

Threaded Binary Tree

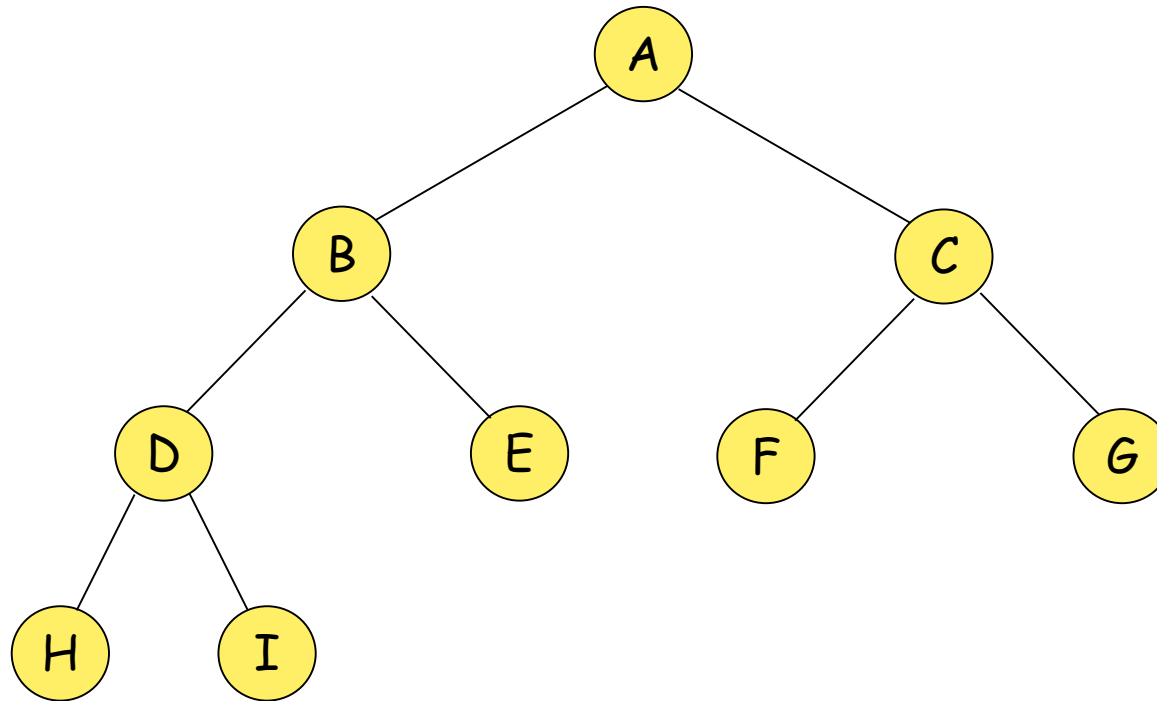
- Threads

- In a linked representation of a binary tree, there are more NULL links than actual pointers.
 - In a binary tree with n nodes containing $2n$ links, there are $n+1$ NULL links.
 - Perlis and Thornton devised a way to make use of NULL links.
 - Here the NULL links are replaced by pointers, called *threads*, to other nodes in the tree.
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Threaded Binary Tree

