

رقم القيد : الاسم: المجموعة:

السؤال الأول (10 درجات): ضع علامة صح (✓) أو خطأ (×) امام كل عبارة **True or False question:**

1. The False Position method is a combination of the secant method and bisection method. ()
2. If we can begin with a good choice x_0 , then: Newton's method will converge to x_r slowly and slower than the secant and the Regula Falsi methods. ()
3. The matrix $a = [1, 2, 3; 2, 4, 6]$ is the output of the next code ()

```
for k = 1:3
    for m = 1:2
        a(m,k) = m*k
    end
end
```
4. The MATLAB command **root** is used to calculate the values of y when $x = 0$. ()
5. The MATLAB command **polyfit(x, y, N)**, returns the coefficients of for the polynomial of degree N and data points x and y . ()
6. This piecewise polynomial is a quadratic spline: $S(x) = \begin{cases} S_0(x) = 0; & -1 \leq x \leq 0 \\ S_1(x) = x^2; & 0 \leq x \leq 1 \end{cases}$ ()
7. Extrapolation is the process of finding the value of $f(x)$ corresponding to any untabulated value of x between x_0 and x_n . ()
8. After executing the next two Matlab commands y vector will contain the values $y = [4, 6, 8]$. ()

```
>> x = linspace(2,10,5);
>> y = x(2:end-1);
```
9. In Cubic spline, since $f(x)$ is cubic in each of the subintervals, so that, $f''(x)$ shall be linear and continuous at each point. ()
10. The Taylor series of a function is an infinite sum of terms that are expressed in terms of the function's derivatives at a single point. ()

السؤال الثاني (20 درجات): أختار الإجابة الصحيحة: choose the right answer:

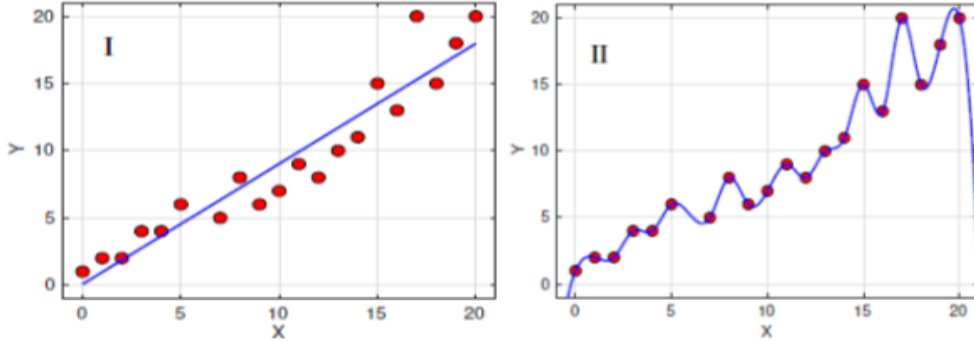
- 1) لماذا متعددة الحدود هذه ليست cubic spline؟ Why this piecewise polynomial is NOT a cubic spline?

$$S(x) = \begin{cases} S_0(x) = 2; & 0 \leq x \leq 1 \\ S_1(x) = 2 + (x-1)^2; & 1 \leq x \leq 2 \end{cases}$$

- (A) $S_0(1) \neq S_1(1)$ (B) $S'_0(1) \neq S'_1(1)$ (C) $S''_0(1) \neq S''_1(1)$

- 2) For each plot, identify the type of approximation that has been performed:

لكل رسم، حدد نوع التقريب الذي تم إجراؤه:



- (A) I = interpolation, II = curve fitting (B) I = curve fitting, II = interpolation (C) I = interpolation, II = extrapolation

- 3) If the step size h between N data points is constants, so that, we can use this Lagrange method to find the polynomial.

إذا كان حجم الخطوة h بين نقاط البيانات N عبارة عن ثوابت، فلا يمكننا استخدام طريقة Lagrange لإيجاد كثيرة الحدود.

- (A) True (B) False

- 4) Consider the fixed point iteration $x_{k+1} = g(x_k)$ with $g(x) = \frac{x}{3} + \frac{4}{3x}$ Which root- finding problem is this equivalent to $f(x)=0$?

