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Master's Thesis in MSc Embedded Systems

Occupancy data driven automatic determination of sensor locations in buildings

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Abstract

Building automation systems (BAS) are getting extremely popular due to increase in the demand to reduce energy consumption in residential and commercial buildings as well as for other applications such as ambient assisted living, smart home, and smart living. As the number of applications increases, the complexity of the systems also increases making the installation and maintenance much more difficult and involved, thus requiring skilled persons to maintain them. One of the main challenges is generating and updating the location meta-data of the sensors. Location meta-data is the primary input for many applications. Currently the location meta-data is being generated and maintained manually, this process is highly cumbersome and also prone to errors. Erroneous location information can make BAS ineffective. Previous investigations have looked at clustering sensors based on their spatial locations, but not at locating the sensors in the space. In this work we propose an automatic sensor data driven sensor location inferencing system. We reduce the problem of determining the location of sensors to a problem of graph matching using the correlation matrix and grid information. Within graph matching the problem belongs to graph monomorphism type, which is an NP-Complete problem. We make use of **VF2** algorithm a popular graph matching algorithm in this work. Furthermore, we validate our algorithm with two different real world testbeds. We are able to locate all the sensors accurately for our experimental testbed and for the Tokyo testbed we observe an error in the determination of sensor location for only 3 out of the 43 sensors.

Location, Location, Location – Harold Samuel

Preface

Indoor spaces are getting smarter day by day with deployment of huge amount of sensors and actuators. Many applications built for maintenance of the building use the sensor data as inputs to actuate the actuators to perform their function. May it be simple turning on and off of lights based on occupancy or a more critical applications like fire detection and alarming, all need data from the sensors. One important meta-data about the sensor, that is crucial for all theses application is the sensor location. Without which the applications cannot perform effectively. Till now the meta-data is being created and maintained manually, which is a cumbersome process and prone to error. In our work here we propose a method to automatically determine the location of the sensor using the data from the sensors.

This work was carried out at Philips Lighting, Eindhoven. Philips Lighting being a market leader in the field of lighting are actively providing lighting control solutions. This work is aimed to help automate the process of creating and maintaining the meta-data of sensor location and thus aiding faster deployment and easier maintenance of the systems.

Before going to the technical details of the thesis, I would like to thank my supervisor Dr.Ashish Pandharipande(Philips Lighting) for giving me an opportunity to carry out my thesis at Philips Lighting. I would also like to thank him and Dr.David Caicedo Fernandez(Philips Lighting) for critically analyzing my work during our regular weekly meetings and giving me valuable suggestions. My sincere gratitude to my university supervisor Dr.Venkatesh Prasad(TU Delft) for all the support and guidance he provided. I would also like to thank my parents and grandparents for their unconditional love and support during all these years. I would like to thank all my friends who have tolerated my constant whining and supported me during my tough times. A special thanks to all the people of FO 52, past and the present who made the stay in Eindhoven so much more pleasant.

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Chapter 1

Introduction

1.1 Motivation

The European Union (EU) has pledged to cut the consumption of primary energy by 20%, by the year 2020. It is estimated that buildings consume 40% of the energy produced¹. This has resulted in an increase in the demand to reduce the energy consumption of buildings. To reduce the consumption of energy, building automation systems (BAS) are being widely employed. BAS are computer-based systems that help to manage, control and monitor building technical services (HVAC, lighting etc.) and the energy consumption of devices used by the building. It is estimated that BAS can save a building between 5 % to 30 % on the utility cost by managing HVAC and lighting systems[1]. Figure 1.1 illustrates a building equipped with BAS.

BAS deploy a huge number of sensors, which provide inputs to perform efficient control of various services. BAS brings with it various benefits, and at the same time offers numerous challenges too. For BAS, sensor measurements alone are not sufficient to understand the condition of the facilities, unless combined with meta-data associated with the sensors. Meta-data as defined in [2] refers to any information associated with the device that helps to contextualize the measurements or control signals regularly being sent from/to the device, such as the location within the building, the physical phenomenon being sensed, etc. One of the major challenges in a BAS system is generating and updating the meta-data of the sensors while they are deployed or replaced. One of the important meta-data required is that of the physical location of the sensor as discussed in [3]. As the size and distribution of the deployed sensors are high, it is highly cumbersome and error prone to manually maintain the meta-data about the sensor placement. Apart from being error prone, the manual configuration has to be repeated every time there is a change in the meta-data. Change in meta-data can

¹according to value published at <https://ec.europa.eu/energy/en/topics/energy-efficiency/buildings>



Figure 1.1: Illustration of a building equipped with BAS.

be due to various reasons, such as a change in the office setup, replacement and/or relocation of sensors. All these factors result in inaccurate information about the location of the sensors. Without accurate information of the location of the sensors, interpreting the data collected from the sensor is difficult and also can be misleading. This could result in the decrease in the effectiveness of the deployed BAS systems. Hence there is a need to develop methods to accurately determine the location of the sensors within the building.

1.2 System Description

Smart lighting control is one of the major components of BAS. Lighting is responsible for 11% and 18% of the energy consumption in case of residential and commercial buildings respectively[4]. State of the art lighting control employs co-located occupancy sensors and light sensors, placed on luminaires which are attached to the ceiling[5–7]. Figure 1.2 shows an illustration of one such system. In this thesis, we consider a centrally controlled lighting systems with such ceiling mounted sensor grid. Occupancy sensors provide

information about the occupancy of the space and the light sensors measure the intensity of the light within the field of view of the sensors. A centrally located controller using this information from the sensors, controls the lights so as to ensure that the space is lit to a suitable intensity level.

In this thesis, we make use of only the occupancy sensors, whose output is binary. We use the notation 1 representing occupancy and 0 representing an unoccupied space, within the sensors field of view. We represent the sensors grid as a graph G with the sensors located on the vertices of the graph. We assume that the Cartesian coordinates, either relative or absolute of the vertices of the grid are available.

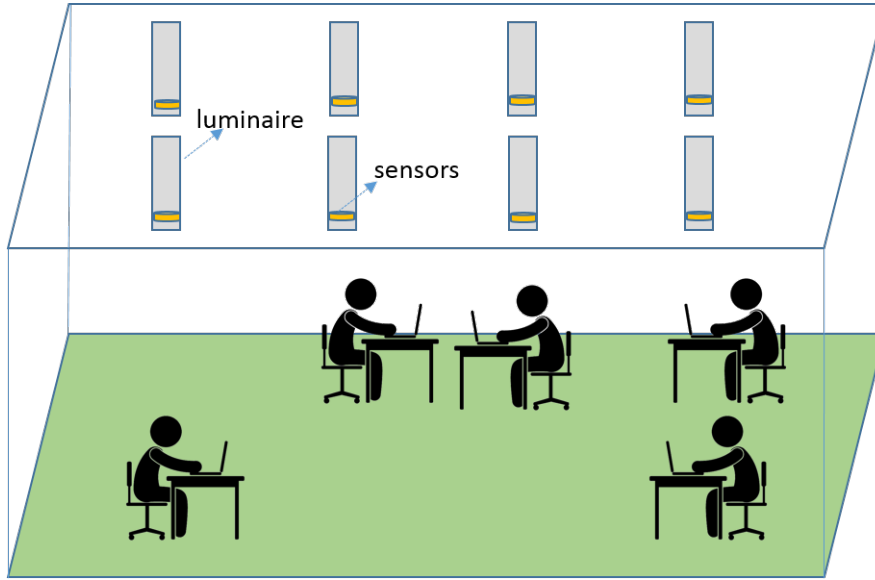


Figure 1.2: Illustration of smart indoor lighting system with co-located sensors

1.3 Problem Statement

Several studies have been carried out to infer the sensor location from sensor data [8–14]. Most of the methods developed so far have identified ways to cluster the sensors that are located within their proximity; however the methods do not identify where exactly on the grid each sensor is located in a dense sensor grid [8–10]. Therefore the research question that is being tackled in this work is:

How to automatically determine the location of the sensors utilizing binary data from the ceiling mounted occupancy sensors and the information about the grid (coordinates of the vertices constituting the grid)?

The major challenges in solving the problem are:

- In a data driven localization method, the first step is identifying the neighbors of a sensor. By neighbors, we refer to all the sensors which have an overlapping field of view with the sensor under consideration. As described earlier we consider binary occupancy sensors in our system. Since in the overlapping region the neighboring sensors observe the same event, these sensors will be triggered simultaneously. Hence a straightforward way of identifying the neighboring sensors would be to look for sensors where simultaneous triggers are observed. But when multiple people are present in the space under consideration, simultaneous triggers can be observed even for non neighboring sensors. This makes it difficult to distinguish between the neighboring and non-neighboring sensors. Also, raw data from the sensors do not provide any extra information about the occupant or the activity that is happening in the space, the challenge is to identify a feature that can be extracted from the sensor's data that will help in differentiating neighboring and non neighboring sensors.
- After identifying sensors within each other's neighborhood, deriving the location information utilizing the grid information is non trivial. There are several possible ways in which these cluster of neighboring sensors can be arranged on the grid. Out of these several possible ways, the challenge is to identify the true arrangement of the sensors on the grid.

1.4 Contributions of the thesis

The main contributions of the thesis are:

- Use of energy feature of the binary occupancy sensor data to distinguish between neighboring and non-neighboring nodes.

From binary occupancy sensor data, we compute the energy feature using a moving window with 50% overlap. We determine the window length empirically. We use this energy feature to calculate the correlation between the sensors. Using these correlation values in this work we develop a method to distinguish between the neighboring and non-neighboring nodes.

- Determine a criteria to obtain the true arrangements of the sensor with the help of correlation coefficients between the sensors.

Given n sensors, these sensors can be arranged on the grid in $n!$ ways. Using the correlation values between the sensors we define a quantity called Grid Correlation Sum (GCS), which is used to identify the precise arrangement of the sensors on the grid.

- Establish a relationship between the correlation coefficients among the sensors and the sensor grid.

In this thesis, we show that there exists a relationship between the maximum spanning tree (MST) obtained from the correlation coefficient between all the sensors and the sensor grid. We show that the MST represents one of the spanning trees for the sensor grid.

- Reducing the problem of determination of sensor locations on the grid to a problem of graph matching [15].

Using the relationship established between the MST of correlation coefficients and the sensor grid, we use graph matching technique to obtain the various mapping between the sensors and the grid vertices. Out of the various mapping obtained using *GCS* we determine the actual mapping between the sensor nodes and the grid vertices.

1.5 Outline of thesis

The rest of the thesis is organized as follows: in Chapter 2, we give a brief overview of related work. In Chapter 3, we present the method that has been developed. In Chapter 4, we describe our testbed setup. Next, in Chapter 5, we present the results obtained by applying the method that we have developed on actual sensor data obtained from 2 different testbeds. In the end in Chapter 6, we conclude the work done and discuss future work.

Chapter 2

Literature Review

2.1 Sensor Localization

There has been an extensive body of research that aims at obtaining the location information of the sensors in wireless sensor networks (WSN). All the approach that has been taken till now has been categorized by Wang et al. in [16] to fall into one of the following categories:

- Proximity based localization
- Range based localization
- Angle based localization

In **proximity based localization** [17–19], WSN is represented as a graph $G(V, E)$. V representing the location of the sensor nodes, E representing the connectivity between two nodes which are within each others proximity. Location of the subset of the nodes, $H \subset V$ called as anchor nodes are known. The goal is to estimate the location of the remaining non anchor nodes relative to the position of the anchor nodes.

Range based localization makes use of ranging techniques using RSSI [20], time of arrival (ToA) [21] and time difference of arrival (TDoA) of the signals [22]. The distance between the nodes is computed using the ranging technique. Computing the locations of the nodes using distance information is non trivial. Range based approach may or may not need anchor nodes. With anchor based approach multilateration technique is used to find the location of the non anchor nodes. Without anchor nodes, multi dimensional scaling (MDS) is adopted for localization.

Angle based localization uses the information of angle of arrival (AoA) of the signals to determine the location of the sensors [23, 24]. To determine the angle, antenna array or multiple receivers on the node are required.

In the case of proximity based localization, the locations of the anchor nodes are required to compute the locations of the remaining nodes, which

might not be available always. The major drawback for the range based and angle based algorithm is that the nodes require specialized hardware to measure ToA/TDoA, AoA [18] thereby, increasing the cost per sensor node. As BAS employs a large number of sensors, using such specialized hardware becomes infeasible as the total cost of the system increases. Calculating distance based on the RSSI is prone to noise of the order of several meters [25], as the propagation of radio waves is non uniform in an indoor environment.

2.1.1 Data driven sensor localization

Data driven sensor localization has gained attention recently. The main advantage of this approach is that it does not require any special hardware, extra processing power on the nodes or extra information like RSSI to perform the localization. It makes use of the sensor data collected for the functioning of the applications deploying the sensors. As our work falls under the same category, we provide an overview of related works using the sensor data to determine the sensor location. For convenience we categorize the works in this area to the following categories:

Sensor Localization in Commercial Buildings

The works presented below consider a system set up in commercial buildings. In [8], Hong et al. apply empirical mode decomposition (EMD) to 15 sensors in 5 rooms to cluster sensors which belong to the same room by analyzing the correlation coefficients of the intrinsic mode functions (IMF). They characterize the correlation coefficient distribution of sensors that are located in the same room and different rooms. They were able to show that there exists a correlation boundary analogous to the physical boundary which can be discovered empirically. In [9], Akinici et al. propose a feature: energy content in HVAC delivered air, which can be derived from HVAC system sensors which could lead to the identification of the space in which the sensors are located. They combine sensor measurements and building characteristics (floor area) for the identification of the space in which the sensors are present. In [10], Koc et al. propose a method to automatically identify the zone temperature and discharge temperature sensors that are closest to each other by using a statistical method on the collected raw data. They explore whether linear correlation or a statistical dependency measure (distance correlation) are better suited to infer the spatial relationship between the sensors. They carry out their analysis on three different testbeds. They also investigate the effects of distance between sensors and measurement periods on the matching results. In the end, the authors conclude that linear correlation coefficient provides better matching results compared to distance correlation. The authors also conclude that as the distance between the sensors increase, the data size needed to infer spatial

relationships also increase.

