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# Boston Housing Prices Prediction

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## Content of the Boston Housing data frame

The Boston data frame contains 489 rows and 4 columns. This data frame contains the following columns:

RM - average number of rooms per dwelling

PTRATIO - pupil-teacher ratio by town

LSTAT - % lower status of the population

MEDV - Median value of owner-occupied homes in \$1000's

The **MEDV** variable is the target variable.

## Statistics of the Boston Housing data frame

The data was analysed using Python software and various statistics were calculated, which are being tabulated below:

	<b>RM</b>	<b>LSTAT</b>	<b>PTRATIO</b>	<b>MEDV</b>
<b>count</b>	489.000000	489.000000	489.000000	489.000000
<b>mean</b>	6.240288	12.939632	18.516564	4.543429e+05
<b>Standard deviation</b>	0.643650	7.081990	2.111268	1.653403e+05
<b>min</b>	3.561000	1.980000	12.600000	1.050000e+05
<b>25%</b>	5.880000	7.370000	17.400000	3.507000e+05
<b>50%</b>	6.185000	11.690000	19.100000	4.389000e+05
<b>75%</b>	6.575000	17.120000	20.200000	5.187000e+05
<b>max</b>	8.398000	37.970000	22.000000	1.024800e+06

### 1. Boxplot of the data

Following boxplot gives us the indication of how the values in the data are spread out.

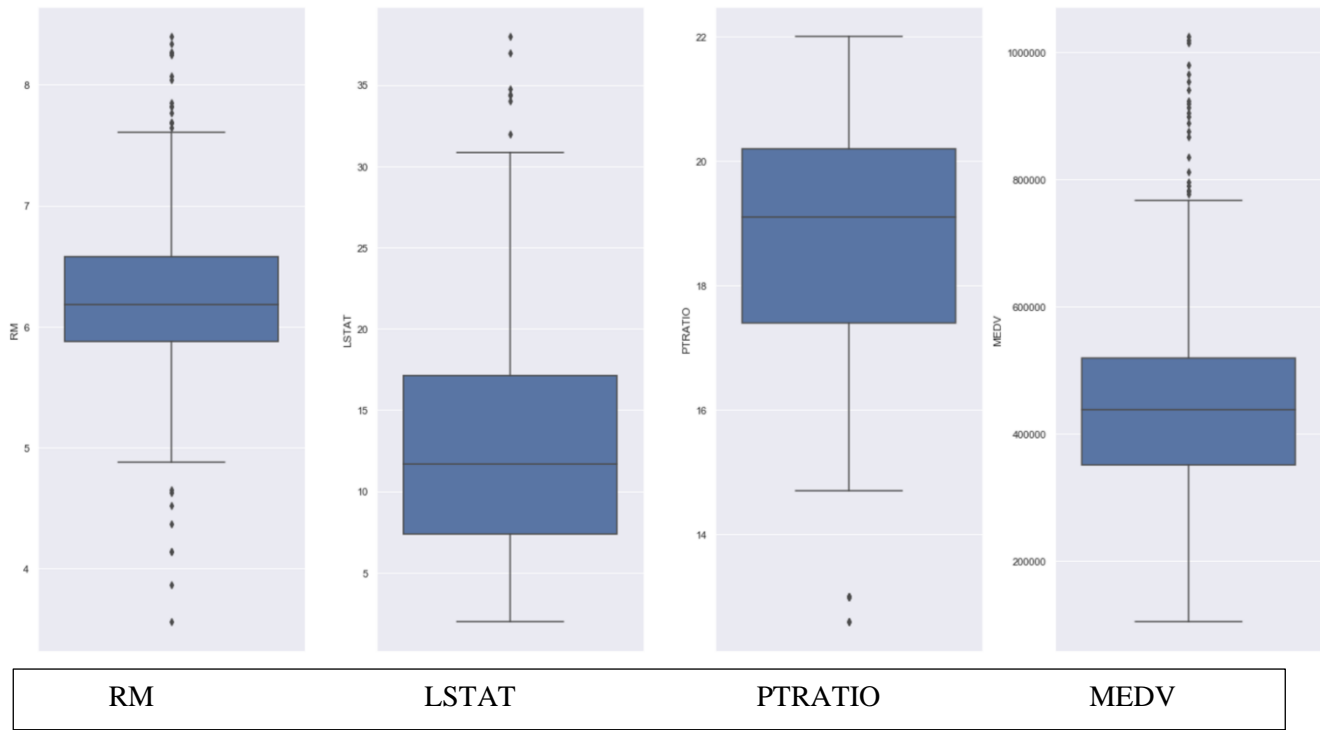
As it can be seen from the boxplot, the % of outliers present in each column are:

RM outliers = 4.50%

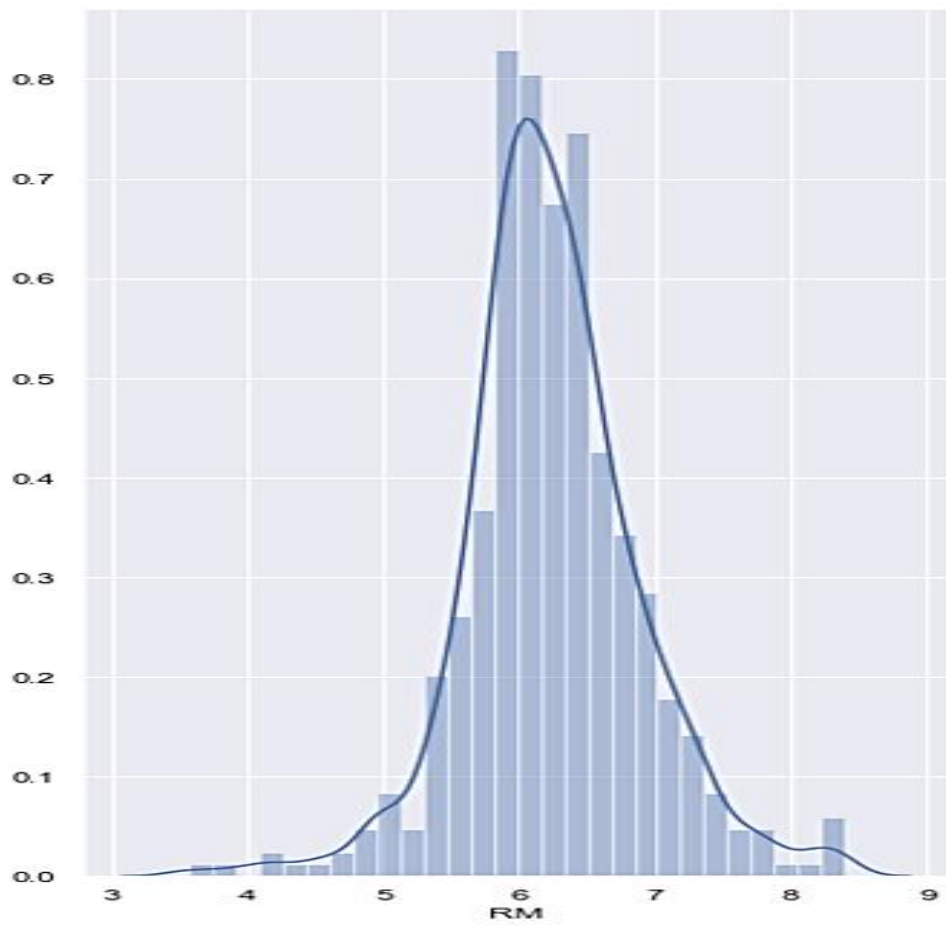
LSTAT outliers = 1.43%

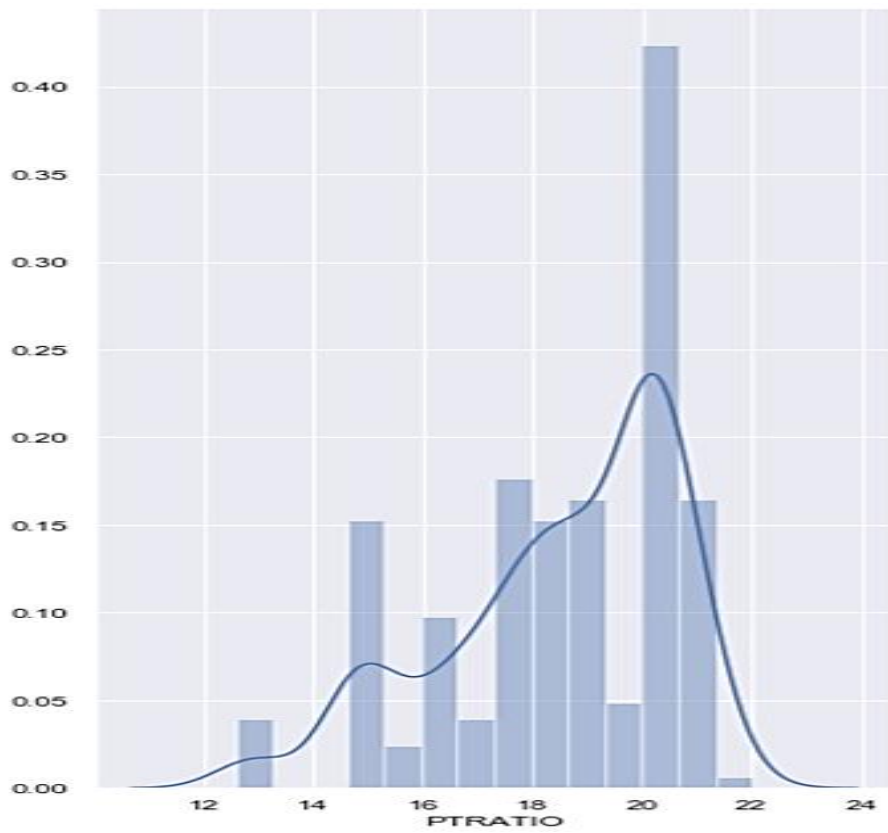
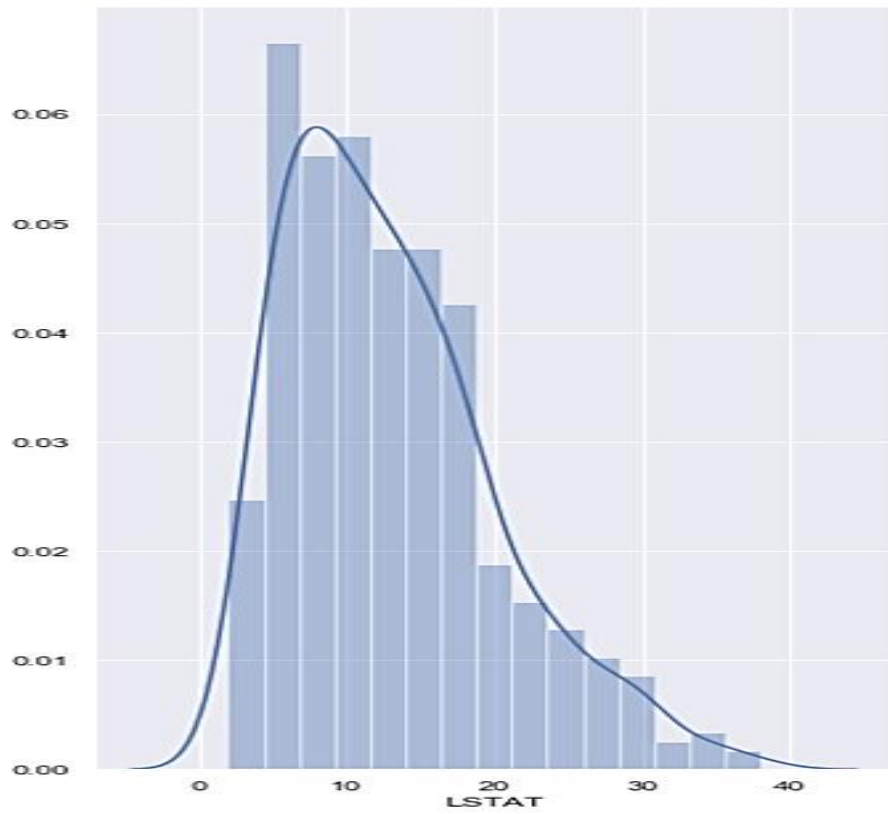
PTRATIO outliers = 2.66%