- Threading Rules
 - A NULL RightChild field at node p is replaced by a pointer to the node that would be visited after p when traversing the tree in inorder. That is, it is replaced by the inorder successor of p.
 - A NULL LeftChild link at node p is replaced by a pointer to the node that immediately precedes node p in inorder (i.e., it is replaced by the inorder predecessor of p).
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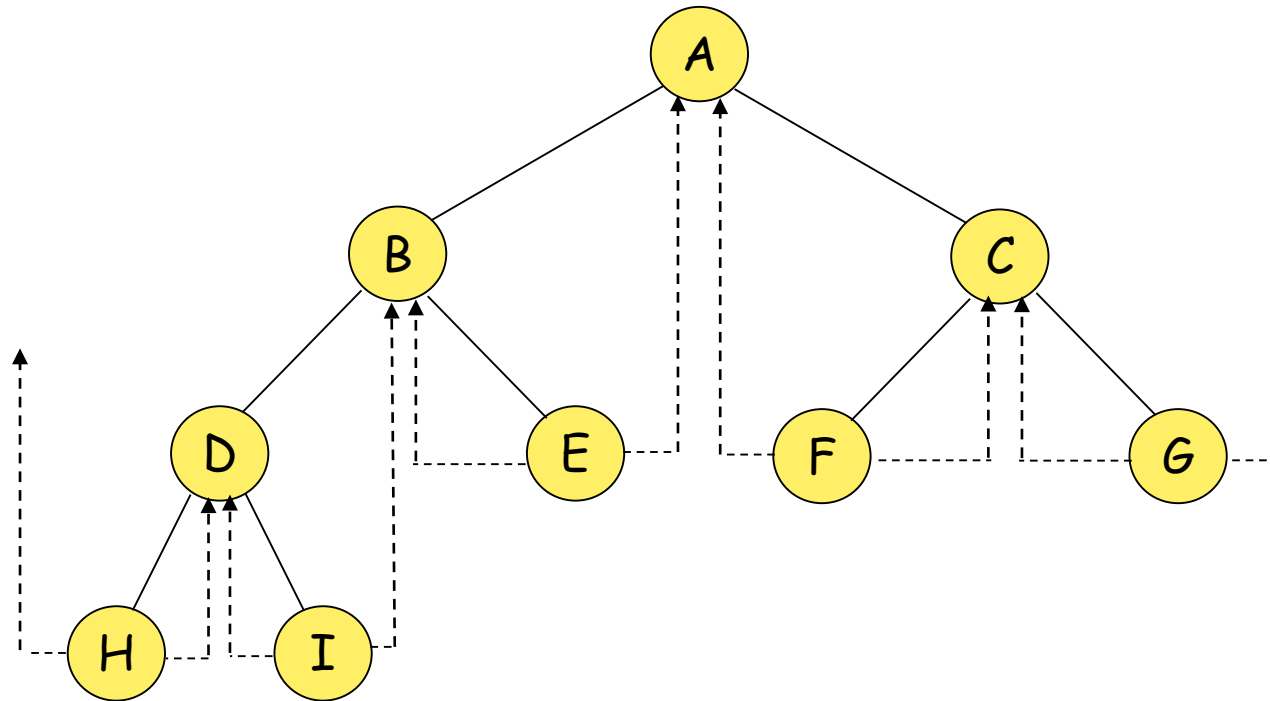
A Binary Tree



Inorder sequence: H, D, I, B, E, A, F, C, G



Threaded Tree Corresponding to Given Binary Tree



Inorder sequence: H, D, I, B, E, A, F, C, G



Threads

- To distinguish between normal pointers and threads, two boolean fields, LeftThread and RightThread, are added to the record in memory representation.
 - t->leftThread= TRUE
⇒ t->lchild is a **thread**
 - t->leftThread= FALSE
⇒ t->lchild is a **pointer** to the left child.
 - t->rightThread= TRUE
⇒ t->rchild is a **thread**
 - t->rightThread= FALSE
⇒ t->rchild is a **pointer** to the right child.

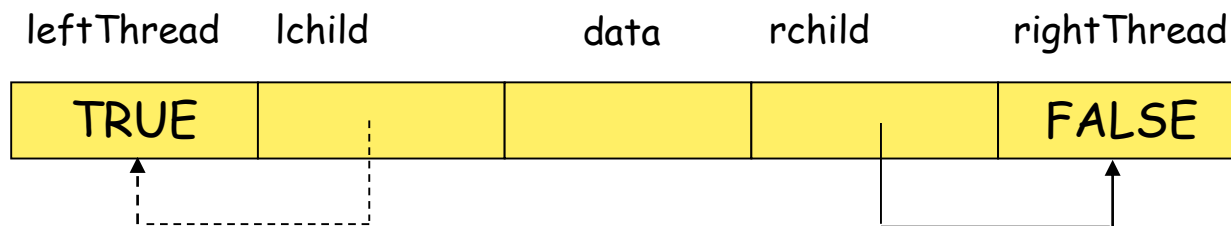
Threaded Binary Tree Node Structure Declaration

```
typedef struct threadedTree *threadedPointer;
```