Sensor Localization in Smart homes

The works presented below, consider a system set up in smart homes. [Lu et al. \[11\]](#) describe a method to generate representative floor plans for a house. Their method clusters sensors to a room and assigns connectivity based on the simultaneous firing of the sensors placed on the door and window jambs. The algorithm gives a small set of possible maps from which the user has to choose the right map. Method requires special placement of the sensors to eliminate false clusters caused due to simultaneous occupancy of multiple rooms. The authors were able to calculate the floor map of 3 out of the 4 houses they evaluated. [Ellis et al. \[12\]](#) proposed an algorithm to compute the room connectivity using PIR and light sensor data. They cluster the sensors present in the same room based on observing the simultaneous triggering of the sensors. After clustering, they compute room connectivity based on, the artificial light spill over between rooms; occupancy detection due to movements between rooms; and fusion of the two. They calculate the transition matrix for the light sensor and occupancy sensor. Fuse both the data together to compute the connectivity graph. Here the authors have considered a situation where there are only one PIR and light sensor per room. [Müller et al. \[13\]](#) define sensor topology as a graph with directed and weighted edges. All pairs of consecutive sensors triggers are interpreted as a user walking from the former to the latter sensing region indicated in the sensor graph by an edge from the former to the latter. Every time a consecutive edge triggers are observed the weight of the edge between the sensors is incremented. They define a method to filter out erroneous edges.

Sensor Localization by activity recognition

In [\[14\]](#), [Marinakis et al.](#) obtain the sensor network topology using Monte Carlo Expectation Maximization. They assign activity to people present in the space to obtain the graph topology. The algorithm requires, the number of people present in the space as the input. They demonstrate the effectiveness of the algorithm using various simulated data.

Limitations

The methods presented in [\[8–10, 13\]](#) look at only clustering the neighboring sensors together. They do not provide the information about where the sensors are located in the sensor grid. [\[11–13\]](#) consider a smart home setting where sensors are sparsely located to identify their positions. Method proposed in [\[11\]](#) requires special placement of sensors in the room to aid them in locating the sensors. In [\[12\]](#), the authors assume that there is only

one sensor per room which makes it not applicable to systems which employ more than one sensor in a room.

The method we propose is able to locate the sensor on the grid. Our approach does not limit the number of sensors present within a room nor does it require any special placement of sensors. The only condition that we apply is that a sensor should have an overlapping field of view with other sensors.

2.2 Meta-data inference

As explained in section 1.1, there is a need to automate the process of determining meta-data information of sensors. Due to which there has been significant interest shown to develop such methods. The works in this area can be classified into two categories: inference from tags and inference from data

2.2.1 Inference from Tags

In general meta-data of the sensors are embedded in the tags that are given to the sensors. These tag names are highly unstructured and inconsistent as different tags are added by different installers. HVAC systems might be installed by a certain company, whereas lighting controls are installed by another company. These installers tag the sensors and actuators based on their own conventions and convenience. Though there has been significant efforts to standardize the convention of naming the tags, no solution has been widely accepted [2]. Hence there have been methods developed to infer the meta-data automatically from these unstructured tags.

In [26], [Bhattacharya et al.](#) developed a technique to convert the tags of the sensors to a common and understandable name space. The method learns from a small number of examples of the tags, which is provided by an expert, such as the building manager. From these representative examples, the method deciphers the rest of the tags of the sensors that are part of the system. In [27], [Schumann et al.](#) use the semantics of the textual labels of the sensor tags for semi-automating the process of inferring the meta data associated with sensors.

2.2.2 Inference from Data

Works [8–14] that were discussed previously fall under this category of inference of meta-data from the sensor measurements. They provide the information about the location of the sensor within the facility. Apart from the inference of location of the sensors, there have been few works which derive the information about the sensor type from the data. In [28], [Calbimonte](#)

et al. observe the similarity in the slopes of the piece wise linear representation of the raw time-series measurements. Sensors which show similar slopes are categorized as of the same type. In [2], Gao et al. extract statistical features from the data stream and train various classifiers to identify the sensor type.

2.3 Graph Matching

We use graph matching technique in our work to determine the location of the sensor on the grid vertices. Depending on the mapping type between the base graph and the pattern graph, graph matching can be categorized into different types. Our problem falls into the category of graph monomorphism. In this section, we present the related works in the area of graph matching in particular we look at works which solve graph monomorphism.

Graph matching is widely used in pattern recognition and image processing applications. Graph matching also finds its application in the field of biomedical and biological applications. Most of the algorithms that are developed for the purpose of graph matching employs tree search to iterate through all the nodes when an unfruitful match is encountered the algorithm backtracks. The key principle is that there will be a partial mapping which will be initially empty and the mappings gets expanded iteratively by adding to it new pairs of matched node. The matched nodes are chosen based on the conditions determined by the matching type.

The first prominent and one of the most widely used algorithm till date in the area of graph matching was proposed by Ullmann [29]. Ullmann algorithm addresses the problem of graph isomorphism, sub graph isomorphism, graph monomorphism. Ullmann algorithm is based on depth-first search with backtracking. The author employs a procedure called *refinement procedure*, which prunes unfruitful matches based on the knowledge of the adjacent nodes and the degree of the nodes that are being matched. Ghahraman et al. in [30], proposed a graph monomorphism algorithm. The authors formulate the graph monomorphism problem as a minimum weight clique problem of weighted nets. The major drawback of the algorithm is that the algorithm uses a $N^2 \times N^2$ matrix to represent netgraph obtained from the cartesian product of the nodes of two graphs under investigation. N representing the number of nodes of the largest graph. This leads to large memory consumption, making the algorithm viable for only small graphs. A more recent algorithm for graph isomorphism, subgraph isomorphism, and monomorphism was proposed by Cordella et al. in [31], popular as VF algorithm. The authors define a set of rules that are based on the sets of nodes connected to the ones that are already mapped. The authors further improved the algorithm in 2001 in their paper [32]. The authors proposed a modification to the algorithm and called it VF2. The authors introduce a

method to restore data structure, which enabled them to reduce the memory consumption from $O(N^2)$ to $O(N)$ where N is the number of nodes in the graph, thus enabling the algorithm to work with large graphs.

2.4 Summary

In this chapter we give a brief overview of the related work in the field of data driven sensor localization in buildings and meta-data inference technique. We also discuss works related to graph matching technique, which we use in our method to map the sensors to their locations on the grid. Table 2.1 summarizes the data driven localization techniques that have been discussed in this chapter. Previous data driven methods as discussed in this chapters have successfully clustered co-located sensors using various approaches. But they do not provide any information about the sensors location with respect to the entire sensor grid. We in our work address this issue and propose a technique to identify the location of the sensors on the sensor grid.

Work	Purpose	Method
Hong et al.[8]	co-locating sensors	Correlation coefficient between the IMF of the sensor data
Akinici et al.[9]	co-locating sensors	Correlation coefficient between the energy content of the HVAC delivered air
Koc et al.[10]	co-locating sensors	Correlation between the raw sensor data.
Lu et al.[11]	floor maps for a house	Clustering based on simultaneous trigger of occupancy sensors. Connectivity between rooms is determined by simultaneous triggering of sensors placed on window jamb and door.
Ellis et al.[12]	room connectivity graph	Transition matrix between the sensors located in different rooms.
Müller et al.[13]	co-locating sensors	Consecutive edge triggers
Marinakis et al.[14]	inferring sensor network topology by assigning activity to users.	Assigning activity to people to obtain the sensor topology

Table 2.1: Summary of data driven localization techniques

Chapter 3

Methodology

This chapter explains the method developed to locate the occupancy sensors in a ceiling mounted sensor grid, using the data obtained from the sensors and information about the locations of the vertices of the grid. Consider a sensor grid as shown in the figure 3.1, consisting of n nodes. There are $N = n!$ ways in which these sensors can be uniquely placed on the grid. Out of these N ways we have to identify the actual locations of the sensors in the grid. Before we explain the method, we introduce the definitions of the

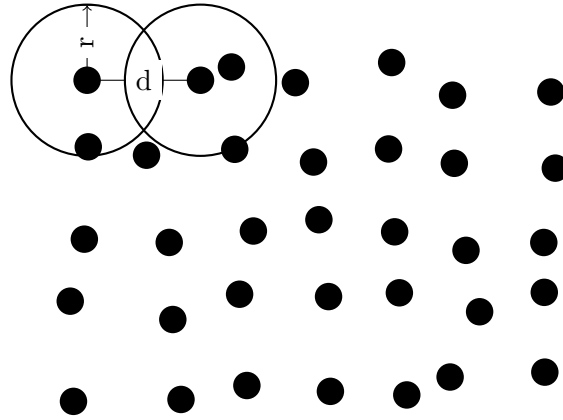


Figure 3.1: A sensor grid with sensors field of view being r .

terms that are used in the thesis.

Definition 3.1. Neighboring sensors: Two sensors are said to be neighbors if they have overlapping field of view.

Definition 3.2. Grid Adjacency Matrix: We represent the sensor grid in the form of an adjacency matrix. Two vertices of the grid i and j are adjacent if the distance between them ($d_{i,j}$) is less than twice the radius (r) of the sensor's field of view.

$$GAM_{i,j} = \begin{cases} 1, & \text{if } d_{i,j} < 2r \forall i \neq j \\ 0, & \text{otherwise} \end{cases}$$

$d_{i,j}$ is the euclidean distance between the vertex $i(x_i, y_i)$ and $j(x_j, y_j)$.

$$d_{i,j} = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}$$

From the definitions 3.1 and 3.2, we can say that sensors placed on neighboring vertices will be neighboring nodes and vise versa. As can be seen in the figure 3.1 there will be an overlap in the field of view between two sensors if the distance (d) between them is less than $2r$.

3.1 Feature

As it has been shown previously in [8–10], that the neighboring sensors can be identified by computing the correlation values for the sensors raw data or a feature extracted from the raw sensor data. We commence our method similarly by identifying a feature which will aid us to do the same. As neighboring sensors have an overlapping field of view, they observe the same events and thus are highly correlated. On the raw signals of the PIR data stream we use a sliding window with 50% overlap between the consecutive windows and compute the energy feature using the equation 3.1. 50% overlapping window has been chosen as it has been shown to be effective for feature extraction previously[33].

$$E_s = \sum_{m=0}^k |a[m]|^2 \quad (3.1)$$

$a[m]$ - Discrete time signal.

For a PIR sensors whose output is binary, computing energy reduces to counting the number of triggers observed within the window.

With the newly computed energy data stream, we compute the cross correlation between all the sensors using equation 3.2

$$r_{X,Y} = \frac{\sum_{i=1}^m (X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^m (X_i - \bar{X})^2} \sqrt{\sum_{i=1}^m (Y_i - \bar{Y})^2}} \quad (3.2)$$

X and Y are data streams.

X_i and Y_i are the i^{th} sample of the data stream X and Y respectively.

\bar{X} and \bar{Y} is the mean value of X and Y respectively.

m is the number of samples.

3.2 Grid Correlation Sum

Using the cross correlation values between the sensors, we define correlation matrix R between the n sensor nodes as shown in the equation 3.3 . The matrix R is constructed such that $R(i, j)$ corresponds to the correlation value between the sensors i and j .

$$R = \begin{bmatrix} r_{1,1} & r_{1,2} & \dots & r_{1,n} \\ r_{2,1} & r_{2,2} & \dots & r_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ r_{n,1} & r_{n,2} & \dots & r_{n,n} \end{bmatrix} \quad (3.3)$$

$r_{\alpha,\beta}$ represents correlation value between the energy stream for sensor α and β .

Using *correlation matrix* (R) and *Grid Adjacency Matrix* (GAM) we define a quantity called *Grid Correlation Sum* (GCS) as given in the equation 3.4. GCS represents the sum of correlation value of the sensor pair residing on neighboring vertices of the grid. As the matrices are symmetrical along the diagonals we only consider the elements of the upper triangle of the matrices excluding the diagonal elements.

$$GCS = \sum_{i=1}^{n-1} \sum_{j=i+1}^n R(\phi(i), \phi(j)) \times GAM(i, j) \quad (3.4)$$

i, j represent i^{th} and j^{th} vertex on the grid.

ϕ is a mapping functions which gives the sensor located at vertex i .

$R(\phi(i), \phi(j))$: correlation coefficient between the sensors placed on vertex i and j .

GAM : Adjacency matrix of the grid as per definition 3.2.