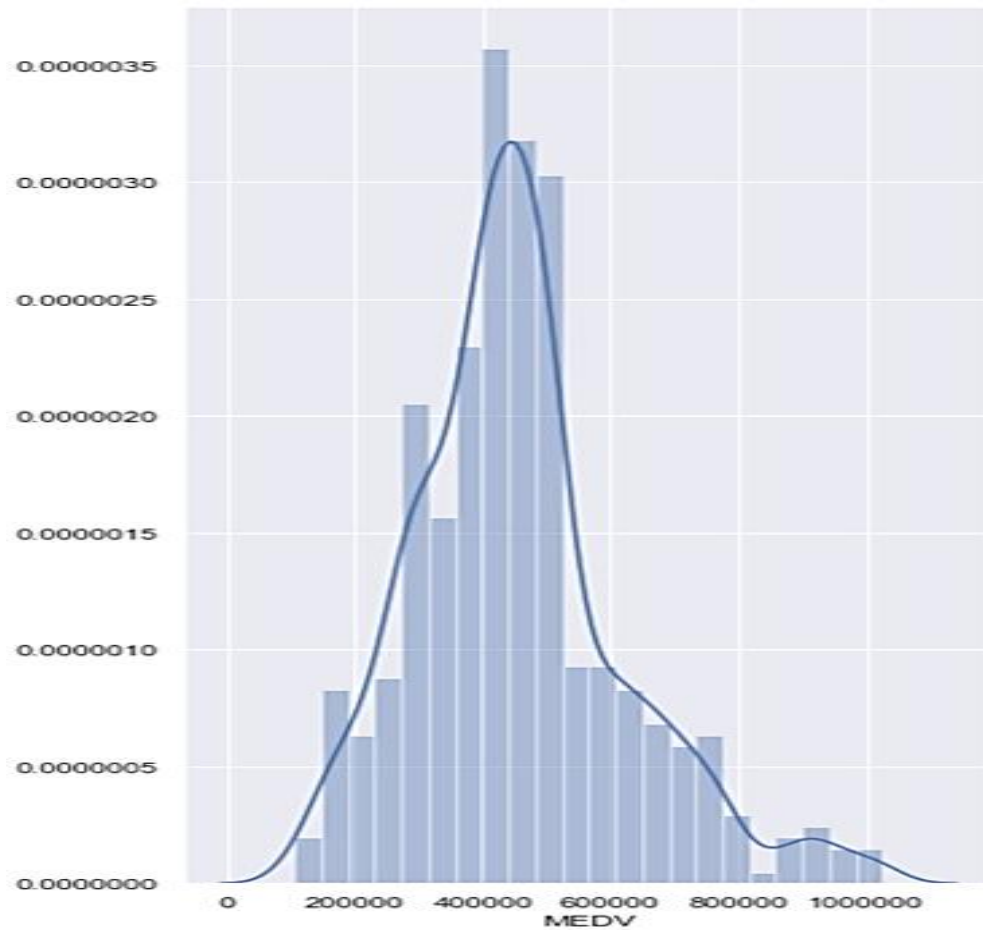
MEDV outliers = 4.50%



## 2. Frequency distribution of data

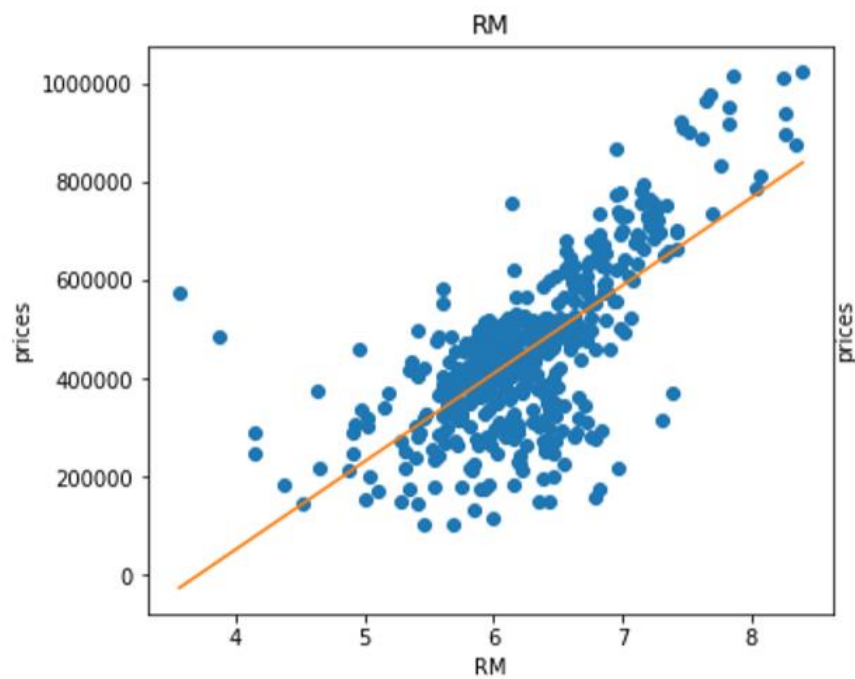


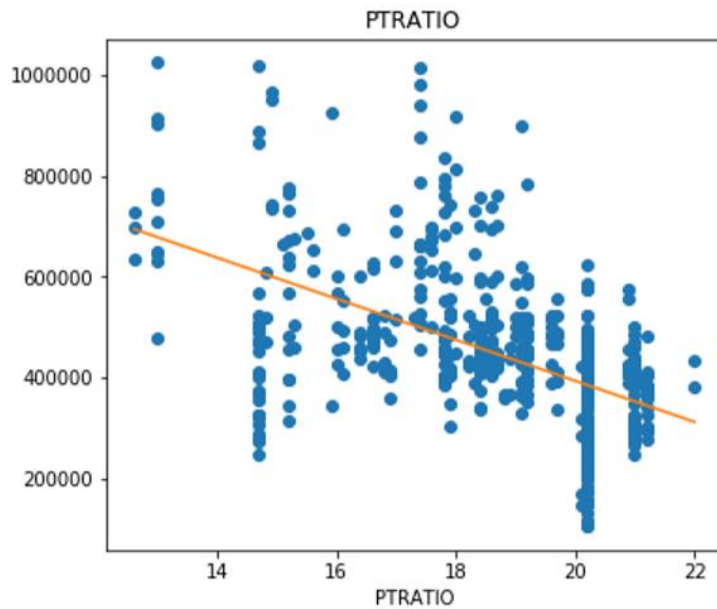
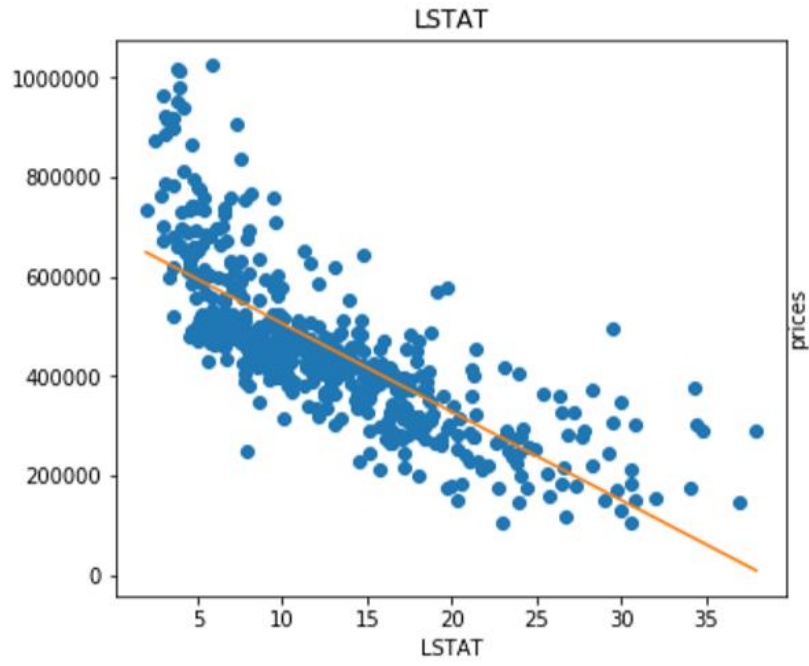




### 3. Regression analysis

Here prices indicate the MEDV variable. As it can be seen, prices are increasing with the RM variable and decreasing with the LSTAT and PTRATIO variable.





#### 4. Correlation matrix

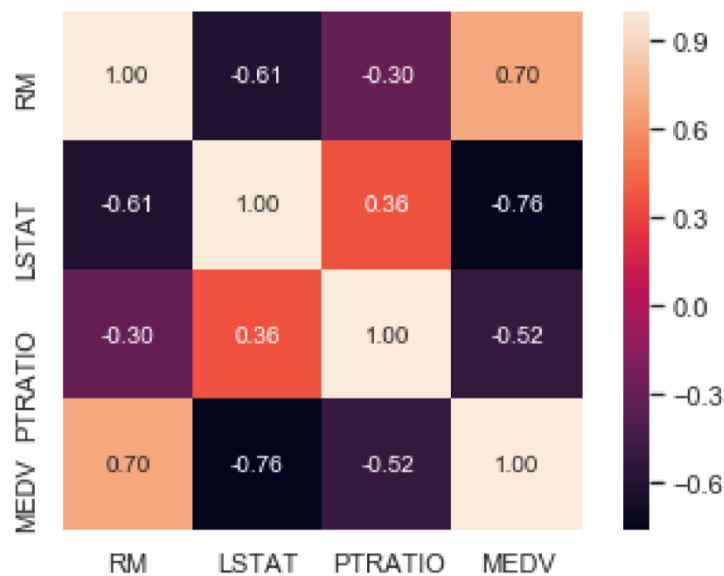
Linear regression and Random Forest models were applied to the given data and R square values were calculated. Based on R square was found that, **Random Forest model** is a better fit for the given data. However, to reach a conclusion with a greater degree of accuracy, we need more data.

A Random Forest is an ensemble technique capable of performing both regression and classification tasks with the use of multiple decision trees and a technique called Bootstrap Aggregation, commonly known

as bagging. The basic idea behind this technique is to combine multiple decision trees in determining the final output rather than relying on individual decision trees.

The r square values came out to be 0.6083795028938159 for Random Forest, and for regression modelling r square values came out to be 0.7726270688507346.

Further, a correlation matrix was tabulated, as shown below, indicating the correlation coefficients between various variables. Each cell in the table shows the correlation between two variables. The values of correlation vary in the range of -1 to 1. More the absolute values of the correlation between the two variables, more the two variables are related to each other.



As it can be seen from the above correlation matrix, the variables “RM” and “MEDV” has the highest correlation value of 0.70 in the matrix. Thus, among all the variables, the variables “RM” and “MEDV” are best related to each other. Further, the variables “RM” and “LSTAT” have correlation value of 0.61 in the matrix. Thus, they are also highly related to each other.

## 5. Z-Test

$H_0 : \mu(\text{actual value}) = \mu(\text{predicted value})$

$H_1 : \mu(\text{actual value}) \neq \mu(\text{predicted value})$

We performed a Z test for linear regression and random forest model at 5% significance.

Z value for linear regression came out to be 0.2684949105149169.

Z value for random forest model came out to be 0.07279780558113479.

Since both the calculated values of Z are less than the critical Z i.e. 1.96, Null Hypothesis is accepted for both the cases.



## 6. Conclusion

Although, both the models provide fairly accurate results in terms of predicting the housing prices, we should choose the Random Classifier model as it gives better results in terms of accuracy

## 7. References

<https://www.kaggle.com/c/boston-housing/data>

<https://towardsdatascience.com/linear-regression-detailed-view-ea73175f6e86>

<https://www.statisticssolutions.com/what-is-linear-regression/>

<https://towardsdatascience.com/understanding-random-forest-58381e0602d2>

## Appendix I – Dataset

Following are the variables present in the dataset:

RM - average number of rooms per dwelling

PTRATIO - pupil-teacher ratio by town

LSTAT - % lower status of the population

MEDV - Median value of owner-occupied homes in \$1000's

<u>RM</u>	<u>LSTAT</u>	<u>PTRATIO</u>	<u>MEDV</u>
6.575	4.98	15.3	504000
6.421	9.14	17.8	453600
7.185	4.03	17.8	728700
6.998	2.94	18.7	701400
7.147	5.33	18.7	760200
6.43	5.21	18.7	602700
6.012	12.43	15.2	480900
6.172	19.15	15.2	569100
5.631	29.93	15.2	346500
6.004	17.1	15.2	396900
6.377	20.45	15.2	315000
6.009	13.27	15.2	396900
5.889	15.71	15.2	455700
5.949	8.26	21	428400
6.096	10.26	21	382200
5.834	8.47	21	417900
5.935	6.58	21	485100
5.99	14.67	21	367500
5.456	11.69	21	424200
5.727	11.28	21	382200
5.57	21.02	21	285600
5.965	13.83	21	411600
6.142	18.72	21	319200
5.813	19.88	21	304500
5.924	16.3	21	327600