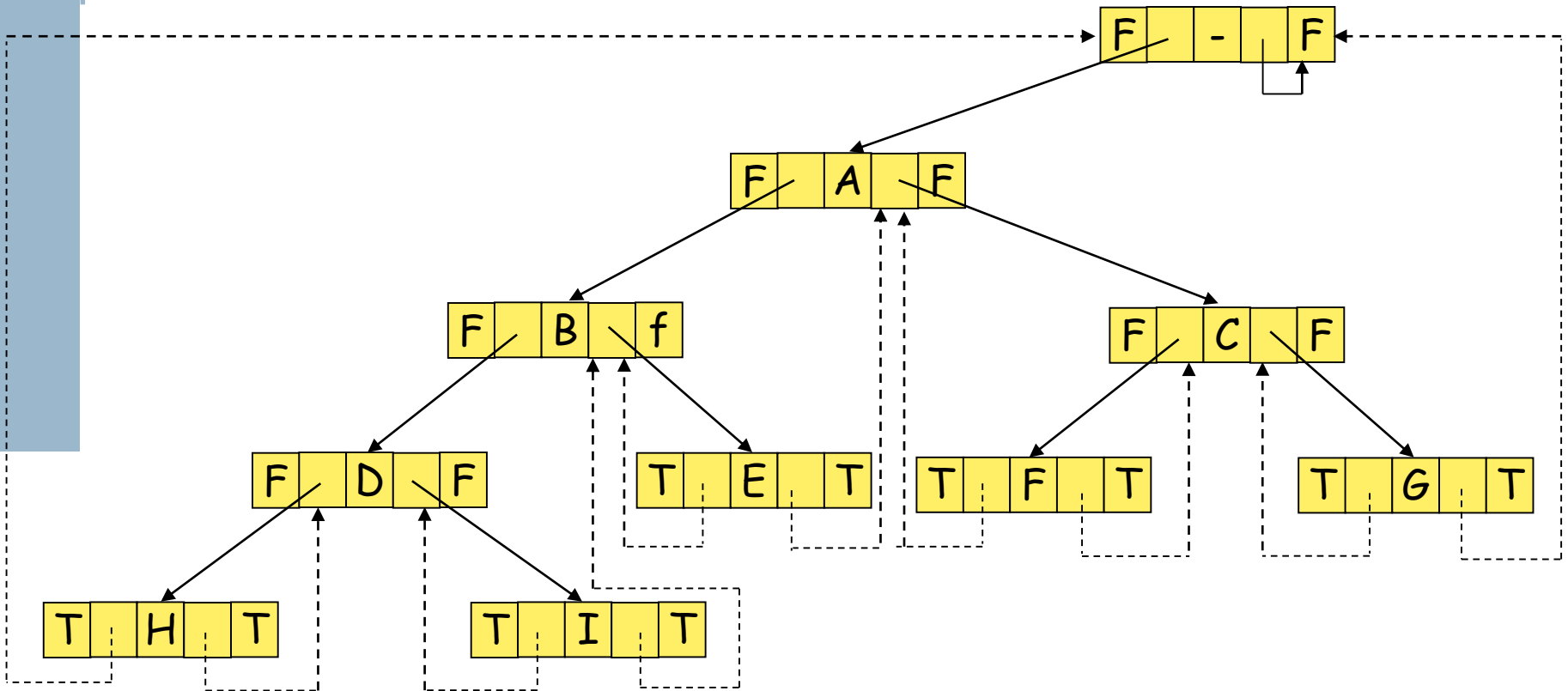
```
struct threadedTree{  
    short int leftThread;  
    threadedPointer lchild;  
    char data;  
    threadedPointer rchild;  
    short int rightThread;  
};
```

Threads (Cont.)

- To avoid dangling threads, a head node is used in representing a binary tree.
- The original tree becomes the left subtree of the head node.
- Empty Binary Tree



Memory Representation of Threaded Tree



Finding the inorder successor without stack

- By using the threads, we can perform an inorder traversal without making use of a stack.

```
threadedPointer insucc(threadedPointer node)
{ //Return the inorder successor of node
    threadedPointer temp = node-> rchild;
    if (node->rightThread==FALSE)
        while (temp->leftThread==FALSE)
            temp = temp -> lchild;
    return temp;
}
```