اعتبر تكرار النقطة الثابتة $x_{k+1} = g(x_k)$ مع $g(x) = \frac{x}{3} + \frac{4}{3x}$ أي من مسائل إيجاد الجذور تكافئ $f(x)=0$ ؟

- (A) $x^2 - 2 = 0$ (B) $\frac{x}{3} + \frac{4}{3x} = 0$ (C) $\frac{1}{3} - \frac{4}{3x^2} = 0$

- 5) The coefficients of the polynomial $f(x) = 3x^3 - 7x^4 + x^5 - 6x^2 + 1$ are:

- (A) $c = [-7 \ 1 \ -6 \ 1]$ (B) $c = [3 \ 0 \ 1 \ -7 \ 0 \ -6 \ 0 \ 1]$

- 6) The linear Lagrange polynomial that interpolates the points (1; 3) and (4; 5) is:

كثير حدود Lagrange الخطي الذي يقحم النقاط (1 ؛ 3) و (4 ؛ 5) هو:

- (A) $P(x) = -x + \frac{5}{3}x$ (B) $P(x) = \frac{-9}{x-4} + \frac{15}{x-1}$ (C) $P(x) = \frac{1}{3}(2x - 7)$

- 7) Fill in the blanks in the table with Newton backward difference:

املا الفراغات في الجدول باستخدام Newton backward

x	y
1	1
3	9
4	16

- (A) $a = 4, b = 7, c = 1$ (B) $a = 8, b = 7, c = 3$ (C) $a = 8, b = 7, c = -1$

8) The output of the next code is:

- (A) 11 (B) 6 (C) 11.5 (D) 1 2 3 ...10

```
x = 1;
while 1 == 1
    x = x+2.5;
    if x > 5
        disp(x)
        break
    end
end
```

9) You are provided with table of points for the function $f(x) = x + 10 - e^x$:

Use this data to perform two steps of the bisection method for solving $f(x) = 0$, assuming the initial interval $[0; 4]$. What is the approximation of the root?

x	0	1	2	3	4
$f(x)$	9.000	8.282	4.611	-7.086	-40.598

- (A) 1 (B) 2 (C) 3 (D) 4

لديك النقاط التالية حسب الجدول للدالة $f(x)=x+10-e^x$ استخدم هذه البيانات بإجراء خطوتين بطريقة التنصيف لحل المعادلة $f(x) = 0$ بفترة ابتدائية $[0; 4]$. ماهو جذر المعادلة بعد الخطوتين:

السؤال الثالث (10 درجات):

Fit a straight line to the following data:

قم بملاءمة خط مستقيم للبيانات التالية:

x	1	3	4	6	8	9	11	14
y	1	2	4	4	5	7	8	9

Also estimate the value of y , when $x=10$.

Given the values

إذا أعطيت القيم التالية

$x:$	5	7	11	13	17
$f(x):$	150	392	1452	2366	5202

evaluate $f(9)$, using *Lagrange's formula* / اوجد قيمة $f(9)$ باستخدام

.....انتهت الأسئلة، مع تمنياتي للجميع بالتوفيق.....

$$f(x+h) = f(x) + f'(x)h + \frac{f''(x)}{2!}h^2 + \frac{f'''(x)}{3!}h^3 + \dots$$

True Error (E_t)= True value – approximate value

$$x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)}$$

$$c = \frac{a+b}{2}$$

$$x_{n+1} = x_n - \frac{x_n^m - a}{mx_n^{m-1}},$$

$$x_{i+1} = x_i - \frac{f(x_i)(x_i - x_{i-1})}{f(x_i) - f(x_{i-1})}$$

$$x_2 = x_0 - f(x_0) \frac{x_1 - x_0}{f(x_1) - f(x_0)}.$$

$$P(x) = y_0 + \frac{\Delta y_0}{h}(x - x_0) + \frac{\Delta^2 y_0}{2!h^2}(x - x_0)(x - x_1) + \dots + \frac{\Delta^n y_0}{n!h^n}(x - x_0)(x - x_1) \dots (x - x_{n-1})$$

$$P(x) = y_n + \frac{\nabla y_n}{h}(x - x_n) + \frac{\nabla^2 y_n}{2!h^2}(x - x_n)(x - x_{n-1}) + \dots + \frac{\nabla^n y_n}{n!h^n}(x - x_n)(x - x_{n-1}) \dots (x - x_1)$$

$$f(z) \approx \sum_{i=1}^N f_i \prod_{\substack{j=1 \\ j \neq i}}^N \frac{z - x_j}{x_i - x_j}.$$

$$a = \frac{N \sum x_i f_i - \sum x_i \sum f_i}{N \sum x_i^2 - (\sum x_i)^2}$$

$$b = \frac{\sum f_i}{N} - a \frac{\sum x_i}{N} = \bar{f} - a \bar{x}$$