

Code obfuscation through Mixed Boolean-Arithmetic expressions

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https://github.com/arnaugamez/talks/raw/master/2022/00_h-c0n/slides.pdf

About



Hacker, Reverse Engineer & Mathematician.

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 @arnaugamez



 @FuraLabs

Warning

This presentation may contain traces of maths and assembly

Agenda



1. Code obfuscation
2. Preliminary MBA concepts
 - Introduction and Motivation
 - Obfuscation vs Cryptography
 - Definitions
 - Polynomial MBA expressions
 - Linear MBA expressions
3. Obfuscation with MBA expressions
 - MBA rewriting
 - Insertion of identities
 - Opaque constants



Code obfuscation

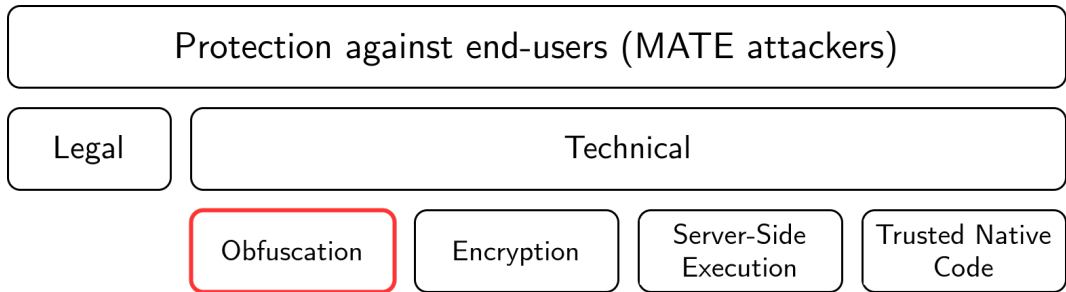
Context



Technical protection against Man-At-The-End (MATE) attacks, where the attacker/analyst has an instance of the program and completely controls the environment where it is executed.



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Code obfuscation is the process of transforming an input program P into a functionally equivalent program P' which is harder to analyze and to extract information that from P .

$$P \longrightarrow \boxed{\text{Obfuscation}} \longrightarrow P'$$



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Motivation: ~~prevent~~ *complicate reverse engineering.*

Presence



Software protection:

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Software protection:
Intellectual property



Software protection:

- Intellectual property

- Digital Rights Management (DRM)



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- Anti-cheating



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Malware threats:



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Malware threats:

- Avoid automatic signature detection



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Malware threats:

- Avoid automatic signature detection

- Slow down analysis → time → money



Apply a **transformation** to mess (complicate) the program's control-flow and/or data-flow at **different abstraction levels** (source code, compiled binary or an intermediate representation) and affecting **different target units** (whole program, function, basic block or instruction).



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Remark: many “weak” techniques can be combined to create a “hard” obfuscation transformation.



Preliminary MBA concepts



In a nutshell, a Mixed Boolean-Arithmetic (MBA) expression is composed of integer arithmetic operators, e.g. $(+, -, \times)$ and bitwise operators, e.g. $(\wedge, \vee, \oplus, \neg)$.



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$$E = (x \oplus y) + 2(x \wedge y)$$



MBA expressions can be leveraged to **obfuscate the data-flow** of code by iteratively applying rewriting rules and function identities that complicate (obfuscate) the initial expression while **preserving its semantic behavior**.



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Combination of operators from these different fields **do not interact well together**: we have no rules (distributivity, factorization...) or general theory to deal with this mixing of operators.

Obfuscation vs Cryptography



In **cryptography**, the MBA expression is the direct result of the algorithm description. The resulting cryptosystem has to verify a set of properties (e.g. non-linearity, high algebraic degree) from a *black-box* point of view.

Obfuscation vs Cryptography



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The complex form of writing is directly related to some kind of intrinsic computational (semantic) complexity for the resulting function: one wants the inverse computation to be difficult to deduce (without knowing the key).

Obfuscation vs Cryptography



In **obfuscation**, the MBA expression is the result of rewriting iterations from a simpler expression which can have very simple *black-box* characteristics.

