```
15, 5, 10, 11, 9, 18,28 (2-3 Tree)
delet (15), injest 21,12, delete 5,
  ///2-3 tree implementation
   #include<stdio.h>
   #include<stdlib.h>
   typedef struct Node
   int key[3];
   int NKeys;
   struct Node *child[4];
   struct Node *Parent;
   }node;
   node *root=NULL;
    node *create()
    node *root;
    root=NULL;
    return(root);
    */
    node *NodeCreate(int key,node *Left, node *Right, node *P)
    {
            node *Node;
            Node=(node *)malloc(sizeof(node));
            Node->key[0]=key;
            Node->key[1]=32767;
            Node->key[2]=32767;
            Node->child[0]=Left;
            Node->child[1]=Right;
            Node->child[2]=NULL;
            Node->child[3]=NULL;
            Node->Parent=P;
            Node->NKeys=1;
            return(Node);
     }
     node *Nodesplit(node *Node)
             int i;
             node *New1,*New2;
             if(Node==root)
             New1=NodeCreate(Node->key[2],Node->child[2],Node->child[3],NULL);
             New2=NodeCreate(Node->key[1],Node,New1,NULL);
             New1->Parent=New2;
             Node->Parent=New2;
              Node->NKeys=1;
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Node->key[1]=32767;
Node->key[2]=32767;
Node->child[2]=NULL;
Node->child[3]=NULL;
root=New2;
return(New2);
if(Node==Node->Parent->child[0])
\label{lem:new1} New1=NodeCreate(Node->key[2],Node->child[2],Node->child[3],Node->Parent);
Node->Parent->key[2]=Node->Parent->key[1];
Node->Parent->key[1]=Node->Parent->key[0];
Node->Parent->key[0]=Node->key[1];
Node->Parent->child[3]=Node->Parent->child[2];
Node->Parent->child[2]=Node->Parent->child[1];
Node->Parent->child[1]=New1;
Node->key[1]=32767;
Node->key[2]=32767;
Node->child[2]=NULL;
Node->child[3]=NULL;
Node->NKeys=1;
Node->Parent->NKeys=Node->Parent->NKeys+1;
return(Node->Parent);
else if(Node==Node->Parent->child[1])
New1=NodeCreate(Node->key[2],Node->child[2],Node->child[3],Node->Parent);
Node->Parent->key[2]=Node->Parent->key[1];
Node->Parent->key[1]=Node->key[1];
Node->Parent->child[3]=Node->Parent->child[2];
Node->Parent->child[2]=New1;
Node->key[1]=32767;
Node->key[2]=32767;
Node->child[2]=NULL;
Node->child[3]=NULL;
Node->NKeys=1;
Node->Parent->NKeys=Node->Parent->NKeys+1;
return(Node->Parent);
else
New1=NodeCreate(Node->key[2],Node->child[2],Node->child[3],Node->Parent);
 Node->Parent->key[2]=Node->key[1];
 Node->Parent->child[3]=New1;
 Node->Parent->child[2]=Node;
 Node->key[1]=32767;
 Node->key[2]=32767;
 Node->child[2]=NULL;
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Node->child[3]=NULL;
        Node->NKeys=1;
       Node->Parent->NKeys=Node->Parent->NKeys+1;
        return(Node->Parent);
}
node *Insert(node *Node, int key)
       int i;
        if(Node==NULL)
               root=NodeCreate(key,NULL, NULL, NULL);
               return(root);
        if(Node->child[0]!=NULL)
               if(Node->key[0]>key)
                       Node=Insert(Node->child[0],key);
               else if(Node->key[0]<key && Node->key[1]>key)
                       Node=Insert(Node->child[1],key);
                else
                       Node=Insert(Node->child[2],key);
                }
        else
                if(Node->key[0]>key)
                        for(i=Node->NKeys;i>0;i--)
                                Node->key[i]=Node->key[i-1];
                        Node->key[0]=key;
                else if(Node->key[0]<key && Node->key[1]>key)
                         Node->key[2]=Node->key[1];
                         Node->key[1]=key;
                 else Node->key[2]=key;
                 Node->NKeys=Node->NKeys+1;
  return(Node);
  }
  void InsertElement(int key)
          node *Node;
          Node=Insert(root,key);
          while(Node->NKeys > 2)
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Node=Nodesplit(Node);
node *Search(node *Node, int key)
if(Node==NULL)
       return(NULL);
else
       if(Node->key[0]>=key)
              if(Node->key[0]==key)
                      return(Node);
               else Node=Search(Node->child[0],key);
       else if(Node->key[0]<key&&Node->key[1]>=key)
               if(Node->key[1]==key)
                      return(Node);
               else Node=Search(Node->child[1],key);
       else
               Node=Search(Node->child[2],key);
