S2_1 Time Series

Carga de librerias

```
library(ggplot2)
library(tsapp)
## Loading required package: Matrix
## Loading required package: vars
## Loading required package: MASS
## Loading required package: strucchange
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
       as.Date, as.Date.numeric
## Loading required package: sandwich
## Loading required package: urca
## Loading required package: lmtest
## Loading required package: fftwtools
library(forecast)
## Registered S3 method overwritten by 'quantmod':
##
                       from
     as.zoo.data.frame zoo
##
## Attaching package: 'forecast'
## The following object is masked from 'package:tsapp':
##
##
       BoxCox
library(scales)
library(stats)
library(TTR)
```

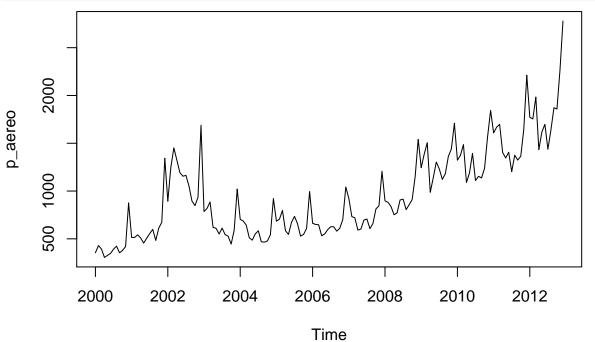
Carga de datos

```
#Carga de datos
Yt <- read.delim("./datatesisaereo.txt", header=T)</pre>
```

```
\#ts para convertir a serie de tiempo
Yt \leftarrow ts(Yt, start = c(2000, 1), freq = 12)
```

Grafico de la seria





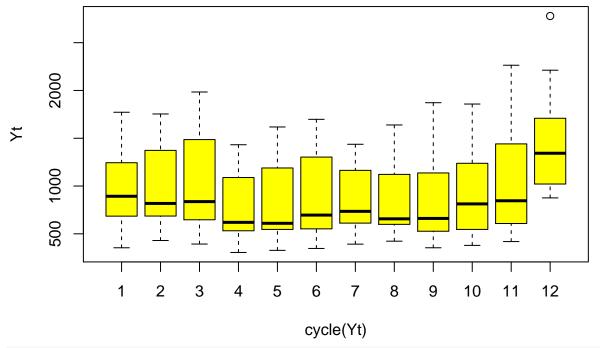
Agrupacion de meses

cycle(Yt)

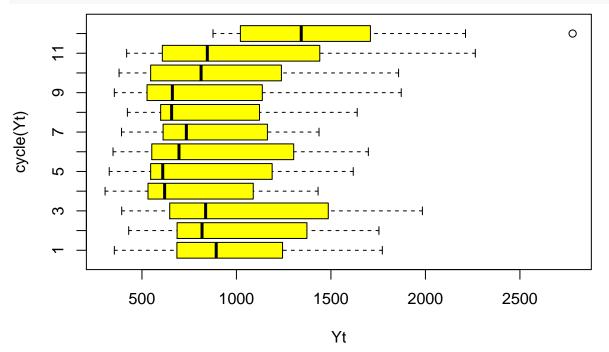
```
Jan Feb Mar Apr May Jun Jul Aug Sep Oct Nov Dec
               2
                                      7
## 2000
           1
                    3
                         4
                             5
                                  6
                                           8
                                               9
                                                  10
                                                       11
                                                            12
## 2001
                    3
           1
                                                   10
                                                       11
                                                            12
## 2002
               2
                    3
                             5
                                      7
                                               9
                                                            12
           1
                                  6
                                           8
                                                  10
                                                       11
## 2003
           1
               2
                    3
                             5
                                  6
                                      7
                                           8
                                               9
                                                  10
                                                       11
                                                            12
## 2004
               2
                    3
                        4
                             5
                                  6
                                      7
                                          8
                                               9
                                                  10
                                                       11
                                                            12
## 2005
               2
                    3
                             5
                                                  10
                                                       11
                                                            12
## 2006
               2
                    3
                        4
                             5
                                  6
                                      7
                                                            12
                                          8
                                               9
                                                  10
                                                       11
           1
               2
                    3
                        4
                                      7
## 2007
                             5
                                  6
                                          8
                                               9
                                                  10
                                                       11
                                                            12
               2
                    3
                        4
                             5
                                      7
## 2008
                                  6
                                           8
                                               9
                                                  10
                                                       11
                                                            12
## 2009
               2
                    3
                             5
                                  6
                                      7
                                           8
                                               9
                                                  10
                                                       11
                                                            12
## 2010
               2
                    3
                         4
                             5
                                      7
                                               9
                                                            12
                                  6
                                                  10
                                                       11
               2
## 2011
                    3
                         4
                             5
                                  6
                                      7
                                               9
                                                       11
                                                            12
                                          8
                                                  10
## 2012
                             5
                                                           12
                                               9
                                                  10
                                                       11
```

