ff[Continent %in% list_continents[[i]]] %>%
    ggplot(., aes(reorder(Country, V1), V1)) +
   geom_point() +
```

```
scale_color_discrete(name = "GM") +
labs(y = "Overlap", x = "") +
facet_wrap(~Continent, scales = "free_y") +
coord_flip() +
theme_AP()
}
dd
```

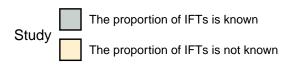
#### ## [[1]]

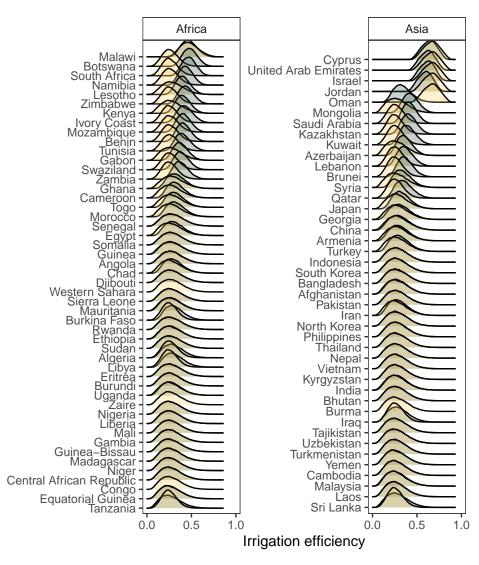


## ## [[2]]



# 3 Uncertainty analysis

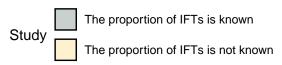


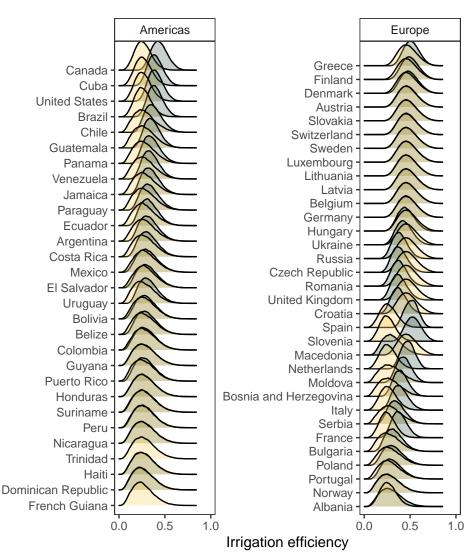