<b>5.599</b>	16.51	21	291900
<b>5.813</b>	14.81	21	348600
<b>6.047</b>	17.28	21	310800
<b>6.495</b>	12.8	21	386400
<b>6.674</b>	11.98	21	441000
<b>5.713</b>	22.6	21	266700
<b>6.072</b>	13.04	21	304500
<b>5.95</b>	27.71	21	277200
<b>5.701</b>	18.35	21	275100
<b>6.096</b>	20.34	21	283500
<b>5.933</b>	9.68	19.2	396900
<b>5.841</b>	11.41	19.2	420000
<b>5.85</b>	8.77	19.2	441000
<b>5.966</b>	10.13	19.2	518700
<b>6.595</b>	4.32	18.3	646800
<b>7.024</b>	1.98	18.3	732900
<b>6.77</b>	4.84	17.9	558600
<b>6.169</b>	5.81	17.9	531300
<b>6.211</b>	7.44	17.9	518700
<b>6.069</b>	9.55	17.9	445200
<b>5.682</b>	10.21	17.9	405300
<b>5.786</b>	14.15	17.9	420000
<b>6.03</b>	18.8	17.9	348600
<b>5.399</b>	30.81	17.9	302400
<b>5.602</b>	16.2	17.9	407400
<b>5.963</b>	13.45	16.8	413700
<b>6.115</b>	9.43	16.8	430500
<b>6.511</b>	5.28	16.8	525000
<b>5.998</b>	8.43	16.8	491400
<b>5.888</b>	14.8	21.1	396900
<b>7.249</b>	4.81	17.9	743400
<b>6.383</b>	5.77	17.3	518700
<b>6.816</b>	3.95	15.1	663600
<b>6.145</b>	6.86	19.7	489300
<b>5.927</b>	9.22	19.7	411600

<b>5.741</b>	13.15	19.7	392700
<b>5.966</b>	14.44	19.7	336000
<b>6.456</b>	6.73	19.7	466200
<b>6.762</b>	9.5	19.7	525000
<b>7.104</b>	8.05	18.6	693000
<b>6.29</b>	4.67	16.1	493500
<b>5.787</b>	10.24	16.1	407400
<b>5.878</b>	8.1	18.9	462000
<b>5.594</b>	13.09	18.9	365400
<b>5.885</b>	8.79	18.9	438900
<b>6.417</b>	6.72	19.2	508200
<b>5.961</b>	9.88	19.2	455700
<b>6.065</b>	5.52	19.2	478800
<b>6.245</b>	7.54	19.2	491400
<b>6.273</b>	6.78	18.7	506100
<b>6.286</b>	8.94	18.7	449400
<b>6.279</b>	11.97	18.7	420000
<b>6.14</b>	10.27	18.7	436800
<b>6.232</b>	12.34	18.7	445200
<b>5.874</b>	9.1	18.7	426300
<b>6.727</b>	5.29	19	588000
<b>6.619</b>	7.22	19	501900
<b>6.302</b>	6.72	19	520800
<b>6.167</b>	7.51	19	480900
<b>6.389</b>	9.62	18.5	501900
<b>6.63</b>	6.53	18.5	558600
<b>6.015</b>	12.86	18.5	472500
<b>6.121</b>	8.44	18.5	466200
<b>7.007</b>	5.5	17.8	495600
<b>7.079</b>	5.7	17.8	602700
<b>6.417</b>	8.81	17.8	474600
<b>6.405</b>	8.2	17.8	462000
<b>6.442</b>	8.16	18.2	480900
<b>6.211</b>	6.21	18.2	525000
<b>6.249</b>	10.59	18.2	432600

<b>6.625</b>	6.65	18	596400
<b>6.163</b>	11.34	18	449400
<b>8.069</b>	4.21	18	812700
<b>7.82</b>	3.57	18	919800
<b>7.416</b>	6.19	18	697200
<b>6.727</b>	9.42	20.9	577500
<b>6.781</b>	7.67	20.9	556500
<b>6.405</b>	10.63	20.9	390600
<b>6.137</b>	13.44	20.9	405300
<b>6.167</b>	12.33	20.9	422100
<b>5.851</b>	16.47	20.9	409500
<b>5.836</b>	18.66	20.9	409500
<b>6.127</b>	14.09	20.9	428400
<b>6.474</b>	12.27	20.9	415800
<b>6.229</b>	15.55	20.9	407400
<b>6.195</b>	13	20.9	455700
<b>6.715</b>	10.16	17.8	478800
<b>5.913</b>	16.21	17.8	394800
<b>6.092</b>	17.09	17.8	392700
<b>6.254</b>	10.45	17.8	388500
<b>5.928</b>	15.76	17.8	384300
<b>6.176</b>	12.04	17.8	445200
<b>6.021</b>	10.3	17.8	403200
<b>5.872</b>	15.37	17.8	428400
<b>5.731</b>	13.61	17.8	405300
<b>5.87</b>	14.37	19.1	462000
<b>6.004</b>	14.27	19.1	426300
<b>5.961</b>	17.93	19.1	430500
<b>5.856</b>	25.41	19.1	363300
<b>5.879</b>	17.58	19.1	394800
<b>5.986</b>	14.81	19.1	449400
<b>5.613</b>	27.26	19.1	329700
<b>5.693</b>	17.19	21.2	340200
<b>6.431</b>	15.39	21.2	378000
<b>5.637</b>	18.34	21.2	300300

<b>6.458</b>	12.6	21.2	403200
<b>6.326</b>	12.26	21.2	411600
<b>6.372</b>	11.12	21.2	483000
<b>5.822</b>	15.03	21.2	386400
<b>5.757</b>	17.31	21.2	327600
<b>6.335</b>	16.96	21.2	380100
<b>5.942</b>	16.9	21.2	365400
<b>6.454</b>	14.59	21.2	359100
<b>5.857</b>	21.32	21.2	279300
<b>6.151</b>	18.46	21.2	373800
<b>6.174</b>	24.16	21.2	294000
<b>5.019</b>	34.41	21.2	302400
<b>5.403</b>	26.82	14.7	281400
<b>5.468</b>	26.42	14.7	327600
<b>4.903</b>	29.29	14.7	247800
<b>6.13</b>	27.8	14.7	289800
<b>5.628</b>	16.65	14.7	327600
<b>4.926</b>	29.53	14.7	306600
<b>5.186</b>	28.32	14.7	373800
<b>5.597</b>	21.45	14.7	323400
<b>6.122</b>	14.1	14.7	451500
<b>5.404</b>	13.28	14.7	411600
<b>5.012</b>	12.12	14.7	321300
<b>5.709</b>	15.79	14.7	407400
<b>6.129</b>	15.12	14.7	357000
<b>6.152</b>	15.02	14.7	327600
<b>5.272</b>	16.14	14.7	275100
<b>6.943</b>	4.59	14.7	867300
<b>6.066</b>	6.43	14.7	510300
<b>6.51</b>	7.39	14.7	489300
<b>6.25</b>	5.5	14.7	567000
<b>5.854</b>	11.64	14.7	476700
<b>6.101</b>	9.81	14.7	525000
<b>5.877</b>	12.14	14.7	499800
<b>6.319</b>	11.1	14.7	499800