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There is no direct relation between the complex form of writing and any intrinsic computational (semantic) complexity of the resulting expression.

On the contrary, when obfuscating simple expressions, one knows that the complex form of writing is related to a semantically simpler expression.



We will be focusing on MBA expressions
in the context of code (de)obfuscation

Definitions



We choose to define MBA expressions by **explicitly describing the different building blocks** (operators) that compose them and how they are bundled together.

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Linear MBA expressions \subset Polynomial MBA expressions

Polynomial MBA expressions



A polynomial MBA expression consists of a **sum of terms**, each one composed by an **n -bit constant** a_i times the **product** of several **bitwise expressions** on **a number t of n -bit variables**.

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$$E = \sum_{i \in I} a_i \cdot \left(\prod_{j \in J_i} e_{i,j}(x_1, \dots, x_t) \right)$$

Polynomial MBA expressions



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Example

$$E = \underline{\underline{\underline{43(x \wedge y \vee z)^2((x \oplus y) \wedge z \vee t)}}} + \underline{\underline{\underline{2x}}} + \underline{\underline{\underline{123(x \vee y)zt^2}}}$$

Linear MBA expressions



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Note: In practice, you can vaguely think of linearity as a restriction not allowing variables to end up being multiplied together.

Linear MBA expressions



$$E = \sum_{i \in I} a_i \cdot e_i(x_1, \dots, x_t)$$

Example

$$E = \underbrace{(x \oplus y)}_{\text{red}} + 2 \underbrace{(x \wedge y)}_{\text{blue}}$$

Linear MBA expressions



Notice that, assuming variables of the same *bit size*, the previous MBA expression example $E = (x \oplus y) + 2(x \wedge y)$ simplifies to $E_{simp} = x + y$.

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Namely, E is a more complex expression than E_{simp} syntactically speaking, but they are semantically equivalent.

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```
from z3 import *
x = BitVec('x', 8)
y = BitVec('y', 8)
E = (x ^ y) + 2 * (x & y)    #  $E = (x \oplus y) + 2(x \wedge y)$ 
E_simp = x + y              #  $E_{simp} = x + y$ 
prove (E == E_simp)         #  $E \stackrel{?}{=} E_{simp}$ 
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```

```
$ python eq.py
proved
```



Obfuscation with MBA expressions

Obfuscation idea



The previous example already suggests a basic obfuscation idea: we could replace the arithmetic sum $+$ of two variables in our code by the more complex expression involving \oplus and \wedge boolean operators, while preserving the code semantics.

Obfuscation idea



Given an MBA expression E_1 , we are interested in generating a **semantically equivalent** expression E_2 which is **syntactically more complex** than the initial expression E_1 .

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MBA rewriting & Insertion of identities



A chosen operator is rewritten with an equivalent MBA expression.



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Example

$$x + y \rightarrow (x \oplus y) + 2 \times (x \wedge y)$$

Insertion of identities



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Note: *For our usage, you can vaguely think of affine functions as those with the form $f(e) = a \cdot e + b$, where a, b are n -bit constants and e is our MBA subexpression.*

Insertion of identities



Example

Let $E_1 = x + y$, and the following functions f and f^{-1} on 8 bits:

$$f : x \mapsto 39x + 23 \qquad f^{-1} : x \mapsto 151x + 111$$

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Then apply the insertion of identities produced by f and f^{-1} :

$$E_{tmp} = f(E_2) = 39 \times E_2 + 23$$

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Finally, expand E_3 to observe the final obfuscated expression:

$$E_3 = 151 \times (39 \times ((x \oplus y) + 2 \times (x \wedge y)) + 23) + 111$$

Practical demo



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$$E_1 = x + y$$

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Practical demo



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Task:

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Practical demo



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Practical demo



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Task:

- 1 Compare syntactic complexity of E_1 , E_2 and E_3 .
- 2 Observe semantic equivalence of E_1 , E_2 and E_3 .
- 3 Prove semantic equivalence of E_1 , E_2 and E_3 .

Practical demo



Task 1: Compare syntactic complexity of E_1 , E_2 and E_3 .

