

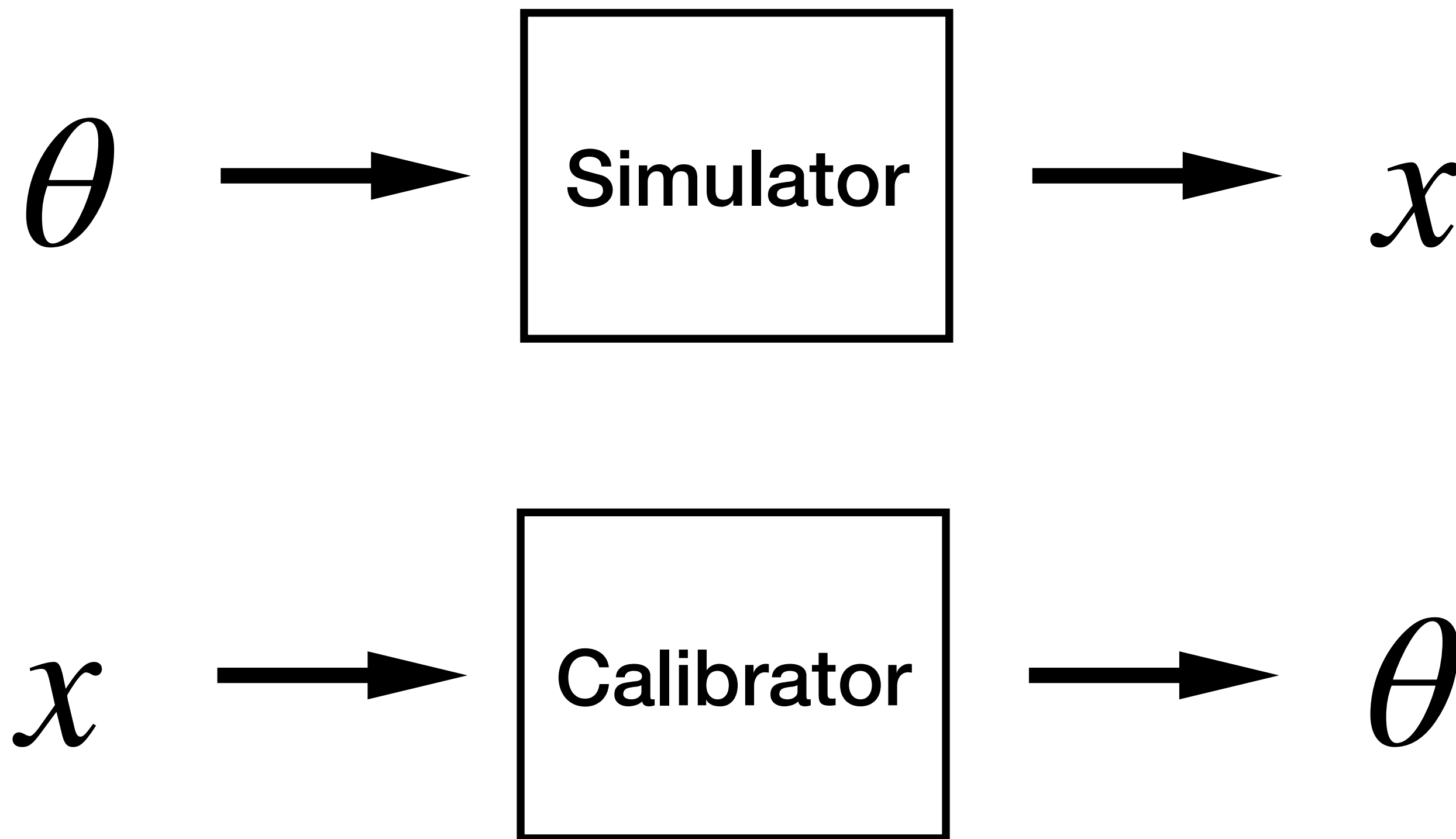
Bayesian calibration of differentiable agent-based models

Arнау Quera-Bofarull, Ayush Chopra, Anisoara Calinescu,
Michael Wooldridge, Joel Dyer

AI4ABM workshop — ICLR 2023



Calibration of ABMs



Why is it hard?

