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Design and Analysis of Algorithm
08
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To use backtracking to solve 15 puzzle problem.
15 puzzle problem
 .If N is odd, then puzzle instance is solvable if number of inversions is even in the input state. 2.If N is even, puzzle instance is solvable if the blank is on an even row counting from the bottom (second-last, fourth-last, etc.) and number of inversions is odd. the blank is on an odd row counting from the bottom (last, third-last, fifth-last, etc.) and number of inversions is even. 3.For all other cases, the puzzle instance is not solvable.

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PROGRAM:
                      #include<stdio.h>
                      int m=0,n=4;
                      int cal(int temp[10][10],int t[10][10])
                            int i,j,m=0;
                             for(i=0; i < n; i++)
                                   for(j=0; j < n; j++)
                                          if(temp[i][j]!=t[i][j])
                                          m++;
                            return m;
                      int check(int a[10][10],int t[10][10])
                            int i,j,f=1;
                             for(i=0; i < n; i++)
                                   for(j=0; j < n; j++)
                                          if(a[i][j]!=t[i][j])
                                                 f=0;
                            return f;
                      void main()
                             int p,i,j,n=4,a[10][10],t[10][10],temp[10][10],r[10][10];
                             int m=0,x=0,y=0,d=1000,dmin=0,l=0;
                             printf("\nEnter the matrix to be solved,space with zero :\n");
                             for(i=0; i < n; i++)
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for(j=0; j < n; j++)
              scanf("%d",&a[i][j]);
printf("\nEnter the target matrix,space with zero :\n");
for(i=0; i < n; i++)
       for(j=0; j < n; j++)
              scanf("%d",&t[i][j]);
printf("\nEntered Matrix is :\n");
for(i=0; i < n; i++)
       for(j=0; j < n; j++)
              printf("%d\t",a[i][j]);
       printf("\n");
}
printf("\nTarget Matrix is :\n");
for(i=0; i < n; i++)
       for(j=0; j < n; j++)
              printf("%d\t",t[i][j]);
       printf("\n");
}
while(!(check(a,t)))
      1++;
       d=1000;
       for(i=0; i < n; i++)
              for(j=0; j < n; j++)
                    if(a[i][j]==0)
                            x=i;
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y=j;
             }
      }
//To move upwards
for(i=0; i < n; i++)
      for(j=0; j < n; j++)
             temp[i][j]=a[i][j];
if(x!=0)
{
      p=temp[x][y];
      temp[x][y]=temp[x-1][y];
      temp[x-1][y]=p;
}
m=cal(temp,t);
dmin=l+m;
if(dmin < d)
{
      d=dmin;
      for(i=0; i < n; i++)
             for(j=0; j < n; j++)
                   r[i][j]=temp[i][j];
}
//To move downwards
for(i=0; i < n; i++)
      for(j=0; j < n; j++)
             temp[i][j]=a[i][j];
if(x!=n-1)
{
      p=temp[x][y];
      temp[x][y]=temp[x+1][y];
      temp[x+1][y]=p;
```

```
m=cal(temp,t);
dmin=l+m;
if(dmin < d)
      d=dmin;
      for(i=0; i < n; i++)
             for(j=0; j < n; j++)
                    r[i][j]=temp[i][j];
}
//To move right side
for(i=0; i < n; i++)
      for(j=0; j < n; j++)
             temp[i][j]=a[i][j];
if(y!=n-1)
{
      p=temp[x][y];
      temp[x][y]=temp[x][y+1];
      temp[x][y+1]=p;
m=cal(temp,t);
dmin=l+m;
if(dmin < d)
      d=dmin;
      for(i=0; i < n; i++)
             for(j=0; j < n; j++)
                    r[i][j]=temp[i][j];
//To move left
for(i=0; i < n; i++)
      for(j=0; j < n; j++)
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temp[i][j]=a[i][j];
      if(y!=0)
             p=temp[x][y];
             temp[x][y]=temp[x][y-1];
             temp[x][y-1]=p;
      m=cal(temp,t);
      dmin=l+m;
      if(dmin < d)
             d=dmin;
             for(i=0; i < n; i++)
                    for(j=0; j < n; j++)
                          r[i][j]=temp[i][j];
      }
      printf("\nCalculated Intermediate Matrix Value :\n");
      for(i=0; i < n; i++)
             for(j=0; j < n; j++)
              printf("%d\t",r[i][j]);
             printf("\n");
      for(i=0; i < n; i++)
             for(j=0; j < n; j++)
              a[i][j]=r[i][j];
              temp[i][j]=0;
      printf("Minimum cost : %d\n",d);
}
```

