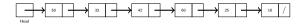
# Singly (Cont.), Doubly Linked Lists and Circular Linked Lists

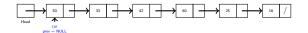
Subhabrata Samajder



IIIT, Delhi Summer Semester, 30<sup>th</sup> May, 2022 Reversing a Linked List

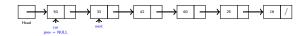


- Use 3 pointers: prev, cur, next
- Start with pointing cur to first node, and prev = NULL.



```
Node *prev = NULL, *cur = NULL, *next = NULL;
cur = pFront;
```

- Use 3 pointers: prev, cur, next
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- Traverse the list in a while loop till cur = NULL.
  - Set next = cur->pNext.



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while (cur != NULL) {

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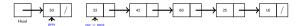
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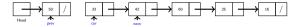
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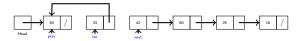
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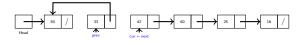
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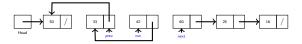
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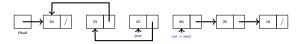
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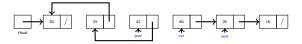
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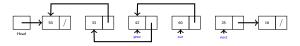
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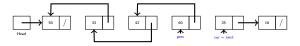
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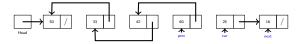
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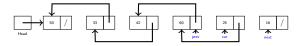
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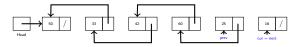
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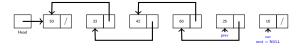
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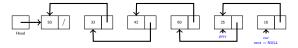
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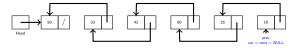
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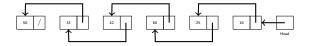
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- Traverse the list in a while loop till cur = NULL.
- Set link for Front = prev.



```
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cur = pFront;

while (cur != NULL) {

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    prev = cur;

    cur = next; }

pFront = prev:
```

#### **Exercises**

- Create a list with each node contain names of student and their CGPA.
- Q Given the above list, find the name of the student having the highest CGPA.
- 3 Given a list, create two lists with alternate elements of first list.
- Append a list at end of another list.
- 6 Check if two lists are identical.

Storing Polynomials in a Linked Lists

#### Advantages of Linked lists

• Dynamic in nature. Memory allocated at run time.

- Insertion and Deletions are constant time operations (without the searching).
- No need to shift nodes as was necessary with arrays.

 Other data structures like queues, stacks are easily implemented using linked lists

## **Polynomials**

Problem: Add the polynomials

$$5 + 2x + 3x^{2}$$
,  
 $7x + 8$ ,  
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Note: We need to store only the coefficients and the exponents.

## Storing Polynomials Using Arrays

• **Polynomial:**  $5 + 2x + 3x^2$  **Array:** [5 2 3]

• **Polynomial:** 7x + 8 **Array:** [8 7 0]

## Storing Polynomials Using Arrays

• **Polynomial:**  $5 + 2x + 3x^2$  **Array:** [5 2 3]

• **Polynomial:** 7x + 8 **Array:** [8 7 0]

• That is, store only the coefficients in proper place.

## Issues in Storing Polynomials Using Arrays

• Polynomial:  $5 + 2x + 3x^2 + 6x^5$ Array:  $[5 \ 2 \ 3 \ 0 \ 0 \ 6]$ 

• Polynomial:  $5 + 2x + 3x^2 + 7x^{31}$ Array:  $\begin{bmatrix} 5 & 2 & 3 & 0 & 0 & 0 & \cdots & 0 & 7 \end{bmatrix}$ 

Need to store so many zeroes in a very large sized array



## Storing Polynomials Using Linked Lists

Let us now see how two polynomials can be added.

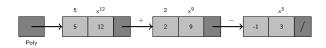
- Let  $P_1$  and  $P_2$  be two polynomials
  - stored as linked lists
  - Each node contains exponent and coefficients values
  - in sorted (decreasing) order of exponents

• Addition Operation: Add terms of like-exponents.