- Expensive simulator

+

- Large parameter space

Calibration requirements

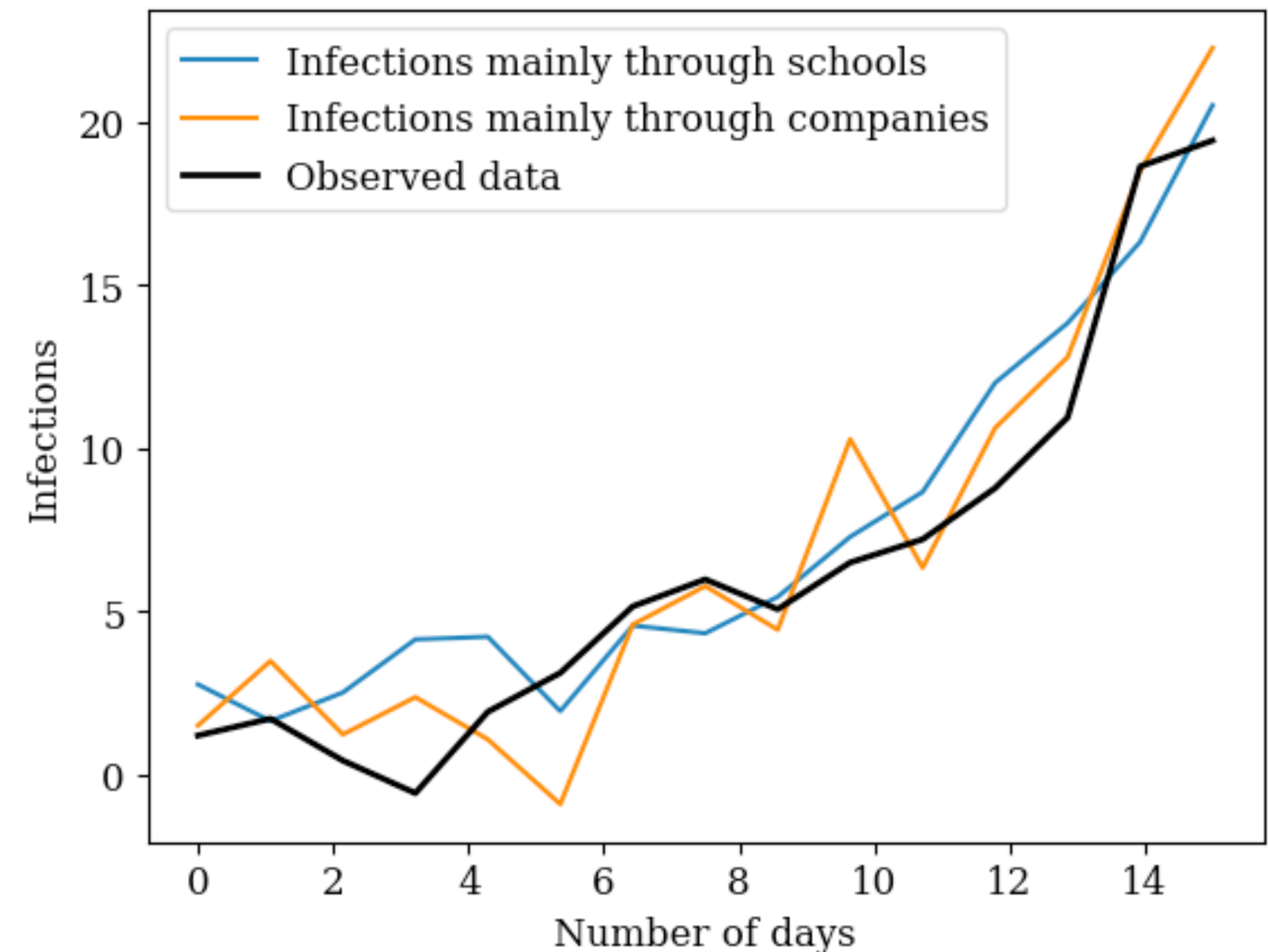
1. Uncertainty quantification

Ideally we want to get all θ that can generate x with a certain probability

Example

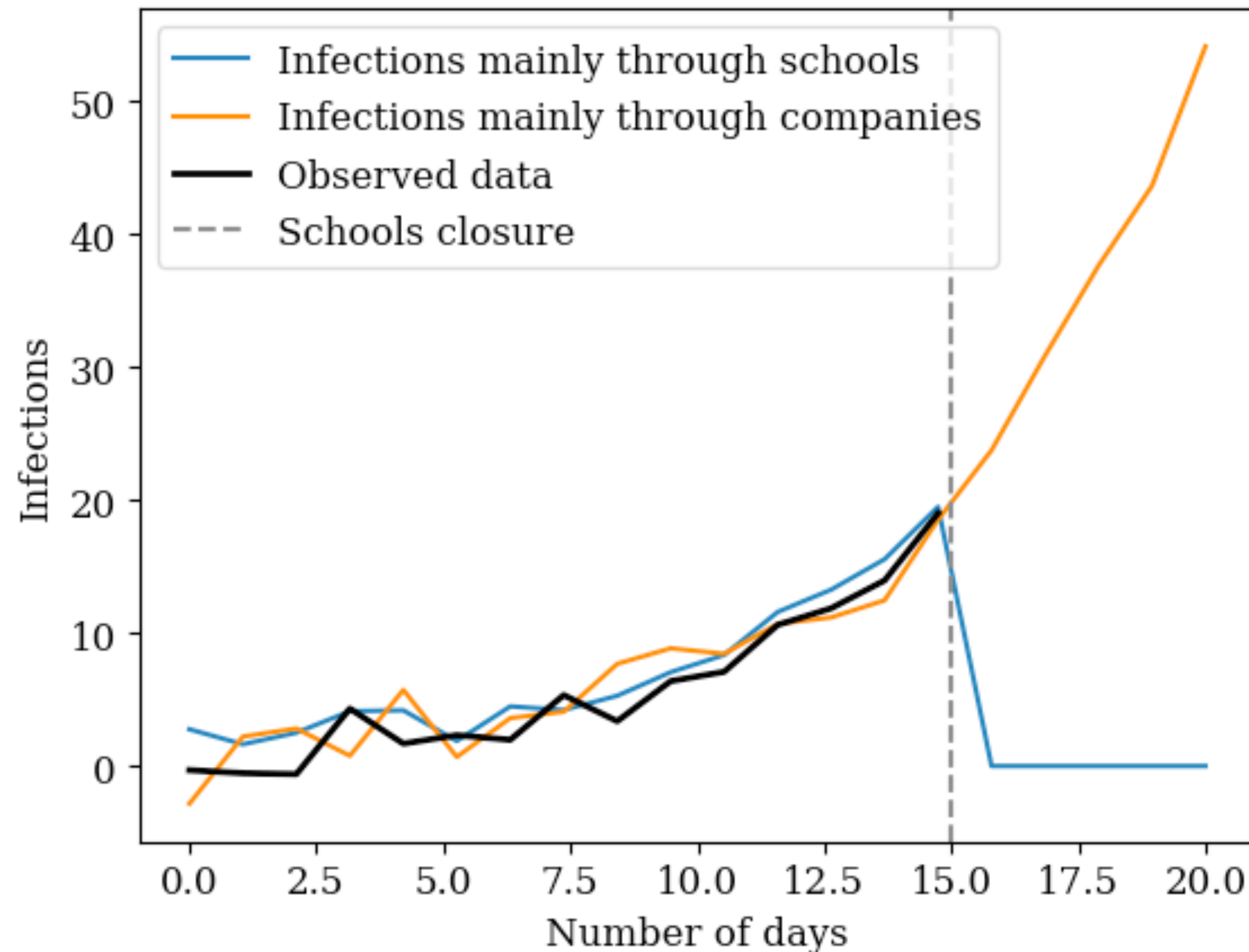
Epidemiological model with 2 parameters:

1. Reproduction number at schools
2. Reproduction number at companies



Calibration of ABMs

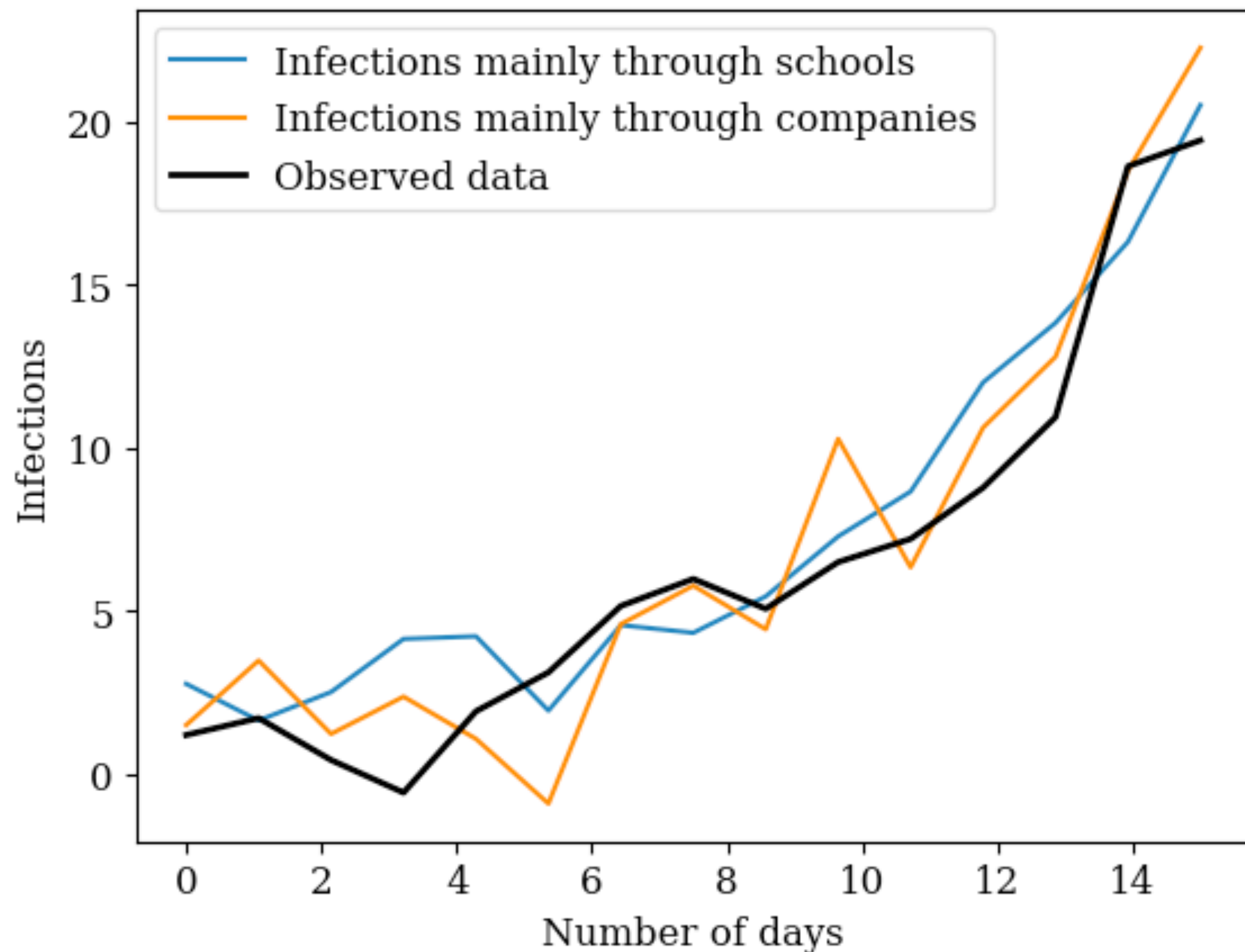
1. Uncertainty quantification (UQ)