We use GCS to identify the correct arrangement out of all the N possible arrangements. We hypothesize that if we compute GCS for all the possible arrangements, the arrangement with the maximum GCS will represent the actual arrangement of the sensors on the grid. The reasoning behind the hypothesis is that, if two non-neighboring sensors are kept on neighboring vertices or vice versa then the correlation value between those two sensors will be low and thus decreasing the GCS . To illustrate this consider a sensor grid as shown in the figure 3.2. It consists of 3×3 grid. GCS for the the grid is :

$$GCS_1 = r(1,2) + r(1,4) + \dots + r(2,3) + \dots + r(5,6) + r(6,9) + \dots + r(8,9)$$

Now consider the arrangement shown in figure 3.3, where the position of the sensors 3 and 6 are interchanged

$$GCS_2 = r(1,2)+r(1,4)+...+r(\mathbf{2,6})+...+r(\mathbf{3,5})+r(\mathbf{3,9})...+r(8,9)$$

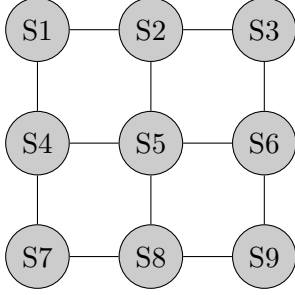


Figure 3.2: Actual arrangement of sensors on the grid.

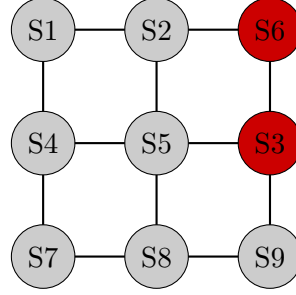


Figure 3.3: Incorrect arrangement of sensors on the grid.

GCS_1 will be greater than GCS_2 as $r(2,3) > r(2,6)$, $r(5,6) > r(3,5)$ and $r(6,9) > r(3,9)$ as sensor pair (2,6), (3,5) and (3,9) are non-neighboring sensor nodes placed on neighboring vertices. Hence we can say that GCS will be maximum for a mapping which maps sensors onto the grid accurately. With this condition, a straightforward way to determine the sensor location will be to carry out a brute force search where GCS is computed for all the N possible arrangements. The brute force search can be carried out only when the number of sensors is low, as the number of sensors increases the number of possible mappings also increase drastically, which makes it impossible to carry out a brute force search. Hence there is a need to reduce the search space.

3.3 Maximum spanning Tree

Having established a criterion to determine the right arrangement of sensors on the grid from possible N arrangements. The next step is to reduce the search space.

According to definitions [3.1, 3.2], in a sensor grid if one of the sensors are placed on a grid vertex then the neighboring vertex has to be occupied by a neighboring sensor. Consider a sensor grid as shown in the figure 3.4, sensor S_1 is mapped to one of the vertex of the grid, vertices a, b, c , and d are its neighboring vertices. Now sensor S_2 , which is a neighboring sensor of S_1 can only occupy one of the vertices among a, b, c or d . If this condition was not employed then S_2 could have occupied any of the unoccupied vertices on the grid and thus increasing the search space. If we are able to identify a neighboring sensor for a sensor node, we can reduce the search space by

eliminating the arrangements which place a non-neighboring sensor node onto a neighboring vertex or vice versa.

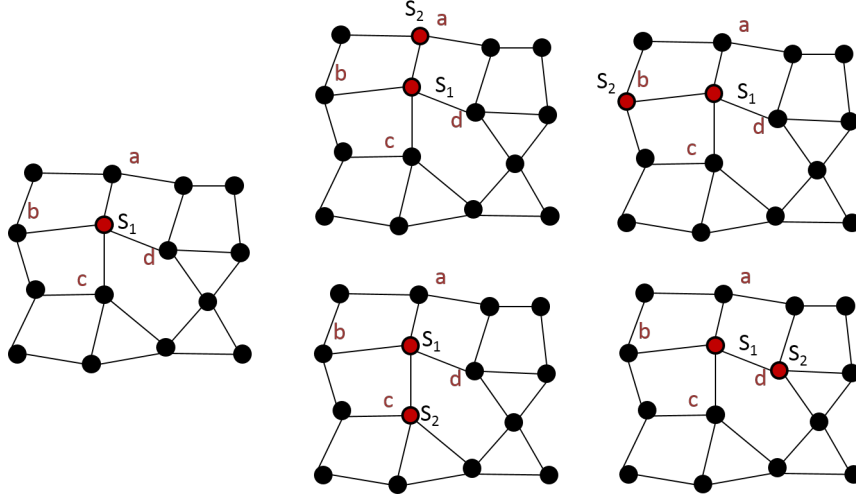


Figure 3.4: Possible arrangements of a sensor node when its neighboring node is already mapped on the grid

To identify neighboring sensors, we build a graph $G(V, E, W)$ such that $V = \{S_1, S_2, S_3 \dots S_n\}$, $E = \{(S_1, S_2), (S_1, S_3) \dots (S_{n-1}, S_n)\}$, $W = R$ and compute the Maximum Spanning Tree (MST) for it. The generated MST consists of all the sensor nodes connected to at least one other node by an edge. The MST chooses an edge for every sensor such that the weight of the edge outgoing from the sensor α to sensor β is the maximum among all the edges starting from sensor α , in graph G . As the weights represent correlation values it implies that the maximum spanning tree connects a node to another with which it has the maximum correlation. As the correlation between the neighboring nodes is maximum we can say that MST connects the neighboring sensors.

To compute MST we make use of Prim's algorithm[34]. Prim's algorithm is originally used to compute the minimum spanning tree. To compute the maximum spanning tree the weights of the graph G are negated and with these weights, minimum spanning tree is computed using Prim's algorithm. The minimum spanning tree thus obtained represents the maximum spanning tree for the original graph G .

As per the definition of $G(V, E, W)$, there is an edge between the neighboring vertices of the grid. The MST as we discussed above is formed by connecting neighboring sensors. Thus we can infer that the *MST* over R represents a spanning tree for the graph G .

It is possible that for a given grid there may be several spanning trees with the same structure. Figure 3.6 shows few of the spanning tree of the

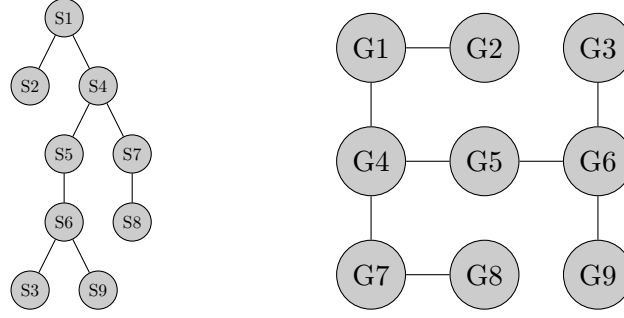


Figure 3.5: A maximum spanning tree incident on the grid

grid similar to the MST obtained for the correlation matrix.

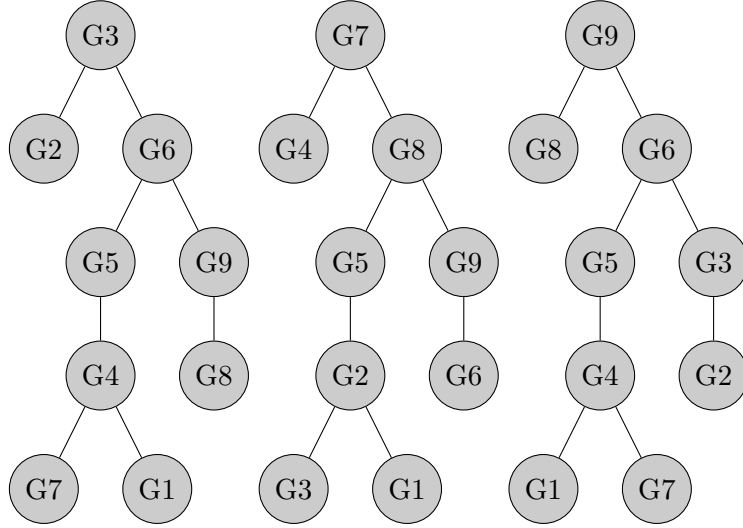


Figure 3.6: Various spanning trees for the grid with similar structure of the MST of the correlation matrix.

If we compute all the possible spanning trees for the grid which maintains the same structure as that of the *MST* for the correlation matrix and map each vertex on the *MST* to the corresponding spanning tree of the grid as shown in the figure 3.7, we obtain several possible mappings of the sensors to grid location. Among the possible mappings, we have to choose the correct arrangement. To choose the true arrangement of the sensor on the grid we make use of *GCS*. The number of arrangements that are obtained from this method is lesser than the N possible arrangements that had to be evaluated for brute force technique.

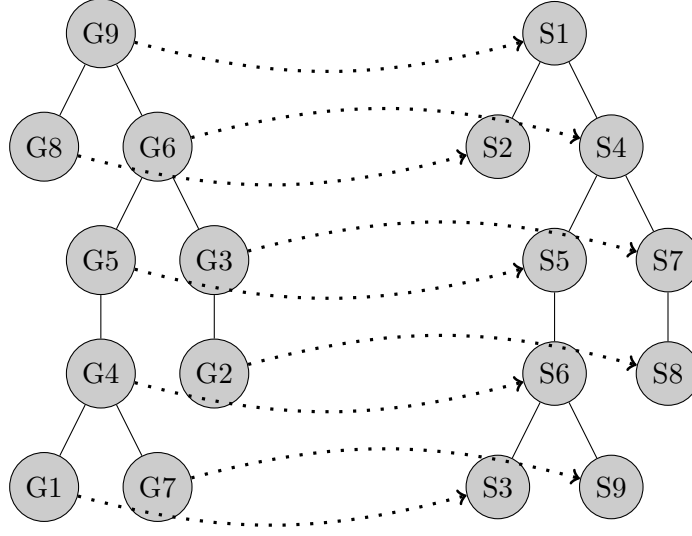


Figure 3.7: Mapping between the grid spanning tree and the MST for the correlation matrix

3.4 Graph Matching

In the previous section, we obtain a maximum spanning tree from R and saw how this represents a spanning tree for the grid. In addition, we observe that there can be multiple spanning trees whose structure is similar to the MST. In this section, we describe a method to obtain all the possible spanning trees that have the same structure as the MST obtained from the correlation matrix of the sensors. The task of checking if a pattern graph H is contained in a base graph G and obtaining all the mappings from G to H is a standard problem of graph matching.

A graph matching process between two graphs $G = (V_G, E_G)$ and $H = (V_H, E_H)$ consists of determining a mapping M which associates nodes of the graph G to H and vice versa. Different constraints can be imposed onto M which results in different mapping types: monomorphism, isomorphism, graph-subgraph isomorphism are the most popular ones [35]. Our problem falls under the category of graph monomorphism.

Two graphs $G = (V_G, E_G)$ and $H = (V_H, E_H)$ are *monomorphic* if and only if there exists an injective (node) mapping $\phi(V_G) \rightarrow V_H$: for which $\forall v, w \in V_G : (v, w) \in E_G \Rightarrow (\phi(v), \phi(w)) \in E_H$. [36].

Monomorphism is often confused with subgraph isomorphism. Monomorphism is a weaker kind of subgraph isomorphism.

Two graphs $G = (V_G, E_G)$ and $H = (V_H, E_H)$ are *sub graph isomorphic* if and only if there exists an injective (node) mapping $\phi(V_G) \rightarrow V_H$: for which $\forall v, w \in V_G : (v, w) \in E_G \Leftrightarrow (\phi(v), \phi(w)) \in E_H$. [36].

The relationship between edges of the graphs are equivalence for subgraph

```

Procedure Match(s)
  INPUT: an intermediate state s; the initial state  $s_0$  has  $M(s_0) = \emptyset$ 
  OUTPUT: the mappings between two graphs
  Match(s)
  IF M(s) covers all the nodes of  $G_2$  THEN
    OUTPUT M(s)
  ELSE
    Compute the set P(s) of the pairs of candidates for inclusion in M(s)
    FOREACH (u,v)  $\in$  P(s)
      IF F(s,u,v) THEN
        Compute the state s' obtained by adding (u,v) to M(s)
        CALL Match(s')
      ENDIF
    ENDFOREACH
    Restore data structure
  ENDIF

```

Figure 3.8: Pseudo code for VF2 algorithm[32]

isomorphism, and for Monomorphism relationship is an implication.

A problem of finding all the Monomorphisms of the pattern graph into the base graph is defined as Monomorphism problem. Graph Monomorphism is an NP-Complete problem [37]. In section 2.3 we present related works in the field of graph matching. In our work, we use the VF2 algorithm to obtain the mappings between the spanning tree and grid graph.

3.4.1 VF2

In this section, we give a brief description of the VF2 algorithm.

The VF2 algorithm is a graph matching algorithm to solve graph isomorphism, monomorphism, and subgraph isomorphism problem. VF2 uses depth-first search method to iterate through all the nodes and recursive backtracking technique to check for all the possible mappings. A process of matching a base graph G to a pattern graph H consists of determining a mapping M which associate nodes of the base graph (G) with nodes of the pattern graph (H) and vice versa, with some constraints. Mapping is expressed as a set of pairs of node (u, v) with $u \in G$ and $v \in H$. In VF2 algorithm the process of finding the mapping function is described by a State Space Representation (SSR). Each state s of the matching process can be associated with a partial mapping solution $M(s)$, which contains only a sub-

set of M . A transition from current state (s) to the next state (s') represents the addition of a mapping (u, v) to the state s .

VF2 algorithm introduces a set of rules which helps to prune the number of possible SSR that needs to be checked before obtaining a valid mapping. Figure 3.8 gives a high-level description of the VF2 algorithm. There are 3 important functionalities in the algorithm:

- generation of possible mappings ($P(s)$) .
- checking of the validity of the mapping ($F(s, u, v)$).
- Restore data structure.