## ## [[2]]

## Picking joint bandwidth of 0.012

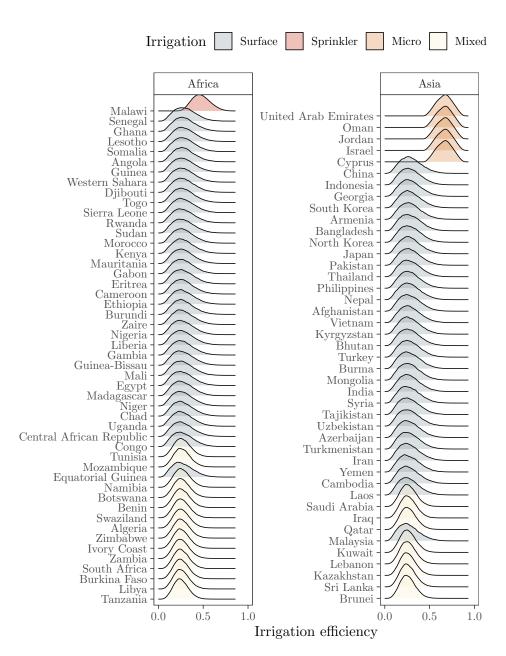
## Picking joint bandwidth of 0.0108





# PLOT UNCERTAINTY IN EACH IRRIGATION TECHNOLOGY ------

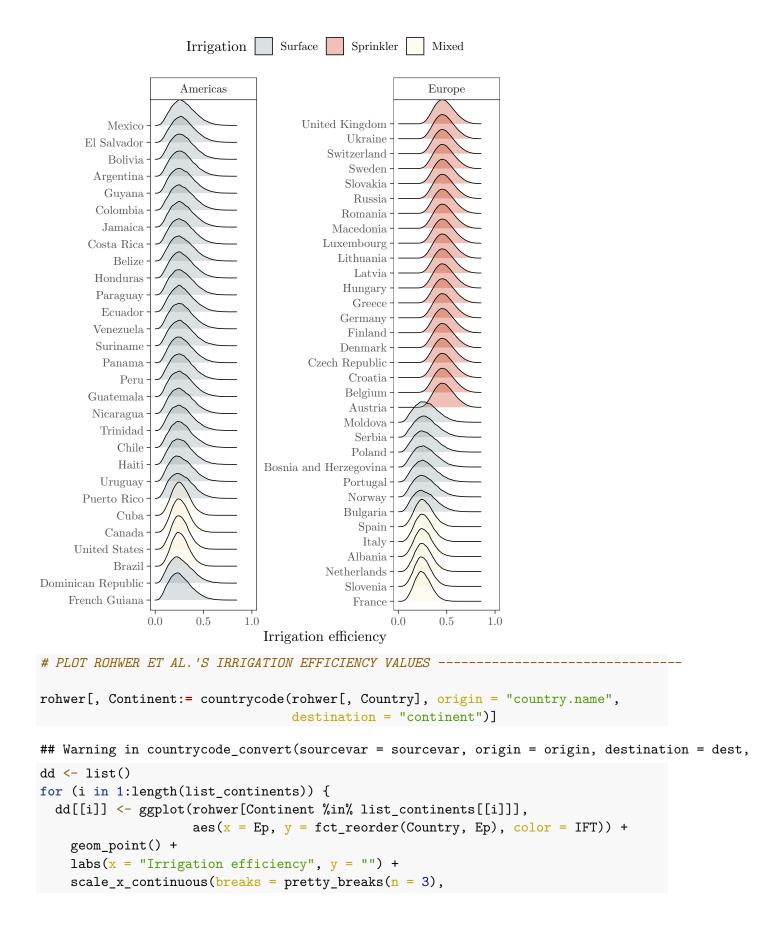
```
## [[1]]
## Picking joint bandwidth of 0.012
## Picking joint bandwidth of 0.012
```



## ## [[2]]

## Picking joint bandwidth of 0.0126

## Picking joint bandwidth of 0.0113

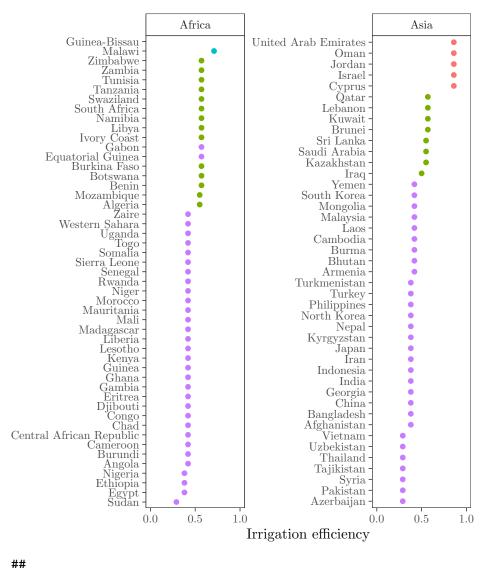