Crucial for policy analysis

Calibration of ABMs

2. Expert (prior) knowledge



**Need to include prior information
in our calibration process**

Bayesian inference

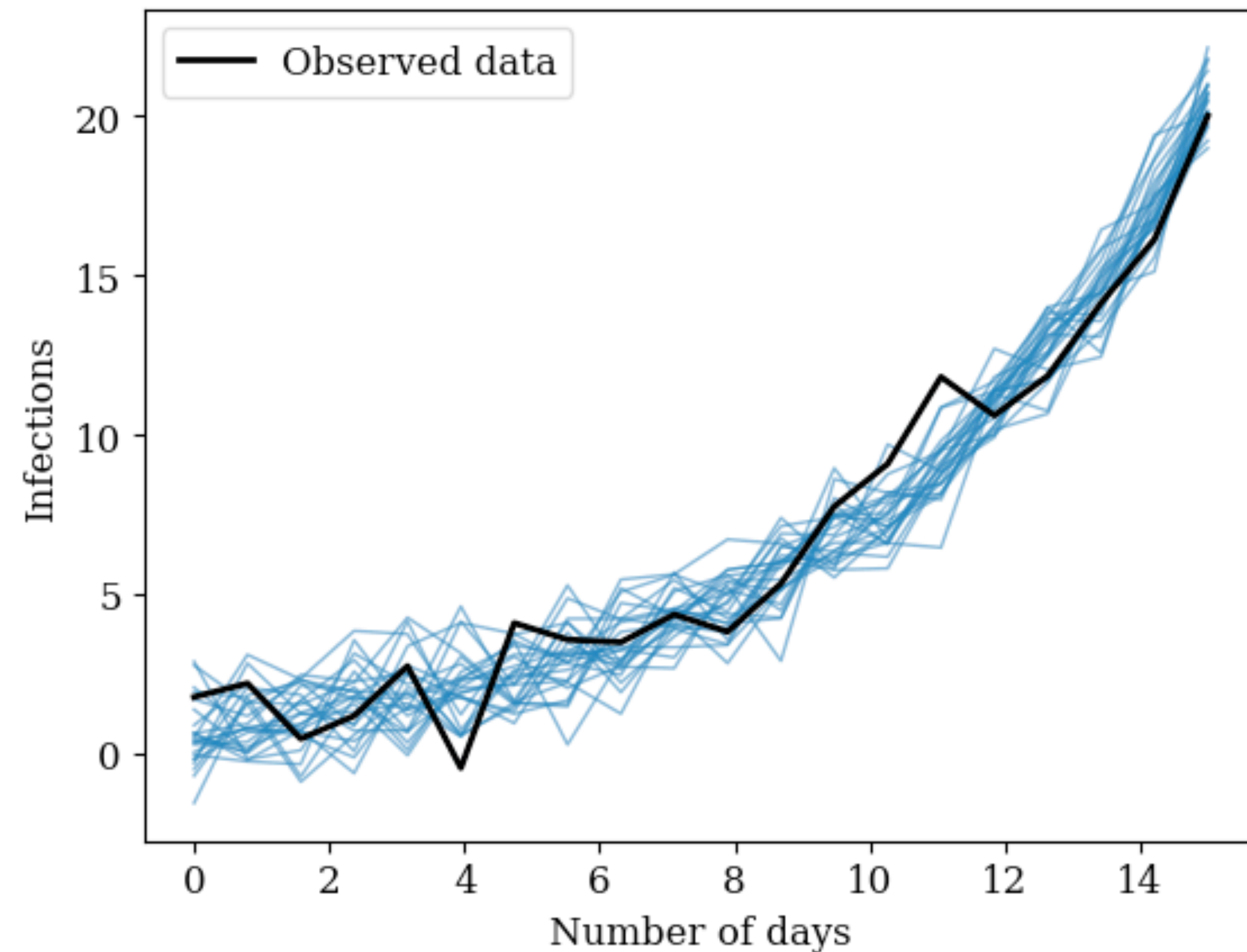
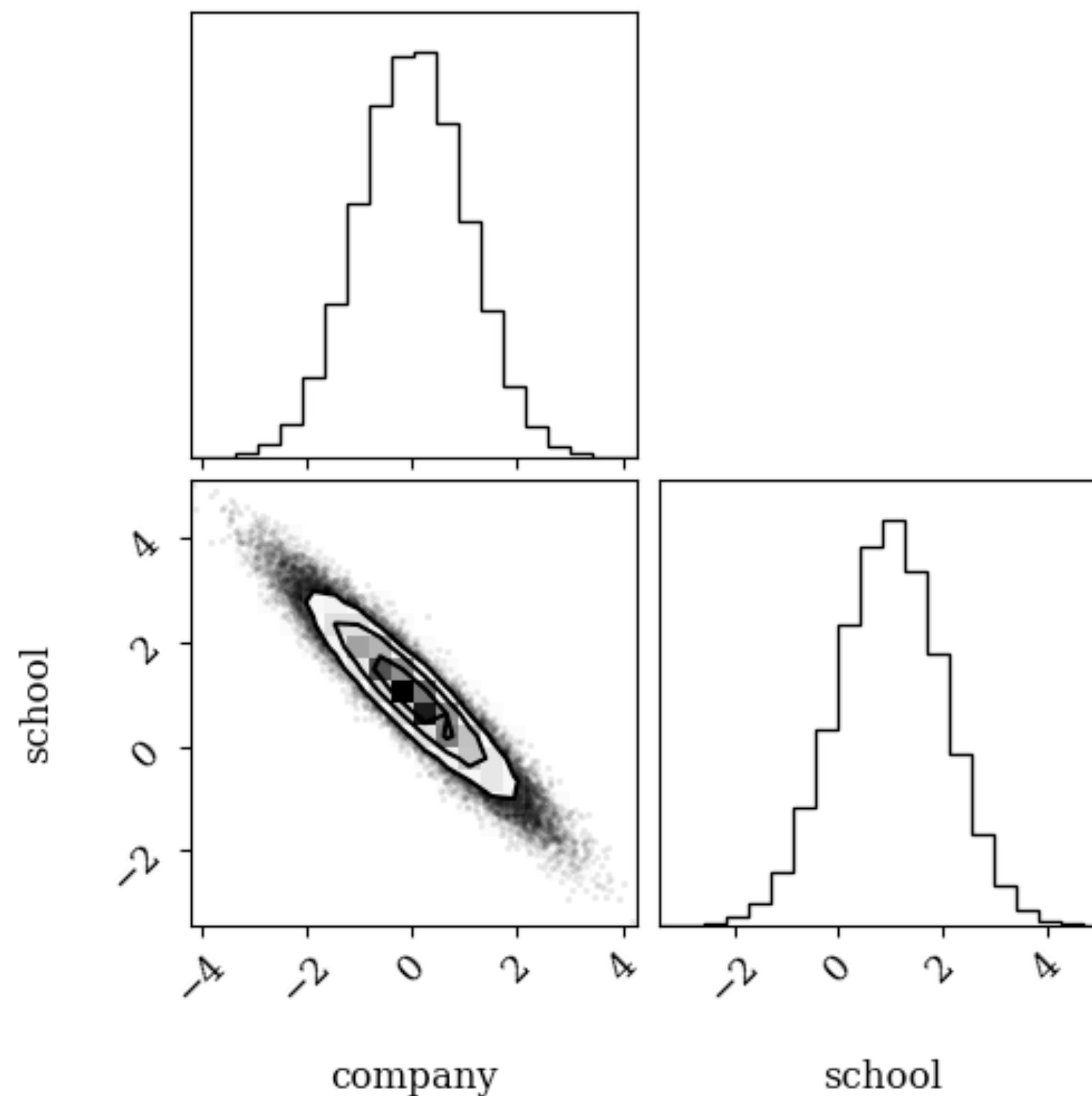
Allows to tackle both problems