Diagrama de Cajas

```
boxplot(Yt ~ cycle(Yt), horizontal = FALSE, col = "YELLOW") ## ALT + 126
```



boxplot(Yt ~ cycle(Yt), horizontal = TRUE, col = "YELLOW") ## ALT + 126



 $\#\# \mathrm{Descomposici\'{o}n}$ de la serie de tipo multiplicativo

```
#Aplicamos la sentencia para un enf. de descomposicion
Yt.ts.desc <- decompose(Yt, type = "multiplicative")
Yt.ts.desc</pre>
```

```
## $x
##
                   Mar
         .Jan
              Feb
                        Apr
                             May
                                   Jun
                                        Jul
                                             Aug
                                                  Sep
                                                       Oct
                                                            Nov
                                                                  Dec
## 2000
         354
              430
                   393
                         305
                              327
                                   347
                                        392
                                             423
                                                  354
                                                        379
  2001
              515
                   542
                                   507
                                        555
                                             599
         514
                        509
                              455
                                                  484
                                                        612
                                                             673 1343
  2002
         893 1248 1452 1323
                            1193 1155 1164
                                            1055
                                                  896
                                                        847
                                                             934 1688
## 2003
         786
              818
                   886
                        620
                             610
                                   550
                                        612
                                             544
                                                  527
                                                        445
                                                             591 1021
  2004
         704
              686
                   644
                         511
                              486
                                   552
                                        584
                                             469
                                                  465
                                                        477
                                                             542
## 2005
         685
              705
                   797
                         585
                              546
                                   673
                                        735
                                             657
                                                  528
                                                        546
                                                             608
                                                                  995
  2006
         662
              651
                   647
                         532
                              551
                                   596
                                        627
                                             626
                                                  580
                                                        610
                                                             702 1042
  2007
         924
              733
                   720
                         592
                              602
                                   696
                                        707
                                             606
                                                  661
                                                       813
                                                            846 1207
  2008
        897
              882
                   837
                        752
                             771
                                   907
                                        915
                                             806
                                                  856
                                                       911 1153 1541
  2009 1244 1387 1505
                        987 1140 1303 1231 1122 1181 1363 1441 1709
  2010 1323 1373 1486 1089 1189 1394 1110 1154 1137 1238 1567 1843
  2011 1609 1668 1698 1403 1346 1406 1203 1375 1324 1364 1643 2212
## 2012 1772 1754 1984 1432 1618 1698 1437 1639 1872 1858 2264 2779
##
## $seasonal
##
              Jan
                        Feb
                                   Mar
                                             Apr
                                                        May
                                                                  Jun
## 2000 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2001 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2002 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2003 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2004 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2005 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2006 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2007 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2008 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2009 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2010 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2011 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
## 2012 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
##
                        Sep
                                   Oct
                                             Nov
                                                        Dec
              Aug
## 2000 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
## 2001 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
## 2002 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
## 2003 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
## 2004 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
## 2005 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
## 2006 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
## 2007 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
  2008 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
## 2009 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
## 2010 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
## 2011 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
## 2012 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
##
## $trend
##
              Jan
                         Feb
                                   Mar
                                             Apr
                                                        May
                                                                  Jun
                                                                             Jul
## 2000
               NA
                         NΑ
                                    NΑ
                                                        NA
                                                                   NΑ
                                                                       423, 2500
                                              NA
         497.2083
                   511.3333
                             524.0833
                                        539.2083
                                                  559.5000
                                                             589.5417
                                                                       624.7917
  2001
## 2002
         986.2083 1030.5833 1066.7500 1093.7083 1114.3750 1139.6250 1149.5417
## 2003
         881.5000
                   837.2083
                             800.5417
                                        768.4167
                                                  737.3750
                                                             695.2917
## 2004
         609.0833
                   604.7917
                             599.0833
                                        597.8333
                                                  597.1250
                                                             590.9167
                                                                       585.9583
## 2005
         627.0417 641.1667
                             651.6250
                                        657.1250
                                                  662.7500
                                                             668.5833
                                                                       670.7083
```