#### Representing a Polynomial Using a Linked List

Store the coefficient and exponent of each term in nodes

```
int item1[] = \{5, 12\};
int item2[] = \{2, 9\};
int item3[] = \{-1, 3\};
```

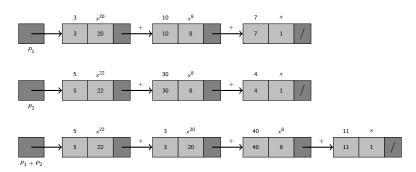


## Operations on Polynomials

- P<sub>1</sub> and P<sub>2</sub> are stored as linked lists and are arranged in decreasing order of exponents.
- Scan these and add like terms.
- Store the resulting term only if it has non-zero coefficient.
- The number of terms in the result  $(P_1 + P_2)$  need not be known in advance.
- Uses as much space as there are terms in  $P_1 + P_2$ .

## Addition of Two Polynomials

One pass down each list:  $\mathcal{O}(n+m)$ .



## Multiplication of Two Polynomials

• Can be done as repeated addition.

• So, multiply  $P_1$  with each term of  $P_2$ .

Add the resulting polynomials.

### **Doubly Linked Lists**

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• Permits traversal of list in both directions.

Useful where navigation in both directions needed.

Used by browsers to navigate forwards and backwards.

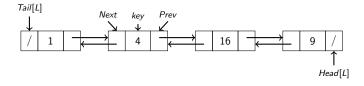
Various applications use this for redo and undo functionalities.

## Doubly Linked List (Cont.)

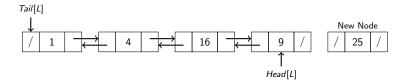
- Each element of a doubly linked list L is an object x with a key (or data) field and two other pointer fields:
  - next[x] points to it successor in the linked list and
  - prev[x] points to its predecessor.
- **Head of** *L*: If prev[x] = nil.
- Tail of L: If next[x] = nil.
- head[L]: Points to the first element of the list L.
- tail[L]: Points to the last element of the list L.
- Empty List: If head[L] = nil.

## C Implementation of a Doubly Linked List Node

```
typedef struct DLNode {
  int nKey;
  struct DLNode *pPrev, *pNext;
} DLNode;
```

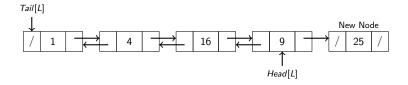


• Create a new node x.



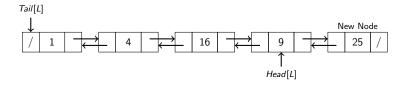
```
DLNode *pTemp;
pTemp = (DLNode *)malloc(sizeof(DLNode));
pTemp->nKey = 25;
pTemp->pPrev = NULL;
pTemp->pNext = NULL;
```

- Create a new node x.
- head[L].prev = x.



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DLNode *pTemp;
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- x.next = head[L].



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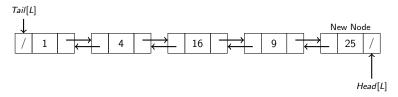
pTemp->pPrev = NULL;

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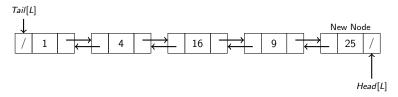
pTemp->pNext = pHead;
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- Create a new node x.
- head[L].prev = x.
- x.next = head[L].
- head[L] = x.



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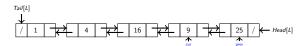


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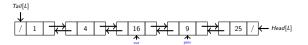
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- Let d = 4.



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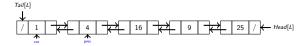
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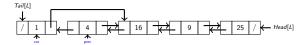
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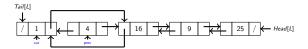
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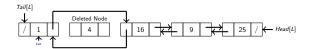
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- Traverse until prev->nKey = 4.
- Set cur->pPrev = prev->pPrev.



- Assume that the list is of length at least 2.
- Let d = 4.
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- Traverse until prev->nKey = 4.
- Set cur->pPrev = prev->pPrev.
- Set prev->pPrev->pNext = cur.



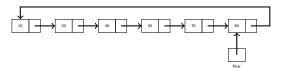
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- Let d = 4.
- Set pointer prev to the first and cur to the second node.
- Traverse until prev->nKey = 4.
- Set cur->pPrev = prev->pPrev.
- Set prev->pPrev->pNext = cur.
- Set free(prev).



