

A projectile is fired from the top of a cliff of height h with a muzzle velocity v_0 at an angle θ with respect to the horizontal. The angle θ that produces the maximum horizontal range is given by the equation

$$\frac{2gh}{v_0} \sin(2\theta) - \frac{v_0}{2} \sin(4\theta) = \cos(2\theta) \sqrt{v_0^2 \sin^2(2\theta) + 8gh \cos^2(\theta)}$$

The maximum horizontal range, x , is given by

$$x = v_0 \cos \theta \left(\frac{v_0 \sin \theta}{g} + \sqrt{\frac{v_0^2 \sin^2(\theta)}{g^2} + \frac{2h}{g}} \right)$$

and the maximum height of the projectile with respect to the ground, y_{\max} , is given by

$$y_{\max} = h + \frac{v_0^2 \sin^2 \theta}{2g}$$

where $h = 2500$ m and $g = 9.81$ m/s².

Write a MATLAB program as follows:

- 1) v_0 will go from 100 m/s to 400 m/s in steps of 50 m/s.
- 2) For each value of v_0 , first call the MATLAB function fzero to calculate the angle θ that gives the maximum horizontal range x , and then use this value of θ to calculate x and y_{\max} . Then print v_0 , θ , x and y_{\max} . Use 40° as the initial guess for θ .

The output of this program should look like this:

$v_0=100$	$\theta=22.36810$	$x= 2477.08519$	$y_{\max}=2573.81376$
$v_0=150$	$\theta=29.28249$	$x= 4090.03544$	$y_{\max}=2774.35143$
$v_0=200$	$\theta=33.83052$	$x= 6083.84233$	$y_{\max}=3131.92127$
$v_0=250$	$\theta=36.81570$	$x= 8511.49383$	$y_{\max}=3643.89722$
$v_0=300$	$\theta=38.81730$	$x=11403.48889$	$y_{\max}=4302.41885$
$v_0=350$	$\theta=40.19885$	$x=14777.27645$	$y_{\max}=5101.06970$
$v_0=400$	$\theta=41.18114$	$x=18643.01160$	$y_{\max}=6035.53998$