Practical demo



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{
    return x+y;
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movzx edx, byte [var_4h]
movzx eax, byte [var_8h]
add     eax, edx
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Practical demo



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uint8_t E2(uint8_t x, uint8_t y)
{
    return (x^y)+2*(x&y);
}
```

```
movzx eax, byte [var_4h]
xor     al, byte [var_8h]
mov     edx, eax
movzx   eax, byte [var_4h]
and     al, byte [var_8h]
add     eax, eax
add     eax, edx
```

Practical demo



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movzx  eax, byte [var_4h]
and    al, byte [var_8h]
add    eax, eax
add    eax, edx
```

```
uint8_t E3(uint8_t x, uint8_t y)
{
    return 151*(39*((x^y)+2*(x&y))+23)+111;
}
```

```
movzx eax, byte [var_4h]
xor    al, byte [var_8h]
movzx  edx, al
movzx  eax, byte [var_4h]
and    al, byte [var_8h]
movzx  eax, al
add    eax, eax
add    eax, edx
imul   eax, eax, 0x27
add    eax, 0x17
mov    edx, 0xffffffff97
imul   eax, edx
add    eax, 0x6f
```


Practical demo



Task 2: Observe semantic equivalence of E_1 , E_2 and E_3 .

Practical demo



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#include <stdio.h>
#include <stdint.h>
#include <stdlib.h>

uint8_t E1(uint8_t x, uint8_t y)
{ return x + y; }
uint8_t E2(uint8_t x, uint8_t y)
{ return (x ^ y) + 2 * (x & y); }
uint8_t E3(uint8_t x, uint8_t y)
{ return 151 * (39 * ((x ^ y) + 2 * (x & y)) + 23) + 111; }

int main(int argc, char* argv[])
{
    uint8_t x = (uint8_t) atoi (argv[1]);
    uint8_t y = (uint8_t) atoi (argv[2]);
    printf ("%s(%d, %d) = %d\n", "E1", x, y, E1(x, y));
    printf ("%s(%d, %d) = %d\n", "E2", x, y, E2(x, y));
    printf ("%s(%d, %d) = %d\n", "E3", x, y, E3(x, y));
    return 0;
}
```

Practical demo



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    printf ("%s(%d, %d) = %d\n", "E2", x, y, E2(x, y));
    printf ("%s(%d, %d) = %d\n", "E3", x, y, E3(x, y));
    return 0;
}
```

```
$ gcc linear_mba.c -o linear_mba
$ ./linear_mba 1 2
E1(1, 2) = 3
E2(1, 2) = 3
E3(1, 2) = 3
$ ./linear_mba 23 89
E1(23, 89) = 112
E2(23, 89) = 112
E3(23, 89) = 112
```

Practical demo

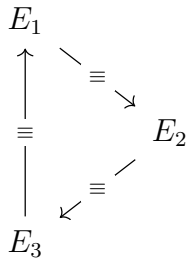


Task 3: Prove semantic equivalence of E_1 , E_2 and E_3 .

Practical demo



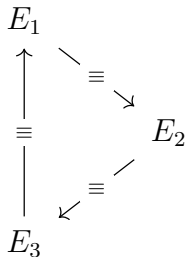
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Practical demo



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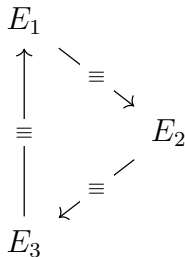


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x = BitVec('x', 8)  
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E1 = x + y  
E2 = (x ^ y) + 2 * (x & y)  
E3 = 151 * (39 * ((x ^ y) + 2 * (x & y)) + 23) + 111  
  
prove (E1 == E2)  
prove (E2 == E3)  
prove (E3 == E1)
```

Practical demo



Task 3: Prove semantic equivalence of E_1 , E_2 and E_3 .



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from z3 import *
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prove (E1 == E2)
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```