Circular Linked Lists

#### Circular Linked Lists

- A Circular Linked List is a special type of Linked List
- It supports traversing from the end of the list to the beginning by making the last node point back to the head of the list.
- A Rear pointer is often used instead of a Head pointer.



#### Motivation

• Usually sorted.

• Useful for playing video and sound files in "looping" mode.

• They are also a stepping stone for implementing graphs.



### Circular Linked List Operations

insertNode(Node \*Rear, int item)//adds a new node to ordered circular linked list

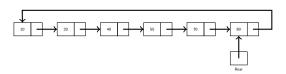
deleteNode(Node \*Rear, int item)//removes a node from circular linked list

print(Node \*Rear) //print the Circular Linked List once

## Traversing a Circular Linked List

```
void print(Node *Rear){
  Node *Cur;

if(Rear != NULL){
    Cur = Rear->pNext;
    do{
        printf("%d, ", Cur->nData);
        Cur = Cur->pNext;
    } while(Cur != Rear->pNext);
}
```



#### • Empty List:

```
Note *New = NULL;

New = (Node *)malloc(sizeof(Node));

New->nData = 10;

Rear = New;

Rear->pNext = Rear;
```



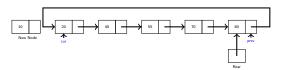
```
Node *New = NULL;

New = (Node *)malloc(sizeof(Node));

New->nData = 10;

cur = Rear->pNext;

prev = Rear;
```



#### • Inserting a Node at the Head:

```
Node *New = NULL;

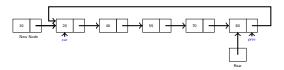
New = (Node *)malloc(sizeof(Node));

New->nData = 10;

cur = Rear->pNext;

prev = Rear;

New->pNext = Cur;
```



```
Node *New = NULL;

New = (Node *)malloc(sizeof(Node));

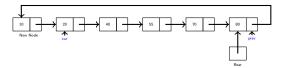
New->nData = 10;

cur = Rear->pNext;

prev = Rear;

New->pNext = Cur;

Prev->pNext = New;
```



#### • Inserting a Node in the Middle:

```
Node *New = NULL;

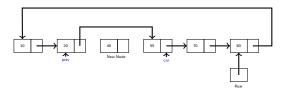
New = (Node *)malloc(sizeof(Node));

New->nData = 40;

cur = Rear.->pNext;

prev = Rear;

//Find the place to insert the node
```



#### • Inserting a Node in the Middle:

```
Node *New = NULL;

New = (Node *)malloc(sizeof(Node));

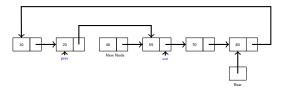
New->nData = 40;

cur = Rear.->pNext;

prev = Rear;

//Find the place to insert the node

New->pNext = Cur;
```



#### • Inserting a Node in the Middle:

```
Node *New = NULL;

New = (Node *)malloc(sizeof(Node));

New->nData = 40;

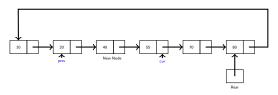
cur = Rear.->pNext;

prev = Rear;

//Find the place to insert the node

New->pNext = Cur;

Prev->pNext = New;
```



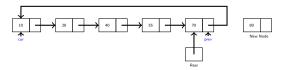
```
Node *New = NULL;

New = (Node *)malloc(sizeof(Node));

New->nData = 80;

cur = Rear->pNext;

prev = Rear;
```



```
Node *New = NULL;

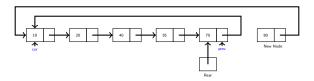
New = (Node *)malloc(sizeof(Node));

New->nData = 80;

cur = Rear->pNext;

prev = Rear;

New->pNext = Cur;
```



```
Node *New = NULL;

New = (Node *)malloc(sizeof(Node));

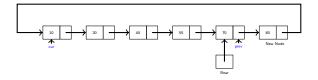
New->nData = 80;

cur = Rear->pNext;

prev = Rear;

New->pNext = Cur;

Prev->pNext = New;
```



```
Node *New = NULL;

New = (Node *)malloc(sizeof(Node));

New->nData = 80;

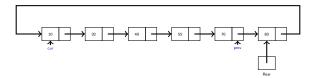
cur = Rear->pNext;

prev = Rear;

New->pNext = Cur;

Prev->pNext = New;

Rear = New;
```