<b>6.402</b>	11.32	14.7	468300
<b>5.875</b>	14.43	14.7	365400
<b>5.88</b>	12.03	14.7	401100
<b>5.572</b>	14.69	16.6	485100
<b>6.416</b>	9.04	16.6	495600
<b>5.859</b>	9.64	16.6	474600
<b>6.546</b>	5.33	16.6	617400
<b>6.02</b>	10.11	16.6	487200
<b>6.315</b>	6.29	16.6	516600
<b>6.86</b>	6.92	16.6	627900
<b>6.98</b>	5.04	17.8	781200
<b>7.765</b>	7.56	17.8	835800
<b>6.144</b>	9.45	17.8	760200
<b>7.155</b>	4.82	17.8	795900
<b>6.563</b>	5.68	17.8	682500
<b>5.604</b>	13.98	17.8	554400
<b>6.153</b>	13.15	17.8	621600
<b>6.782</b>	6.68	15.2	672000
<b>6.556</b>	4.56	15.2	625800
<b>7.185</b>	5.39	15.2	732900
<b>6.951</b>	5.1	15.2	777000
<b>6.739</b>	4.69	15.2	640500
<b>7.178</b>	2.87	15.2	764400
<b>6.8</b>	5.03	15.6	653100
<b>6.604</b>	4.38	15.6	611100
<b>7.287</b>	4.08	12.6	699300
<b>7.107</b>	8.61	12.6	636300
<b>7.274</b>	6.62	12.6	726600
<b>6.975</b>	4.56	17	732900
<b>7.135</b>	4.45	17	690900
<b>6.162</b>	7.43	14.7	506100
<b>7.61</b>	3.11	14.7	888300
<b>7.853</b>	3.81	14.7	1018500
<b>5.891</b>	10.87	18.6	474600
<b>6.326</b>	10.97	18.6	512400

<b>5.783</b>	18.06	18.6	472500
<b>6.064</b>	14.66	18.6	512400
<b>5.344</b>	23.09	18.6	420000
<b>5.96</b>	17.27	18.6	455700
<b>5.404</b>	23.98	18.6	405300
<b>5.807</b>	16.03	18.6	470400
<b>6.375</b>	9.38	18.6	590100
<b>5.412</b>	29.55	18.6	497700
<b>6.182</b>	9.47	18.6	525000
<b>5.888</b>	13.51	16.4	489300
<b>6.642</b>	9.69	16.4	602700
<b>5.951</b>	17.92	16.4	451500
<b>6.373</b>	10.5	16.4	483000
<b>6.951</b>	9.71	17.4	560700
<b>6.164</b>	21.46	17.4	455700
<b>6.879</b>	9.93	17.4	577500
<b>6.618</b>	7.6	17.4	632100
<b>8.266</b>	4.14	17.4	940800
<b>8.04</b>	3.13	17.4	789600
<b>7.163</b>	6.36	17.4	663600
<b>7.686</b>	3.92	17.4	980700
<b>6.552</b>	3.76	17.4	661500
<b>5.981</b>	11.65	17.4	510300
<b>7.412</b>	5.25	17.4	665700
<b>8.337</b>	2.47	17.4	875700
<b>8.247</b>	3.95	17.4	1014300
<b>6.726</b>	8.05	17.4	609000
<b>6.086</b>	10.88	17.4	504000
<b>6.631</b>	9.54	17.4	527100
<b>7.358</b>	4.73	17.4	661500
<b>6.481</b>	6.36	16.6	497700
<b>6.606</b>	7.37	16.6	489300
<b>6.897</b>	11.38	16.6	462000
<b>6.095</b>	12.4	16.6	422100
<b>6.358</b>	11.22	16.6	466200



<b>6.393</b>	5.19	16.6	497700
<b>5.593</b>	12.5	19.1	369600
<b>5.605</b>	18.46	19.1	388500
<b>6.108</b>	9.16	19.1	510300
<b>6.226</b>	10.15	19.1	430500
<b>6.433</b>	9.52	19.1	514500
<b>6.718</b>	6.56	19.1	550200
<b>6.487</b>	5.9	19.1	512400
<b>6.438</b>	3.59	19.1	520800
<b>6.957</b>	3.53	19.1	621600
<b>8.259</b>	3.54	19.1	898800
<b>6.108</b>	6.57	16.4	459900
<b>5.876</b>	9.25	16.4	438900
<b>7.454</b>	3.11	15.9	924000
<b>7.333</b>	7.79	13	756000
<b>6.842</b>	6.9	13	632100
<b>7.203</b>	9.59	13	709800
<b>7.52</b>	7.26	13	905100
<b>8.398</b>	5.91	13	1024800
<b>7.327</b>	11.25	13	651000
<b>7.206</b>	8.1	13	766500
<b>5.56</b>	10.45	13	478800
<b>7.014</b>	14.79	13	644700
<b>7.47</b>	3.16	13	913500
<b>5.92</b>	13.65	18.6	434700
<b>5.856</b>	13	18.6	443100
<b>6.24</b>	6.59	18.6	529200
<b>6.538</b>	7.73	18.6	512400
<b>7.691</b>	6.58	18.6	739200
<b>6.758</b>	3.53	17.6	680400
<b>6.854</b>	2.98	17.6	672000
<b>7.267</b>	6.05	17.6	697200
<b>6.826</b>	4.16	17.6	695100
<b>6.482</b>	7.19	17.6	611100
<b>6.812</b>	4.85	14.9	737100

<b>7.82</b>	3.76	14.9	953400
<b>6.968</b>	4.59	14.9	743400
<b>7.645</b>	3.01	14.9	966000
<b>7.088</b>	7.85	15.3	676200
<b>6.453</b>	8.23	15.3	462000
<b>6.23</b>	12.93	18.2	422100
<b>6.209</b>	7.14	16.6	487200
<b>6.315</b>	7.6	16.6	468300
<b>6.565</b>	9.51	16.6	520800
<b>6.861</b>	3.33	19.2	598500
<b>7.148</b>	3.56	19.2	783300
<b>6.63</b>	4.7	19.2	585900
<b>6.127</b>	8.58	16	501900
<b>6.009</b>	10.4	16	455700
<b>6.678</b>	6.27	16	600600
<b>6.549</b>	7.39	16	569100
<b>5.79</b>	15.84	16	426300
<b>6.345</b>	4.97	14.8	472500
<b>7.041</b>	4.74	14.8	609000
<b>6.871</b>	6.07	14.8	520800
<b>6.59</b>	9.5	16.1	462000
<b>6.495</b>	8.67	16.1	554400
<b>6.982</b>	4.86	16.1	695100
<b>7.236</b>	6.93	18.4	758100
<b>6.616</b>	8.93	18.4	596400
<b>7.42</b>	6.47	18.4	701400
<b>6.849</b>	7.53	18.4	592200
<b>6.635</b>	4.54	18.4	478800
<b>5.972</b>	9.97	18.4	426300
<b>4.973</b>	12.64	18.4	338100
<b>6.122</b>	5.98	18.4	464100
<b>6.023</b>	11.72	18.4	407400
<b>6.266</b>	7.9	18.4	453600
<b>6.567</b>	9.28	18.4	499800
<b>5.705</b>	11.5	18.4	340200

<b>5.914</b>	18.33	18.4	373800
<b>5.782</b>	15.94	18.4	415800
<b>6.382</b>	10.36	18.4	485100
<b>6.113</b>	12.73	18.4	441000
<b>6.426</b>	7.2	19.6	499800
<b>6.376</b>	6.87	19.6	485100
<b>6.041</b>	7.7	19.6	428400
<b>5.708</b>	11.74	19.6	388500
<b>6.415</b>	6.12	19.6	525000
<b>6.431</b>	5.08	19.6	516600
<b>6.312</b>	6.15	19.6	483000
<b>6.083</b>	12.79	19.6	466200
<b>5.868</b>	9.97	16.9	405300
<b>6.333</b>	7.34	16.9	474600
<b>6.144</b>	9.09	16.9	415800
<b>5.706</b>	12.43	16.9	359100
<b>6.031</b>	7.83	16.9	407400
<b>6.316</b>	5.68	20.2	466200
<b>6.31</b>	6.75	20.2	434700
<b>6.037</b>	8.01	20.2	443100
<b>5.869</b>	9.8	20.2	409500
<b>5.895</b>	10.56	20.2	388500
<b>6.059</b>	8.51	20.2	432600
<b>5.985</b>	9.74	20.2	399000
<b>5.968</b>	9.29	20.2	392700
<b>7.241</b>	5.49	15.5	686700
<b>6.54</b>	8.65	15.9	346500
<b>6.696</b>	7.18	17.6	501900
<b>6.874</b>	4.61	17.6	655200
<b>6.014</b>	10.53	18.8	367500
<b>5.898</b>	12.67	18.8	361200
<b>6.516</b>	6.36	17.9	485100
<b>6.635</b>	5.99	17	514500
<b>6.939</b>	5.89	19.7	558600
<b>6.49</b>	5.98	19.7	480900