```
limits = c(0, 1)) +
facet_wrap(~Continent, scales = "free") +
scale_color_discrete(name = "Irrigation") +
theme_AP()
}
dd
```

## [[1]]

## Warning: Removed 1 rows containing missing values (geom\_point).





## ## [[2]]



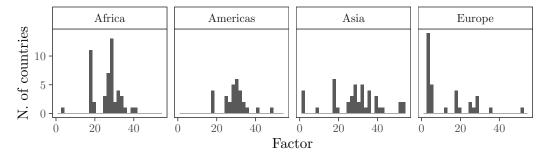


```
# CALCULATE THE UNCERTAINTY IN THE RANGES ------
selection_continents <- c("Africa", "Asia", "Americas", "Europe")

factor_unc <- uncertainty.dt[, .(min = min(V1), max = max(V1)), .(Continent, Country)] %>%
    .[Continent %in% selection_continents] %>%
    .[, factor:= max / min]

ggplot(factor_unc, aes(factor)) +
    geom_histogram() +
    facet_wrap(~Continent, ncol = 4) +
    labs(x = "Factor", y = "N. of countries") +
    theme_AP()
```

## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



```
# Number of countries whose irrigation water withdrawals fluctuate a factor of x
# due to uncertainty in irrigation efficiency
factor_unc %>%
    .[, factor:= floor(max / min)] %>%
    .[, .(number.countries = .N), factor] %>%
    .[order(factor)] %>%
    print()
```

##		factor	number.countries
##	1:	2	4
##	2:	3	15
##	3:	4	1
##	4:	5	4
##	5:	8	1
##	6:	12	1
##	7:	17	10
##	8:	18	18
##	9:	20	1
##	10:	24	6
##	11:	25	4
##	12:	26	8
##	13:	27	11
##	14:	28	14
##	15:	29	10
##	16:	30	5
##	17:	31	8
##	18:	32	6
##	19:	33	4
##	20:	34	3
##	21:	35	5
##	22:	36	1
##	23:	38	1
##	24:	39	3
##	25:	40	2
##	26:	41	1
##	27:	42	1
##	28:	47	1
##	29:	51	1
##	30:	52	3

```
## 31: 53 1
## factor number.countries
```

#### 3.1 Retrieve data from ISIMIP