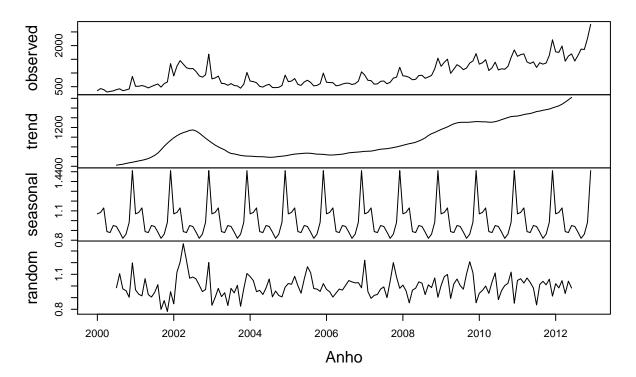
```
## 2006 637.8333 632.0417 632.9167 637.7500 644.3333
                                                           650.2083 663.0833
        707.8333 710.3333 712.8750
                                       724.7083
                                                 739.1667
                                                                     757.7917
## 2007
                                                           752.0417
## 2008 832.5000 849.5000 865.9583 878.1667
                                                 895.0417
                                                           921.7500
## 2009 1158.8333 1185.1667 1211.8750 1244.2500 1275.0833 1294.0833 1304.3750
## 2010 1320.0417 1316.3333 1315.8333 1308.7917 1308.8333 1319.6667 1337.1667
## 2011 1435.4583 1448.5417 1465.5417 1478.5833 1487.0000 1505.5417 1527.7083
## 2012 1624.6667 1645.4167 1679.2500 1722.6667 1769.1250 1818.6250
##
              Aug
                        Sep
                                  Oct
                                            Nov
                                                      Dec
## 2000
        433.4583
                   443.2083
                             457.9167
                                       471.7500
                                                 483.7500
## 2001
        671.1250
                  739.5833
                             811.4167
                                       876.0833
                                                 933.8333
## 2002 1127.1667 1085.6667 1032.7917
                                       979.2083
                                                 929.7083
                           624.9583
                                       615.2500
## 2003
        655.1667
                  639.5833
                                                 610.1667
## 2004
        585.9583
                  593.1250
                             602.5833
                                       608, 1667
                                                 615.7083
        667.5000
                  659.0000
## 2005
                             650.5417
                                       648.5417
                                                 645.5417
        677.4167
                   683.8750
                             689.4167
## 2006
                                       694.0417
                                                 700.3333
## 2007
         762.8750
                  773.9583
                             785.5000
                                       799.2083
                                                 815.0417
        985.6250 1034.5000 1072.1250 1097.2917 1129.1667
## 2008
## 2009 1307.0833 1305.7083 1309.1667 1315.4583 1321.2917
## 2010 1361.3750 1382.5000 1404.4167 1424.0417 1431.0833
## 2011 1538.0833 1553.5833 1566.7083 1579.2500 1602.7500
## 2012
               NΑ
                         NΑ
                                   NΑ
                                             NΑ
                                                       NA
##
## $random
##
              Jan
                        Feb
                                  Mar
                                            Apr
                                                      Mav
                                                                 Jun
## 2000
               NA
                         NA
                                   NA
                                             NA
                                                       NA
                                                                 NA 0.9847995
## 2001 0.9665576 0.9291326 0.9152001 1.0628835 0.9258034 0.9049274 0.9445316
## 2002 0.8466147 1.1171360 1.2045396 1.3620178 1.2187554 1.0664495 1.0766808
## 2003 0.8336874 0.9013518 0.9794153 0.9084884 0.9417788 0.8323691 0.9799131
## 2004 1.0806846 1.0463884 0.9512962 0.9624213 0.9265706 0.9829538 1.0597534
## 2005 1.0214032 1.0143615 1.0823749 1.0023799 0.9378867 1.0592045 1.1652319
## 2006 0.9704067 0.9501887 0.9046381 0.9392596 0.9735281 0.9645262 1.0054446
## 2007 1.2205174 0.9519549 0.8937915 0.9197778 0.9271748 0.9738400 0.9920380
## 2008 1.0074215 0.9578109 0.8553534 0.9641961 0.9806603 1.0354149 1.0239979
## 2009 1.0036965 1.0796217 1.0989952 0.8931697 1.0178265 1.0595037 1.0034929
## 2010 0.9370769 0.9622308 0.9993901 0.9368754 1.0342011 1.1115239 0.8826655
## 2011 1.0480174 1.0622815 1.0253134 1.0684060 1.0304848 0.9826816 0.8373054
## 2012 1.0197706 0.9833956 1.0455467 0.9359793 1.0411840 0.9824599
##
                        Sep
                                  Oct.
              Aug
                                            Nov
## 2000 1.1053238 0.9747901 0.9599994 0.9032465 1.1981337
## 2001 1.0109273 0.7986822 0.8748341 0.7812208 0.9515438
## 2002 1.0601341 1.0072268 0.9512374 0.9700094 1.2012900
## 2003 0.9404671 1.0056092 0.8258994 0.9768773 1.1071320
## 2004 0.9065726 0.9568029 0.9181623 0.9063185 0.9897072
## 2005 1.1148350 0.9778320 0.9734995 0.9533884 1.0198139
## 2006 1.0466825 1.0350636 1.0262810 1.0286218 0.9844305
## 2007 0.8997373 1.0423165 1.2005011 1.0765012 0.9798275
## 2008 0.9262321 1.0098550 0.9855784 1.0685907 0.9029563
## 2009 0.9722682 1.1038739 1.2075889 1.1140150 0.8557867
## 2010 0.9601178 1.0037165 1.0224519 1.1190525 0.8520843
## 2011 1.0125567 1.0400858 1.0098211 1.0580126 0.9131487
## 2012
               NA
                         NA
                                   NA
                                             NA
                                                       NA
##
## $figure
## [1] 1.0695399 1.0839904 1.1300115 0.8881280 0.8784004 0.9503415 0.9404621
```

```
[8] 0.8828837 0.8193779 0.8621479 0.9833222 1.5113946
##
## $type
   [1] "multiplicative"
##
## attr(,"class")
## [1] "decomposed.ts"
Yt.ts.desc$x
##
              Feb
                                                    Sep
                                                                    Dec
         Jan
                    Mar
                         Apr
                               May
                                    Jun
                                         Jul
                                               Aug
                                                         Oct
                                                               Nov
                                               423
                    393
                                                                    876
## 2000
         354
              430
                         305
                               327
                                    347
                                         392
                                                    354
                                                          379
                                                               419
  2001
         514
              515
                    542
                               455
                                    507
                                         555
                                               599
                                                    484
                                                          612
                                                               673 1343
                         509
## 2002
         893 1248 1452
                        1323
                              1193
                                   1155 1164
                                             1055
                                                    896
                                                          847
## 2003
         786
              818
                    886
                         620
                               610
                                    550
                                         612
                                               544
                                                    527
                                                          445
                                                               591 1021
## 2004
         704
              686
                    644
                         511
                               486
                                    552
                                         584
                                               469
                                                    465
                                                          477
                                                               542
## 2005
         685
              705
                    797
                         585
                               546
                                    673
                                         735
                                               657
                                                    528
                                                         546
                                                               608
                                                                    995
  2006
         662
              651
                    647
                         532
                               551
                                    596
                                         627
                                               626
                                                    580
                                                          610
                                                               702 1042
              733
                    720
                                               606
  2007
         924
                         592
                               602
                                    696
                                         707
                                                    661
                                                         813
                                                               846 1207
  2008
         897
              882
                    837
                         752
                               771
                                    907
                                         915
                                               806
                                                    856
                                                          911 1153 1541
## 2009 1244 1387 1505
                         987 1140 1303 1231 1122 1181 1363 1441 1709
## 2010 1323 1373 1486 1089 1189 1394 1110 1154 1137 1238 1567 1843
## 2011 1609 1668 1698 1403 1346 1406 1203 1375 1324 1364 1643 2212
## 2012 1772 1754 1984 1432 1618 1698 1437 1639 1872 1858 2264 2779
```