3.4.2 Computation of candidate pair set $P(s)$

This section explains the method to compute the candidate pair set $P(S)$ for an undirected graph G and H . For every intermediate state s the algorithm computes $P(s)$, a set of possible mapping pairs. For each pair p belonging to $P(s)$ the feasibility of its addition $F(s, u, v)$ is checked : if the check is successful the next state $s' = s \cup p$ and the whole process recursively applies to s' .

To compute $P(S)$ set $T_1(s)$ and $T_2(s)$ are defined for Graph G and H respectively. T_1 and T_2 are the set of nodes in G and H , which are neighbors of the set of nodes included in the partial mapping state $M(s)$ but are not included in $M(s)$. Set $P(s)$ will be made of all the node pairs (u, v) with u being a node in T_1 with the smallest label and v being a node in T_2 . If T_1 and T_2 sets are empty then the set $P(s)$ be calculated by using the sets of nodes not contained in either $G(s)$, $H(s)$.

3.4.3 Feasibility Rules

Feasibility Rules are used to check the consistency of the partial solution s' obtained by adding nodes n, m and prune the search tree. The functionality of the rules is as explained below.

In the algorithm, those candidates (u, v) are pruned if for every neighbor u' of u in the partial mapping, the corresponding node v' is a neighbor of v , and vice versa.

The algorithm also compares the number of neighboring nodes of each u and v that are connected to nodes in $M(s)$ but are not included in $M(s)$. The number of such nodes in the base graph must be greater than or equal to the number of such nodes in the pattern graph.

Finally, the number of neighboring nodes of each of u and v that are not directly connected to nodes in $M(s)$ are compared. The number of such nodes in the base graph must be greater than or equal to the number of such nodes in the pattern graph.

3.4.4 Restore data structure

In VF2 algorithm all the vectors that are used to store data have the following property: If an element is assigned a value in a state s , it will remain assigned in all states descending from s . This property, together with the depth-first strategy of the search is used to avoid the need to store a different copy of the vectors for each state. When the algorithm backtracks, it restores the previous value of the vectors. This was the improvement introduced in the VF2 algorithm. This is illustrated in the figure 3.9. Consider every block to hold the mappings between the base graph and the pattern graph. As can be seen from the figure as one goes down in the tree, a new variable is created for every level, but with restore data structure the same variable is used at every level. When the algorithm has finished traversing all the levels of the search tree, the algorithm without restore data structure will have N variables, whereas one with restore data structure will have only one variable created. Thus reducing the space complexity of the VF2 algorithm to $O(N)$ from $O(N^2)$, which was the case in the VF algorithm.

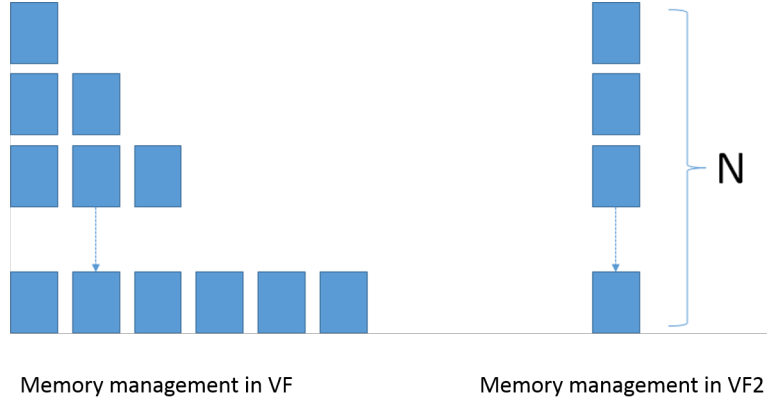


Figure 3.9: Memory cells occupied at each state without and with restore data

3.4.5 Computation Complexity

Computational complexity of the VF2 depends on two factors:

- The time required to calculate the feasibility of every SSR's , computation of the node pair mappings.
- Number of SSR visited.

According to the authors, the former has a computational complexity of $O(N)$. For the latter the authors consider a best case; where only one of the potential mappings are feasible which makes the computation complexity

$O(N)$ and thus making the overall complexity $O(N^2)$. In the worst case, the algorithm has to explore all the states. This can happen when every node is connected to every other node (the base graph is a complete graph) and the graph exhibits strong symmetry. The authors show that the complexity in such a condition is $O(N!)$ and thus making the total complexity $O(N!N)$.

The authors compute the computation complexity in the case of an average graph as the reduction in the visited states compared to that of the worst case condition. This reduction is computed using a parameter called η which represents the probability of an edge being present between 2 distinct nodes of the graph. The authors show that the average reduction in the number of states visited is:

$$R_f(N) = \prod_{i=1}^N 1 - (1 - \eta)^i$$

Variation of R_f for different values of η and the number of nodes are as shown in the figure 3.10. As can be seen in the figure R_f value converges to a constant as N increases depending on the value of η . It can also be noticed that as η decreases the number of states visited for the same value of N also decreases.

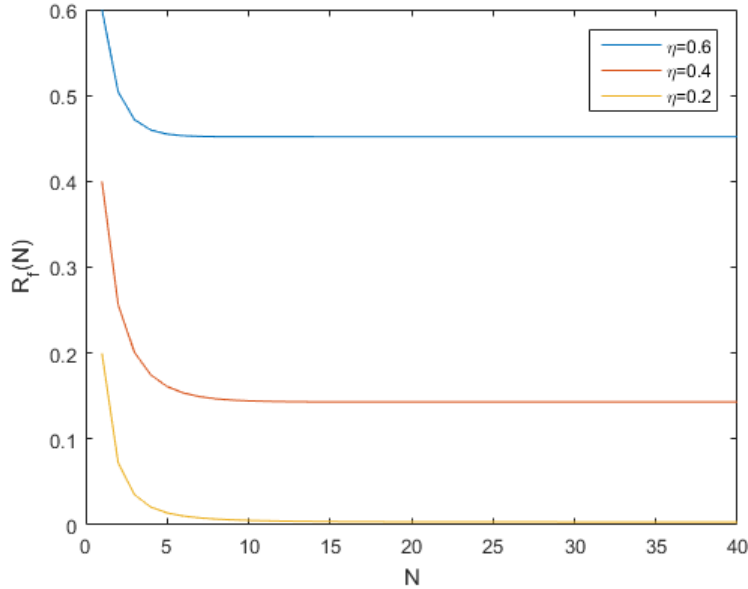


Figure 3.10: Variation of R_f with η and number of nodes N [35]

3.5 Determination of sensor placement

After we obtain the various mappings. We need to decide which out of the various mappings gives the actual placement of the sensors on the grid. To identify the correct mapping we compute *GCS* as explained in section 3.2. We calculate the grid correlation sum for all the mappings obtained and the mappings which give the maximum sum will be the actual placement of the sensors on the grid.

3.5.1 Limitations

Our method can identify the location of the sensors up to rotational symmetry. A graph is said to possess rotational symmetry if there exists a point so that the object when rotated a certain number of degrees (or radians) about said point, looks precisely the same as it did originally[38]. *GCS* remains the same for a sensor arrangement which is rotationally symmetrical to the original sensor arrangements as the adjacency between the sensor nodes is maintained, illustrated in the two arrangements that are shown in the figure 3.11 and 3.12. Therefore when we pick the mappings which have the highest *GCS* we get multiple mappings. These mappings include the actual arrangement and arrangements which are rotationally symmetrical to the actual arrangement.

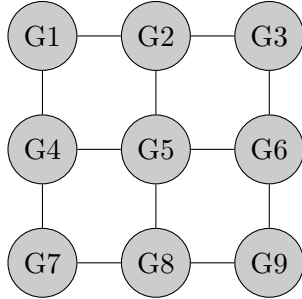


Figure 3.11: Actual arrangement

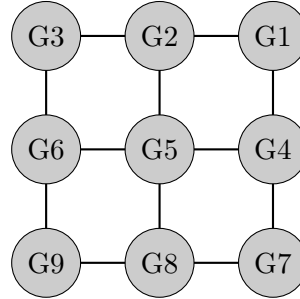


Figure 3.12: Sensors arrangement rotationally symmetric to the actual arrangement

3.5.2 Special case when the grid is $n \times 2$ or $2 \times n$

Consider a $2 \times n$ sensor grid with diagonally opposite nodes connected as shown in the figure 3.13. These grid structure possesses a special case of symmetry. As shown in the figure 3.14 nodes 1 and 2 are interchanged; it is as if the whole structure was rotated with edge (1,2) fixed. The diagonally opposite edges (1,3) in figure 3.13 becomes non diagonal edges in the figure 3.14. To overcome this error we use a *Weighted Grid Adjacency Matrix (WGAM)*

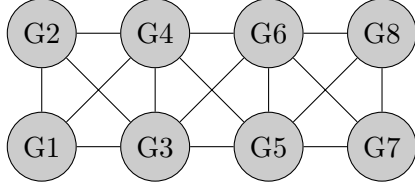


Figure 3.13: Actual arrangement of 2×4 grid.

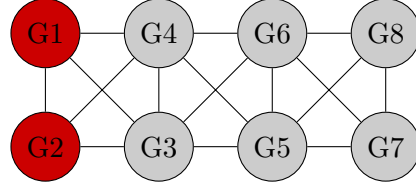


Figure 3.14: Incorrect arrangement of 2×4 grid with the same GCS values.

instead of a binary grid adjacency matrix. We compute ($WGAM$) first by taking the reciprocal of the distance between the nodes which has an edge between them in the GAM and then normalizing it by multiplying with the least distance (d_{min}) that exists between two nodes in the entire grid. All the values in the $WGAM$ lie between 0 and 1. A value close to 1 signifies that the 2 vertices are close to each other and a value close to 0 signifies that the 2 vertices are far away from each other.

$$WGAM_{i,j} = \begin{cases} \frac{d_{min}}{d_{i,j}}, & \text{if } GAM_{i,j} = 1 \\ 0, & \text{otherwise} \end{cases} \quad (3.5)$$

We use $WGAM$ instead of GAM to compute GCS in equation 3.4. The reasoning behind the use of $WGAM$ matrix instead of the GAM is that we hypothesize that the correlation values for the sensor which are closer are higher than the one compared to sensors which are further apart. By assigning weights to the edges in this manner, more importance is given to the edges between the sensors that are close to the each other. Doing so the sensors which are close by contribute more to the GCS . Now if we consider arrangement as shown in the figure 3.13 and 3.14 though their GCS remain the same, when computed using GAM , GCS won't remain the same when GAM is substituted by $WGAM$. The contribution of the correlation between the sensors placed on the nondiagonal edges is more compared to the contribution made by the diagonal edges to GCS . Therefore if we place the non-diagonally located sensors on the diagonals of the grid, GCS decreases. Thus by using a *Weighted Grid Adjacency Matrix* we are able to obtain the mapping of the sensors onto the grid upto rotational symmetry.

3.6 Summary

In this chapter, we describe a method to locate the sensor on the grid making use of sensor data and grid vertices information up-to rotational symmetry. Figure 3.15 gives the summary of steps involved in the form of a flowchart.

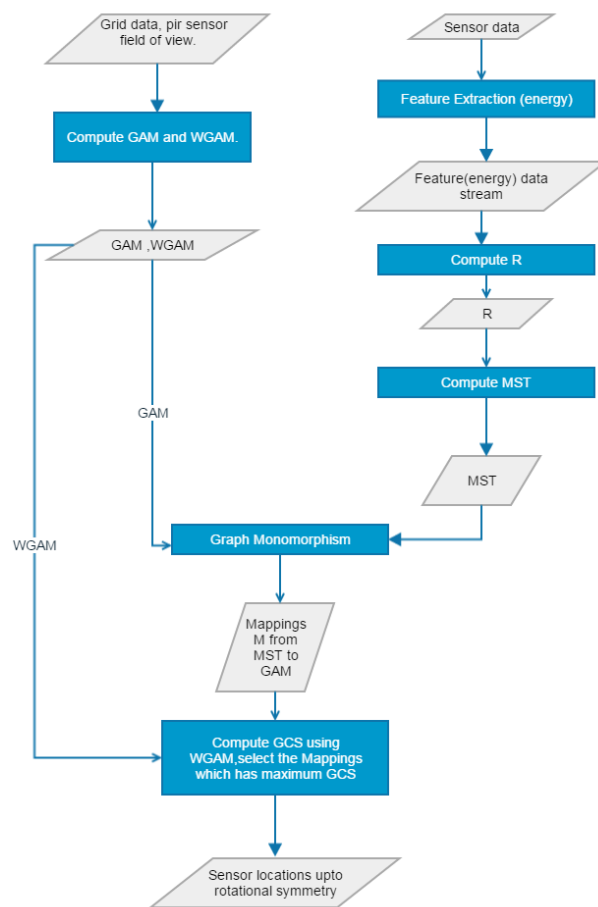


Figure 3.15: Flowchart summarizing the developed method.

Chapter 4

Test Bed

We setup our testbed in an $8m \times 6m$ office space. Sensors are mounted on the ceiling which is at a height of 3m. The sensors are placed 2.5m apart in the horizontal direction and 2.2m apart in the vertical direction. A schematic representation of the lab is as shown in the figure 4.1 with the positions of the sensors marked. We use PIR sensor, EKMB1101112 from Panasonic. The output of the sensor is binary, with 1 indicating occupancy and 0 if the region is unoccupied. We use the sensors with eZ430-RF2500 toolkit which consists of MSP430 micro-controller and CC2500 multi-channel RF transceiver for wireless communication. The testbed uses simpliciTI a TI proprietary low-power RF network protocol. We mount all the 8 sensors on the ceiling of the room as shown in the figure 4.2. All the 8 nodes communicate directly to a centrally located access point which is connected to a laptop, which stores the data.

