

# A Hybrid Encryption Algorithm based on RSA and Diffie-Hellman

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**Abstract** - Internet and Network applications have seen a tremendous growth in the last decade. As a result incidents of cyber attacks and compromised security are increasing. This requires more focus on strengthening and securing our communication. One way to achieve this is cryptography. Although a lot of work has been done in this area but this problem still has scope of improvement. In this paper we have focused on asymmetric cryptography and proposed a novel method by combining the two most popular algorithms RSA and Diffie-Hellman in order to achieve more security.

**Keywords**- RSA, Diffie-Hellman, Encryption, Public Key, Data Encryption

## I. INTRODUCTION

One of the most important techniques to secure communication in the presence of third party is cryptography. The 4 main requirements of cryptography are: to maintain confidentiality, data integrity, authentication and non-repudiation from unauthenticated users. Distributed Cryptography involves distribution of keys and encryption of data using this key. This encrypted data is sent over the public network. The secret key is shared among set of users so that the intended recipient can decrypt the data.

Encryption is the process of conversion of data (called plain text) into an unreadable form (called a cipher text), this cipher text cannot be easily understood by unauthorized people. Decryption is the process of converting encrypted data back into its original form, so that it can be understood by the people who are authorized to read that data [3]. There exist many encryption algorithms that are widely used for information security. They can be categorized into symmetric (private) and asymmetric (public) key encryption. In practice, in order to achieve the optimal efficiency, the symmetric key algorithms and public key cryptography algorithms are generally combined together. Also Public-key cryptography can be used with secret-key cryptography to get the best of both worlds. Thus in this paper we have proposed a hybrid cryptographic algorithms by a combination of RSA and

Diffie-Hellman. This combined approach is intended to get security advantage of public key system and speed advantage of secret key system.

## II. ASYMMETRIC CRYPTOGRAPHY

In Asymmetric cryptography a pair of keys is used to encrypt and decrypt a message so that it is transmitted securely. Initially, a network user receives a public and private key pair from a Certificate Authority. The process of encryption using asymmetric cryptography can be explained by following steps -

- Use a key (public key) to encrypt a message.
- Another (private key) to decrypt a message.
- Private Key known to owner and used only by owner.

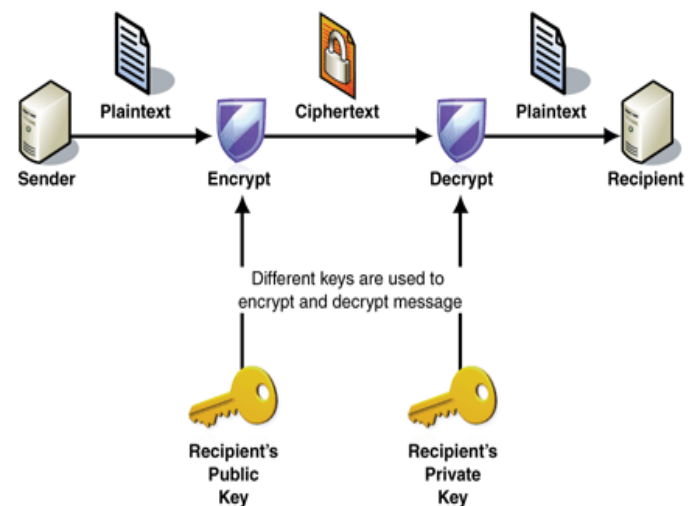


Figure 1: Asymmetric Key Encryption

The advantage of using asymmetric key encryption is that it provides better key distribution and scalability in comparison of symmetric systems. RSA, Elliptic Curve Cryptosystem (ECC), Diffie-Hellman, El Gamal, Digital Signature Algorithm (DSA), Knapsack are some of the standard Asymmetric Key Algorithms.

### III. RSA ALGORITHM

A public key encryption algorithm developed by Ronald Rivest, Adi Shamir, and Leonard Adleman in 1978 that became a de facto standard. RSA formed the basis for a number of encryption programs, including Pretty Good Privacy (PGP). RSA is an algorithm for public key encryption. It was the first algorithm known to be suitable for signing as well as encryption, and one of the first great advances in public key encryption. It involves three steps: key generation, encryption and decryption. It is still widely used in electronic commerce protocols, and is believed security depends on the difficulty of decomposition of large numbers [4].