$$p(\theta | x) \propto p(x | \theta) p(\theta)$$

posterior

likelihood

prior



Likelihood $p(x | \theta)$ is intractable for ABMs

Proposed solutions include



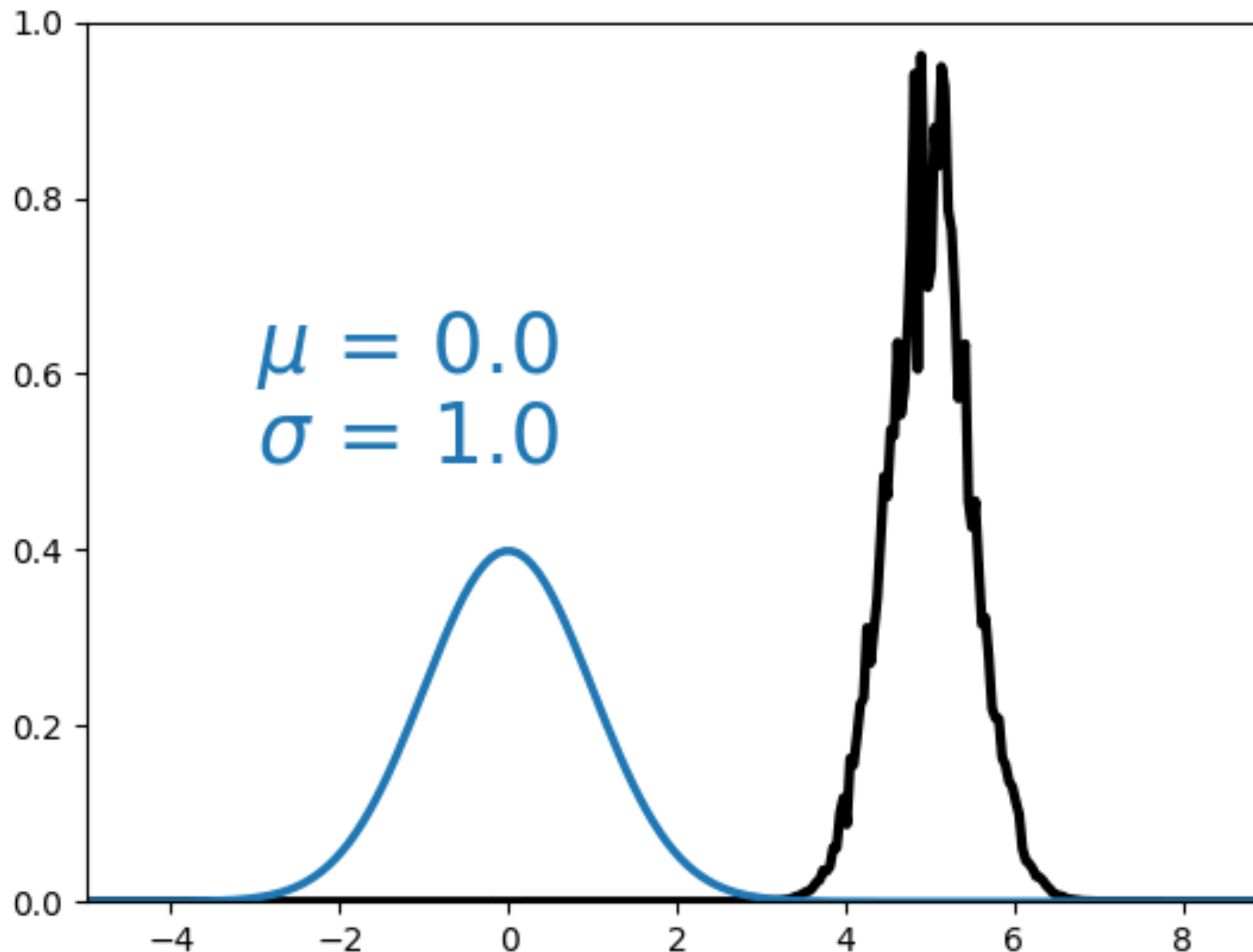
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graph TD; A[Proposed solutions include] --> B[Emulation]; A --> C[Approximate Bayesian Computation]; A --> D[Neural density ratio estimation];
```

Emulation

Approximate Bayesian Computation

Neural density ratio estimation

Variational Inference: Bayesian inference as an optimisation problem



1. Assume posterior can be approximated by a family of distributions
