

$$\begin{aligned}
p(y_i | X, \beta, w) &= \int p(y_i | X, \beta, w, \lambda_i) p(\lambda_i | X, \beta, w) d\lambda_i \\
&= \int p(y_i | X, \beta, w, \lambda_i) p(\lambda_i) d\lambda_i \\
&\propto \int (\lambda_i w)^{1/2} \exp\left(-\frac{w\lambda_i}{2} (y_i - x_i^\top \beta)^2\right) \lambda_i^{h/2-1} \exp\left(-\frac{h}{2} \lambda_i\right) d\lambda_i \\
&\propto \underbrace{\int \lambda_i^{h/2-1/2} \exp\left(-\left(\frac{w}{2} (y_i - x_i^\top \beta)^2 + \frac{h}{2}\right) \lambda_i\right) d\lambda_i}_{\Gamma\left(\frac{h+1}{2}, \frac{w}{2} (y_i - x_i^\top \beta)^2 + \frac{h}{2}\right)} \\
&\propto \Gamma\left(\frac{h+1}{2}\right) \left(\frac{w}{2} (y_i - x_i^\top \beta)^2 + \frac{h}{2}\right)^{-\frac{h+1}{2}} \\
&\propto \left(\frac{w}{h} (y_i - x_i^\top \beta)^2 + 1\right)^{-\frac{h+1}{2}} \\
y_i | X, \beta, w &\sim t_h(x_i^\top \beta, w^{-1/2})
\end{aligned}$$