Steps of Algorithm for Key Generation:

1. Choose two distinct prime numbers P and Q.
2. Calculate  $N = P \times Q$ . (n is used as mod for both the public and private keys)
3. Select the public key (i.e. encryption key) E such that it is not a factor of  $(P - 1)$  and  $(Q - 1)$ .
4. Select the private key (i.e. the decryption key) D such that the following equation is true  $(D \times E) \bmod (P - 1) \times (Q - 1) = 1$ .
5. For encryption, calculate the cipher text CT from the plain text PT as follows:  $CT = PTE \bmod N$ .
6. Then send CT as the cipher text to the receiver.
7. For decryption, calculate the plain text PT from the cipher text CT as follows:  $PT = CTD \bmod N$ .

This algorithm is based on the theory of Prime Numbers and the fact that it is easy to find and multiply large prime numbers together, but it is extremely difficult to factor their product. The private and public keys in RSA are based on very large (100 or more digits) prime numbers. Real challenge in the case of RSA is the selection and generation of public and private keys.

#### Problems In RSA Algorithm

- If any one of p, q, e, d is known, then the other values can be calculated. So secrecy is important.
- It is important to make sure that message length should be less than bit length otherwise the algorithm will fail.
- Due to the usage of public key RSA is much slower than any other symmetric cryptosystems.
- The length of plain text that can be encrypted is limited to the size of  $n=p \times q$ .

- Each time RSA initialization process requires the random selection of two very large prime numbers (p and q).

#### Advantages Of RSA Algorithm

- it uses Public Key encryption which means that the text will be encrypted with someone's Public Key (which everyone knows about) but only the person intended for can read it, by using their private key (which only they know about).
- Use of public key in RSA provides digital signatures that cannot be repudiated.
- Ciphering & deciphering algorithm are same.

### IV. DIFFIE – HELLMAN ALGORITHM

Whitfield Diffie and Martin Hellman discovered what is now known as the Diffie-Hellman (DH) algorithm in 1976. It is an amazing and ubiquitous algorithm found in many secure Connectivity protocols on the Internet [8, 1]. In an era when the lifetime of "old" technology can sometimes be measured in months, this algorithm is now celebrating its 25th anniversary while it is still playing an active role in important Internet protocols.

DH is a method for securely exchanging a shared secret between two parties A and B over a public network and each holding public/private key to agree on a shared secret value [5]. This shared secret is important between two parties who may not have ever communicated previously, so that they can encrypt their communications. As such, it is used by several protocols, including Secure Sockets Layer (SSL), Secure Shell (SSH), and Internet Protocol Security (IPSec). These protocols will be discussed in terms of the technical use of the DH algorithm and the status of the protocol standards established or still being defined.

Diffie–Hellman establishes a shared secret key that can be used for secret communications by exchanging data over a public network

Steps of this algorithm are as:

1. Taking two numbers "P" and "G" "P" is a large prime number "G" is called the base.
2. Picks a secret number "A" as first secret number = A, then picks another secret number "B" as second secret number = B.
3. Computes first public number  $X = GA \bmod P$ , and public number = X. Then computes second public number  $Y = GB \bmod P$ , and public number = Y.
4. Exchange their public numbers.
5. First knows P, G, A, X, Y, Second knows P, G, B, X, Y.
6. Computes First session key as  $KA = YA \bmod P$  OR  $KA = (GB \bmod P)A \bmod P$  OR  $KA = (GB)A \bmod P$  OR  $KA = GBA \bmod P$ .

7. Computes second session key as  $KB = XB \text{ mod } P$  OR  $KB = (GA \text{ mod } P)B \text{ mod } P$  OR  $KB = (GA) B \text{ mod } P$  OR  $KB = GAB \text{ mod } P$ .
8. Fortunately for Both by the laws of algebra, First session key “KA” is the same as Second session key “KB”, or  $KA = KB = K$ .
9. Know we have both the secret value as “K”.

#### Advantages Of Diffie Hellmen Algorithm

- No known successful attack strategies until now, so it is secure.
- Diffie-Hellman protocol generates a “shared-secret”-an identical cryptographic key shared by each side of the communication.