2. Optimise for optimal parameters

Generalized Variational Inference (GVI)

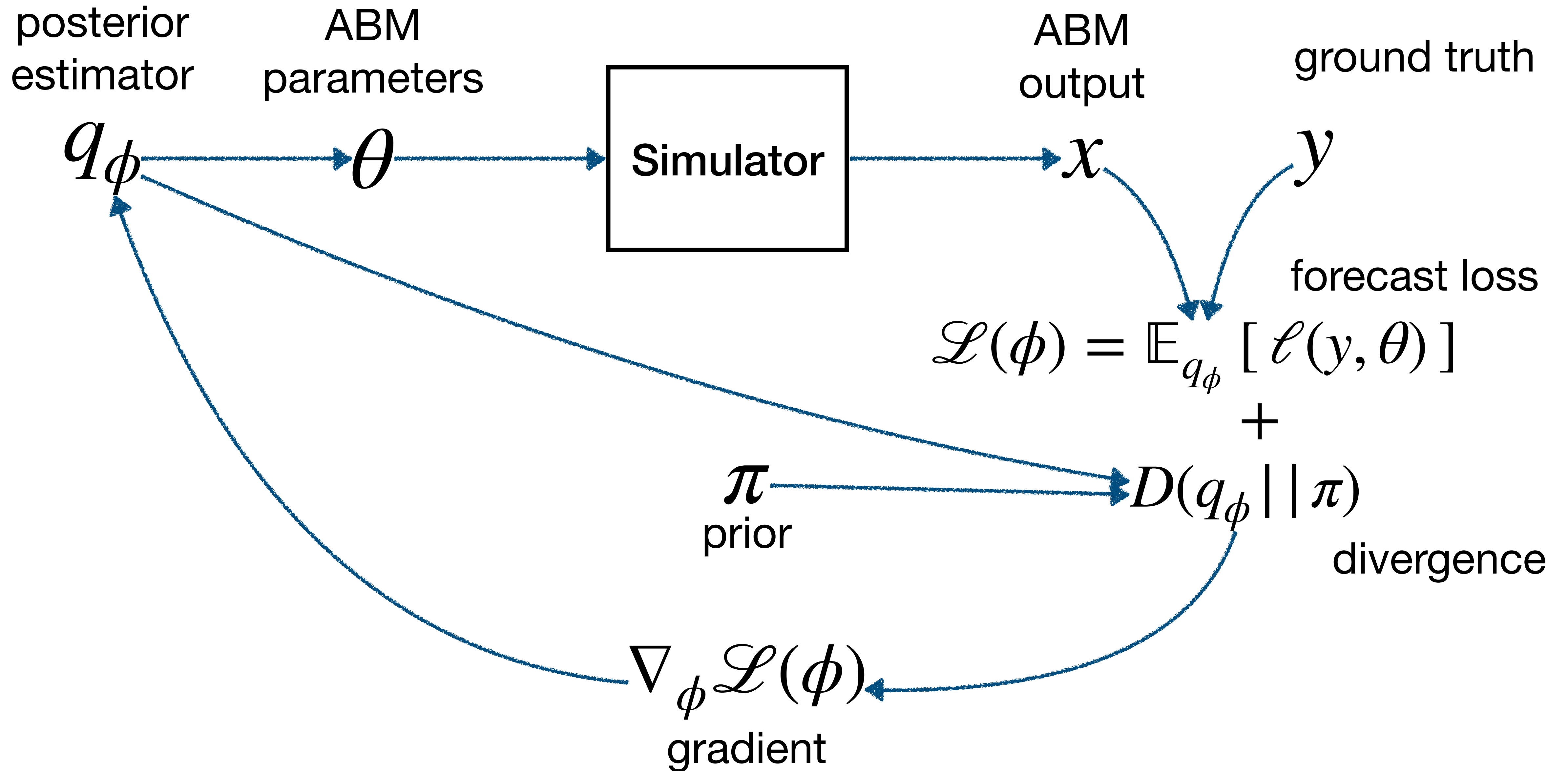
Knoblauch et al., (2022)

Target optimization to **generalised posterior**



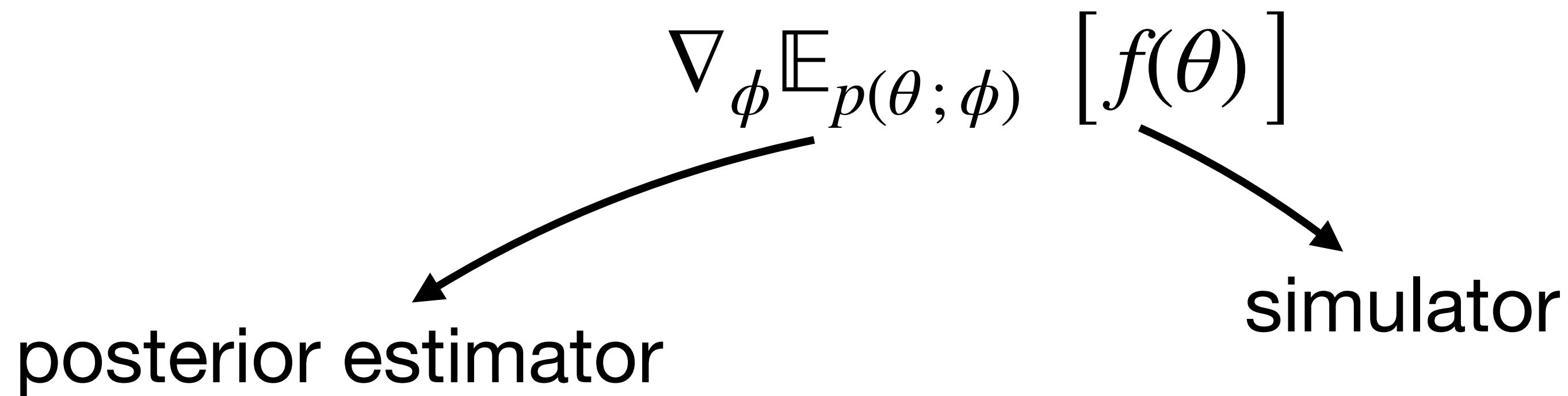
More robust to model miss-specification than classical posterior

Generalised Variational Inference



Gradients: path-wise vs score

- Gradient-assisted calibration algorithms need



- Two ways of obtaining the gradient:
 1. Differentiating the measure (**score-based gradient**)
 2. Differentiating the simulator (**path-wise gradient**)