```
# FUNCTIONS TO EXTRACT DATA FROM .NC FILES -
coords2country = function(points) {
  countriesSP <- rworldmap::getMap(resolution = 'low')</pre>
  pointsSP = sp::SpatialPoints(points, proj4string=CRS(proj4string(countriesSP)))
  indices = sp::over(pointsSP, countriesSP)
  indices$ADMIN
}
# Function to load and extract data from .nc files from ISIMIP
open_nc_files <- function(file, dname, selected.years, vec) {
 ncin <- nc_open(file)</pre>
  # get longitude, latitude, time
 lon <- ncvar_get(ncin, "lon")</pre>
  lat <- ncvar_get(ncin, "lat")</pre>
  # Get variable
  tmp_array <- ncvar_get(ncin, dname)</pre>
 m <- lapply(selected.years, function(x) vec[[x]])</pre>
  out <- lapply(m, function(x) {
    tmp_slice <- lapply(x, function(y) tmp_array[, , y])</pre>
    # create dataframe -- reshape data
    # matrix (nlon*nlat rows by 2 cols) of lons and lats
    lonlat <- as.matrix(expand.grid(lon,lat))</pre>
    # vector of `tmp` values
    tmp_vec <- lapply(tmp_slice, function(x) as.vector(x))</pre>
    # create dataframe and add names
    tmp_df01 <- lapply(tmp_vec, function(x) data.frame(cbind(lonlat, x)))</pre>
    names(tmp_df01) \leftarrow x
    da <- lapply(tmp_df01, data.table) %>%
      rbindlist(., idcol = "month") %>%
      na.omit()
    # Convert coordinates to country
    Country <- coords2country(da[1:nrow(da), 2:3])</pre>
    df <- cbind(Country, da)</pre>
    setDT(df)
    out <- na.omit(df)[, .(Water.Withdrawn = sum(x)), Country]</pre>
    out[, Water.Withdrawn:= Water.Withdrawn * 10000]
    out[, Continent:= countrycode(out[, Country],
                                    origin = "country.name",
                                    destination = "continent")] %>%
      .[, Code:= countrycode(out[, Country],
```

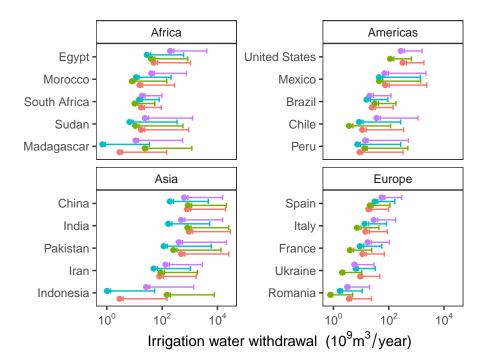
```
origin = "country.name",
                              destination = "un")] %>%
      .[, Country:= countrycode(out[, Code],
                                 origin = "un",
                                 destination = "country.name")] %>%
      .[!Continent == "Oceania"]
    setcolorder(out, c("Country", "Continent", "Code", "Water.Withdrawn"))
 })
 return(out)
}
# READ IN NC FILES ---
# Define settings
vecs <- 1:((2010 - 1970) * 12)
vec <- split(vecs, ceiling(seq_along(vecs) / 12))</pre>
names(vec) <- 1971:2010
selected.years <- "2010"
dname <- "pirrww"</pre>
files <- list("h08 wfdei nobc hist varsoc co2 pirrww global monthly 1971 2010.nc",
              "pcr-globwb_wfdei_nobc_hist_varsoc_co2_pirrww_global_monthly_1971_2010.nc",
              "lpjml wfdei nobc hist varsoc co2 pirrww global monthly 1971 2010.nc",
              "watergap2_wfdei_nobc_hist_varsoc_co2_pirrww_global_monthly_1971_2010.nc")
names.isimip <- c("HO8", "PCR-GLOBWB", "LPJmL", "WaterGap")</pre>
isimip.dt <- mclapply(files, function(x)</pre>
  open_nc_files(file = x, dname = dname, selected.years = selected.years, vec = vec),
mc.cores = detectCores() * 0.75)
# EXTRACT CORRECTIVE COEFFICIENTS FOR IRRIGATION EFFICIENCY FOR LPJML ------
ncin <- nc_open("irrigation_project_efficiencies.nc")</pre>
lon <- ncvar_get(ncin, "lon")</pre>
lat <- ncvar_get(ncin, "lat")</pre>
tmp_array <- ncvar_get(ncin)</pre>
lonlat <- as.matrix(expand.grid(lon,lat))</pre>
da <- na.omit(cbind(lonlat, as.vector(tmp_array))) %>%
  data.frame() %>%
 na.omit()
Country <- coords2country(da[1:nrow(da), 1:2])</pre>
lpjml_efficiencies <- cbind(Country, da) %>%
 na.omit() %>%
  data.table() %>%
 [, (Ep = mean(V3)), Country]
```

