

Proof: Using Prop. 8

a) The zero vector, $\vec{0} = 0\vec{v}_1 + 0\vec{v}_2 + \dots + 0\vec{v}_p$ is a linear combination of \vec{v} 's.

b) If $w_1 = c_1\vec{v}_1 + c_2\vec{v}_2 + \dots + c_p\vec{v}_p$ & $w_2 = d_1\vec{v}_1 + \dots + d_p\vec{v}_p$ are 2 linear combinations then

$$w_1 + w_2 = (c_1 + d_1)\vec{v}_1 + \dots + (c_p + d_p)\vec{v}_p$$

c) If c is any scalar, & using w_1 from above

$$cw_1 = c(c_1\vec{v}_1 + \dots + c_p\vec{v}_p) \text{ is again a linear combination.}$$