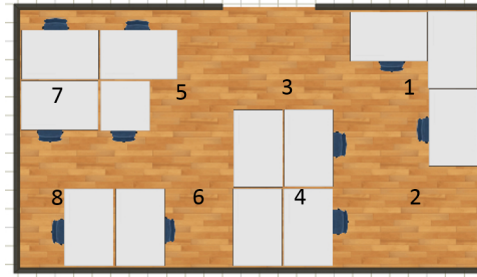


Figure 4.1: Room layout of the testbed.

4.1 Packet Loss

To avoid collision between the transmitted packets CSMA/CA is employed in our testbed. Even though CSMA/CA is employed, during our initial tests we observed packet loss as high as 23% for few nodes as shown in the figure

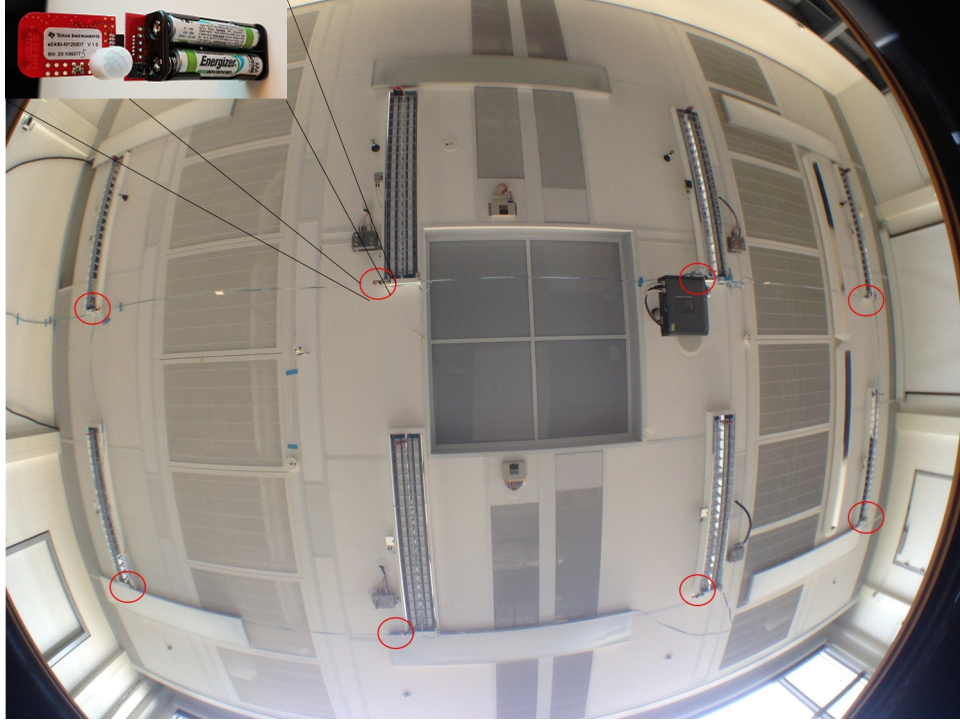
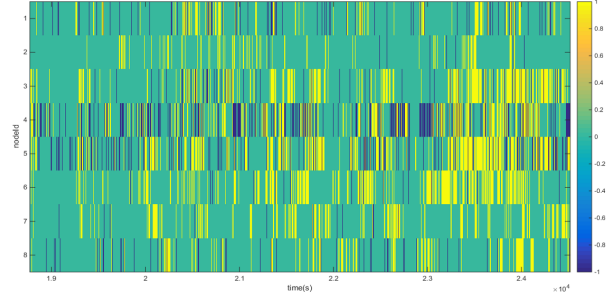


Figure 4.2: Photo of the lab setup with the sensors highlighted in red

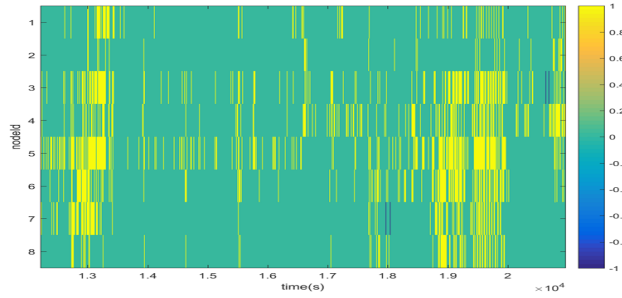
4.3a and table 4.1. To decrease the packet loss we enable acknowledgment. An acknowledgment (ack) is sent from the AP if the packets are received. If no ack is received by a node, the node retransmits its data a maximum of 5 times until an ack is received from the AP. If no ack is received even after 5 retransmission the packet is dropped and the next packet is prepared for transmission. From the figure 4.3b and table 4.1 we can see that there was a decrease in the packet loss per node after ack was enabled.

Node	Packet loss Without ack(%)	Packet loss With ack(%)
1	7.66	0
2	1.01	0
3	5.65	0.32
4	23.67	0
5	14.05	0
6	1.48	0
7	0.96	2.20
8	4.54	0

Table 4.1: Packet loss without and with ack for all the sensor nodes



(a) Data before ack was enabled



(b) Data after ack was enabled

Figure 4.3: Data from the test bed. - 1 indicates the lost data , 1 indicates occupancy, 0 indicates unoccupied space

4.2 Time synchronization

In our testbed, each sensor node has a local clock running on it, with each clock tick corresponding to 1ms. Environment fluctuations, difference in battery levels or imperfection in clock construction can result in one of the clocks ticking faster than the other. To overcome this drift between the clocks we implement one-way synchronization as explained in [39]. In this method, all the local clocks are synchronized to a centrally located node which has a clock running on it. This node transmits the packets periodically after every minute, containing the timestamp corresponding to the local time on the node. The sensor node upon receiving the packets set their local clock to the time specified in the received packet.

To test the time synchronization we place two sensor nodes opposite to each other as shown in the figure 4.4. We sample the sensors at 10ms. To limit the field of view of the sensors we cover the sensor with paper roll. We introduce an obstacle swiftly between the sensor for a short period. This process is repeated 10 times and the worst case time synchronization error is as shown in the figure 4.5. As can be seen in the figure the worst case time synchronization error is approximately equal to 40ms, which is acceptable for our application.



Figure 4.4: Setup to test time synchronization

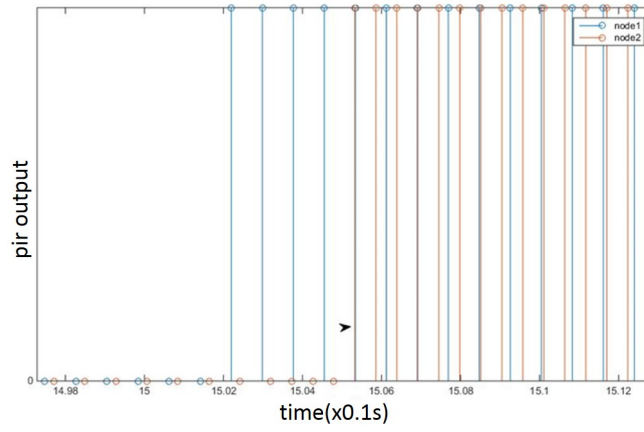


Figure 4.5: Worst case time synchronization error between two nodes

4.3 Packet Structure

In our testbed, we sample our occupancy sensors once every 100ms. Since the data is binary we combine 32 samples and transmit the packet every 3.2s. This decreases the traffic in the sensor network. The transmitted packet is an array of one byte. Consisting of 14 bytes of payload. The payload structure is as shown in the figure 4.6

0	1	2	3	4	5	6	7	8	9	10	11	12	13
Mac id	packet number	start time				end time			data				

Figure 4.6: Packet Structure

- Mac Id - unique identifier for each node.
- Packet number- Keeps track of the packets that are being transmitted from a node. It helps to identify the lost packets as well as repeated packets.
- Start time - 4 byte array corresponding to the time of first PIR sample of the PIR sensor in the packet.
- End time - 4 byte array corresponding to the time of the last sample of the PIR sensor in the packet.
- Data - 32 samples of the PIR sensor.

4.4 Data Collection

Data was collected for a span of 2 months. During the course of the evaluation, the occupants were notified of data gathering, but were never instructed to behave in any particular way or was there any constrained applied on the activity or the number of people in the room.

Chapter 5

Results

In order to verify the proposed method, we test it with data obtained from two different testbeds. First, we apply our method to the data collected from the test bed which is described in chapter 4. Next, we make use of the data released by the WSU smart home project¹ [40]. We use C++ implementation of the VF2 algorithm released by the authors available at [41] for finding the mappings between the grid graph and the MST of correlation Matrix (R).

5.1 Error Metrics

To evaluate the results we define an error metrics as follows:

$$error = \frac{\text{Number of misplaced sensors}}{\text{Number of sensors}} \quad (5.1)$$

5.2 Data Length

An important aspect to know in a data-driven method is, how much of data is required in order to get accurate results? To answer this question, the entire dataset of length T is divided into blocks of time interval t as shown in the figure 5.1. We iteratively increment t until a value beyond which error observed for all the blocks of data of length t is zero. This is done because there can be parts of the data which might give pseudo high correlation value between two nonneighboring nodes or vice versa due to various reasons like noise in the sensor data, large period of inactivity etc. As the data length increases, the effect of the data influencing the false correlation values between the non neighboring sensors diminishes.

¹<http://ailab.wsu.edu/casas/datasets/>

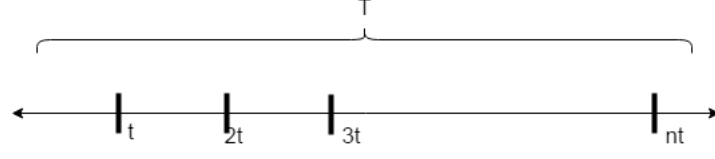


Figure 5.1: Data divided into blocks of period t

5.3 Experimental testbed

As described earlier, the testbed consists of 8 sensors arranged as a 2×4 grid. The field of view of the sensors used in the testbed has a radius of 2.6m. Using the coordinates of the vertex of the grid and the field of view of the sensors we can determine the neighboring vertices for every vertex of the grid. All the vertices of the grid with the field of view marked around them are as shown in the figure 5.2. The co-ordinates of the vertices, calculation of the field of view for the sensor and the computation of GAM is explained in detail in appendix A.

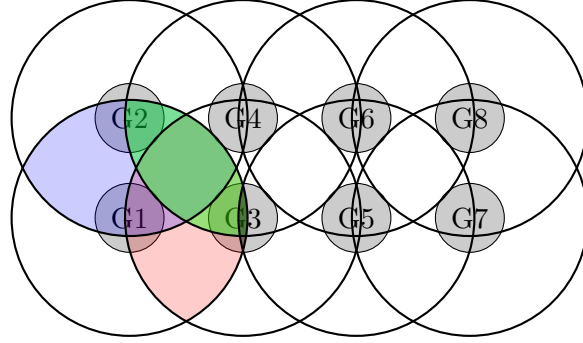


Figure 5.2: Field of view of the sensors on the vertex with the overlapping field of view for sensor 1 highlighted in color

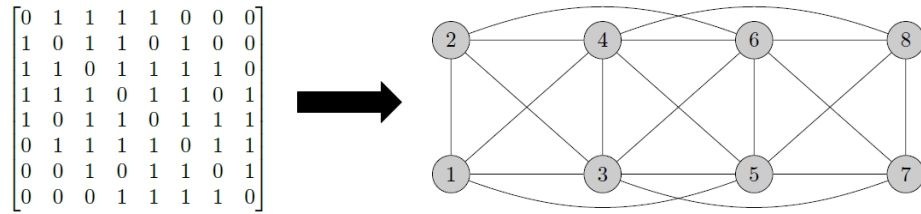
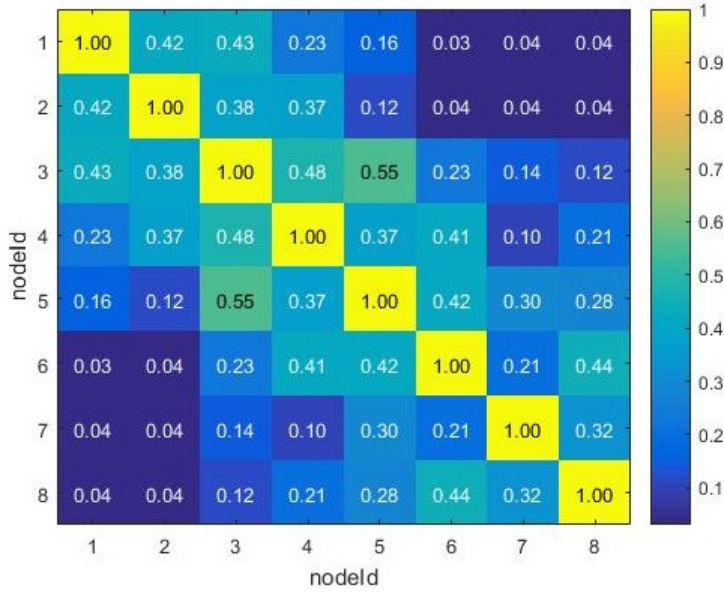


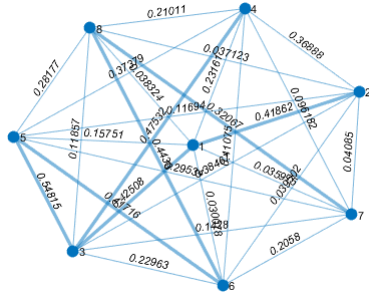
Figure 5.3: Grid adjacency matrix for the grid and its corresponding adjacency graph

5.3.1 Results

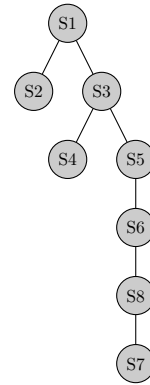
The Grid adjacency matrix for the grid and the corresponding grid graph is as shown in figure 5.3. Computed correlation matrix (R), its corresponding graph $G(V, E, W)$ and MST for one of the dataset are as shown in figure 5.4. As can be seen from figure 5.4a the correlation values between the neighboring sensors are higher than the correlation values between non-neighboring sensors. In the MST we can observe that every sensor is connected to at least one of its neighboring nodes.