```
# ARRANGE NC FILES -----
names(isimip.dt) <- names.isimip</pre>
isimip.dt <- lapply(isimip.dt, function(x) rbindlist(x)) %>%
  rbindlist(., idcol = "Model") %>%
  na.omit() %>%
  # To correct for duplicate country in Cyprus
  .[, .(Water.Withdrawn = mean(Water.Withdrawn)), .(Model, Country, Continent, Code)]
lpjml_harmonized <- merge(isimip.dt[Model == "LPJmL"], lpjml_efficiencies, all.x = TRUE) %>%
  .[, Water.Withdrawn:= Water.Withdrawn * Ep] %>%
  .[, Ep:= NULL]
isimip.dt <- rbind(isimip.dt[!Model == "LPJmL"], lpjml_harmonized)</pre>
fwrite(isimip.dt, "isimip.dt")
# MERGE UNCERTAINTY IN EP WITH ISIMIP DATA -----
efficiency.dt <- copy(uncertainty.dt) %>%
  setnames(., "V1", "Ep")
ghm.dt <- dcast(isimip.dt, Country + Continent + Code ~ Model, value.var = "Water.Withdrawn")</pre>
full.dt <- merge(efficiency.dt, ghm.dt, by = c("Country", "Continent"), all.x = TRUE) %>%
  .[, (names.isimip):= lapply(.SD, function(x) x / Ep), .SDcols = names.isimip]
tmp.dt <- melt(full.dt, measure.vars = names.isimip, variable.name = "Model",</pre>
               value.name = "IWW_corrected")
ghm.large <- melt(ghm.dt, measure.vars = names.isimip, variable.name = "Model",</pre>
     value.name = "IWW")
gm.uncertainty <- tmp.dt[, .(min = min(IWW_corrected), max = max(IWW_corrected)),</pre>
                          .(Country, Continent, Model)]
gm.dt <- merge(ghm.large, gm.uncertainty)</pre>
# PLOT UNCERTAINTY IN EP WITH ISIMIP DATA -----
countries_list <- c("Egypt", "Sudan", "South Africa", "Morocco", "Madagascar",</pre>
                    "United States", "Mexico", "Brazil", "Chile", "Peru",
                    "India", "China", "Pakistan", "Iran", "Indonesia",
                    "Italy", "Spain", "France", "Ukraine", "Romania")
gm.dt[Country %in% countries_list] %>%
  ggplot(., aes(reorder(Country, IWW), IWW, color = Model)) +
  geom_point(position = position_dodge(0.7)) +
  geom_errorbar(aes(ymin = min,
                    ymax = max),
                position = position_dodge(0.7)) +
  scale_y_log10(breaks = trans_breaks("log10", function(x) 10 ^ (2 * x)),
```

```
labels = trans_format("log10", math_format(10 ^ .x))) +
scale_color_discrete(name = "GM") +
labs(y = expression(paste("Irrigation water withdrawal ", " ", "(", 10^9, m^3/year, "", ")")
        x = "") +
facet_wrap(~Continent, scales = "free_y") +
coord_flip() +
theme_AP()
```

## Warning: Removed 1 rows containing missing values (geom\_point).

GM → H08 → PCR-GLOBWB → LPJmL → WaterGap



```
position = position_dodge(0.7)) +
  scale_y_log10(breaks = trans_breaks("log10", function(x) 10 ^ (2 * x)),
                 labels = trans_format("log10", math_format(10 ^ .x))) +
  scale_color_manual(name = "GM", values = wes_palette("Royal1")) +
  labs(y = expression(paste("Irrigation water withdrawal ", " ", "(", 10^9, m^3/year, "", ")")
       x = "") +
  facet_wrap(~Continent, scales = "free_y") +
  coord flip() +
  theme_AP() +
  guides(color = guide_legend(nrow = 2, byrow = TRUE))
                      WaterGap, LPJmL, H08, PCR-GLOBWB
             GM
                      WaterGap, LPJmL, H08, PCR-GLOBWB
                      + uncertainty in irrigation efficiency
                Africa
                                            Americas
     Egypt -
                                 Mexico ·
                            United States -
    Sudan
Madagascar
                                  Chile ·
  Morocco
                                   Peru ·
South Africa
                                  Brazil
                 Asia
                                             Europe
     India -
                                  Spain -
  Pakistan
                                   Italy
     China ·
                                 France
 Indonesia -
                                Ukraine
      Iran
                                Romania
                 10<sup>2</sup>
                       10<sup>4</sup>
          10<sup>0</sup>
                                              10^{2}
              Irrigation water withdrawal (109m3/year)
# PLOT RANGES OF STRUCTURAL UNCERTAINTY AND RANGES OF
# STRUCTURAL UNCERTAINTY + UNCERTAINTY IN IRRIGATION EFFICIENCY (COMPLETE)
dd <- list()
for (i in 1:length(list_continents)) {
  dd[[i]] <- rbind(range.gm, range.study) %>%
    .[, mean:= (min + max) / 2] \%
    .[Continent %in% list_continents[[i]]] %>%
    ggplot(., aes(reorder(Country, mean), mean, color = Approach)) +
    geom_errorbar(aes(ymin = min,
                        ymax = max),
                   position = position_dodge(0.7)) +
    scale_y_log10(breaks = trans_breaks("log10", function(x) 10 ^ (2 * x)),
                    labels = trans_format("log10", math_format(10 ^ .x))) +
    scale_color_manual(name = "GM", values = wes_palette("Royal1")) +
    labs(y = expression(paste("Irrigation water withdrawal ", " ", "(", 10^9, m^3/year, "", ")
         x = "") +
```

facet\_wrap(~Continent, scales = "free\_y") +

