

# BPE, WordPiece Numerical Examples

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# Subword Tokenization

- BPE and WordPiece
- Detailed Numerical Walkthrough

# Corpus Used

- low (5)
- lower (2)
- newest (6)
- widest (3)

# Why Subword Tokenization?

- Controls vocabulary size
- Handles unseen or out of vocabulary words
- Balances granularity

# BPE: Initial Setup

- Split words into characters + </w>
- Initial vocab size = 11

# BPE Pair Frequencies (Iter 1)

- $(e,s)=9$ ,  $(s,t)=9$ ,  $(t,</w>)=9$
- $(l,o)=7$ ,  $(o,w)=7$ ,  $(w,e)=8$

# BPE Merge 1

- Merge (e,s) → es
- Vocab = 12

# BPE Merge 2

- Merge (es,t) → est
- Vocab = 13

# BPE Merge 3

- Merge (est,</w>) → est</w>
- Vocab = 14

# BPE Merge 4 & 5

- (l,o) → lo
- (lo,w) → low
- Vocab = 16

# BPE Merge 6–9

- we, nwe, newest</w>, wi
- Stop at vocab = 20

# Final BPE Vocabulary

- 11 base symbols + 9 merges = 20

# WordPiece: Initial Setup

- Uses continuation marker ##
- Initial vocab size = 11

# Initial WordPiece Tokenization

- low → l ##o ##w
- lower → l ##o ##w ##e ##r
- newest → n ##e ##w ##e ##s ##t
- widest → w ##i ##d ##e ##s ##t

# WordPiece Token Frequencies

- $|=7, n=6, w=3$
- $\#\#\text{o}=7, \#\#\text{w}=13, \#\#\text{e}=17$
- $\#\#\text{s}=9, \#\#\text{t}=9, \#\#\text{i}=3, \#\#\text{d}=3$

# WordPiece Scoring Formula

- $\text{score}(x,y) = \text{count}(xy) / (\text{count}(x) * \text{count}(y))$

# WordPiece Merge 1

- I + ##o → Io (highest score)
- Vocab = 12

# WordPiece Merge 2

- $\#\#s + \#\#t \rightarrow \#\#st$
- Vocab = 13

# WordPiece Merge 3

- lo + ##w → low
- Vocab = 14

# WordPiece Merge 4

- ##e + ##st → ##est
- Vocab = 15

# WordPiece Merge 5

- $w + \#\#i \rightarrow wi$
- Vocab = 16

# WordPiece Merge 6

- $wi + \#\#d \rightarrow wid$
- Vocab = 17

# WordPiece Merge 7

- wid + ##est → widest
- Vocab = 18

# WordPiece Merge 8

- n + ##e → ne
- Vocab = 19

# WordPiece Merge 9 (Stop)

- ne + ##w → new
- Vocab = 20 → STOP

# Final WordPiece Vocabulary

- Base tokens + 9 learned WordPieces = 20

# BPE vs WordPiece

- BPE → Frequency based
- WordPiece → Likelihood based
- Both stop at vocab limit

# Conclusion

- BPE favors frequent patterns
- WordPiece favors informative patterns