(a) R



(b) Graph $G(V, E, W)$ for R , with MST highlighted



(c) Maximum spanning tree of R

Figure 5.4: Correlation Matrix R and it's corresponding graph G and the maximum spanning tree derived from it

Using the method described in section 5.2, we determine that the minimum data length required to compute the sensors location accurately to be 6hrs. Hence we divide our data into blocks of 6hrs length, from which we choose 10 blocks randomly and apply our method to evaluate its performance. 10 different datasets of 6hrs each are used to evaluate the performance of our method. For all the mappings in M we compute the GCS using $WGAM$. The mappings which gave the maximum GCS are as shown in the figure 5.6. These mappings correspond to the actual arrangements of the sensors on the grid and its rotationally symmetrical arrangements. We also evaluate the datasets using brute force search method and we obtain the same set of mappings as the solution that is obtained from our method. The results for both brute force and our method is presented in table 5.1. As can be seen from table we obtain 0% error for all the datasets. Further table 5.1 also provides details about the number of states visited (including all the intermediate states), number of mappings between the MST and the grid, the number of mappings obtained as the solution from the developed method. Figure 5.5 shows the comparison between the search space for the brute force method and our method. The number of states visited and the number of mappings is lesser than number of mappings which has to be checked in case of brute force search.

dataset	Graph Matching method				Brute Force		
	Number of states visited	Mappings	Solution Mapping	Error	Mappings	Solution Mapping	Error
1	11888	2744	4	0	40320	4	0
2	12360	2744	4	0	40320	4	0
3	12144	2664	4	0	40320	4	0
4	11984	2752	4	0	40320	4	0
5	11736	2592	4	0	40320	4	0
6	11888	2744	4	0	40320	4	0
7	11776	2736	4	0	40320	4	0
8	11368	2664	4	0	40320	4	0
9	11752	2656	4	0	40320	4	0
10	11368	2664	4	0	40320	4	0

Table 5.1: Results obtained for experimental testbed.

5.4 WSU Tokyo testbed

To further validate the effectiveness of our method, we use the data from WSU smart workplace testbed[42], a publicly available data set. The testbed called Tokyo is located in a lab, where students perform their normal work routine. Data was collected over a period of 4 months. The testbed consists

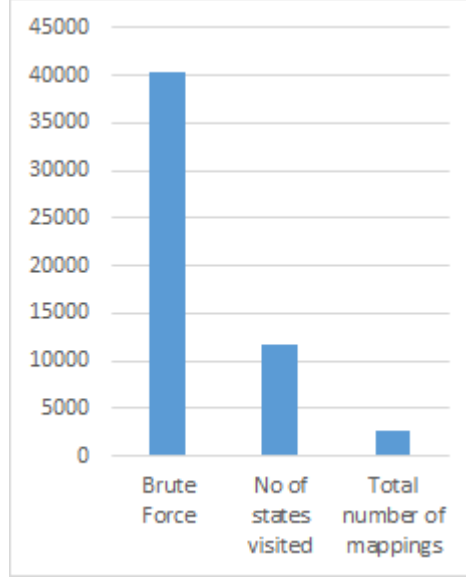


Figure 5.5: Comparing the search space for brute force and our method

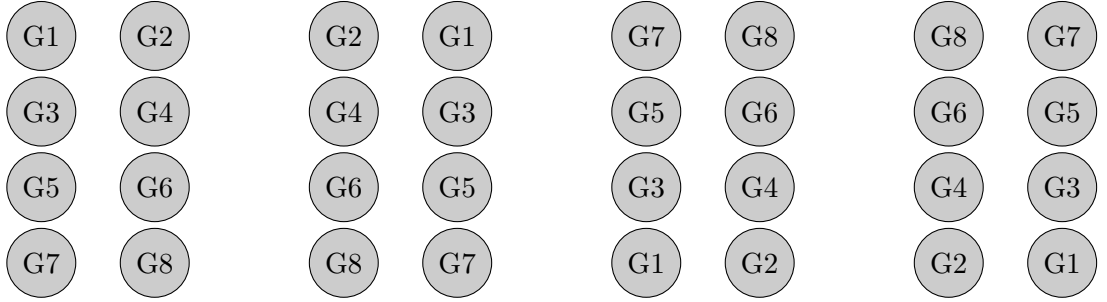


Figure 5.6: Arrangements obtained as solution for the experimental testbed

of 43² motion sensors, placed as shown in the figure 5.7. The sensors field of view is $1.2m \times 1.2m$. In appendix B we provide a detailed explanation about how we obtain the co-ordinates and the grid adjacency matrix for the testbed. The data from the WSU testbed is represented in the form of a four-tuple as shown in table 5.2.

5.4.1 Pre processing

The plot of the dataset for a period of 12hrs is as shown in the figure 5.8. As can be inferred from the figure the dataset mainly consists of parts which are largely inactive. There should be a certain amount of activity happening in the space to observe correlation values between the sensors. Also if no

²Sensor 38 has been ignored as no triggers were found for it throughout the dataset

Date	Time	sensor	state
2008-01-02	08:02:19.58542	M39	ON
2008-01-02	08:02:19.884461	M41	OFF
2008-01-02	08:02:20.297468	M32	ON
2008-01-02	08:02:20.297468	M32	ON
2008-01-02	08:02:20.689425	M31	ON
2008-01-02	08:02:21.957307	M44	OFF
2008-01-02	08:02:22.517275	M39	OFF

Table 5.2: Data structure of the WSU data.

activity is observed in the space it will result in all the sensors having the same values(0) and unfairly influencing the correlation values between the sensors, as correlation value is a measure of similarity between two datasets. For these reasons we filter out the parts of the data where we do not observe any trigger for a sensor for a time period of more than 3hrs. The resulting data is sampled at 100ms and is used to verify our method to find the location of the sensors.

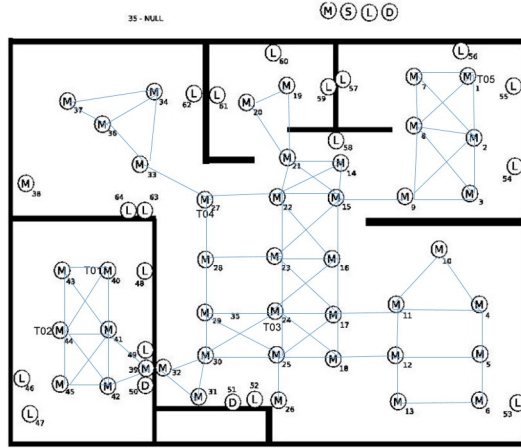


Figure 5.7: Floor plan for WSU CASAS office testbed, named Tokyo with adjacency marked.

5.4.2 Sub layout

Before we use the complete layout of the grid, we carry out our analysis on a 4×3 sub-layout which includes sensors 27, 22, 15, 28, 23, 16, 29, 24, 17, 30, 25, 18. This grid was chosen as it is mentioned in [42] that the region covered by these sensors is more active compared to other regions in the testbed. After processing, the data reduces to a span of 207hrs.

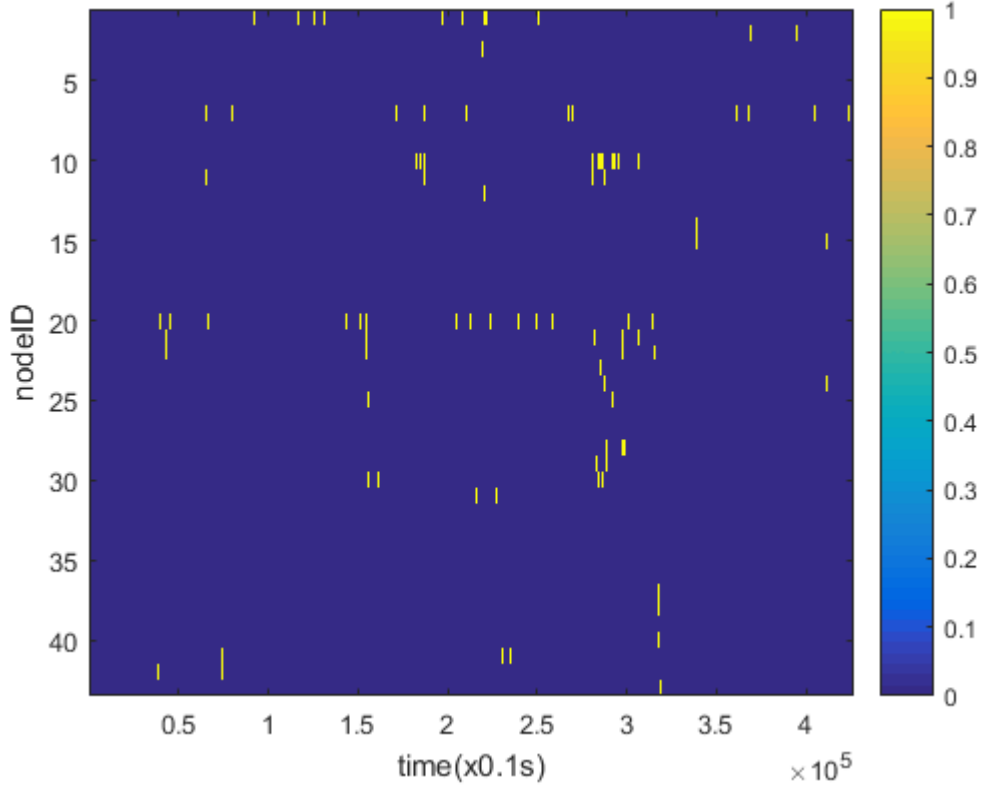


Figure 5.8: Occupancy sensors data with 1 indicating occupancy and 0 indicating non occupancy.

5.4.3 Data Length

By using the method described in section 5.2 we determine that 85hrs of processed data is required to obtain the location of the sensors accurately. Figure 5.9 gives an account of error for every block of data of length t , over the entire length of the data, with t varying from 10 to 100 hours. As it can be seen from the figure, for $t > 85hrs$ the error observed for the blocks of data is 0. Hence to carry out our analysis we use data of length 85hrs. The required length of the data in case of WSU data set is much larger compared to that of our experimental testbed, the main reason can be because of the overlapping area in our experimental testbed is much higher than the overlapping area in Tokyo testbed, and the usage patterns are also different for both the testbed. Our experimental testbed is more active compared to Tokyo testbed.

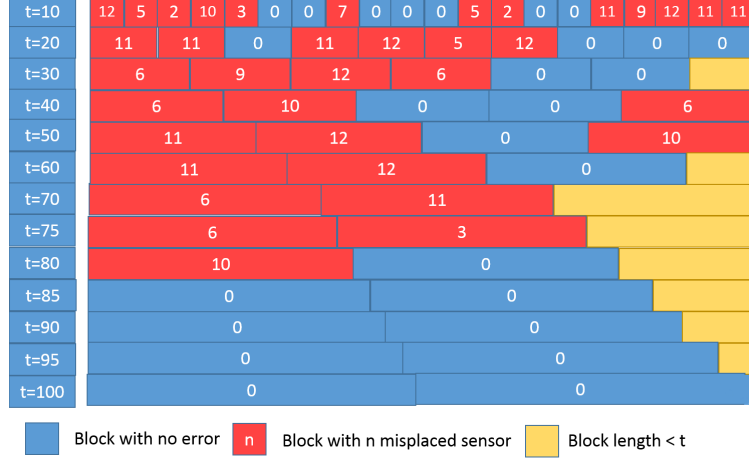


Figure 5.9: Error per block of length t for various values of t across the 200 hours of data for the 4×3 layout.

5.4.4 Results

Data is split into two datasets of 85hrs each. The grid graph is as shown in the figure 5.7. The obtained MST for both the datasets are as shown in figure 5.10. The result obtained from the method is presented in the table 5.3. Both brute force and our method give the same locations of the sensors as the result, but the number of arrangements that had to be checked in case of brute-force is 479001600 whereas with our method the number of mappings that had to be checked was 2120 and 1811 for dataset 1 and 2 respectively. A brute force search for the 12 sensor arrangement required approximately 27hrs to compute the results. Whereas our method needed on an average 10 seconds to compute the results. As can be seen from the table 5.1 and 5.3 the number of mappings obtained is larger in the case of sensor topology of our testbed compared to a 4×3 sub-layout topology of Tokyo testbed, even though the number of sensors is more in the case of the latter. This is because the arrangement in our experimental testbed exhibits rotational symmetry. Due to which for every valid mapping between the MST and grid, the mappings which are rotationally symmetric will also be valid. Thus increasing the number of mappings.

5.4.5 Complete Layout of Tokyo testbed

After validating the 4×3 sub-layout, we apply our method to the complete layout of Tokyo testbed.