Ploteo de la descomposion

```
plot(Yt.ts.desc, xlab = 'Anho')
```

Decomposition of multiplicative time series



Resumen de la tendencia

```
tendencia <- data.frame(Yt.ts.desc$trend)
tendencia</pre>
```

```
Yt.ts.desc.trend
## 1
## 2
                      NA
## 3
                      NA
## 4
                      NA
## 5
                      NA
## 6
                      NA
## 7
                423.2500
## 8
                433.4583
## 9
                443.2083
## 10
                457.9167
## 11
                471.7500
## 12
                483.7500
## 13
                497.2083
## 14
               511.3333
## 15
               524.0833
               539.2083
## 16
## 17
                559.5000
## 18
               589.5417
## 19
                624.7917
## 20
                671.1250
## 21
                739.5833
## 22
               811.4167
## 23
                876.0833
## 24
                933.8333
## 25
               986.2083
## 26
               1030.5833
## 27
               1066.7500
## 28
               1093.7083
## 29
               1114.3750
## 30
               1139.6250
## 31
               1149.5417
## 32
               1127.1667
## 33
               1085.6667
## 34
               1032.7917
               979.2083
## 35
## 36
                929.7083
## 37
                881.5000
## 38
                837.2083
## 39
                800.5417
                768.4167
## 40
## 41
                737.3750
## 42
                695.2917
## 43
                664.0833
## 44
                655.1667
## 45
                639.5833
## 46
                624.9583
## 47
                615.2500
## 48
               610.1667
```