```
$ python prove.py
proved
proved
proved
```

Opaque constants



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A permutation polynomial is a polynomial that acts as a permutation of the elements of the set they apply to (in our case, n -bit values), i.e. they define a 1-to-1 map (bijection).

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A permutation polynomial is a polynomial that acts as a permutation of the elements of the set they apply to (in our case, n -bit values), i.e. they define a 1-to-1 map (bijection).

Thus, for any permutation polynomial P , there exists another one Q that defines the inverse map, i.e., for all n -bit X values we have that:

$$P(Q(X)) = X$$

Opaque constants



Let:

K be an n -bit target constant to hide,

Opaque constants



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P and Q polynomials with n -bit coefficients and acting as inverse 1-to-1 maps, i.e. $P(Q(X)) = X$ for all X ,

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E be an MBA expression of n -bit variables non-trivially equal to zero, i.e. $E(x_1, \dots, x_t) = 0$ for any input variables x_1, \dots, x_t .

Then, the constant K can be replaced by $P(E + Q(K))$ for any values taken by (x_1, \dots, x_t) .

Practical demo



Working on 8-bit values, let:

$$P(X) = 97X + 248X^2$$

$$Q(X) = 161X + 136X^2$$

$$E(x, y) = x - y + 2(\neg x \wedge y) - (x \oplus y)$$

Practical demo



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Practical demo



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- 2 Check that E defines a non-trivially equal to zero MBA expression, i.e. $E(x, y) = 0$ for all x, y .
- 3 Create an opaque constant function using P , Q and E to hide the constant $K = 123$.

Practical demo



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Task:

- 1 Check that P and Q define inverse maps, i.e. $P(Q(X)) = X$ for all X .
- 2 Check that E defines a non-trivially equal to zero MBA expression, i.e. $E(x, y) = 0$ for all x, y .
- 3 Create an opaque constant function using P , Q and E to hide the constant $K = 123$.
- 4 Check the previous opaque constant.

Practical demo



Task 1: Check that P and Q define inverse maps (bruteforce).

Practical demo



Task 1: Check that P and Q define inverse maps (bruteforce).

```
#include <stdio.h>
#include <stdint.h>
#include <stdlib.h>

uint8_t P(uint8_t x) { return 97*x + 248*x*x; }
uint8_t Q(uint8_t x) { return 161*x + 136*x*x; }

int main(int argc, char* argv[])
{
    uint8_t i = 0;
    do
    {
        if (P(Q(i)) != i) { printf("P(Q(X)) != X\n"); return -1; }
        i++;
    } while (i != 0);
    printf("P(Q(X)) = X\n");
    return 0;
}
```

Practical demo



Task 1: Check that P and Q define inverse maps (bruteforce).

```
#include <stdio.h>
#include <stdint.h>
#include <stdlib.h>

uint8_t P(uint8_t x) { return 97*x + 248*x*x; }
uint8_t Q(uint8_t x) { return 161*x + 136*x*x; }

int main(int argc, char* argv[])
{
    uint8_t i = 0;
    do
    {
        if (P(Q(i)) != i) { printf("P(Q(X)) != X\n"); return -1; }
        i++;
    } while (i != 0);
    printf("P(Q(X)) = X\n");
    return 0;
}
```

```
$ gcc check_poly.c -o check_poly
$ ./check_poly
P(Q(X)) = X
```

Practical demo



Task 1: Check that P and Q define inverse maps (SMT).



Task 1: Check that P and Q define inverse maps (SMT).

```
from z3 import *
X = BitVec('X', 8)

def P(X): return 97*X + 248*X*X
def Q(X): return 161*X + 136*X*X

prove(P(Q(X)) == X)
```



Task 1: Check that P and Q define inverse maps (SMT).

```
from z3 import *  
X = BitVec('X', 8)  
  
def P(X): return 97*X + 248*X*X  
def Q(X): return 161*X + 136*X*X  
  
prove(P(Q(X)) == X)
```

```
$ python check_poly.py  
proved
```

Practical demo



Task 2: Check that E is non-trivially equal to zero (bruteforce).

Practical demo



Task 2: Check that E is non-trivially equal to zero (bruteforce).