```
coord_flip() +
    theme_AP() +
    guides(color = guide_legend(nrow = 2, byrow = TRUE))
}
dd
```

## [[1]]

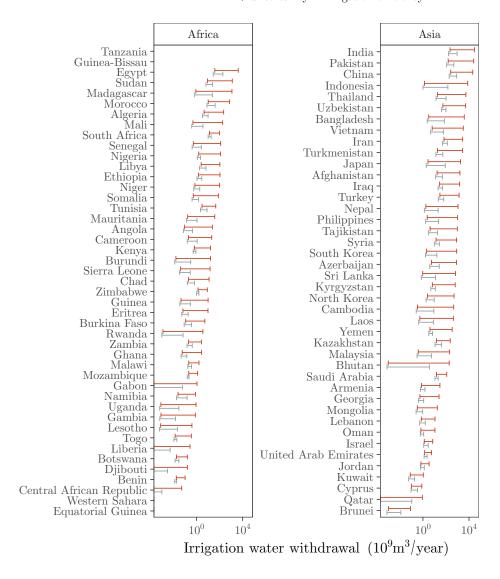
## Warning: Transformation introduced infinite values in continuous y-axis

Warning: Transformation introduced infinite values in continuous y-axis

## Warning: Transformation introduced infinite values in continuous y-axis

WaterGap, LPJmL, H08, PCR-GLOBWB

GMWaterGap, LPJmL, H08, PCR-GLOBWB + uncertainty in irrigation efficiency

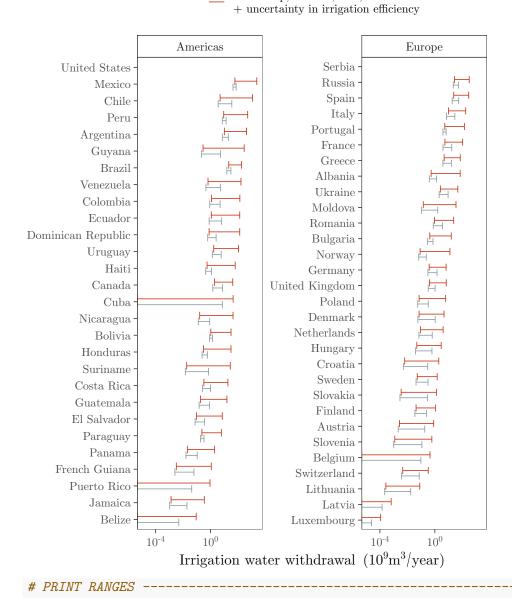


```
##
## [[2]]
```

## Warning: Transformation introduced infinite values in continuous y-axis

— WaterGap, LPJmL, H08, PCR-GLOBWB

GM \_\_\_ WaterGap, LPJmL, H08, PCR-GLOBWB



# print(range.study, n = Inf)

## 4 Sensitivity analysis

# SAMPLE MATRIX DISTRIBUTIONS ----# Define labels