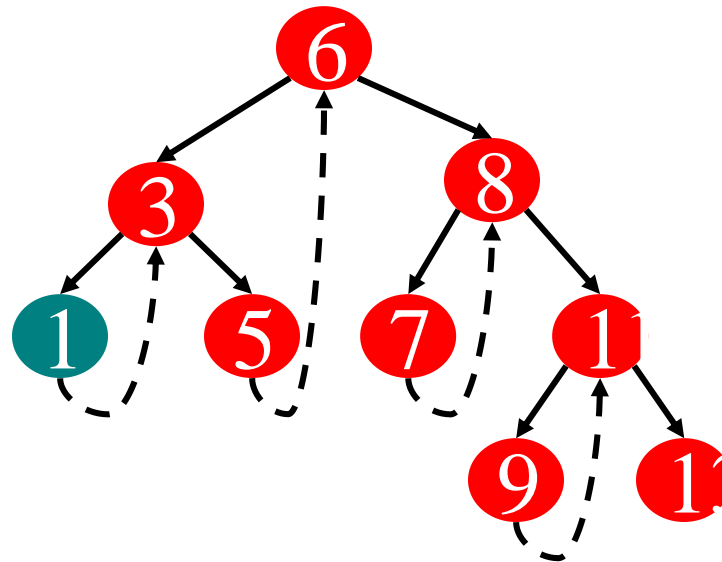
Inorder Traversal of a threaded Binary Tree

```
void tinorder(threadedPointer treehead)
{
    threadedPointer temp = treehead;
    while(1){
        temp = insucc(temp);
        if (temp == treehead) break;
        printf("%c", temp->data);
    }
}
```

Threaded Tree Traversal

- We start at the leftmost node in the tree, print it, and follow its right thread
- If we follow a thread to the right, we output the node and continue to its right
- If we follow a link to the right, we go to the leftmost node, print it, and continue