Typically **path-wise gradient** has (much) lower variance (see Mohamed (2019))

Differentiable simulators

- Leverage Automatic Differentiation to build simulators
- Use “reparameterisation” techniques to differentiate through randomness.

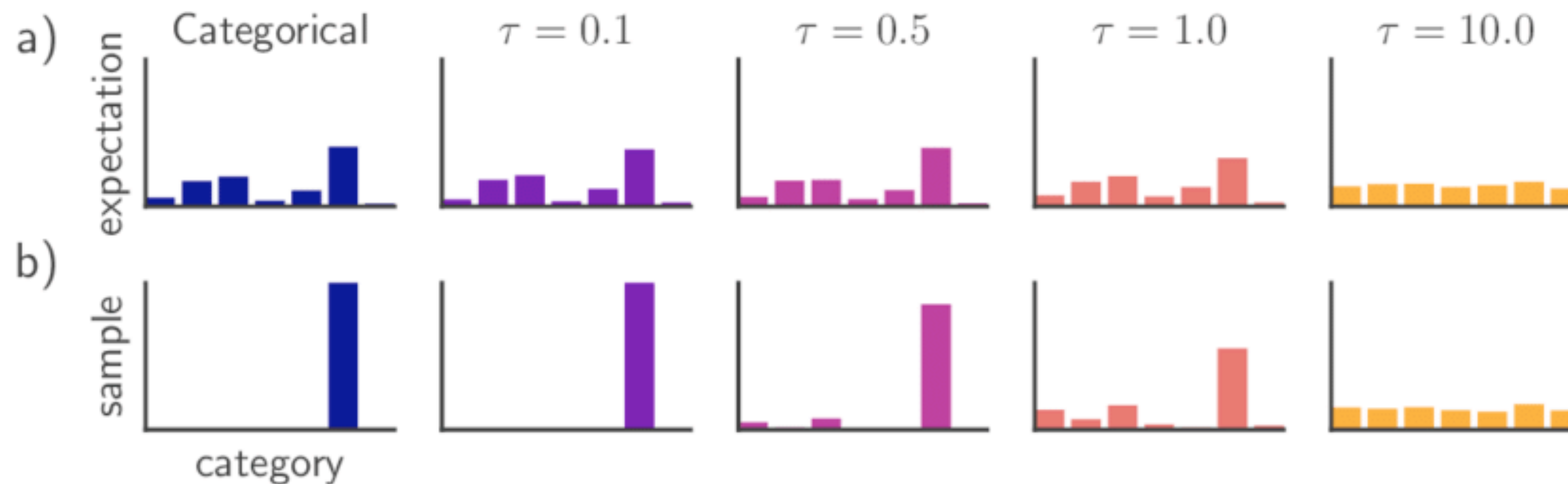
$$x \sim \mathcal{N}(\mu, \sigma) \quad \Longleftrightarrow \quad x = \mu + \sigma r \quad r \sim \mathcal{N}(0,1)$$

$$\frac{dx}{d\mu} = 1 \quad \frac{dx}{d\sigma} = r$$

Differentiable ABMs

The problem of discrete randomness

- Discrete sampling + flow control = no differentiability?
- Gumbel-Softmax



Jang et al. (2016)