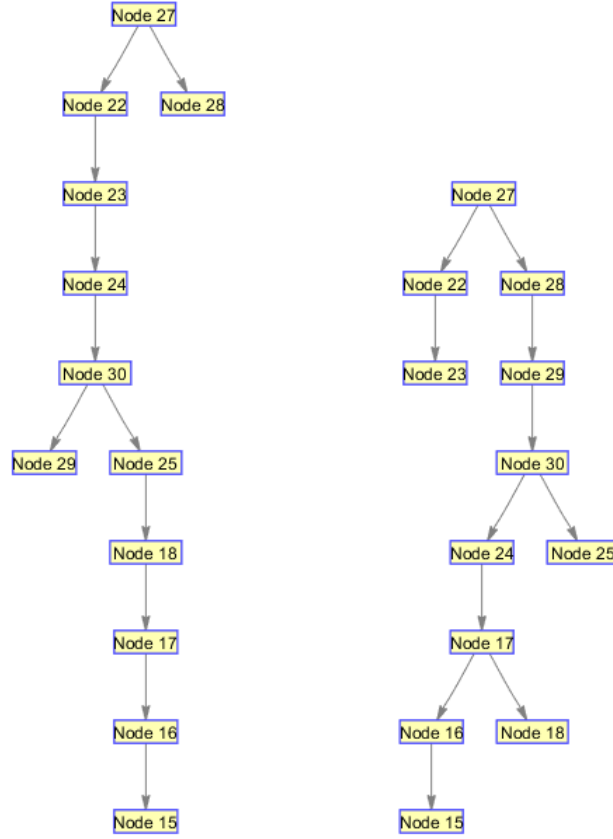


Figure 5.10: MST for the 4×3 layout

Dataset	1		2	
	Brute force	Graph Matching	Brute force	Graph Matching
Mappings	479001600	2120	479001600	1811
states visited	NA	52664	NA	48909
Solutions	1	1	1	1
Error	0	0	0	0

Table 5.3: Results obtained for WSU Tokyo testbed for 4×3 grid

5.4.6 Data length

After applying the processing step considering all the sensors, we are left with 27hrs of data. The main reason for this is that sensor 1 and 4 are highly inactive and very fewer triggers are observed as a result majority of the data had to be filtered out. We perform our analysis on the processed

data.

5.4.7 Results

We use the obtained data to compute the location of the sensors. The MST for the complete layout is as shown in figure 5.11. We obtain two different mappings. Nodes 20 and 19 show rotational symmetry with respect to node 21 so in one arrangement nodes 19 and 20 are mapped to their respective locations in the other mapping nodes 20 and 19 locations are interchanged. As the sensors are equidistant from node 21, the locations cannot be uniquely identified using a *WGAM*. The result is as shown in the table 5.4. We observe an error of 6.9% as the location of three sensors are incorrectly mapped. Brute force search for 43 sensors was not computed as the search space is of the order of 10^{52} , and is computationally prohibitive. While our proposed method was able to compute the sensor location within 414s \approx 6mins.

Dataset	states visited	Solution Mappings	Error(%)
1	70656	2	6.9

Table 5.4: Results for the complete layout of WSU testbed

5.4.8 Understanding the errors

We observe error in the mappings of sensors S34, S36 and S37. Senors S34, S36 and S37 are mapped to the grid locations G36, G37 and G34 respectively. The correlation values between the sensors are as shown in the figure 5.12b and the positions of the sensors obtained from our method is as shown in the figure 5.12c. Since we are computing *GCS* using *WGAM* higher correlation values are placed on the edges which are closer to each other. Among sensors S34, S36 and S37, the maximum correlation is observed between the sensors S34 and S36. The edge with the maximum weight (vertices which are close) is between vertices G36 and G37. Therefore sensors S34 and S36 are to be placed on vertices G36 and G37 and the remaining sensor S37 will be placed on G34. The next step would be to identify which sensor should be placed on which vertex out of the two. This is decided by looking at the correlation values with sensor S37 placed on vertex G34, weight of edge (G36, G34) is greater than the weight of edge (G34, G37). Therefore sensors with higher correlation with S37 will be placed on vertex G36, which in this case would be S34. Thus we get the arrangement computed in figure 5.12c.

One of the reasons for such distribution of correlation can be due to the short duration of the sensor data available. Therefore to verify, we consider only these 3 sensors and apply the preprocessing step for the parent dataset.

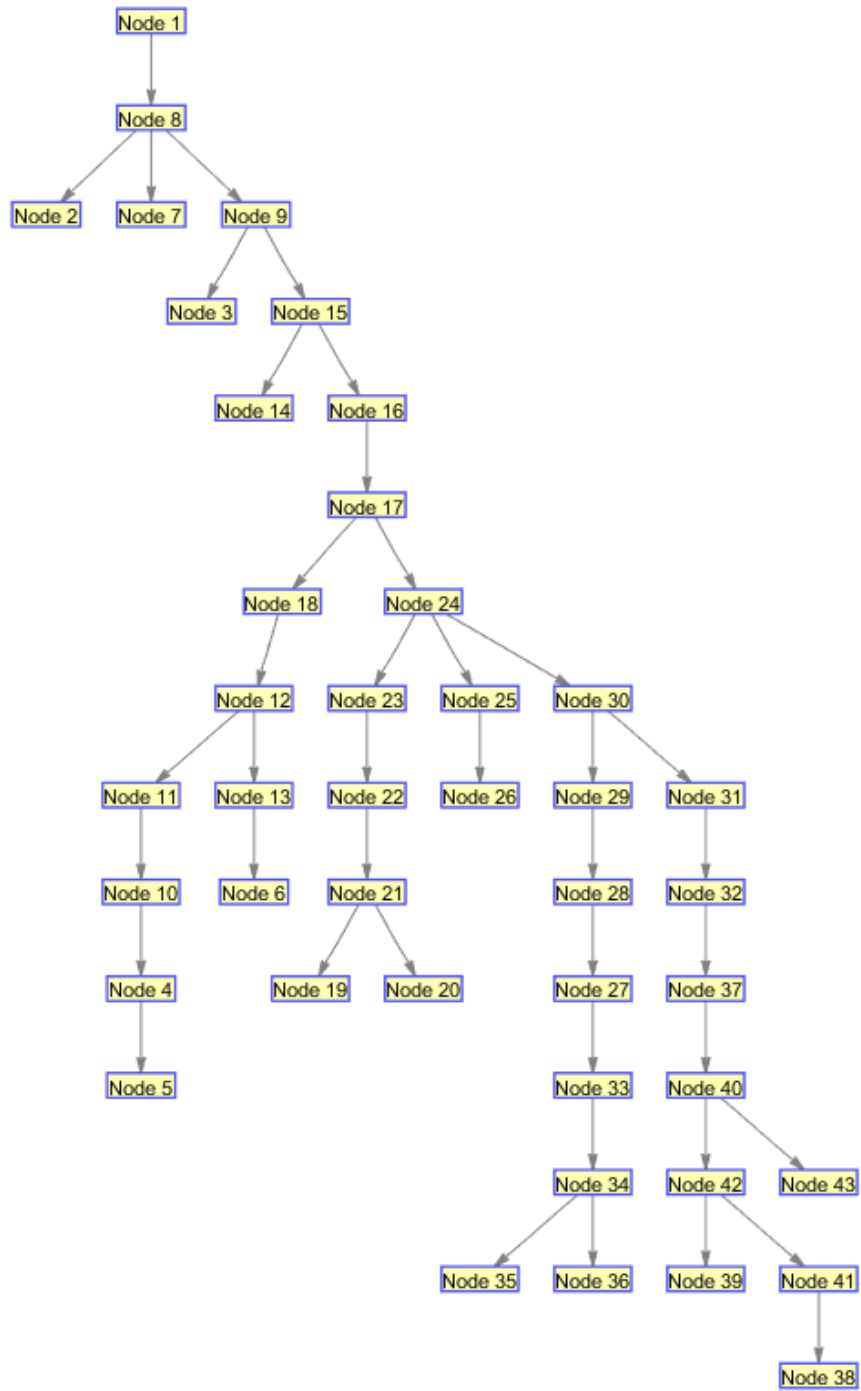


Figure 5.11: MST for the complete layout

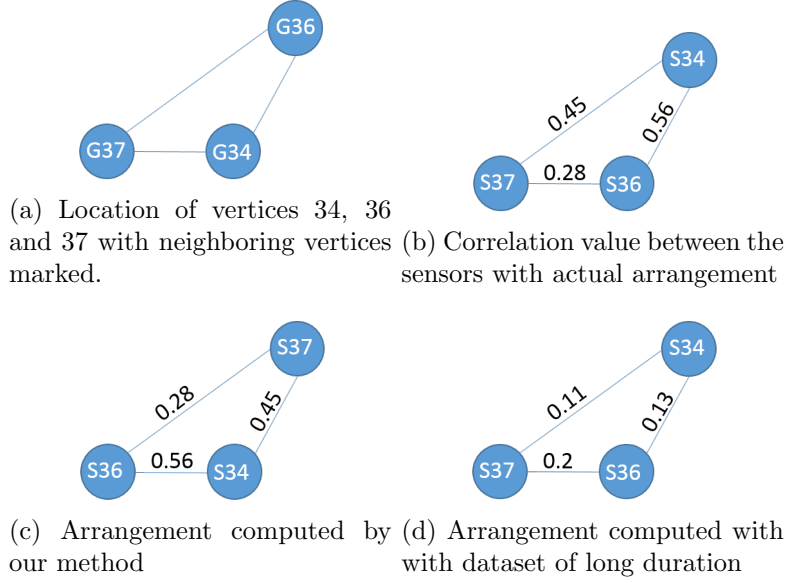


Figure 5.12: Arrangement of sensors and there correlation coefficient

We get resultant data of around 97hrs. Using this data we compute the correlation values. The values obtained are as shown in the figure 5.12d. For which when the *GCS* is calculated using *WGAM*, the maximum value of *GCS* corresponds to the actual arrangement as shown in figure 5.12d. Confirming that the error was caused due to the shortage of data.

5.5 Summary

In this chapter, we present the results obtained for the proposed method. Table 5.5 summarizes the results for our experimental testbed and the Tokyo testbed. As can be seen, the proposed method is able to determine the locations of the sensors with no error for our experimental testbed and sub layout of Tokyo testbed. For the complete layout of the testbed, we obtain an error with respect to the location of three sensors, on further investigation we see that the main reason for the error is due to the shortage of the data. From our analysis, we can conclude that the accuracy of the results mainly depends on the data length and the level of activity happening in the space under consideration. We also see that the amount of data required for analysis becomes more if the overlapping region between the sensors are less.

Testbed	Brute force Mappings	Graph matching mappings	Error(%)
Experimental testbed	40320	2696	0
Tokyo (sublayout)	479001600	1966	0
Tokyo(complete layout)	6.04×10^{52}	70656	6.9

Table 5.5: Search space comparison of brute force and our method

Chapter 6

Conclusions and Future Work

6.1 Conclusions

We present a new data driven method to identify the location meta-data associated with the sensors within a facility. We first identify a feature for the occupancy sensor data and calculate the correlation coefficient for the obtained feature data stream between the sensors. From the correlation values, we build correlation matrix (R) which aids in identifying the neighboring sensor nodes. By computing the MST for R we could identify at least one of the neighbors per sensor node. With the help of the coordinates of the vertices of the grid location, we model the grid as a graph and using the grid graph and the MST we reduce the problem of locating the sensors on the grid to a well-known problem of graph matching. We use the VF2 algorithm, a well known graph matching algorithm to obtain various possible matching between the sensor and the grid. To identify the true arrangement out of these various mapping we define a quantity called *Grid Correlation Sum (GCS)*. With the help of *GCS*, we are able to identify the true arrangement of the sensors up to rotational symmetry.

We validate the method developed with data from two different testbeds. We are able to identify the sensor locations with 0% error for our experimental testbed and 4×3 sub-layout grid for Tokyo testbed. For the entire layout of the Tokyo testbed, we were able to identify the location of all the 43 sensors except 3. During our investigation, we found that the accuracy of the result depend on the available duration of the data. We find that the accuracy increases with the increase in the available duration of the data.

to be submitted to IoTDI in CPS Week

6.2 Future Work

The results are encouraging, going forward we would like to address the following issues in the future:

- Determine the effect of overlapping region on the performance of the algorithm: As could be seen while evaluating the performance of our results with the Tokyo testbed, we could notice that the length of data required to obtain accurate results varied. One of the main factors could be the extent of overlap between the sensors. In the future, we would like to investigate the effect of overlapping region on the performance of our algorithm.
- We are only able to identify the location of the sensors up to rotational symmetry. To overcome rotational symmetry and obtain the exact location of the sensors, extra information about the space is required. For our testbed, we can make use of the location of the door and observe the sensors which are triggered last before a large period of inactivity. This basically represents the last person leaving the room. The sensors which observe the last triggers can be placed on the side of the door and thus eliminating rotational symmetry in one direction. But this method cannot be generalized to all testbeds. Therefore we would like to investigate methods which will be effective to eliminate the problem caused due to rotational symmetry.
- Apply our approach to work with other sensors: In our work, we determine the location of the sensors using the correlation matrix obtained from the occupancy sensor data. In the future, we would like to extend our method to other sensors. The modification that would have to be done to our approach would be to identify the feature for the sensor data stream for which we can compute meaningful correlation values for the sensors.