#### Problems In Diffie Hellmen Algorithm

- It is easily susceptible to man-in-the-middle attacks.
- The algorithm cannot be used to encrypt messages.
- There is also a lack of authentication.
- The computational nature of the algorithm could be used in a denial-of-service attack very easily.

#### V. PROPOSED HYBRID ALGORITHM

RSA algorithm is used as Public key cryptography method. It is widely used in Electronic commerce protocol .It has a public key and private-key. Public key is known to everyone and used for encryption and Private Key is used for decryption. The RSA algorithm can be used for both public key encryption and digital signatures [8]. It is based on the theory of Prime Numbers. Its security is based on the difficulty of factoring large integers. The amount of time it takes to factor a number of  $x$  bits is asymptotically the same as the time it takes to solve a discrete log over a field of size  $x$  bits [7]. It is the world’s most popular Asymmetric Key Encryption algorithm.

Diffie Hellman algorithm is used as key exchange method that allows two parties that have no prior knowledge to each other to jointly share a secret key [2]. DH is a method for securely exchanging a shared secret between two parties, in real-time, over an untrusted network.

In our paper we use both RSA and Diffie- Hellman for providing more security.

#### Steps of this algorithm are as

1. Choose two large prime numbers  $P$  and  $Q$ .
  - a. Calculate  $N = P \times Q$ .
  - b. Select public key (i.e encryption key)  $E$  such that it is not a factor of  $(P - 1)$  and  $(Q - 1)$ .
  - c. Select the private key (i.e. the decryption key)  $D$  such that the following equation is true  $(D \times E) \text{ mod } (P - 1) \times (Q - 1) = 1$
  - d. Suppose  $R$ ,  $S$  and  $G$  is automatic generated prime constants.
  - e. And put the value of  $E$  and  $D$  from above as secret number such that  $A=E$  and  $B=D$ .

2. Now calculate following as public number

$$X = G^A \text{ mod } R$$

$$Y = G^B \text{ mod } R$$

3. Calculate session key with formula

$$K_A = Y^A \text{ mod } R \text{ or } K_A = (G^B \text{ mod } R)^A \text{ mod } R \text{ or } K_A = (G^B)^A \text{ mod } R \text{ or } K_A = G^{BA} \text{ mod } R.$$

$$K_B = X^B \text{ mod } R \text{ or } K_B = (G^A \text{ mod } R)^B \text{ mod } R \text{ or } K_B = (G^A)^B \text{ mod } R \text{ or } K_B = G^{AB} \text{ mod } R.$$

$$\text{Such that } K_A = K_B = K.$$

4. For Encryption we use session key  $K$  with Plain text  $PT$  that will generate a new Cipher text  $CT$  Then send  $CT$  as the cipher text to the receiver and for decryption, calculate the plain text  $PT$  from the cipher text  $CT$

Firstly to use RSA each user must (privately) choose two large random numbers  $P$  and  $Q$  to create his own encryption and decryption keys. These numbers must be large so that it is not computationally feasible for anyone to factor  $N = P \times Q$  [6]. Next step (b & c) is to generate  $E$  and  $D$ . After this we put  $E$  and  $D$  as inputs  $A$  and  $B$  to Diffie-Hellman and compute  $X_A$  and  $X_B$ , through which we generate session key  $K_A$  and  $K_B$  such that  $K_A = K_B = K$ . Then we XOR our input Plain text with the session key ( $K$ ) for Encryption or to produce Cipher text and for Decryption again XOR Cipher text with session key ( $K$ ) to produce original Plain text.