```
label_facets <- c("Ea_surf" = "$E_{a_{su}})",
                   "Ec_surf" = "$E_{c_{su}}$",
                   "Ea_sprinkler" = "$E_{a_{sp}}$",
                   "Ec_sprinkler" = "E_{c_{sp}}",
                   "Ea_micro" = "$E_{a_{mi}}$",
                   "Ec_micro" = "$E_{c_{mi}}$",
                   "Proportion_large" = "$f_L$",
                   "m" = "$m$",
                   "r_L" = "$r_L$")
mat <- data.table(full_sample_matrix(IFT = "Jager", Country = "Spain")$matrix)</pre>
mat <- mat[, Proportion_large:= NULL]</pre>
## Warning in `[.data.table`(mat, , `:=`(Proportion_large, NULL)): Column
## 'Proportion_large' does not exist to remove
melt(mat, measure.vars = colnames(mat)) %>%
  ggplot(., aes(value)) +
  geom_histogram() +
  labs(x = "Value", y = "Counts") +
  scale_x_continuous(breaks = pretty_breaks(n = 3)) +
  facet_wrap(~variable) +
  theme_AP()
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
           Ea surf
                    Ea sprinkler
                                Ec surf
                                          Ec sprinkler
  150000
  100000
   50000
       0
                     Ec_micro
          Ea_micro
                                             r_L
Counts 150000 50000 50000
                                  2
                                     4
                                         0
                                            2
  150000
  100000
   50000
                       2
                            Value
# EXTRACT SOBOL' INDICES ----
ind <- lapply(y$`Rohwer et al. 2007`, function(x) x[["indices"]]$results)</pre>
```

names(ind) <- rohwer\$Country</pre>

ind <- rbindlist(ind, idcol = "Country")</pre>

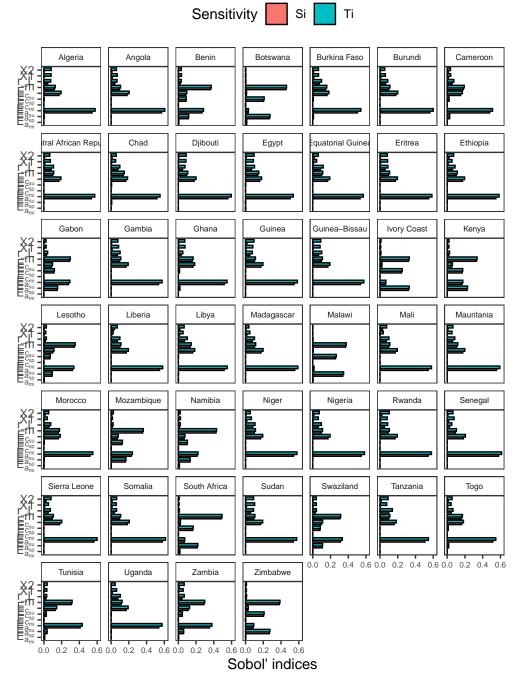
```
ind[, Continent:= countrycode(ind[, Country], origin = "country.name",
                                destination = "continent")]
## Warning in countrycode_convert(sourcevar = sourcevar, origin = origin, destination = dest,
tmp.ift <- split(rohwer, rohwer$IFT)</pre>
out <- list()</pre>
for(i in names(tmp.ift)) {
  out[[i]] <- ind[Country %in% tmp.ift[[i]][, Country]]</pre>
}
# PLOT SOBOL' INDICES ----
ind.dt <- rbindlist(out, idcol = "IFT") %>%
  .[, IFT:= factor(IFT, levels = c("Surface", "Sprinkler", "Micro", "Mixed"))]
tmp <- ind.dt[, .(mean = mean(original), sd = sd(original)),</pre>
               .(sensitivity, parameters, IFT)]
tmp2 <- tmp[!IFT == "Mixed"][, parameters:= ifelse(parameters == "Ea_surf", "$E_a$",</pre>
                                                       ifelse(parameters == "Ec_surf", "$E_c$",
                                                               ifelse(parameters == "Ea_sprinkler",
                                                                       ifelse(parameters == "Ec_spring)
                                                                              ifelse(parameters == "]
                                                                                      ifelse(paramete
rbind(tmp[IFT == "Mixed"], tmp2) %>%
  ggplot(., aes(parameters, mean, fill = sensitivity), color = black) +
  geom_bar(stat = "identity", position = position_dodge(0.6), color = "black") +
  geom_errorbar(aes(ymin = mean - sd, ymax = mean + sd), position = position_dodge(0.6)) +
  scale_x_discrete(labels = label_facets) +
  scale_fill_discrete(name = "Sensitivity", labels = c("$S_i$", "$T_i$")) +
  labs(x = "", y = "Sobol' indices") +
  facet_grid(~IFT, space = "free_x", scale = "free_x") +
  theme_AP()
                           Sensitivity
            Surface
                           Sprinkler
                                       Micro
                                                         Mixed
Sopol, indices 0.6 0.2 0.0
                                     E_a E_c m E_{a_{sp}}E_{a_{su}}E_{c_{sp}}E_{c_{su}} m r_L X1 X2
      E_a E_c m r_L X1 X2
                          E_a E_c m
```

# EXTRACT SOBOL' INDICES FOR JAGER --