##	49	609.0833
##	50	604.7917
##	51	599.0833
##	52	597.8333
##	53	597.1250
##		590.9167
##		585.9583
##		585.9583
##		593.1250
##		602.5833
##		608.1667
##		615.7083
##	61	627.0417
##	62	641.1667
##	63	651.6250
##	64	657.1250
##	65	662.7500
##	66	668.5833
##	67	670.7083
##	68	667.5000
##	69	659.0000
##	70	650.5417
##	71	648.5417
##	72	645.5417
##	73	637.8333
##	74	632.0417
##	7 -1 75	632.9167
##	76 77	637.7500 644.3333
##	77	
##	78	650.2083
##		663.0833
##		677.4167
##		683.8750
##	82	689.4167
##	83	694.0417
##	84	700.3333
##	85	707.8333
##	86	710.3333
##	87	712.8750
##	88	724.7083
##	89	739.1667
##	90	752.0417
##	91	757.7917
##	92	762.8750
##	93	773.9583
##	94	785.5000
##	95	799.2083
##	96	815.0417
##	97	832.5000
##	98	849.5000
##	99	865.9583
##	100	878.1667
	100	895.0417
##		
##	102	921.7500

##	103	950.1250
##	104	985.6250
##	105	1034.5000
##	106	1072.1250
##	107	1097.2917
##	108	1129.1667
##	109	1158.8333
##	110	1185.1667
##	111	1211.8750
##	112	1244.2500
##	113	1275.0833
##		1294.0833
##	115	1304.3750
##	116	1307.0833
##	117	1305.7083
##	118	1309.1667
##	119	1315.4583
##	120	1321.2917
##	121	1320.0417
##	122	1316.3333
##	123	1315.8333
##	124	1308.7917
##	125	1308.8333
##	126	1319.6667
##	127	1337.1667
##	128	1361.3750
##	129	1382.5000
##	130	1404.4167
##	131	1424.0417
##	132	1431.0833
##	133	1435.4583
##	134	1448.5417
##	135	1465.5417
##	136	1478.5833
##	137	1487.0000
##	138	1505.5417
##	139	1527.7083
##	140	1538.0833
##	141	1553.5833
##	142	1566.7083
##	143	1579.2500
##	144	1602.7500
##	145	1624.6667
##	146	1645.4167
##	147	1679.2500
##	148	1722.6667
##	149	1769.1250
##	150	1818.6250
##	151	NA
##	152	NA
##	153	NA
##	154	NA
##	155	NA
##	156	NA

```
summary(tendencia)
   Yt.ts.desc.trend
          : 423.2
##
   Min.
   1st Qu.: 645.2
## Median: 806.0
## Mean
         : 939.6
## 3rd Qu.:1296.7
## Max.
          :1818.6
## NA's
           :12
Remplazar valores nulos por 0
tendencia$Yt.ts.desc.trend[is.na(tendencia$Yt.ts.desc.trend)]=0
```

Modelamiento de la tendencia

```
tendencia$x <- seq(1:nrow(tendencia))</pre>
tendencia$x
##
     [1]
           1
               2
                   3
                       4
                           5
                                6
                                    7
                                        8
                                            9
                                               10
                                                       12
                                                           13
                                                               14
                                                                    15
                                                                        16
                                                                            17
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## [109] 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126
## [127] 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144
## [145] 145 146 147 148 149 150 151 152 153 154 155 156
modelo <- lm(Yt.ts.desc.trend ~x, data= tendencia)
tendencia_estimada <- modelo$fitted.values</pre>
head(tendencia_estimada)
                            3
                                      4
                                               5
## 455.4575 460.7720 466.0865 471.4010 476.7155 482.0300
```

Estacionalidad

```
estacional <- data.frame(Yt.ts.desc$seasonal)
head(estacional)</pre>
```

Estimacion de la serie en base a un modelo multiplicativo

```
dataf <- data.frame(tendencia_estimada,estacional)
colnames(dataf) <- c('tend_est','estacionalidad')

dataf$Yt_est <- dataf$tend_est*dataf$estacionalidad</pre>
```

Grafico del modelo final

```
plot(Yt, col = "red")
points(dataf$Yt_est, type = 'l', col = 'blue')
```