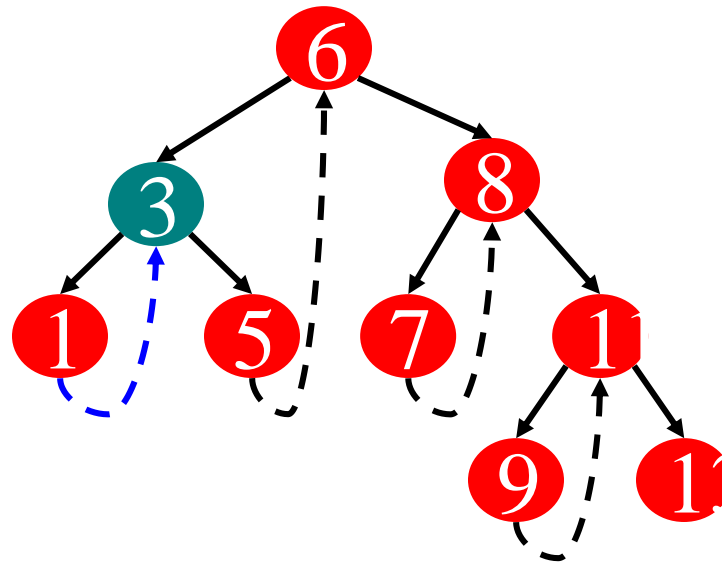
Threaded Tree Traversal



Output
1

Start at leftmost node, print it

Threaded Tree Traversal

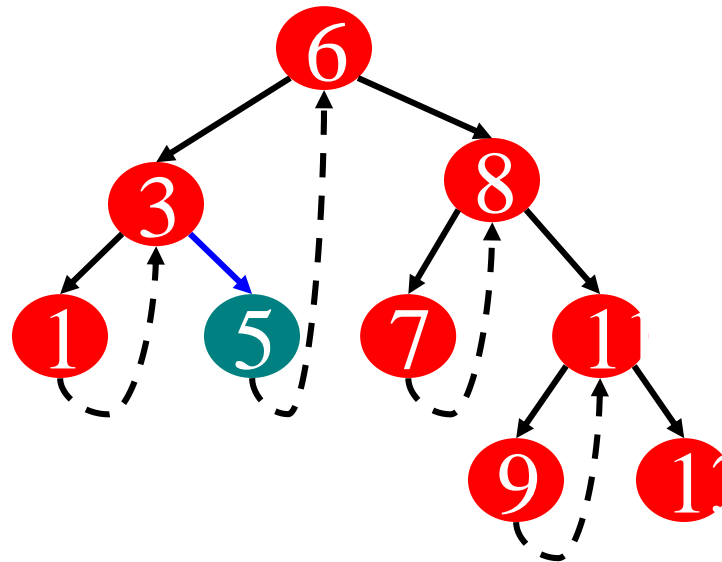


Output

1
3

Follow thread to right, print node

Threaded Tree Traversal

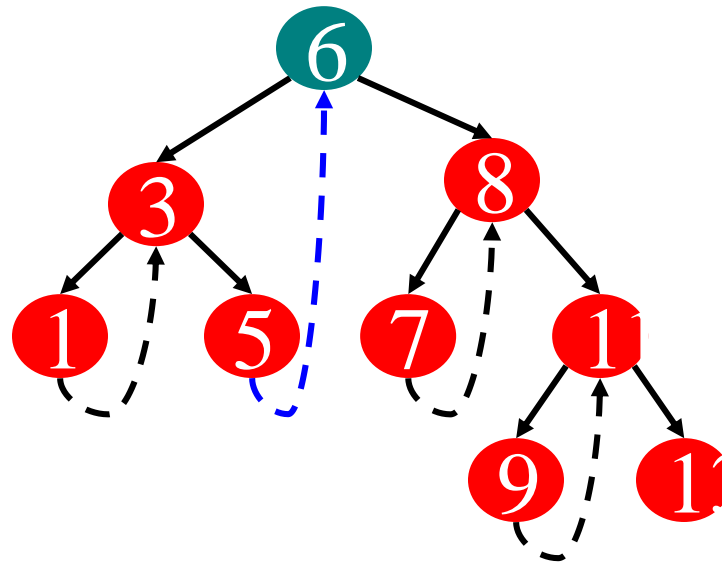


Output

1
3
5

Follow link to right, go to
leftmost node and print

Threaded Tree Traversal

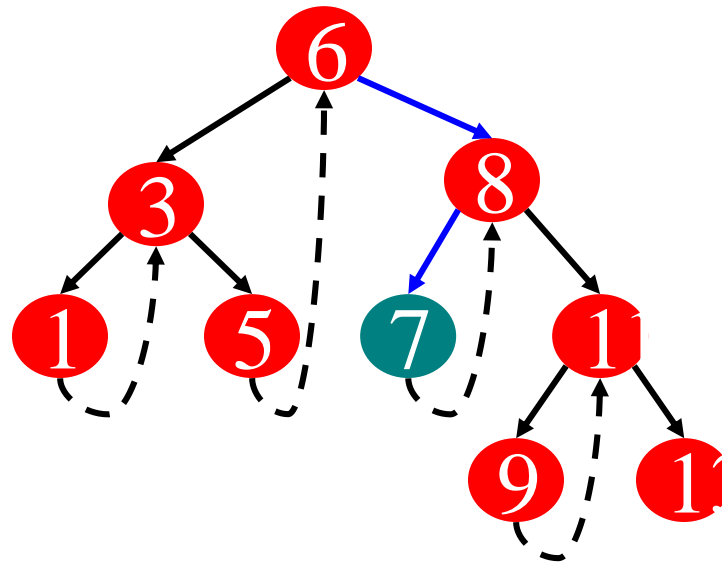


Output

1
3
5
6

Follow thread to right, print node

Threaded Tree Traversal

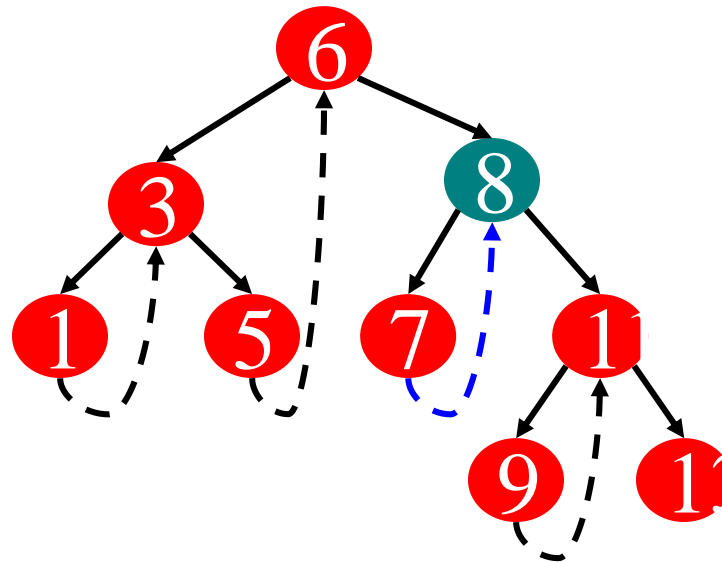


Output

1
3
5
6
7

Follow link to right, go to