```
jager.tmp <- lapply(y[["Jägermeyr et al. 2015"]], function(x) x$indices$results)</pre>
names(jager.tmp) <- new.rohwer$Country</pre>
jager.ind <- rbindlist(jager.tmp, idcol = "Country") %>%
  .[, Continent:= countrycode(.[, Country],
                             origin = "country.name",
                             destination = "continent")] %>%
  .[, parameters:= ifelse(parameters == "Ea_surf", "E[a[su]]",
                         ifelse(parameters == "Ec_surf", "E[c[su]]",
                                 ifelse(parameters == "Ea_sprinkler", "E[a[sp]]",
                                        ifelse(parameters == "Ec_sprinkler", "E[c[sp]]",
                                               ifelse(parameters == "Ea_micro", "E[a[mi]]",
                                                      ifelse(parameters == "Ec_micro", "E[c[mi]]
                                                              ifelse(parameters == "Proportion_1:
## Warning in countrycode_convert(sourcevar = sourcevar, origin = origin, destination = dest,
Continent_vector <- c("Africa", "Americas", "Asia", "Europe")</pre>
lapply(Continent_vector, function(x)
  ggplot(jager.ind[Continent == x], aes(parameters, original, fill = sensitivity), color = bla
    geom_bar(stat = "identity", position = position_dodge(0.6), color = "black") +
    scale_fill_discrete(name = "Sensitivity", labels = c("Si", "Ti")) +
    labs(x = "", y = "Sobol' indices") +
    scale_x_discrete(labels = ggplot2:::parse_safe) +
    coord_flip() +
    scale_y_continuous(breaks = pretty_breaks(n = 3)) +
    facet_wrap(~Country) +
    theme AP() +
    theme(strip.text.x = element_text(size = 6),
          axis.text.x = element_text(size = 6)) +
    ggtitle(x)
```

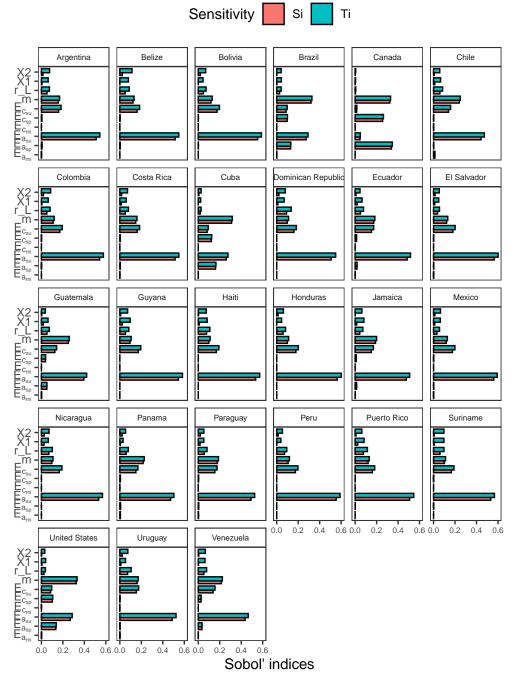
## [[1]]

## Africa



## ## [[2]]

## **Americas**



## ## [[3]]

## Asia



## ## [[4]]

# Europe