<b>6.579</b>	5.49	18.3	506100
<b>5.884</b>	7.79	18.3	390600
<b>6.728</b>	4.5	17	632100
<b>5.663</b>	8.05	22	382200
<b>5.936</b>	5.57	22	432600
<b>6.212</b>	17.6	20.2	373800
<b>6.395</b>	13.27	20.2	455700
<b>6.127</b>	11.48	20.2	476700
<b>6.112</b>	12.67	20.2	474600
<b>6.398</b>	7.79	20.2	525000
<b>6.251</b>	14.19	20.2	417900
<b>5.362</b>	10.19	20.2	436800
<b>5.803</b>	14.64	20.2	352800
<b>3.561</b>	7.12	20.2	577500
<b>4.963</b>	14	20.2	459900
<b>3.863</b>	13.33	20.2	485100
<b>4.906</b>	34.77	20.2	289800
<b>4.138</b>	37.97	20.2	289800
<b>7.313</b>	13.44	20.2	315000
<b>6.649</b>	23.24	20.2	291900
<b>6.794</b>	21.24	20.2	279300
<b>6.38</b>	23.69	20.2	275100
<b>6.223</b>	21.78	20.2	214200
<b>6.968</b>	17.21	20.2	218400
<b>6.545</b>	21.08	20.2	228900
<b>5.536</b>	23.6	20.2	237300
<b>5.52</b>	24.56	20.2	258300
<b>4.368</b>	30.63	20.2	184800
<b>5.277</b>	30.81	20.2	151200
<b>4.652</b>	28.28	20.2	220500
<b>5</b>	31.99	20.2	155400
<b>4.88</b>	30.62	20.2	214200
<b>5.39</b>	20.85	20.2	241500
<b>5.713</b>	17.11	20.2	317100
<b>6.051</b>	18.76	20.2	487200

<b>5.036</b>	25.68	20.2	203700
<b>6.193</b>	15.17	20.2	289800
<b>5.887</b>	16.35	20.2	266700
<b>6.471</b>	17.12	20.2	275100
<b>6.405</b>	19.37	20.2	262500
<b>5.747</b>	19.92	20.2	178500
<b>5.453</b>	30.59	20.2	105000
<b>5.852</b>	29.97	20.2	132300
<b>5.987</b>	26.77	20.2	117600
<b>6.343</b>	20.32	20.2	151200
<b>6.404</b>	20.31	20.2	254100
<b>5.349</b>	19.77	20.2	174300
<b>5.531</b>	27.38	20.2	178500
<b>5.683</b>	22.98	20.2	105000
<b>4.138</b>	23.34	20.2	249900
<b>5.608</b>	12.13	20.2	585900
<b>5.617</b>	26.4	20.2	361200
<b>6.852</b>	19.78	20.2	577500
<b>5.757</b>	10.11	20.2	315000
<b>6.657</b>	21.22	20.2	361200
<b>4.628</b>	34.37	20.2	375900
<b>5.155</b>	20.08	20.2	342300
<b>4.519</b>	36.98	20.2	147000
<b>6.434</b>	29.05	20.2	151200
<b>6.782</b>	25.79	20.2	157500
<b>5.304</b>	26.64	20.2	218400
<b>5.957</b>	20.62	20.2	184800
<b>6.824</b>	22.74	20.2	176400
<b>6.411</b>	15.02	20.2	350700
<b>6.006</b>	15.7	20.2	298200
<b>5.648</b>	14.1	20.2	436800
<b>6.103</b>	23.29	20.2	281400
<b>5.565</b>	17.16	20.2	245700
<b>5.896</b>	24.39	20.2	174300
<b>5.837</b>	15.69	20.2	214200

<b>6.202</b>	14.52	20.2	228900
<b>6.193</b>	21.52	20.2	231000
<b>6.38</b>	24.08	20.2	199500
<b>6.348</b>	17.64	20.2	304500
<b>6.833</b>	19.69	20.2	296100
<b>6.425</b>	12.03	20.2	338100
<b>6.436</b>	16.22	20.2	300300
<b>6.208</b>	15.17	20.2	245700
<b>6.629</b>	23.27	20.2	281400
<b>6.461</b>	18.05	20.2	201600
<b>6.152</b>	26.45	20.2	182700
<b>5.935</b>	34.02	20.2	176400
<b>5.627</b>	22.88	20.2	268800
<b>5.818</b>	22.11	20.2	220500
<b>6.406</b>	19.52	20.2	359100
<b>6.219</b>	16.59	20.2	386400
<b>6.485</b>	18.85	20.2	323400
<b>5.854</b>	23.79	20.2	226800
<b>6.459</b>	23.98	20.2	247800
<b>6.341</b>	17.79	20.2	312900
<b>6.251</b>	16.44	20.2	264600
<b>6.185</b>	18.13	20.2	296100
<b>6.417</b>	19.31	20.2	273000
<b>6.749</b>	17.44	20.2	281400
<b>6.655</b>	17.73	20.2	319200
<b>6.297</b>	17.27	20.2	338100
<b>7.393</b>	16.74	20.2	373800
<b>6.728</b>	18.71	20.2	312900
<b>6.525</b>	18.13	20.2	296100
<b>5.976</b>	19.01	20.2	266700
<b>5.936</b>	16.94	20.2	283500
<b>6.301</b>	16.23	20.2	312900
<b>6.081</b>	14.7	20.2	420000
<b>6.701</b>	16.42	20.2	344400
<b>6.376</b>	14.65	20.2	371700

<b>6.317</b>	13.99	20.2	409500
<b>6.513</b>	10.29	20.2	424200
<b>6.209</b>	13.22	20.2	449400
<b>5.759</b>	14.13	20.2	417900
<b>5.952</b>	17.15	20.2	399000
<b>6.003</b>	21.32	20.2	401100
<b>5.926</b>	18.13	20.2	401100
<b>5.713</b>	14.76	20.2	422100
<b>6.167</b>	16.29	20.2	417900
<b>6.229</b>	12.87	20.2	411600
<b>6.437</b>	14.36	20.2	487200
<b>6.98</b>	11.66	20.2	625800
<b>5.427</b>	18.14	20.2	289800
<b>6.162</b>	24.1	20.2	279300
<b>6.484</b>	18.68	20.2	350700
<b>5.304</b>	24.91	20.2	252000
<b>6.185</b>	18.03	20.2	306600
<b>6.229</b>	13.11	20.2	449400
<b>6.242</b>	10.74	20.2	483000
<b>6.75</b>	7.74	20.2	497700
<b>7.061</b>	7.01	20.2	525000
<b>5.762</b>	10.42	20.2	457800
<b>5.871</b>	13.34	20.2	432600
<b>6.312</b>	10.58	20.2	445200
<b>6.114</b>	14.98	20.2	401100
<b>5.905</b>	11.45	20.2	432600
<b>5.454</b>	18.06	20.1	319200
<b>5.414</b>	23.97	20.1	147000
<b>5.093</b>	29.68	20.1	170100
<b>5.983</b>	18.07	20.1	285600
<b>5.983</b>	13.35	20.1	422100
<b>5.707</b>	12.01	19.2	457800
<b>5.926</b>	13.59	19.2	514500
<b>5.67</b>	17.6	19.2	485100
<b>5.39</b>	21.14	19.2	413700

5.794	14.1	19.2	384300
6.019	12.92	19.2	445200
5.569	15.1	19.2	367500
6.027	14.33	19.2	352800
6.593	9.67	21	470400
6.12	9.08	21	432600
6.976	5.64	21	501900
6.794	6.48	21	462000
6.03	7.88	21	249900

## Appendix II – Python Code

stats\_boston\_housing

November 13, 2019

```
In [64]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
df=pd.read_csv(' housing.csv' )
```

```
In [65]: #RM - average number of rooms per dwelling
#PTRATIO - pupil-teacher ratio by town
#LSTAT - % lower status of the population #MEDV
- Median value of owner-occupied homes
```

```
In [66]: df.head()
Out[66]:
```



```

M      T  PTRATIO      MEDV 0  6.575  4.98
R      15.3    504000.0  1    6.421  9.14
      17.8    453600.0  2    7.185  4.03
      17.8    728700.0  3    6.998  2.94
L      18.7    701400.0  4    7.147  5.33
S      18.7    760200.0
T
A

```

In [67]: df.shape

Out[67]: (489, 4)

In [68]: df.describe()      RM            LSTAT            PTRATIO            MEDV

