

BPE, WordPiece Numerical Examples

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Subword Tokenization

- BPE and WordPiece
- Detailed Numerical Walkthrough

Corpus Used

- low (5)
- lower (2)
- newest (6)
- widest (3)

Why Subword Tokenization?

- Controls vocabulary size
- Handles unseen or out of vocabulary words
- Balances granularity

BPE: Initial Setup

- Split words into characters + `</w>`
- Initial vocab size = 11

BPE Pair Frequencies (Iter 1)

- $(e,s)=9, (s,t)=9, (t,</w>)=9$
- $(l,o)=7, (o,w)=7, (w,e)=8$

BPE Merge 1

- Merge (e,s) \rightarrow es
- Vocab = 12

BPE Merge 2

- Merge (es,t) \rightarrow est
- Vocab = 13

BPE Merge 3

- Merge (est,</w>) → est</w>
- Vocab = 14

BPE Merge 4 & 5

- $(l,o) \rightarrow lo$
- $(lo,w) \rightarrow low$
- Vocab = 16

BPE Merge 6–9

- we, nwe, newest</w>, wi
- Stop at vocab = 20

Final BPE Vocabulary

- 11 base symbols + 9 merges = 20

WordPiece: Initial Setup

- Uses continuation marker ##
- Initial vocab size = 11

Initial WordPiece Tokenization

- low → l ##o ##w
- lower → l ##o ##w ##e ##r
- newest → n ##e ##w ##e ##s ##t
- widest → w ##i ##d ##e ##s ##t

WordPiece Token Frequencies

- $l=7, n=6, w=3$
- $##o=7, ##w=13, ##e=17$
- $##s=9, ##t=9, ##i=3, ##d=3$

WordPiece Scoring Formula

- $\text{score}(x,y) = \text{count}(xy) / (\text{count}(x) * \text{count}(y))$

WordPiece Merge 1

- $l + \#\#o \rightarrow lo$ (highest score)
- Vocab = 12

WordPiece Merge 2

- $##s + ##t \rightarrow ##st$
- Vocab = 13

WordPiece Merge 3

- lo + ##w \rightarrow low
- Vocab = 14

WordPiece Merge 4

- $##e + ##st \rightarrow ##est$
- Vocab = 15

WordPiece Merge 5

- $w + \#\#i \rightarrow wi$
- Vocab = 16

WordPiece Merge 6

- $wi + \#\#d \rightarrow wid$
- Vocab = 17

WordPiece Merge 7

- `wid + ##est` → `widest`
- Vocab = 18

WordPiece Merge 8

- $n + \#\#e \rightarrow ne$
- Vocab = 19

WordPiece Merge 9 (Stop)

- $ne + \#\#w \rightarrow new$
- $Vocab = 20 \rightarrow STOP$

Final WordPiece Vocabulary

- Base tokens + 9 learned WordPieces = 20

BPE vs WordPiece

- BPE → Frequency based
- WordPiece → Likelihood based
- Both stop at vocab limit

Conclusion

- BPE favors frequent patterns
- WordPiece favors informative patterns