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# Abstract

(Farazmand and Haller 2012)

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<b>Sammendrag</b>

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<b>Preface</b>

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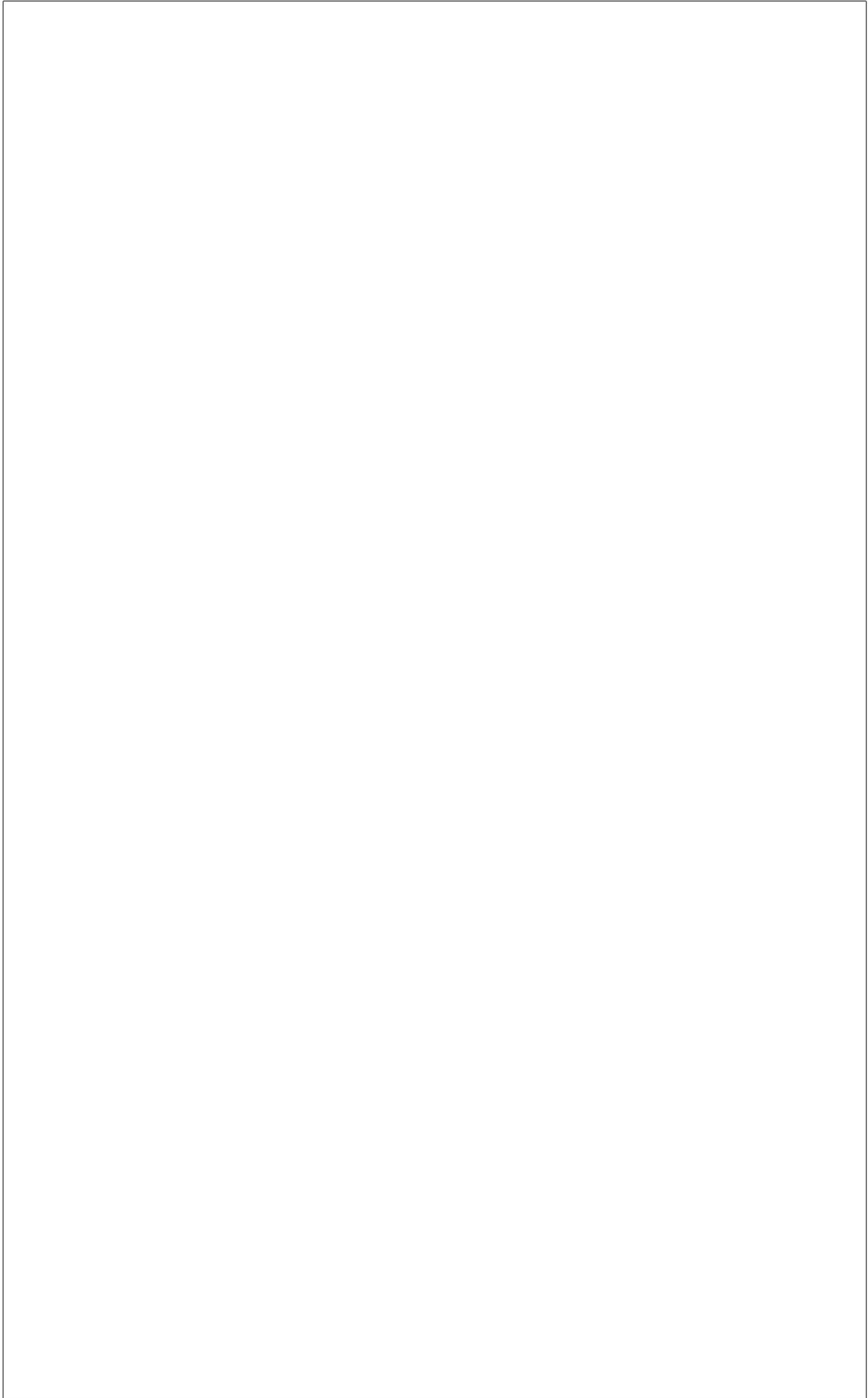
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Notation



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# 1 Introduction

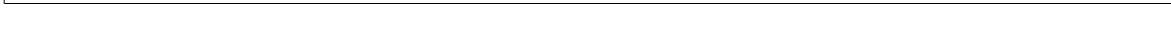




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## 2 Theory



**3 Method**

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<b>4 Results</b>
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## 5 Discussion

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## 6 Conclusions

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<b>A Appendix A</b>