Out[68]:

count	489.000000	489.000000	489.000000	4.890000e+02	mean
6.240288	12.939632	18.516564	4.543429e+05		std
0.643650	7.081990	2.111268	1.653403e+05		min
3.561000	1.980000	12.600000	1.050000e+05		25%
5.880000	7.370000	17.400000	3.507000e+05		50%
6.185000	11.690000	19.100000	4.389000e+05		75%
6.575000	17.120000	20.200000	5.187000e+05		max
8.398000	37.970000	22.000000	1.024800e+06		

In [69]: #Checks for blanks

```

zero_counts={ 'RM': df['RM'].isnull().sum() , 'LSTAT': df['LSTAT'].isnull().sum() , 'PTRATIO': df['PTRATIO'].isnull().sum() , 'MEDV': df['MEDV'].isnull().sum()}
zero_counts

```

```
Out[69]: {'RM': 0, 'LSTAT': 0, 'PTRATIO': 0, 'MEDV': 0}
```

```
In [70]: prices = df['MEDV']  
         features = df.drop('MEDV', axis = 1)
```

```
In [71]: minimum_price = np.mean(prices)
```

```
         maximum_price = np.max(prices)
```

```
         mean_price = np.mean(prices)
```

```
         median_price = np.median(prices)
```

```
         std_price = np.std(prices)
```

```
print("Statistics for Boston housing dataset:\n")  
print("Minimum price: ${:,.2f}".format(minimum_price))  
print("Maximum price: ${:,.2f}".format(maximum_price))  
print("Mean price: ${:,.2f}".format(mean_price))  
print("Median price ${:,.2f}".format(median_price))  
print("Standard deviation of prices: ${:,.2f}".format(std_price))
```

Statistics for Boston housing dataset:

Minimum price: \$454,342.94

Maximum price: \$1,024,800.00

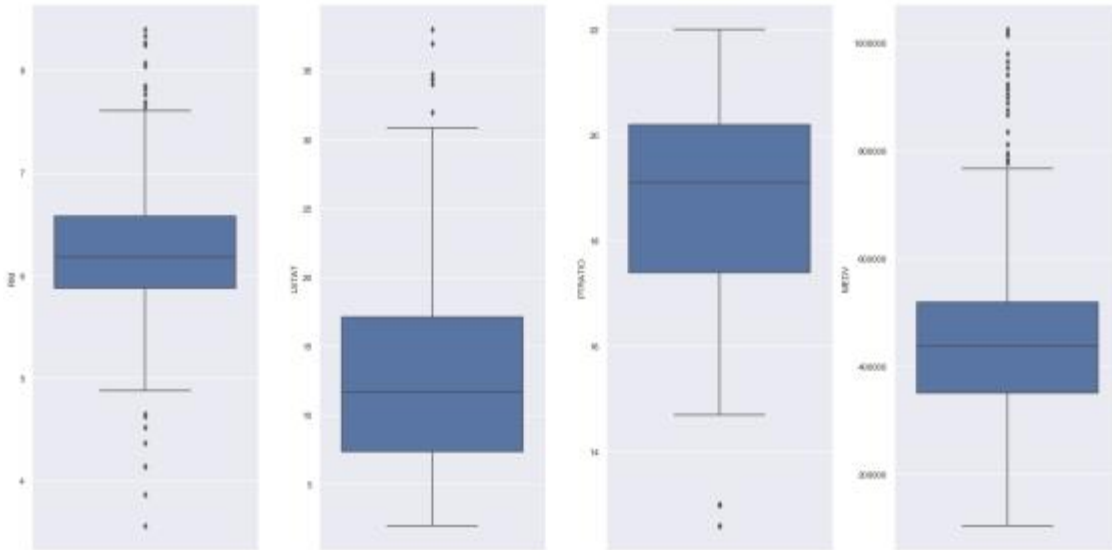
Mean price: \$454,342.94

Median price \$438,900.00

Standard deviation of prices: \$165,171.13

```
In [72]: import seaborn as sns  
         import matplotlib.pyplot as plt  
         from scipy import stats
```

```
fig, axs = plt.subplots(ncols=4, nrow=1, figsize=(20, 10)) index =  
0  
axs = axs.flatten()  
for k,v in df.items():  
    sns.boxplot(y=k, data=df, ax=axs[index])  
    index += 1  
plt.tight_layout(pad=0.4, w_pad=0.5, h_pad=5.0)
```



```
In [73]: for k, v in df.items():
          q1 = v.quantile(0.25)
          q3 = v.quantile(0.75)
          irq = q3 - q1

          v_col = v[(v <= q1 - 1.5 * irq) | (v >= q3 + 1.5 * irq)]
          perc = np.shape(v_col)[0] * 100.0 / np.shape(df)[0]
          print("Column %s outliers = %.2f%%" % (k, perc))
```

Column RM outliers = 4.50%

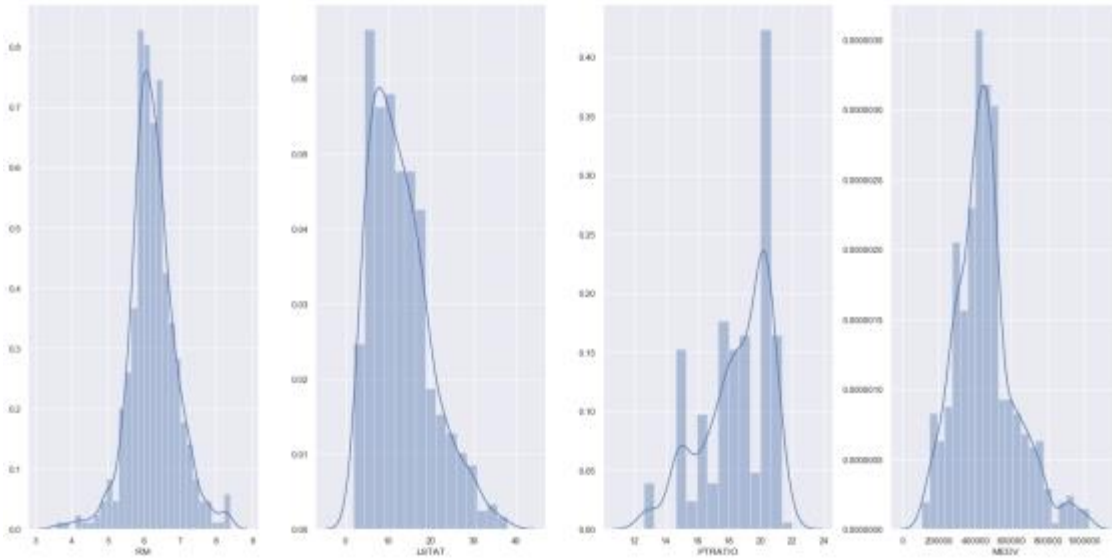
Column LSTAT outliers = 1.43%

Column PTRATIO outliers = 2.66%

Column MEDV outliers = 4.50%

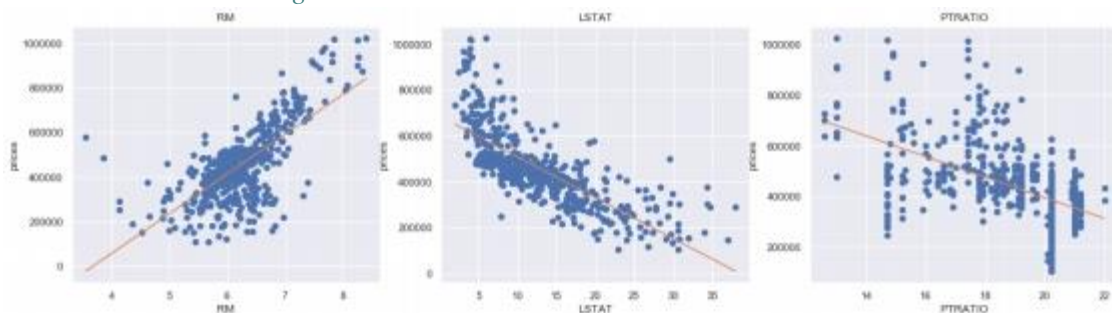
```
In [74]: fig, axs = plt.subplots(ncols=4, nrows=1, figsize=(20, 10))
          index = 0
          axs = axs.flatten()
          for k,v in df.items():
              sns.distplot(v, ax=axs[index])
              index += 1
          plt.tight_layout(pad=0.4, w_pad=0.5, h_pad=5.0)
```

```
C:\ProgramData\Anaconda3\lib\site-packages\scipy\stats\stats.py:1713: FutureWarning: Using a no
return np.add.reduce(sorted[indexer] * weights, axis=axis) / sumval
```



```
In [75]: import matplotlib.pyplot as plt
plt.figure(figsize=(20, 5))
```

```
for i, col in enumerate(features.columns):
    plt.subplot(1, 3, i+1)
    x = df[col]
    y = prices
    plt.plot(x, y, 'o')
    # Create regression line
```