leftmost node and print

Threaded Tree Traversal

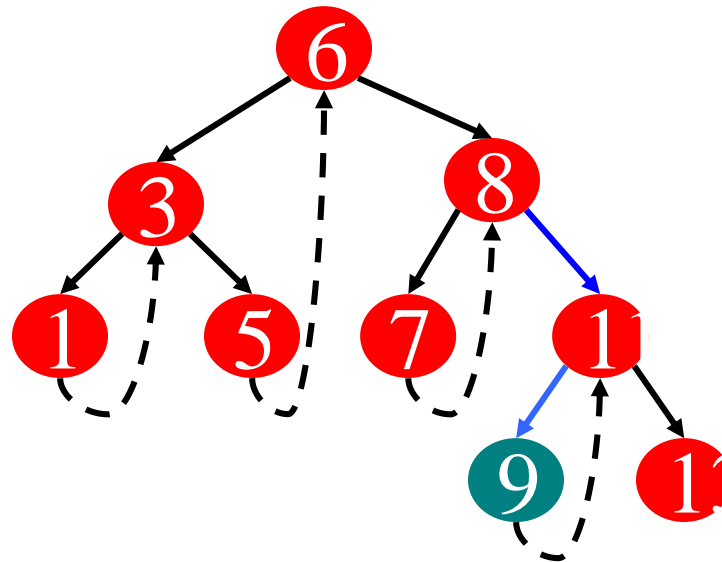


Output

1
3
5
6
7
8

Follow thread to right, print node

Threaded Tree Traversal

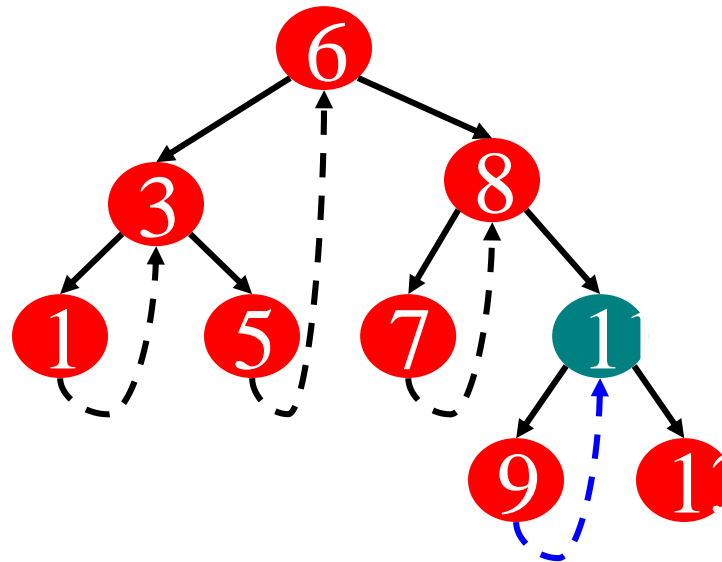


Output

1
3
5
6
7
8
9

Follow link to right, go to
leftmost node and print

Threaded Tree Traversal

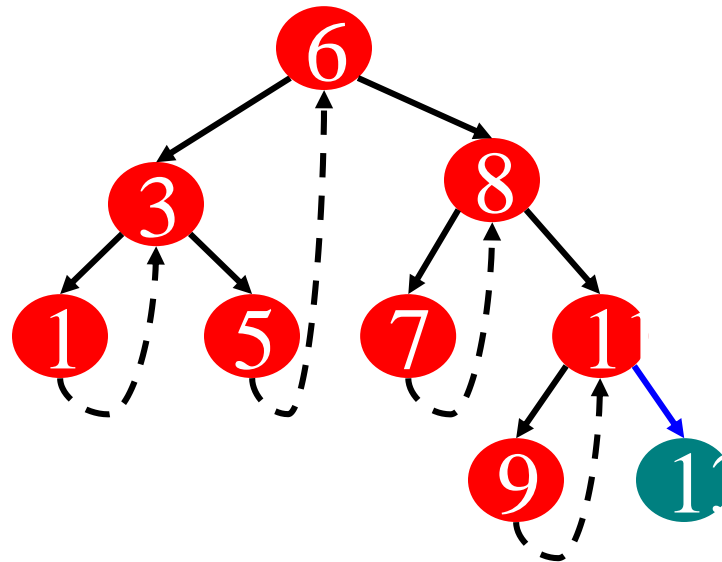


Output

1
3
5
6
7
8
9
11

Follow thread to right, print node

Threaded Tree Traversal



Output

1
3
5
6
7
8
9
11
13

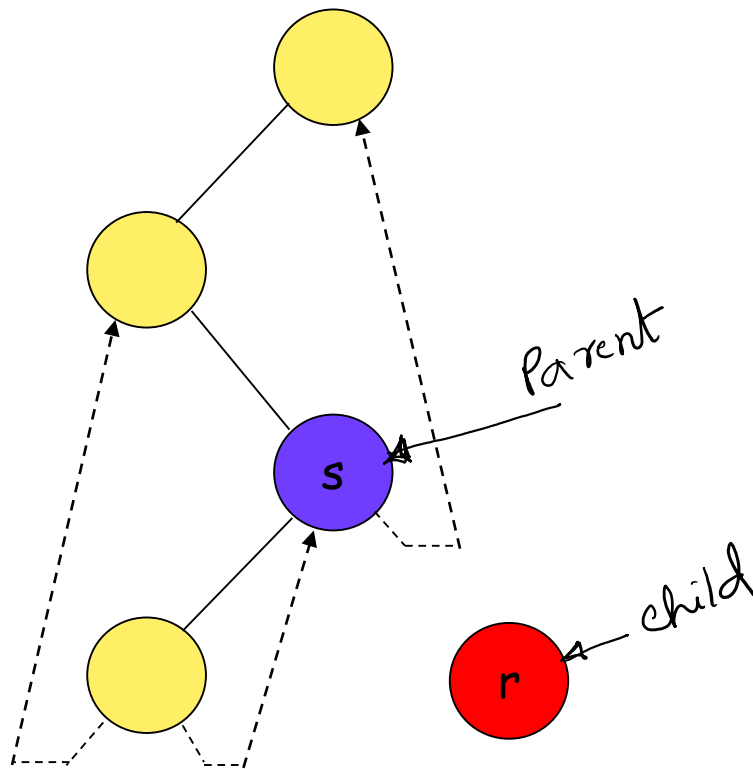
Follow link to right, go to
leftmost node and print

Inserting A Node to A Threaded Binary Tree