```
#include <stdio.h>
#include <stdint.h>
#include <stdlib.h>

uint8_t E(uint8_t x, uint8_t y) { return x-y + 2*(~x&y) - (x^y); }

int main(int argc, char* argv[])
{
    uint8_t i = 0; uint8_t j = 0;
    do
    {
        do
        {
            if (E(i, j) != 0) { printf("E(x, y) != 0\n"); return -1; }
            j++;
        } while (j != 0);
        i++;
    } while (i != 0);
    printf("E(x, y) = 0\n"); return 0;
}
```

Practical demo



Task 2: Check that E is non-trivially equal to zero (bruteforce).

```
#include <stdio.h>
#include <stdint.h>
#include <stdlib.h>
```

```
uint8_t E(uint8_t x, uint8_t y) { return x-y + 2*(~x&y) - (x^y); }
```

```
int main(int argc, char* argv[])
{
    uint8_t i = 0; uint8_t j = 0;
    do
    {
        do
        {
            if (E(i, j) != 0) { printf("E(x, y) != 0\n"); return -1; }
            j++;
        } while (j != 0);
        i++;
    } while (i != 0);
    printf("E(x, y) = 0\n"); return 0;
}
```

```
$ gcc check_mba.c -o check_mba
$ ./check_mba
E(x, y) = 0
```

Practical demo



Task 2: Check that E is non-trivially equal to zero (SMT).



Task 2: Check that E is non-trivially equal to zero (SMT).

```
from z3 import *  
x = BitVec('x', 8)  
y = BitVec('y', 8)  
  
def E(x, y): return x-y + 2*(~x&y) - (x^y)  
  
prove(E(x, y) == 0)
```



Task 2: Check that E is non-trivially equal to zero (SMT).

```
from z3 import *  
x = BitVec('x', 8)  
y = BitVec('y', 8)  
  
def E(x, y): return x-y + 2*(~x&y) - (x^y)  
  
prove(E(x, y) == 0)
```

```
$ python check_mba.py  
proved
```

Practical demo



Task 3: Create an opaque constant function.

Practical demo



Task 3: Create an opaque constant function.

```
from z3 import *

X = BitVec('X', 8)
def P(X): return 97*X + 248*X*X
def Q(X): return 161*X + 136*X*X

x = BitVec('x', 8)
y = BitVec('y', 8)
def E(x, y): return x-y + 2*(~x&y) - (x^y)

K = BitVecVal(123, 8)

# Opaque Constant
OC = P(E(x,y) + Q(K))

# Apply basic simplification rules
print (simplify(OC))
```

Practical demo



Task 3: Create an opaque constant function.

```
from z3 import *

X = BitVec('X', 8)
def P(X): return 97*X + 248*X*X
def Q(X): return 161*X + 136*X*X

x = BitVec('x', 8)
y = BitVec('y', 8)
def E(x, y): return x-y + 2*(~x&y) - (x^y)

K = BitVecVal(123, 8)

# Opaque Constant
OC = P(E(x,y) + Q(K))

# Apply basic simplification rules
print (simplify(OC))
```

```
$ python create_oc.py
195 +
97*x +
159*y +
194*~(x | ~y) +
159*(x ^ y) +
(163 + x + 255*y + 2*~(x | ~y) + 255*(x ^ y))*
(232 + 248*x + 8*y + 240*~(x | ~y) + 8*(x ^ y))
```

Practical demo



Task 4: Check an opaque constant function (bruteforce).

Practical demo



Task 4: Check an opaque constant function (bruteforce).

```
#include <stdio.h>
#include <stdint.h>
#include <stdlib.h>

uint8_t OC(uint8_t x, uint8_t y)
{
    return 195 + 97*x + 159*y +
        194*~(x | ~y) + 159*(x ^ y) +
        (163 + x + 255*y + 2*~(x | ~y) + 255*(x ^ y))*
        (232 + 248*x + 8*y + 240*~(x | ~y) + 8*(x ^ y));
}

int main(int argc, char* argv[])
{
    uint8_t i = 0; uint8_t j = 0;
    do
    {
        /* ... */
    }
```

```
do
{
    if (OC(i, j) != 123)
    {
        printf("OC(x, y) != 123\n");
        return -1;
    }
    j++;
} while (j != 0);
i++;
} while (i != 0);
printf("OC(x, y) = 123\n"); return 0;
}
```

Practical demo



Task 4: Check an opaque constant function (bruteforce).