In [76]: # *Correlation Matrix*

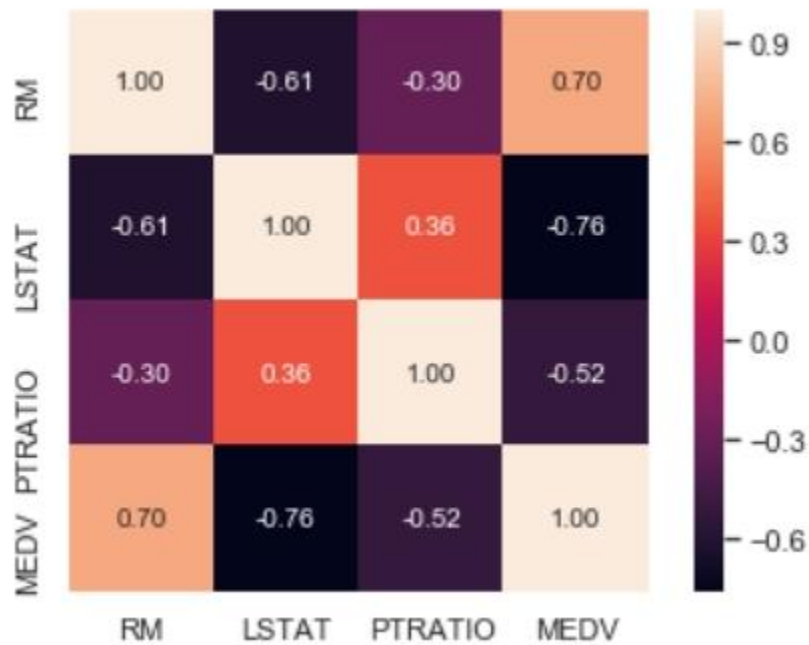
```

cor_matrix = np.corrcoef(df[df.columns].values.T) # We transpose to get the data by co
sns.set(font_scale=1)

cor_heat_map = sns.heatmap(cor_matrix,
                             cbar=True,
                             annot=True,
                             square=True,
                             fmt='.2f',
                             annot_kws={ 'size':10} ,
                             yticklabels=df.columns,
                             xticklabels=df.columns)

plt.show()

```



```

In [77]: # Creating deep copy of original dataframe
dff=df.copy(deep=True)

```

```

In [78]: dff.head()

```



Out[78]:

	RM	LSTAT	PTRATIO		MEDV	
0	6.575					
4.98		15.3	504000.0	1	6.421	9.14
17.8	453600.0	2	7.185		4.03	17.8
728700.0	3	6.998	2.94	18.7	701400.0	4
7.147	5.33		18.7	760200.0		

In [79]: # *Standardizing values*

```
#from sklearn.preprocessing import StandardScaler
#num_values1=dff.select_dtypes(['float64','int64']).columns
#scaler = StandardScaler()

#scaler.fit(dff[num_values1])
#dff[num_values1]=scaler.transform(dff[num_values1])
```

In [80]: dff.head()

Out[80]:

	RM	LSTAT	PTRATIO		MEDV
0	6.575	4.98	15.3	504000.0	1
	6.421	9.14	17.8	453600.0	2
	7.185	4.03	17.8	728700.0	3
	6.998	2.94	18.7	701400.0	4
	7.147	5.33	18.7	760200.0	

In [81]: x = dff.drop(['MEDV'],axis = 1)  
y = dff['MEDV']

In [82]: x.head()

Out[82]:

	RM	LSTAT	PTRATIO
0	6.575	4.98	15.3
1	6.421	9.14	17.8
2	7.185	4.03	17.8
3	6.998	2.94	18.7
4	7.147	5.33	18.7

In [83]: y.head()

Out[83]:

0	504000.0
1	453600.0
2	728700.0

```
3    701400.0
4    760200.0
Name: MEDV, dtype: float64
```

```
In [84]: from sklearn.model_selection import train_test_split
X_train,X_test,y_train,y_test = train_test_split(x,y,test_size = 0.3,random_state = 33
```

In [85]: *# Applying linear regression*

```
from sklearn.linear_model import LinearRegression
lr = LinearRegression()
lr.fit(X_train,y_train)
y_pred_lr = lr.predict(X_test)
```

In [86]: *#R^2 score*

```
lr.score(X_test, y_test)
```

Out[86]: 0.6083795028938153

In [87]: *# Applying random forest*

```
from sklearn import metrics
from sklearn.ensemble import RandomForestRegressor
rfr = RandomForestRegressor()
rfr.fit(X_train,y_train)
y_pred_rfr = rfr.predict(X_test)
```

In [88]: *#R^2 score*

```
rfr.score(X_test,y_test)
```

Out[88]: 0.7878366795445423

In [89]: `dff['PRED_MEDV_LR']=lr.predict(df.drop(['MEDV'],axis = 1))`

In [90]: `dff['PRED_MEDV_RF']=rfr.predict(df.drop(['MEDV'],axis = 1))` In

[91]: `dff.head(10)`

Out[91]:

	RM	LSTAT	PTRATIO	MEDV	PRED_MEDV_LR	PRED_MEDV_RF	0
6.575	4.98	15.3	504000.0	630636.304650	602280.0	1	6.421
9.14	17.8	453600.0	523271.934059	491400.0	2	7.185	4.03
17.8	728700.0	653678.257698	726180.0	3	6.998	2.94	18.7
701400.0	628424.758645	728910.0	4	7.147	5.33	18.7	
760200.0	618840.932373	726390.0	5	6.430	5.21	18.7	
602700.0	547283.553374	523320.0	6	6.012	12.43	15.2	
480900.0	498391.389281	469560.0	7	6.172	19.15	15.2	
569100.0	445153.237224	546420.0	8	5.631	29.93	15.2	
346500.0	278762.002770	292110.0	9	6.004	17.10	15.2	
396900.0	449292.443893	407820.0					

```
In [92]: # standard deviation of the dataframe
        dff.std()
```

```
Out[92]: RM                0.643650
        LSTAT              7.081990
        PTRATIO            2.111268
        MEDV              165340.277653
        PRED_MEDV_LR       144887.135403
        PRED_MEDV_RF       159297.471406
        dtype: float64
```

```
In [93]: dff.mean()
```

```
Out[93]: RM                6.240288
        LSTAT             12.939632
        PTRATIO           18.516564
        MEDV             454342.944785
        PRED_MEDV_LR      451673.698602
        PRED_MEDV_RF      453587.116564
        dtype: float64
```

```
In [95]: dff.shape
```

```
Out[95]: (489, 6)
```

```
In [97]: # Z score for Linear Regression
```

```
import math
s1=165340.277653
s2=144887.135403
n1=489
n2=489
x1=454342.944785
x2=451673.698602

den=math.sqrt((s1*s1)/n1+(s2*s2)/n2)
Z=(x1-x2)/den
print(Z)
```

```

if Z<1.96:
    print("Since calculated value of Z is less than the critical Z i.e. 1.96, Null Hyp
else:
    print("Null hypothesis is rejected for Linear Regression")

```

0.2684949105149169

Since calculated value of Z is less than the critical Z i.e. 1.96, Null Hypothesis is accepted

In [98]: *# Z score for Random Forest*

```

import math
s1=165340.277653
s2=159297.471406
n1=489
n2=489
x1=454342.944785
x2=453587.116564
den=math.sqrt((s1*s1)/n1+(s2*s2)/n2)
Z=(x1-x2)/den
print(Z)
if Z<1.96:
    print("Since calculated value of Z is less than the critical Z i.e. 1.96, Null Hyp
else:
    print("Null hypothesis is rejected for Random Forest")

```

0.07279780558113479

Since calculated value of Z is less than the critical Z i.e. 1.96, Null Hypothesis is accepted

In [ ]