### Delete Node

#### • List of Size 1:

```
free(Rear);
Rear = NULL;
```

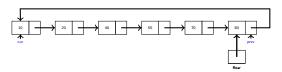


### Delete Node

#### • Deleting the Head Node:

```
cur = Rear->pNext;

prev = Rear;
```

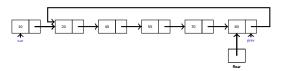


#### • Deleting the Head Node:

```
cur = Rear -> pNext;

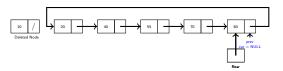
prev = Rear;

prev -> pNext = cur -> pNext;
```



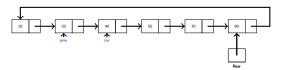
## Deleting the Head Node:

```
cur = Rear->pNext;
prev = Rear;
prev->pNext = cur->pNext;
free(cur);
cur = NULL;
```



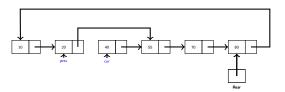
## Deleting a Middle Node:

```
\begin{split} & \mathsf{cur} = \mathsf{Rear}\text{-}\!>\!\mathsf{pNext}; \\ & \mathsf{prev} = \mathsf{Rear}; \\ & //\mathsf{Find} \ \mathsf{the} \ \mathsf{node} \ \mathsf{to} \ \mathsf{delete} \end{split}
```



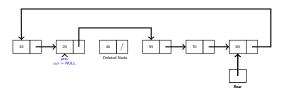
## • Deleting a Middle Node:

```
\begin{split} & \mathsf{cur} = \mathsf{Rear}\text{-}\!>\!\mathsf{pNext}; \\ & \mathsf{prev} = \mathsf{Rear}; \\ & //\mathsf{Find} \ \mathsf{the} \ \mathsf{node} \ \mathsf{to} \ \mathsf{delete} \\ & \mathsf{prev}\text{-}\!>\!\mathsf{pNext} = \mathsf{Cur}\text{-}\!>\!\mathsf{pNext}; \end{split}
```



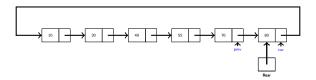
## Deleting a Middle Node:

```
cur = Rear->pNext;
prev = Rear;
//Find the node to delete
prev->pNext = Cur->pNext;
free(cur);
cur = NULL;
```



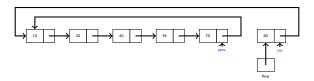
#### • Deleting the Node at the End:

```
\begin{split} &\text{cur} = \text{Rear->pNext;} \\ &\text{prev} = \text{Rear;} \\ &\text{//Traverse till the end of the list, i.e., till cur} == \text{Rear} \end{split}
```



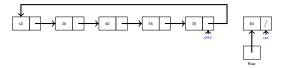
## Deleting the Node at the End:

```
\begin{split} & cur = Rear->pNext; \\ & prev = Rear; \\ & //Traverse\ till\ the\ end\ of\ the\ list,\ i.e.,\ till\ cur == Rear \\ & prev->pNext = cur->pNext; \end{split}
```



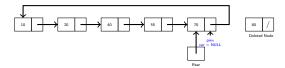
## Deleting the Node at the End:

```
\begin{split} & cur = Rear -> pNext; \\ & prev = Rear; \\ & // Traverse \ till \ the \ end \ of \ the \ list, \ i.e., \ till \ cur == Rear \\ & prev -> pNext = cur -> pNext; \\ & free(cur); \end{split}
```



## Deleting the Node at the End:

```
cur = Rear->pNext;
prev = Rear;
//Traverse till the end of the list, i.e., till cur == Rear
prev->pNext = cur->pNext;
free(cur);
Rear = prev;
cur = NULL
```



## **Exercises**

Assuming that there can exists at most one loop in a singly linked list, find an algorithm to determine whether a single linked list has a loop or not.

## **Books Consulted**

Chapter 10.2 of Introduction to Algorithms by Thomas H Cormen, Charles E Leiserson, Ronald L Rivest, Clifford Stein.

Thank You for your kind attention!

# Questions!!