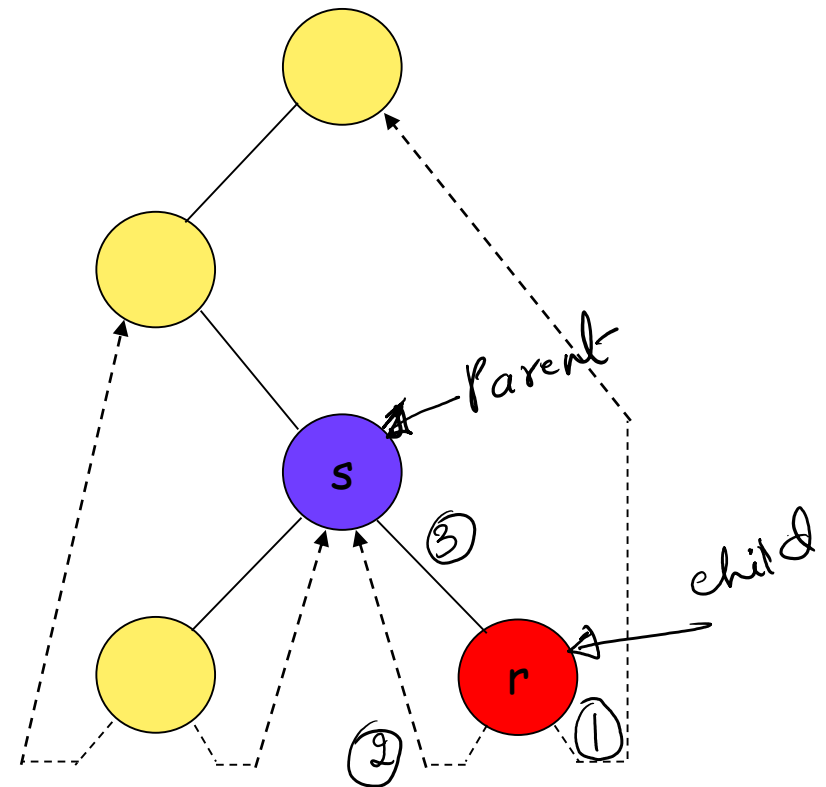
- Inserting a node r as the right child of a node s .
 - If s has an empty right subtree, then the insertion is simple (as shown in diagram next slide)
 - If the right subtree of s is not empty, then, this right subtree is made the right subtree of r after insertion. When this is done, r becomes the inorder predecessor of a node that has a `leftThread==TRUE` field, and consequently there is an thread which has to be updated to point to r . The node containing this thread was previously the inorder successor of s . Figure illustrates the insertion for this case.