Differentiable Agent-Based Epidemiology

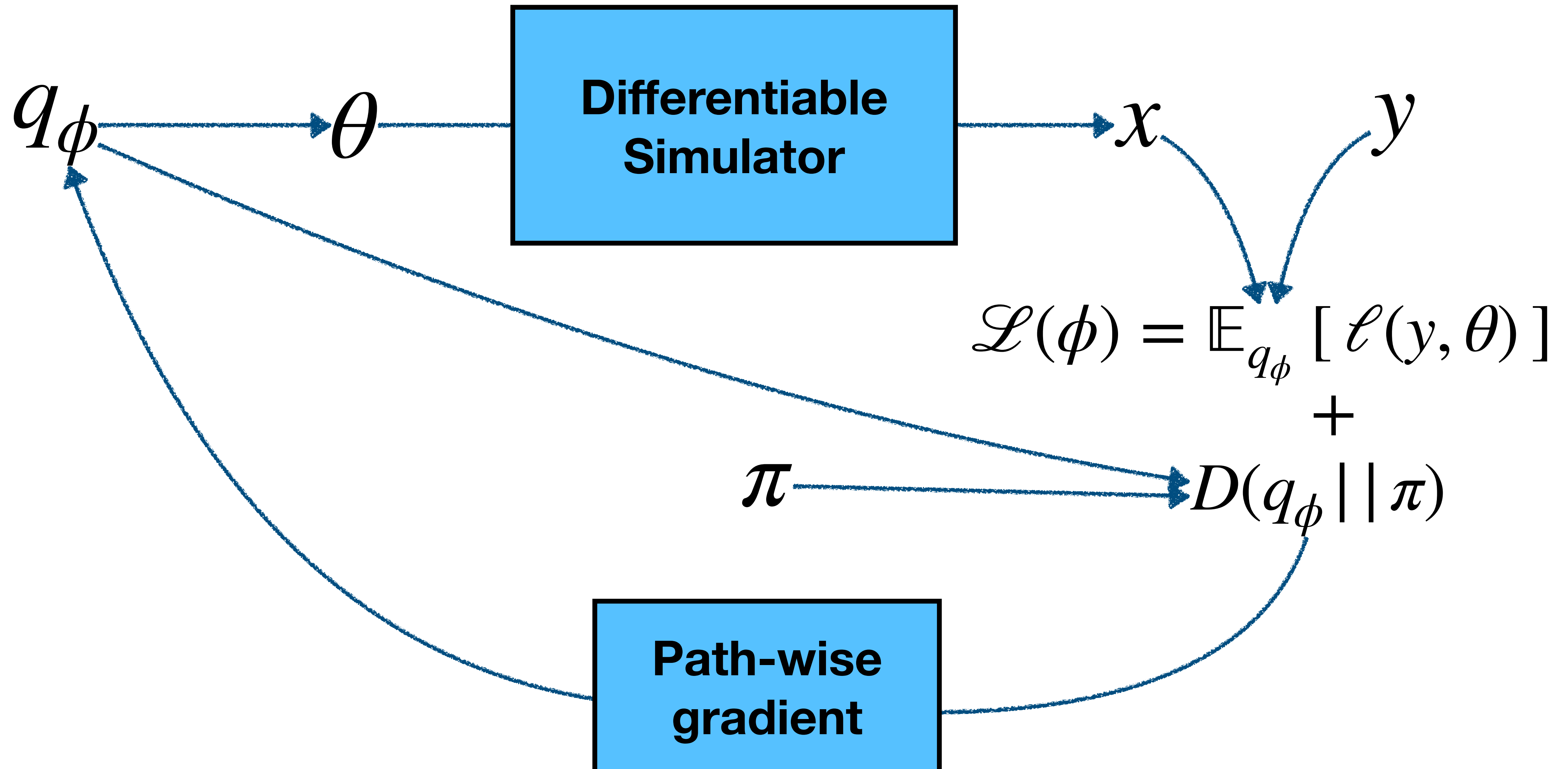
Chopra et al. (2023), Quera-Bofarull et al. (2023)

JUNE model 8 M agents (London)

	Simulation
JUNE	50 hours
GRADABM-JUNE (CPU)	5 minutes
GRADABM-JUNE (GPU)	5 seconds

x40,000 speed-up !

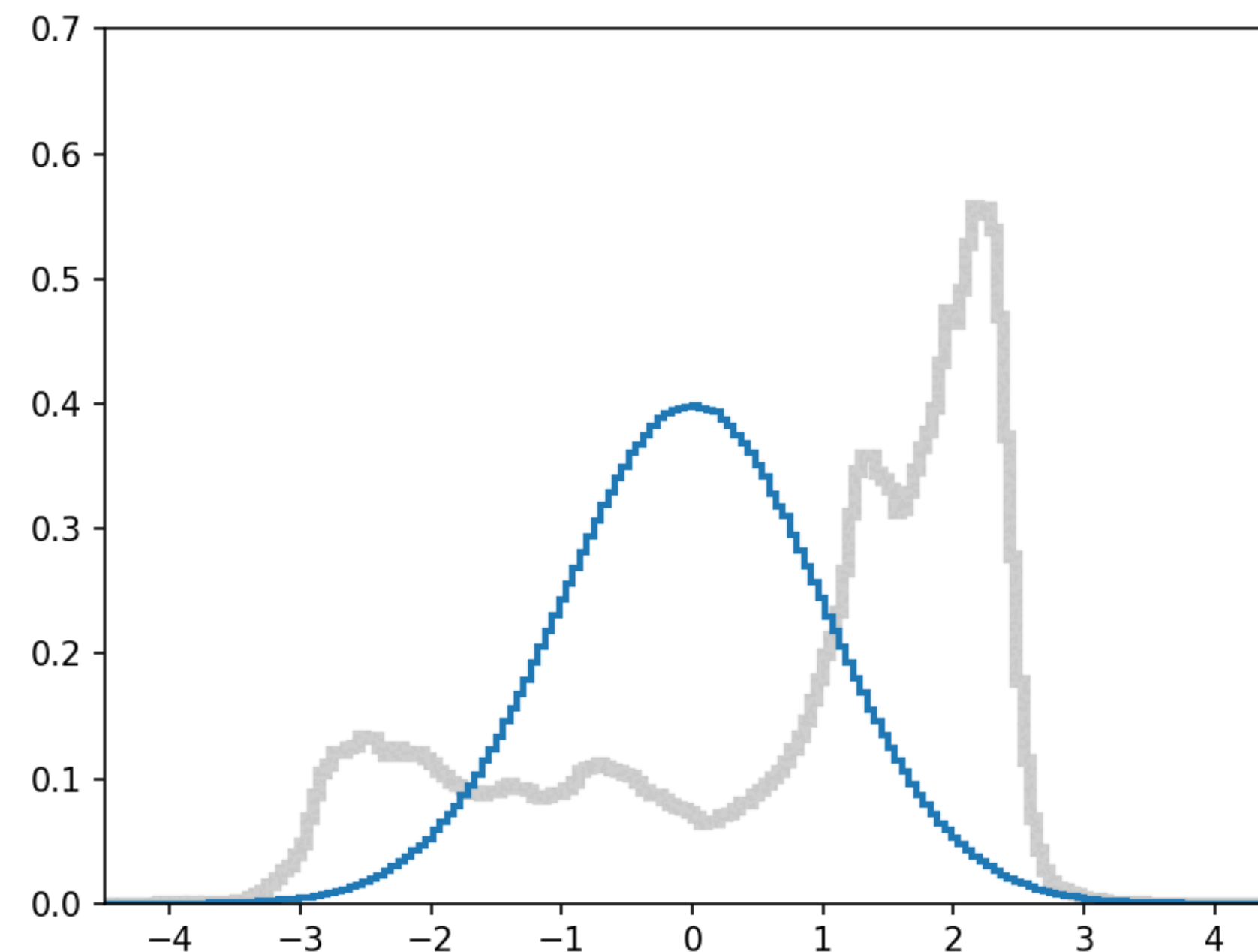
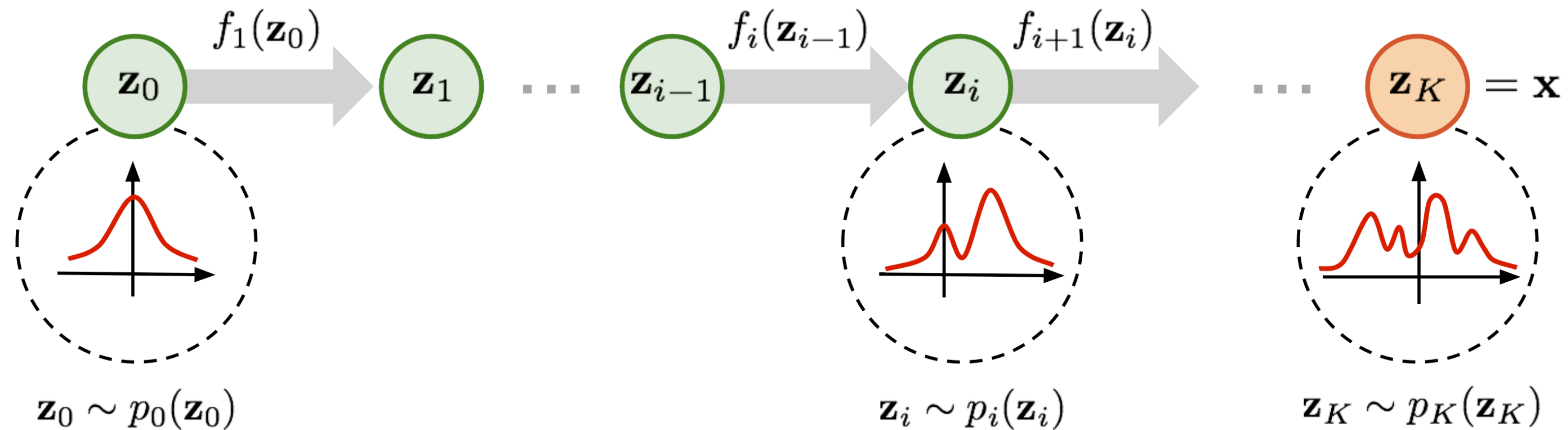
Bayesian Inference for Differentiable Simulators (BIRDS)



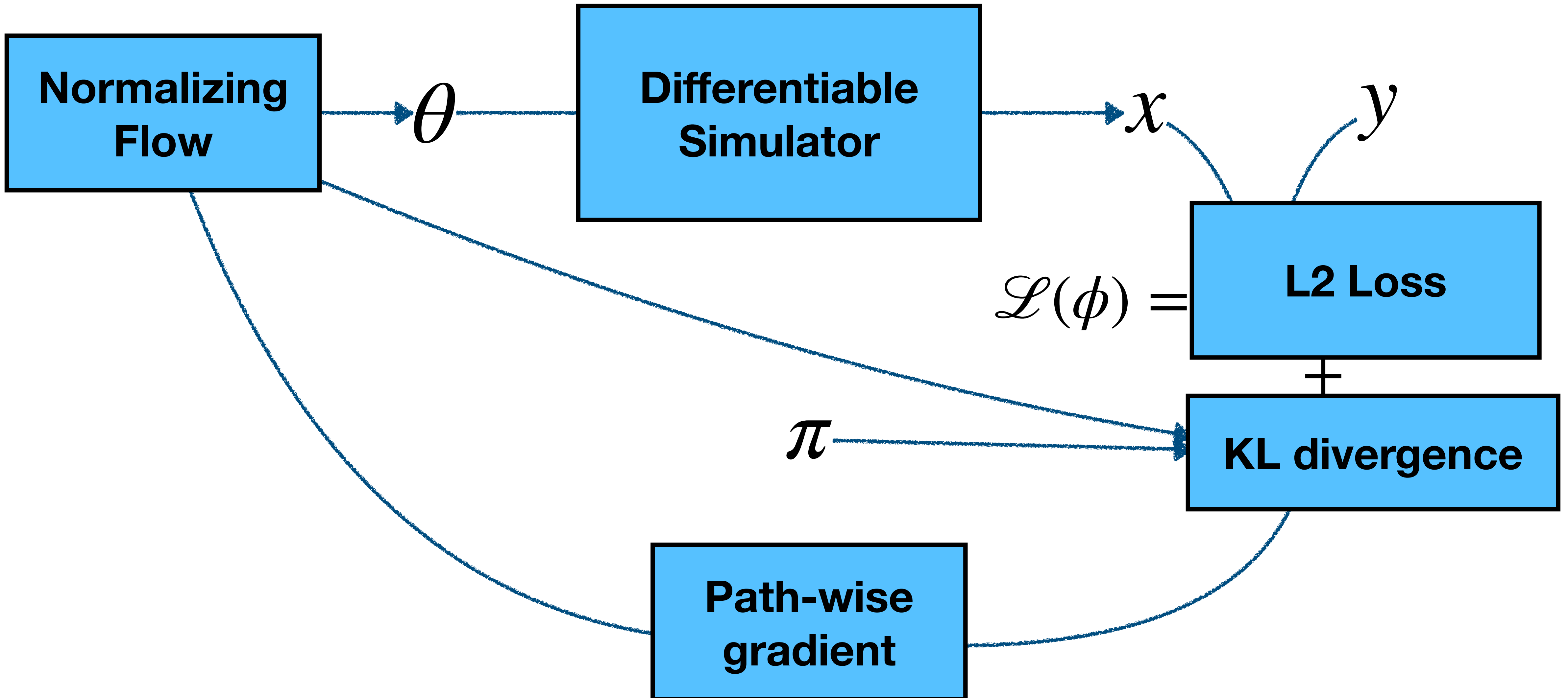
Normalizing Flows

What do we choose for q ?

Image credit: Lilian Weng



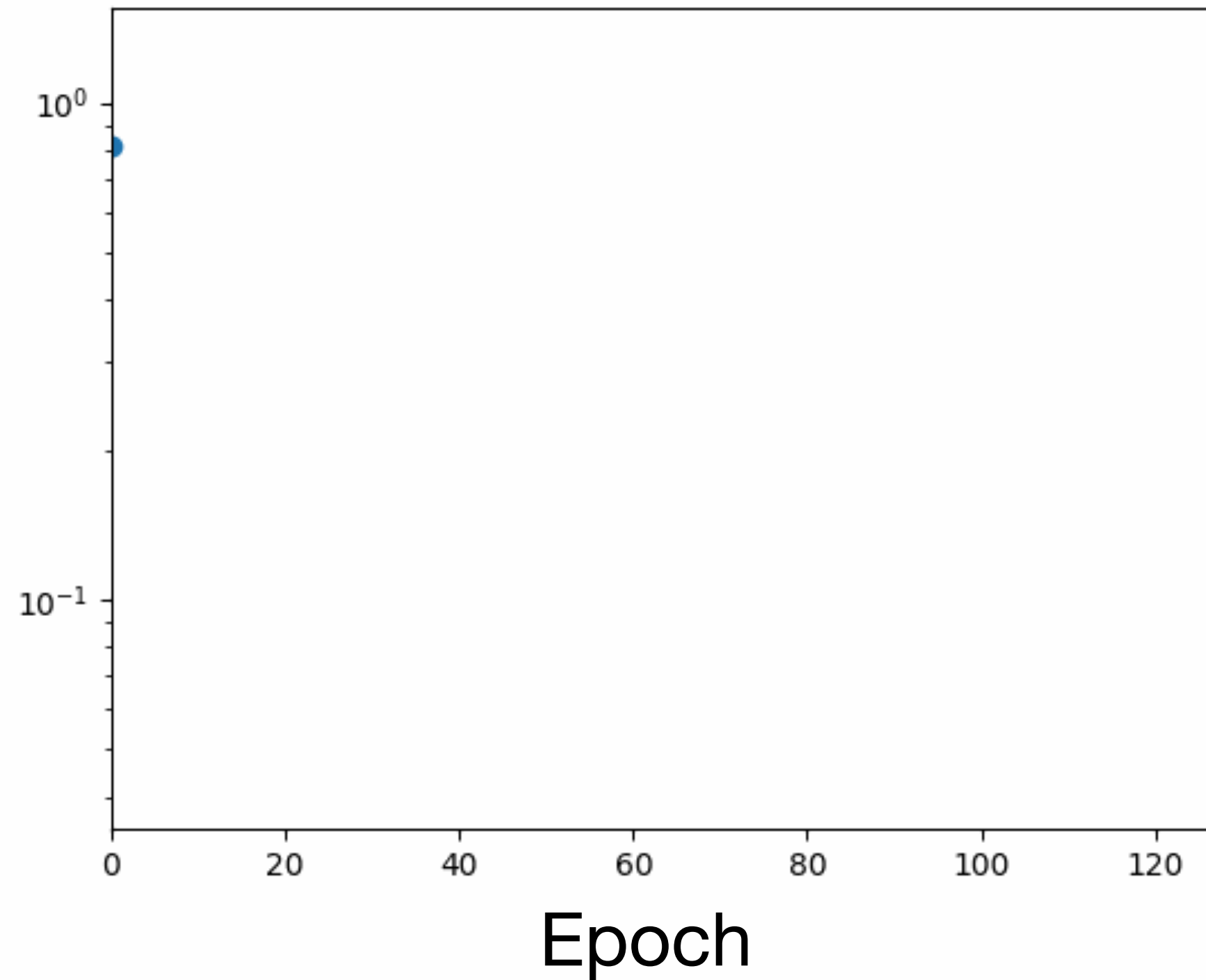
Bayesian Inference for Differentiable Simulators (BIRDS)