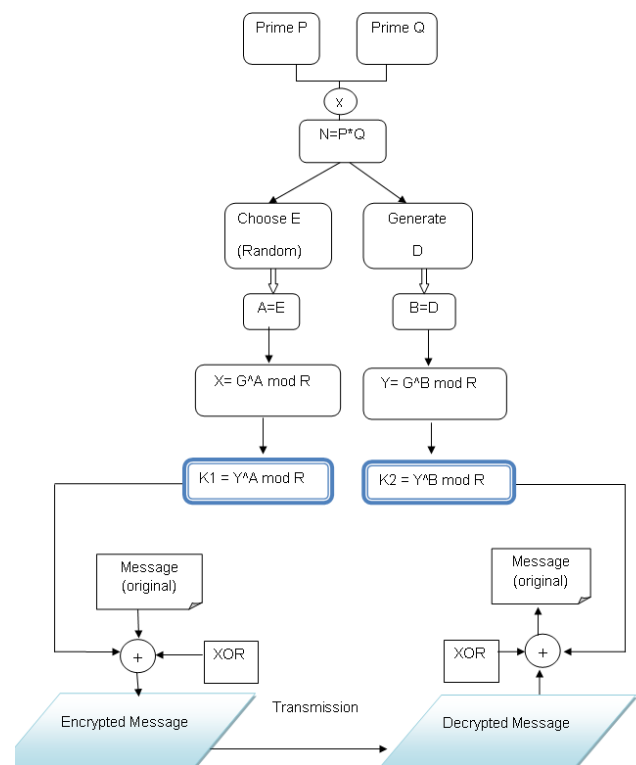


Figure 2: A Hybrid RSA & Diffie-Hellman

## VII. RESULTS

The RSA keys were taken as input to Diffie Hellman in this Implementation. The required keys are generated by the main program. A GUI was developed using java Applet. It provides options to input a user message and to upload a file.

In this approach the Diffie Hellman is not only used for the key generation but also for the generation of more secure cipher text. Generation of prime number for both RSA and Diffie is not all easy, so to guess that number and find out the key is impossible.

```

C:\Windows\system32\cmd.exe
Usage: java [-options] <source files>
  -help for a list of possible options

C:\Program Files\Java\jdk1.6.0\bin>javac rsa_diffie/Main.java
C:\Program Files\Java\jdk1.6.0\bin>java rsa_diffie/Main.java
First Private Key = 685906176751123608628046990836014379997162057122250041915614
591782236762365595014165663749983936350820141183640728434985023466308930889724474
612718618720075894885553086381567564852872365908972213838763107149684531236428
1918670753482934449493595291597273509323306874457488084501615559848290017750703
440976151
First Public Key = 65537
Second Private Key = 10994858763724301460687166204054152028185572914222968627227
8646444892207026232994682565505399724326260204657454002159936357940304042208200
2930301410133657372293110172270894160625235888614447644631533326883073054686
543229051108884991258952154958333087615538057147423101015143947558319425791406
95704873823
Second Public Key = 12774424367649092524598479720946225319125728231198812307749460
326957710131717960830965524230562614737145840579877097376814164100453161528506287
30862154231364051473227884582299452257568022640973581296570168764921764286791805
6314308698567472889816080479909157485264139886856230638968620081145376439740760
822276036
First Session Key = 100739681986612911258490934246669003844765778479558244018589
465071722197613657037928790640431556491945649838354794478842850280679823383166
60301811450564254268223163244937969973704128676326145872609519512094473328886671
54257622927358853809208898241439709130255627881950570619408032625919273652009
951134009
Second Private Key = 10073968198661291125849093424666900384476577847955824401858
946507172219764365703792879064043155649194564983835479447884285028067982338316
06030181145056425426822316324493796997370412867632614587260951951209447332888667
154257622927358853809208898241439709130255627881950570619408032625919273652009
9951134009
message = 1952805748
encrypted = 1264445630295515972441206205790962456203306497059576417289237682367
65704669728557977671318249247019672140897633068296200913573416209435927095807376
0736326018492760601714648459915301044649724454021830506164925103262651529739800
15750361090970437728490223062169508009209413052897149764401353739446407169055928
8
decrypted = 1952805748
  
```

Figure 3: Key Generation

Figure 4: Encrypted & Decrypted Message

## VII. CONCLUSION AND FUTURE SCOPE

The proposed approach will be of great use for the secure communication. It will be easy for user to send and receive messages and files which are the most confidential to them. On a long run, this will prove to be of immense help in security services and encryption technique. Presently, the usability of proposed Algorithm is demonstrated with very few concept and ideas which in future can be expand. The efficiency in terms of time complexity can be revised for better working of algorithm. The key size for encryption and decryption purpose can be reduces further. Currently the Algorithm is used for encryption and decryption purpose only. Further it can be used for digital signature generation.

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