Insertion of r As A Right Child of s in A Threaded Binary Tree

case (a) (Empty rt subtree for s)



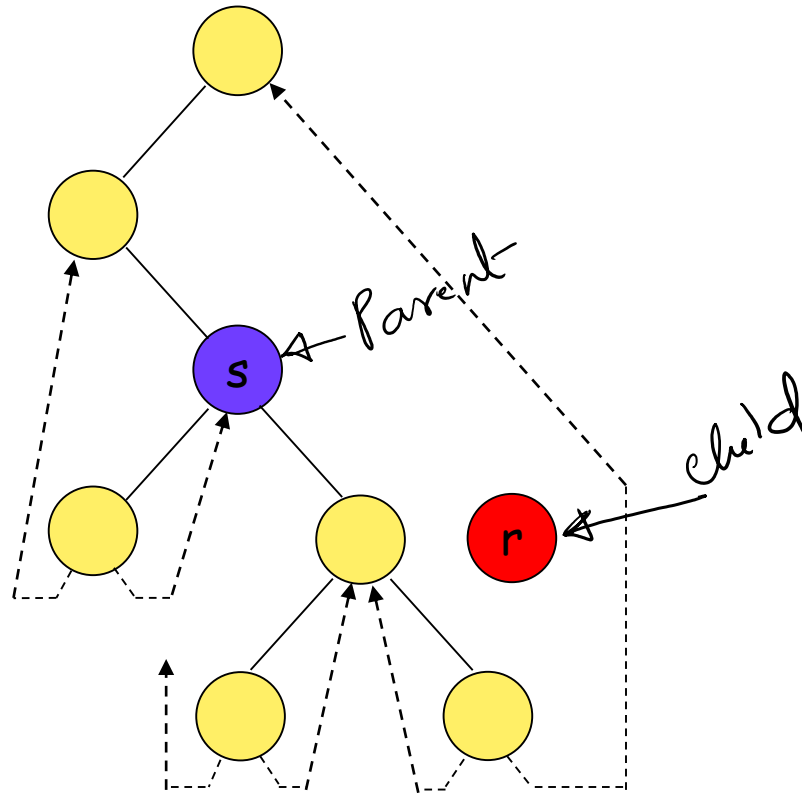
before



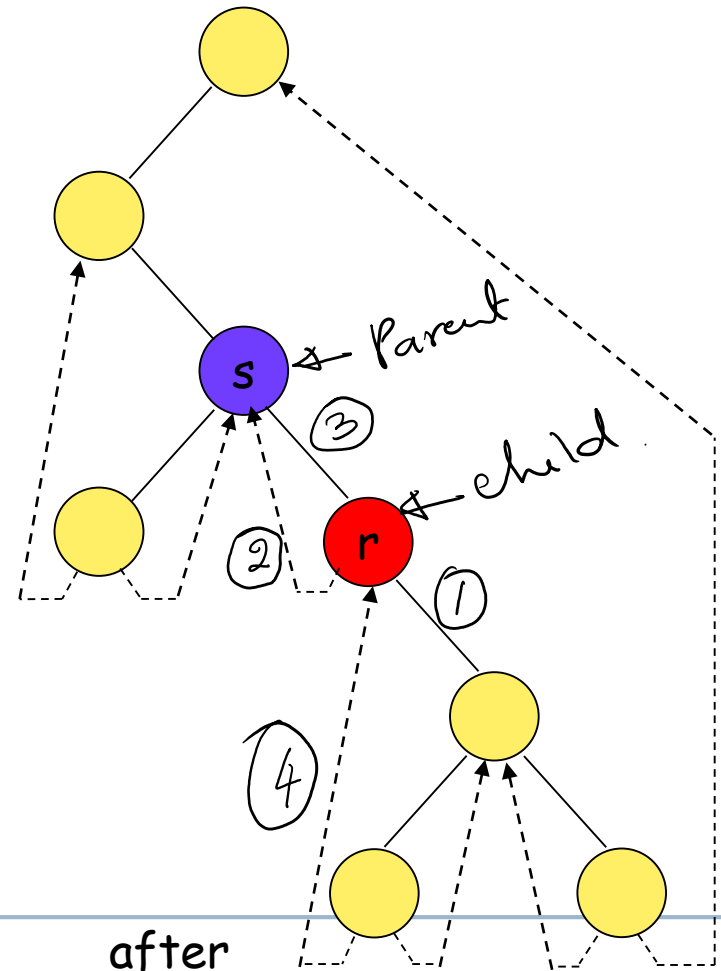
after

Insertion of r As A Right Child of s in A Threaded Binary Tree (Cont.)

Case (b) (nonempty right subtree for s)



before



after