```
#include <stdio.h>
#include <stdint.h>
#include <stdlib.h>

uint8_t OC(uint8_t x, uint8_t y)
{
    return 195 + 97*x + 159*y +
        194*~(x | ~y) + 159*(x ^ y) +
        (163 + x + 255*y + 2*~(x | ~y) + 255*(x ^ y))*
        (232 + 248*x + 8*y + 240*~(x | ~y) + 8*(x ^ y));
}

int main(int argc, char* argv[])
{
    uint8_t i = 0; uint8_t j = 0;
    do
    {
        /* ... */
    }
}
```

```
do
{
    if (OC(i, j) != 123)
    {
        printf("OC(x, y) != 123\n");
        return -1;
    }
    j++;
} while (j != 0);
i++;
} while (i != 0);
printf("OC(x, y) = 123\n"); return 0;
}
```

```
$ gcc check_oc.c -o check_oc
$ ./check_oc
OC(x, y) = 123
```

Practical demo



Task 4: Check an opaque constant function (SMT).



Task 4: Check an opaque constant function (SMT).

```
from z3 import *

x = BitVec('x', 8)
y = BitVec('y', 8)

def OC(x, y):
    return 195 + 97*x + 159*y +\
        194*~(x | ~y) + 159*(x ^ y) +\
        (163 + x + 255*y + 2*~(x | ~y) + 255*(x ^ y))*\
        (232 + 248*x + 8*y + 240*~(x | ~y) + 8*(x ^ y))

prove(OC(x, y) == 123)
```



Task 4: Check an opaque constant function (SMT).

```
from z3 import *
```

```
x = BitVec('x', 8)
```

```
y = BitVec('y', 8)
```

```
def OC(x, y):
```

```
    return 195 + 97*x + 159*y +\  
    194*~(x | ~y) + 159*(x ^ y) +\  
    (163 + x + 255*y + 2*~(x | ~y) + 255*(x ^ y))*\  
    (232 + 248*x + 8*y + 240*~(x | ~y) + 8*(x ^ y))
```

```
prove(OC(x, y) == 123)
```

```
$ python check_oc.py  
proved
```

Summary



We have seen how to apply several MBA obfuscation techniques: MBA rewriting, insertion of identities and opaque constants.

Summary



We have seen how to apply several MBA obfuscation techniques: MBA rewriting, insertion of identities and opaque constants.

For this purpose, we have used: rewrite rules, affine functions, non-trivially equal to zero MBA expressions and permutation polynomials.

What would come next?



Learn methods to generate:

What would come next?



Learn methods to generate:

- Non-trivially equal to zero MBA expressions

What would come next?



Learn methods to generate:

- Non-trivially equal to zero MBA expressions
- Linear MBA rewrite rules

What would come next?



Learn methods to generate:

- Non-trivially equal to zero MBA expressions
- Linear MBA rewrite rules
- Pairs of inverse affine functions

What would come next?



Learn methods to generate:

- Non-trivially equal to zero MBA expressions
- Linear MBA rewrite rules
- Pairs of inverse affine functions
- Pairs of inverse permutation polynomials



*Code deobfuscation by program synthesis-aided simplification of Mixed Boolean-Arithmetic expressions*¹ – Arnau Gàmez i Montolio

*Obfuscation with Mixed Boolean Arithmetic Expressions*² – Ninon Eyrolles

*Information Hiding in Software with Mixed Boolean-Arithmetic Transforms*³
– Y. Zhou et al.

¹<https://github.com/arnaugamez/tfg>

²<https://tel.archives-ouvertes.fr/tel-01623849/document>


³https://link.springer.com/chapter/10.1007/978-3-540-77535-5_5



https://github.com/arnaugamez/talks/tree/master/2022/00_h-c0n

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