Bibliography

- [1] Building Automation System. <http://www.buildingautomationsystem.org/Benefits-Of-Building-Automation-Systems.html>. [Online; accessed 22-July-2016].
- [2] J. Gao, J. Ploennigs, and M. Berges. A data-driven meta-data inference framework for building automation systems. In *Proceedings of the 2nd ACM International Conference on Embedded Systems for Energy-Efficient Built Environments*, pages 23–32. ACM, 2015.
- [3] X. Liu and B. Akinci. Requirements and evaluation of standards for integration of sensor data with building information models. *Computing in Civil Engineering*, 2009:10, 2009.
- [4] Center For Climate And Energy Solutions. <http://www.c2es.org/technology/factsheet/LightingEfficiency/>, 2008. [Online; accessed 05-August-2016].
- [5] A. Pandharipande and D. Caicedo. Smart indoor lighting systems with luminaire-based sensing: A review of lighting control approaches. *Energy and Buildings*, 104:369–377, 2015.
- [6] D. Caicedo, S. Li, and A. Pandharipande. Smart lighting control with workspace and ceiling sensors. *Lighting Research and Technology*, 2016.
- [7] N. van de Meughevel, A. Pandharipande, D. Caicedo, and P. Van Den Hof. Distributed lighting control with daylight and occupancy adaptation. *Energy and Buildings*, 75:321–329, 2014.
- [8] D. Hong, J. Ortiz, K. Whitehouse, and D. Culler. Towards automatic spatial verification of sensor placement in buildings. In *Proceedings of the 5th ACM Workshop on Embedded Systems For Energy-Efficient Buildings*, BuildSys’13, pages 13:1–13:8, New York, NY, USA, 2013. ACM.
- [9] B. Akinci, M. Berges, and A. G. Rivera. *Exploratory Study Towards Streamlining the Identification of Sensor Locations Within a Facility*, chapter 226, pages 1820–1827.

- [10] M. Koc, B. Akinci, and M. Bergés. Comparison of linear correlation and a statistical dependency measure for inferring spatial relation of temperature sensors in buildings. In *Proceedings of the 1st ACM Conference on Embedded Systems for Energy-Efficient Buildings*, BuildSys '14, pages 152–155, New York, NY, USA, 2014. ACM.
- [11] J. Lu, Y. T. Shams, and K. Whitehouse. Smart blueprints: How simple sensors can collaboratively map out their own locations in the home. *ACM Trans. Sen. Netw.*, 11(1):19:1–19:23, Aug. 2014.
- [12] C. Ellis, J. Scott, I. Constandache, and M. Hazas. Creating a room connectivity graph of a building from per-room sensor units. In *Proceedings of the Fourth ACM Workshop on Embedded Sensing Systems for Energy-Efficiency in Buildings*, pages 177–183. ACM, 2012.
- [13] S. Müller, A. Helmer, E.-E. Steen, M. Frenken, and A. Hein. Automated clustering of home sensor networks to functional regions for the deduction of presence information for medical applications. *Wohnen–Pflege–Teilhabe–Besser leben durch Technik*, 2014.
- [14] D. Marinakis, G. Dudek, and D. J. Fleet. Learning sensor network topology through monte carlo expectation maximization. In *Proceedings of the 2005 IEEE International Conference on Robotics and Automation*, pages 4581–4587. IEEE, 2005.
- [15] D. Conte, P. Foggia, C. Sansone, and M. Vento. Thirty years of graph matching in pattern recognition. *International journal of pattern recognition and artificial intelligence*, 18(03):265–298, 2004.
- [16] J. Wang, R. K. Ghosh, and S. K. Das. A survey on sensor localization. *Journal of Control Theory and Applications*, 8(1):2–11, 2010.
- [17] N. Bulusu, J. Heidemann, and D. Estrin. Gps-less low-cost outdoor localization for very small devices. *IEEE personal communications*, 7(5):28–34, 2000.
- [18] P. Agrawal, R. K. Ghosh, and S. K. Das. Localization of wireless sensor nodes using proximity information. In *Computer Communications and Networks, 2007. ICCCN 2007. Proceedings of 16th International Conference on*, pages 485–490, Aug 2007.
- [19] Y. Shang, W. Ruml, Y. Zhang, and M. P. Fromherz. Localization from mere connectivity. In *Proceedings of the 4th ACM international symposium on Mobile ad hoc networking & computing*, pages 201–212. ACM, 2003.

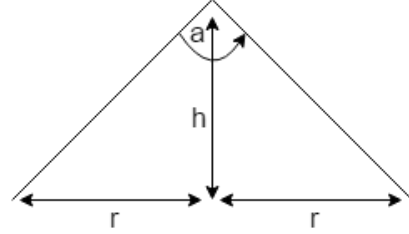
- [20] G. Mao, B. D. Anderson, and B. Fidan. Path loss exponent estimation for wireless sensor network localization. *Computer Networks*, 51(10): 2467–2483, 2007.
- [21] R. L. Moses, D. Krishnamurthy, and R. M. Patterson. A self-localization method for wireless sensor networks. *EURASIP Journal on Advances in Signal Processing*, 2003(4):1–11, 2003.
- [22] J. Xiao, L. Ren, and J. Tan. Research of tdoa based self-localization approach in wireless sensor network. In *2006 IEEE/RSJ International Conference on Intelligent Robots and Systems*, pages 2035–2040, Oct 2006.
- [23] A. Nasipuri and K. Li. A directionality based location discovery scheme for wireless sensor networks. In *Proceedings of the 1st ACM international workshop on Wireless sensor networks and applications*, pages 105–111. ACM, 2002.
- [24] P. Rong and M. L. Sichitiu. Angle of arrival localization for wireless sensor networks. In *2006 3rd annual IEEE communications society on sensor and ad hoc communications and networks*, volume 1, pages 374–382. IEEE, 2006.
- [25] J. Bachrach and C. Taylor. Localization in sensor networks. *Handbook of sensor networks: Algorithms and Architectures*, 1, 2005.
- [26] A. Bhattacharya, D. E. Culler, J. Ortiz, D. Hong, and K. Whitehouse. Enabling portable building applications through automated metadata transformation. Technical report, Technical Report UCB/EECS-2014-159, EECS Department, University of California, Berkeley, 2014.
- [27] A. Schumann, J. Ploennigs, and B. Gorman. Towards automating the deployment of energy saving approaches in buildings. In *Proceedings of the 1st ACM Conference on Embedded Systems for Energy-Efficient Buildings*, BuildSys ’14, pages 164–167, New York, NY, USA, 2014. ACM.
- [28] J.-P. Calbimonte, Z. Yan, H. Jeung, O. Corcho, and K. Aberer. Deriving semantic sensor metadata from raw measurements. In *Proceedings of the 5th International Conference on Semantic Sensor Networks-Volume 904*, pages 33–48. CEUR-WS. org, 2012.
- [29] J. R. Ullmann. An algorithm for subgraph isomorphism. *J. ACM*, 23(1):31–42, Jan. 1976.
- [30] D. E. Ghahraman, A. K. C. Wong, and T. Au. Graph optimal monomorphism algorithms. *IEEE Transactions on Systems, Man, and Cybernetics*, 10(4):181–188, April 1980.

- [31] L. P. Cordella, P. Foggia, C. Sansone, and M. Vento. Fast graph matching for detecting cad image components. In *Pattern Recognition, 2000. Proceedings. 15th International Conference on*, volume 2, pages 1034–1037 vol.2, 2000.
- [32] L. P. Cordella, P. Foggia, C. Sansone, and M. Vento. An improved algorithm for matching large graphs.
- [33] L. Bao and S. S. Intille. Activity recognition from user-annotated acceleration data. In *International Conference on Pervasive Computing*, pages 1–17. Springer, 2004.
- [34] R. C. Prim. Shortest connection networks and some generalizations. *Bell System Technical Journal*, 36(6):1389–1401, 1957.
- [35] L. P. Cordella, P. Foggia, C. Sansone, and M. Vento. Performance evaluation of the vf graph matching algorithm. In *Image Analysis and Processing, 1999. Proceedings. International Conference on*, pages 1172–1177. IEEE, 1999.
- [36] J. Singler. Graph isomorphism implementation in leda 5.1. Technical report, Technical Report, 2005.
- [37] M. R. Garey and D. S. Johnson. *Computers and Intractability: A Guide to the Theory of NP-Completeness*. W. H. Freeman & Co., New York, NY, USA, 1979.
- [38] C. Stover. Rotational symmetry. From MathWorld—A Wolfram Web Resource. <http://mathworld.wolfram.com/RotationalSymmetry.html>. Last visited on 10/8/2016.
- [39] B. Kerkez and K. Pister. Adaptive time synchronization and frequency channel hopping for wireless sensor networks. *Electrical Engineering and Computer Sciences University of California at Berkeley*, 56, 2012.
- [40] D. J. Cook and M. Schmitter-Edgecombe. Assessing the quality of activities in a smart environment. *Methods of information in medicine*, 48(5):480, 2009.
- [41] VF Library. <http://mivia.unisa.it/datasets/graph-database/vflib/>, 2008. [Online; accessed 22-July-2016].
- [42] D. J. Cook, A. Crandall, G. Singla, and B. Thomas. Detection of social interaction in smart spaces. *Cybernetics and Systems: An International Journal*, 41(2):90–104, 2010.
- [43] A. Crandall and D. Cook. Tracking systems for multiple smart home residents. *Human Behavior Recognition Technologies: Intelligent Applications for Monitoring and Security*, pages 111–129, 2011.

Appendix A

Experimental Testbed

The coordinates of the vertices are as given in the table [A.1](#). We use EKMB1101112 PIR sensors from Panasonic, with detection angle of 82° . PIR nodes are placed on the ceiling which is at a height of 3m. From this information we can compute the radius of the field of view of the PIR sensors as follows:



$$\begin{aligned}h &= 3m, a = 82^\circ \\r &= h \cdot \tan\left(\frac{a}{2}\right) \\r &= 2.6m\end{aligned}$$

The distances between all the sensor nodes are represented in a matrix form and is as given in the table [A.2](#). The radius of the PIR sensor is 2.6m thus any 2 sensors located less than 5.2m($2r$) apart are considered

vetrex	x	y
1	0	0
2	0	2.2
3	2.5	0
4	2.5	2.2
5	5	0
6	5	2.2
7	7.5	0
8	7.5	2.2

Table A.1: Coordinates of the vertices of the sensor network

vertices	1	2	3	4	5	6	7	8
1	0.00	2.00	2.50	3.20	5.00	5.39	7.50	7.76
2	2.00	0.00	3.20	2.50	5.39	5.00	7.76	7.50
3	2.50	3.20	0.00	2.00	2.50	3.20	5.00	5.39
4	3.20	2.50	2.00	0.00	3.20	2.50	5.39	5.00
5	5.00	5.39	2.50	3.20	0.00	2.00	2.50	3.20
6	5.39	5.00	3.20	2.50	2.00	0.00	3.20	2.50
7	7.50	7.76	5.00	5.39	2.50	3.20	0.00	2.00
8	7.76	7.50	5.39	5.00	3.20	2.50	2.00	0.00

Table A.2: Euclidean distances between vertices

vertices	1	2	3	4	5	6	7	8
1	0	1	1	1	1	0	0	0
2	1	0	1	1	0	1	0	0
3	1	1	0	1	1	1	1	0
4	1	1	1	0	1	1	0	1
5	1	0	1	1	0	1	1	1
6	0	1	1	1	1	0	1	1
7	0	0	1	0	1	1	0	1
8	0	0	0	1	1	1	1	0

Table A.3: Adjacency matrix

neighboring sensors. The adjacency matrix is obtained as shown in the table [A.3](#)

Appendix B

Tokyo Testbed

The coordinates of the vertices in Tokyo testbed are not explicitly specified. The information available are the room layout map as shown in figure 5.7, pir sensor field of view given as $1.2m \times 1.2m$ and the average distance between the sensors as 1.2m in [43]. Assuming that the given layout is to scale and the distance between sensors 27 and 22 as 1.2m, the coordinates of all the sensors are computed. We start by placing the origin(0,0) at vertex 30 and measure the distance of every vertex from the x and y axis which gives the coordinates of all vertices on the grid. The coordinates thus obtained are as shown in the table B.1. No triggers was found for sensor 38 in the dataset, hence sensor 38 is not considered.

Adjacency between two vertices is determined if the square of dimension 1.2×1.2 drawn around the vertices have any overlap. If there is any overlap then the vertices are considered neighbors.

vertices	x	y	vertices	x	y
1	4.40	5.60	23	1.20	2.00
2	4.40	4.00	24	1.20	0.80
3	4.40	3.20	25	1.20	0.00
4	4.80	1.20	26	1.20	-1.20
5	4.80	0.00	27	0.00	3.20
6	4.80	-1.20	28	0.00	2.00
7	3.40	5.60	29	0.00	0.80
8	3.40	4.40	30	0.00	0.00
9	3.40	3.20	31	0.00	-1.20
10	3.90	2.00	32	-1.20	-0.40
11	3.60	1.20	33	-0.60	3.80
12	3.60	0.00	34	-0.60	5.00
13	3.60	-1.20	36	-1.40	4.40
14	2.40	3.60	37	-1.80	4.80
15	2.40	3.20	39	-1.40	-0.20
16	2.40	2.00	40	-2.20	1.88
17	2.40	0.80	41	-2.20	0.68
18	2.40	0.00	42	-2.20	-0.52
19	1.20	4.80	43	-3.40	1.88
20	0.60	4.64	44	-3.40	0.68
21	1.20	3.60	45	-3.40	-0.52
22	1.20	3.20			

Table B.1: Coordinates obtained for the vertices