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SUBJECT	Design and Analysis of Algorithm
EXPERIMENT NO :	03
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AIM:	To multiply two matrices using strassen's matrix multiplication.
PROBLEM STATEMENT 1:	Strassen's matrix multiplication on a generalized 2x2 matix.
ALGORITHM and THEORY:	<p>In this context, using Strassen's Matrix multiplication algorithm, the time consumption can be improved a little bit.</p> <p>Strassen's Matrix multiplication can be performed only on square matrices where n is a power of 2. Order of both of the matrices are $n \times n$.</p> <p>Divide X, Y and Z into four $(n/2) \times (n/2)$ matrices as represented below –</p> <p>$Z = \begin{bmatrix} I & K & J & L \end{bmatrix}$ $\Rightarrow \begin{bmatrix} ? & ? & ? & ? \end{bmatrix}$ $X = \begin{bmatrix} A & C & B & D \end{bmatrix}$ $\Rightarrow \begin{bmatrix} ? & ? & ? & ? \end{bmatrix}$ and $Y = \begin{bmatrix} E & G & F & H \end{bmatrix}$ $\Rightarrow \begin{bmatrix} ? & ? & ? & ? \end{bmatrix}$</p> <p>Using Strassen's Algorithm compute the following –</p> <div> $M_2 := (B + D) \times (G + H) \Rightarrow 2 := (\diamond + \diamond) \times (\diamond + \diamond)$ $M_3 := (A - D) \times (E + H) \Rightarrow 3 := (\diamond - \diamond) \times (\diamond + \diamond)$ </div>

	<div data-bbox="495 201 1596 388" data-label="Equation-Block"> $\begin{aligned} M_4 &:= A \times (F - H) \quad \diamond 4 := \diamond \times (\diamond - \diamond) \\ M_5 &:= (C + D) \times (E) \quad \diamond 5 := (\diamond + \diamond) \times (\diamond) \\ M_6 &:= (A + B) \times (H) \quad \diamond 6 := (\diamond + \diamond) \times (\diamond) \\ M_7 &:= D \times (G - E) \quad \diamond 7 := \diamond \times (\diamond - \diamond) \end{aligned}$ </div> <p>Then,</p> <div data-bbox="495 464 1596 646" data-label="Equation-Block"> $\begin{aligned} I &:= M_2 + M_3 - M_6 - M_7 \quad \diamond := \diamond 2 + \diamond 3 - \diamond 6 - \diamond 7 \\ J &:= M_4 + M_6 \quad \diamond := \diamond 4 + \diamond 6 \\ K &:= M_5 + M_7 \quad \diamond := \diamond 5 + \diamond 7 \\ L &:= M_1 - M_3 - M_4 - M_5 \end{aligned}$ </div> <p>Analysis</p> <p>$T(n) = \begin{cases} c_7 \times T(n/2) + d \times n^2 & \text{if } n = 1 \\ \text{otherwise} \end{cases}$ $T(n) = \begin{cases} 17 \times T(n/2) + \dots \end{cases}$ where c and d are constants</p> <p>Using this recurrence relation, we get $T(n) = O(n \log 7)$.</p> <p>Hence, the complexity of Strassen's matrix multiplication algorithm is $O(n \log 7)$.</p>
<p>PROGRAM:</p>	<pre> #include<stdio.h> #include<time.h> void main() { int a[2][2],b[2][2],c[2][2],i,j; int p[7]; int s[10]; clock_t start,end; printf("Enter the elements of 1st matrix:"); for(i=0;i<2;i++) { for(j=0;j<2;j++) { scanf("%d",&a[i][j]); } } printf("Enter the elements of 2nd matrix:"); </pre>

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for(i=0;i<2;i++)
{
    for(j=0;j<2;j++)
    {
        scanf("%d",&b[i][j]);
    }
}
start=clock();
s[0]=b[0][1]-b[1][1];
s[1]=a[0][0]+a[0][1];
s[2]=a[1][0]+a[1][1];
s[3]=b[1][0]-b[0][0];
s[4]=a[0][0]+a[1][1];
s[5]=b[0][0]+b[1][1];
s[6]=a[0][1]-a[1][1];
s[7]=b[1][0]+b[1][1];
s[8]=a[0][0]-a[1][0];
s[9]=b[0][0]+b[0][1];

p[0]=s[0]*a[0][0];
p[1]=s[1]*b[1][1];
p[2]=s[2]*b[0][0];
p[3]=s[3]*a[1][1];
p[4]=s[4]*s[5];
p[5]=s[6]*s[7];
p[6]=s[8]*s[9];

c[0][0]=p[4]+p[3]-p[1]+p[5];
c[0][1]=p[0]+p[1];
c[1][0]=p[2]+p[3];
c[1][1]=p[4]+p[0]-p[2]-p[6];

for(i=0;i<10;i++)
{

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        printf("\nS%d=%d ",i+1,s[i]);
    }
    printf("\n");
    for(j=0;j<7;j++)
    {
        printf("\np%d=%d ",j+1,p[j]);
    }
    printf("\n\n");
    printf("MATRIX A:-\n");
    for(i=0;i<2;i++)
    {
        printf("\n");
        for(j=0;j<2;j++)
        {
            printf("%d\t",a[i][j]);
        }
    }
    printf("\n");
    printf("MATRIX B:-\n");
    for(i=0;i<2;i++)
    {
        printf("\n");
        for(j=0;j<2;j++)
        {
            printf("%d\t",b[i][j]);
        }
    }
    printf("\n");
    printf("MATRIX C:-\n\n");
    printf("%d\t%d\n%d\t%d\n",c[0][0],c[0][1],c[1][0],c[1][1]);
    end=clock();
    printf("The time taken by the program: ");
    printf("%lf",(double)(end-start)/CLOCKS_PER_SEC);
}

```

OUTPUT:

```
students@students-HP-280-G3-MT:~$ ./a.out
Enter the elements of 1st matrix:1 3 7 5
Enter the elements of 2nd matrix:6 8 4 2

S1=6
S2=4
S3=12
S4=-2
S5=6
S6=8
S7=-2
S8=6
S9=-6
S10=14

p1=6
p2=8
p3=72
p4=-10
p5=48
p6=-12
p7=-84

MATRIX A:-

1      3
7      5
MATRIX B:-

6      8
4      2
MATRIX C:-

18     14
62     66
The time taken by the program: 0.000209students@students-HP-280-G3-MT:~$
```

CONCLUSION:

By performing above experiment I have understood how the time complexity of strassen's matrix multiplication is better than that of normal $m \times n$ matrix multiplication.