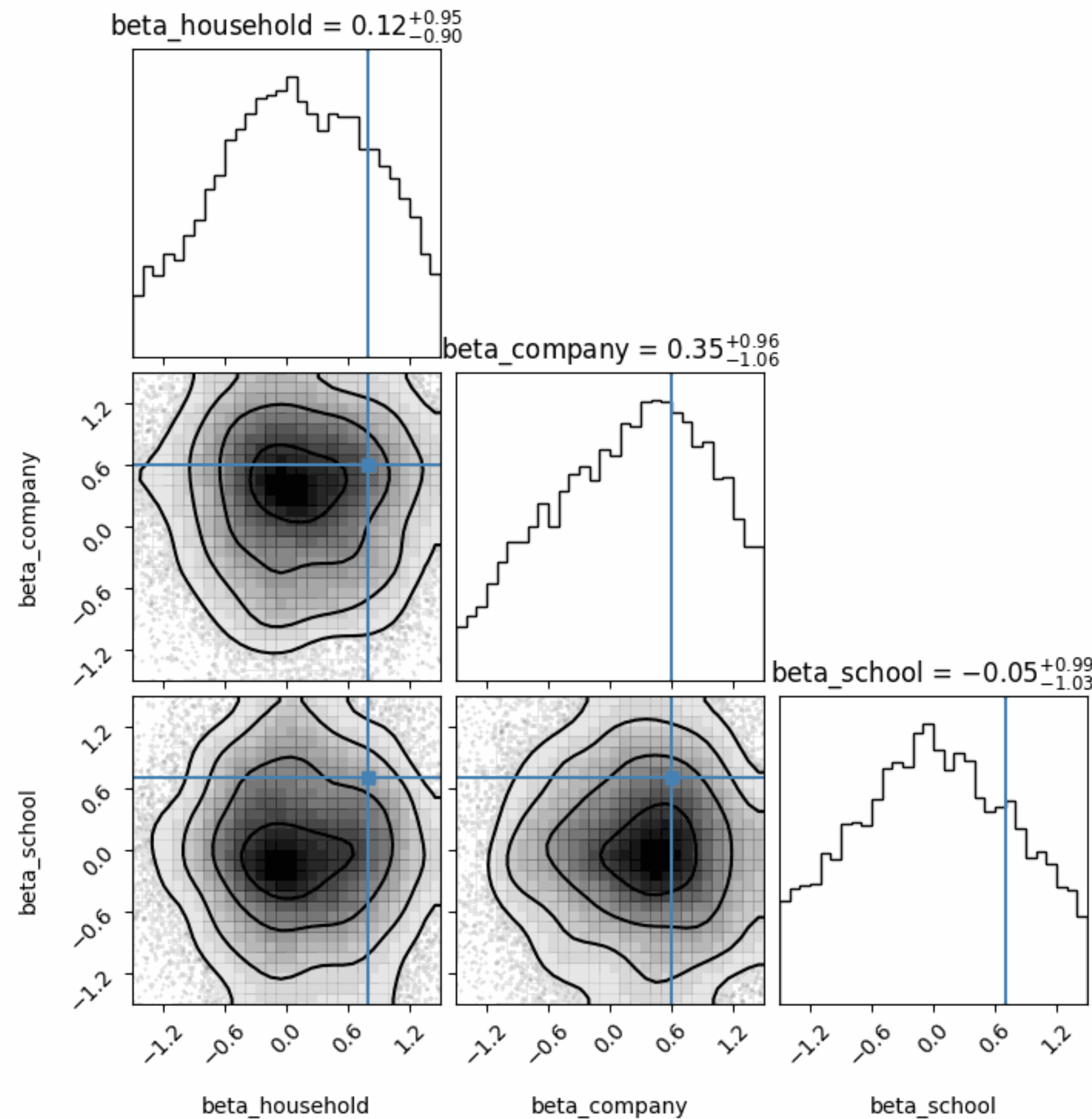
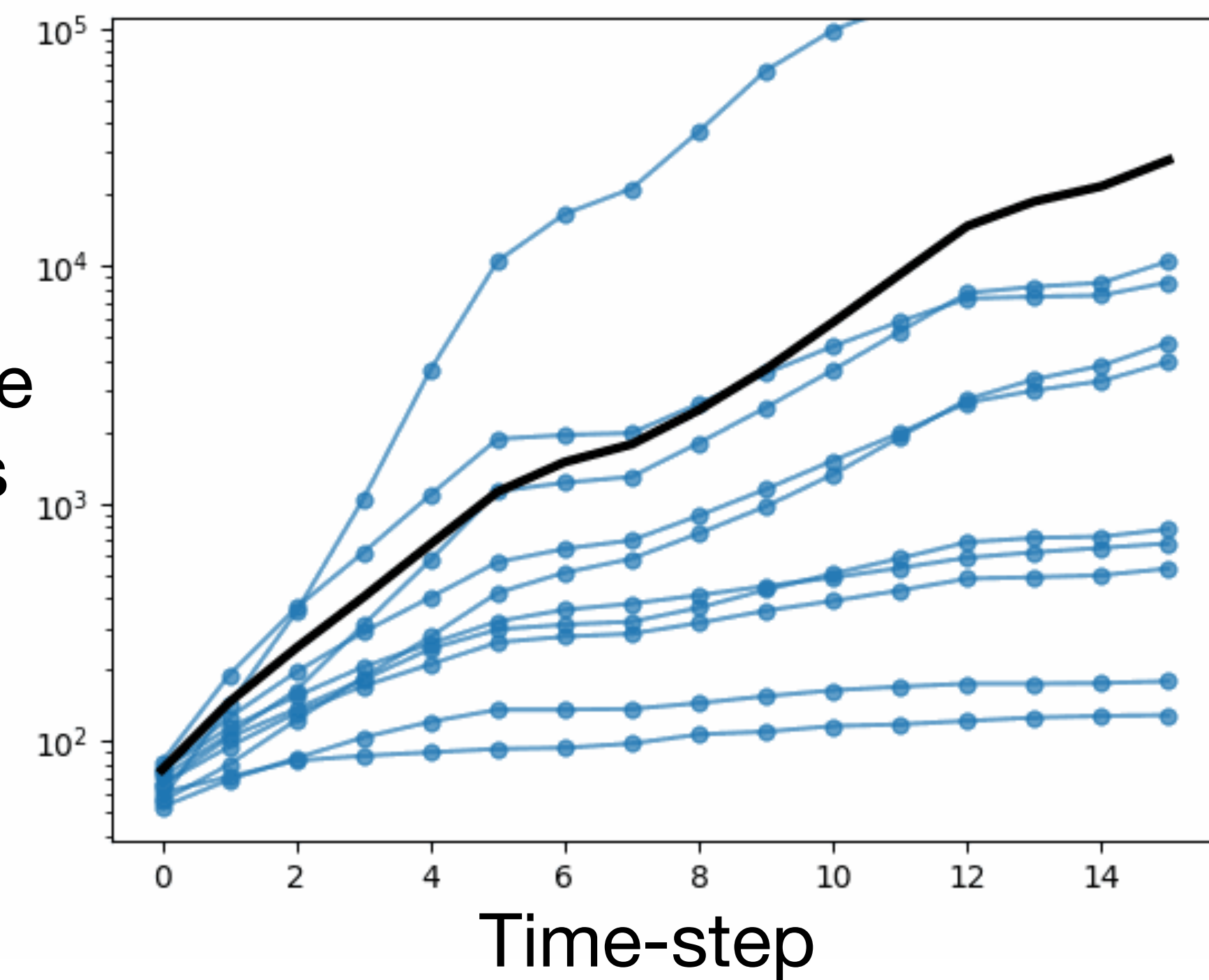
Experiment with JUNE

- ABM model of Covid19
- Model
 - ~200k agents
 - 3 layers of interactions (household, company, school)
 - Calibrate to synthetic data

Loss



Cumulative
Infections



Conclusions

1. **Bayesian** approaches to calibrating ABMs have numerous benefits
2. ABMs can be made **differentiable** even with discrete randomness and control flow
3. Diff simulators + Bayesian inference (via **Normalizing Flows**) promising route to calibrate large-scale ABMs efficiently

Paper + slides: www.arnau.ai/iclr