       return(Node);
}
node *LeftMostNode(node *Node)
while(Node->child[0]!=NULL)
       Node=Node->child[0];
return(Node);
}
void MergeNode(node *Node)
node *Node1;
       if(Node==Node->Parent->child[0])
               {
                      Node1=Node->Parent->child[1];
                      Node->key[0]=Node->Parent->key[0];
                      Node->Parent->NKeys=Node->Parent->NKeys-1;
                      Node->key[1]=Node1->key[0];
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Node->key[2]=Node1->key[1];
              if(Node->child[0]!=NULL)
              Node->child[1]=Node1->child[0];
              Node->child[2]=Node1->child[1];
              Node->child[3]=Node1->child[2];
              if(Node->Parent->child[1]->NKeys==2)
                     Node->NKeys=3;
              else Node->NKeys=2;
              Node->Parent->child[1]=Node->Parent->child[2];
              Node->Parent->child[2]=Node->Parent->child[3];
              Node->Parent->key[0]=Node->Parent->key[1];
              Node->Parent->key[1]=Node->Parent->key[2];
else if(Node==Node->Parent->child[1])
              Node=Node->Parent->child[0];
               Node1=Node->Parent->child[1];
              Node->key[Node->NKeys]=Node->Parent->key[0];
               Node->NKeys=Node->NKeys+1;
               Node->Parent->key[0]=Node->Parent->key[1];
               Node->Parent->key[1]=Node->Parent->key[2];
               Node->Parent->NKeys=Node->Parent->NKeys-1;
               Node->Parent->child[1]=Node->Parent->child[2];
               Node->Parent->child[2]=Node->Parent->child[3];
               if(Node1->child[0]!=NULL)
                      Node->child[Node->NKeys+1]=Node1->child[0];
else if(Node==Node->Parent->child[2])
               Node=Node->Parent->child[1];
               Node1=Node->Parent->child[2];
               Node->key[Node->NKeys]=Node->Parent->key[1];
               Node->NKeys=Node->NKeys+1;
                Node->Parent->key[1]=Node->Parent->key[2];
                Node->Parent->NKeys=Node->Parent->NKeys-1;
                Node->Parent->child[2]=Node->Parent->child[3];
                if(Node1->child[0]!=NULL)
                       Node->child[Node->NKeys+1]=Node1->child[0];
 free(Node1);
 if(Node->NKeys>2)
         Nodesplit(Node);
 else if(Node->Parent->NKeys==0)
                if(Node->Parent==root)
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Node1==root;
                              root=Node;
                              Node->Parent==NULL;
                      else MergeNode(Node->Parent);
               }
}
void Delete(int key)
node *Node, *LMNode;
Node=Search(root,key);
int flag=0;
if(Node->key[0]==key)
       if(Node->child[1]!=NULL)
               flag=1;
               LMNode=LeftMostNode(Node->child[1]);
               Node->key[0]=LMNode->key[0];
       else
               Node->key[0]=Node->key[1];
               Node->key[1]=Node->key[2];
               Node->NKeys=Node->NKeys-1;
       }
else
       if(Node->child[1]!=NULL)
              flag=1;
              LMNode=LeftMostNode(Node->child[2]);
              Node->key[1]=LMNode->key[0];
              }
       else
              Node->key[1]=Node->key[2];
              Node->NKeys=Node->NKeys-1;
if(flag==1)
       if(LMNode->NKeys==2)
              LMNode->key[0]=LMNode->key[1];
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```
LMNode->key[1]=LMNode->key[2];
              LMNode->NKeys=1;
       else
               LMNode->key[0]=LMNode->key[1];
               LMNode->NKeys=0;
               MergeNode(LMNode);
if(Node->NKeys==0)
       MergeNode(Node);
void traversal(node *myNode)
    int i;
    if (myNode!=NULL)
         for (i = 0; i < myNode->NKeys; i++)
                traversal(myNode->child[i]);
             printf("%d, ", myNode->key[i]);
                traversal(myNode->child[i]);
        }
        }
void main()
 InsertElement(15);
 InsertElement(5);
 InsertElement(10);
 InsertElement(11);
 InsertElement(9);
 traversal(root);
 printf("\n");
 InsertElement(18);
 InsertElement(28);
 Delete(15);
 traversal(root);
 printf("\n");
 InsertElement(21);
 InsertElement(12);
 Delete(5);
 traversal(root);
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printf("\n");
}

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