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# QuickSort - GeeksforGeeks

11-14 minutes

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Like [Merge Sort](#), QuickSort is a Divide and Conquer algorithm. It picks an element as pivot and partitions the given array around the picked pivot. There are many different versions of quickSort that pick pivot in different ways.

1. Always pick first element as pivot.
2. Always pick last element as pivot (implemented below)
3. Pick a random element as pivot.
4. Pick median as pivot.

The key process in quickSort is partition(). Target of partitions is, given an array and an element x of array as pivot, put x at its correct position in sorted array and put all smaller elements (smaller than x) before x, and put all greater elements (greater than x) after x. All this should be done in linear time.

## Pseudo Code for recursive QuickSort function :

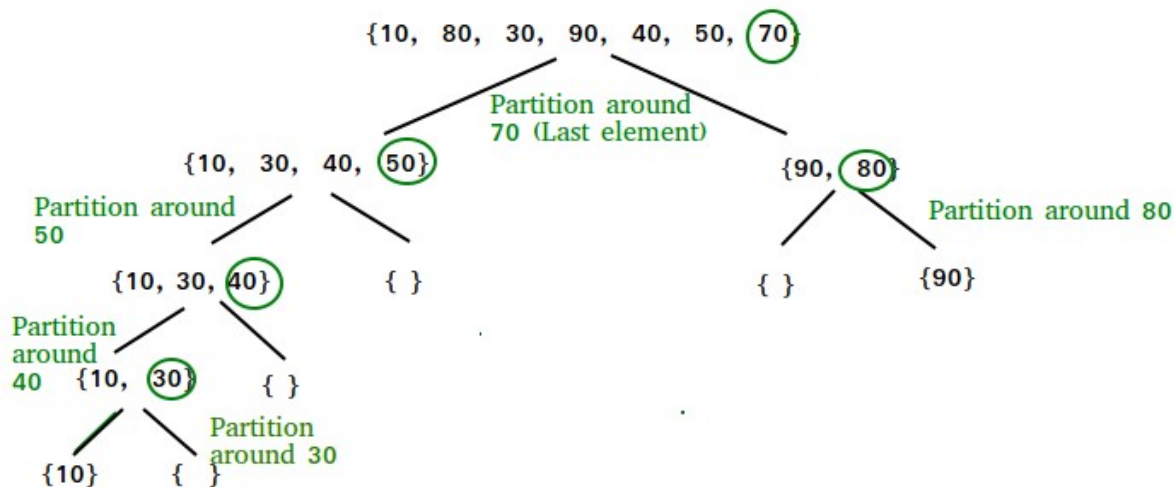
```
/* low --> Starting index, high --> Ending
index */
quickSort(arr[], low, high)
{
    if (low < high)
    {
        /* pi is partitioning index, arr[pi] is
now
        at right place */
```

```

    pi = partition(arr, low, high);

    quickSort(arr, low, pi - 1); // Before pi
    quickSort(arr, pi + 1, high); // After pi
}
}

```



## Partition Algorithm

There can be many ways to do partition, following pseudo code adopts the method given in CLRS book. The logic is simple, we start from the leftmost element and keep track of index of smaller (or equal to) elements as *i*. While traversing, if we find a smaller element, we swap current element with *arr[i]*. Otherwise we ignore current element.

```

/* low --> Starting index, high --> Ending
index */
quickSort(arr[], low, high)
{
    if (low < high)
    {
        /* pi is partitioning index, arr[p] is now
        at right place */
        pi = partition(arr, low, high);
    }
}

```

```
        quickSort(arr, low, pi - 1); // Before pi
        quickSort(arr, pi + 1, high); // After pi
    }
}
```

### Pseudo code for partition()

```
/* This function takes last element as pivot,
places
    the pivot element at its correct position in
sorted
    array, and places all smaller (smaller than
pivot)
    to left of pivot and all greater elements to
right
    of pivot */
partition (arr[], low, high)
{
    // pivot (Element to be placed at right
position)
    pivot = arr[high];

    i = (low - 1) // Index of smaller element

    for (j = low; j <= high- 1; j++)
    {
        // If current element is smaller than or
        // equal to pivot
        if (arr[j] <= pivot)
        {
            i++; // increment index of smaller
element

            swap arr[i] and arr[j]
        }
    }
}
```

```
        swap arr[i + 1] and arr[high])
    return (i + 1)
}
```

### Illustration of partition() :

```
arr[] = {10, 80, 30, 90, 40, 50, 70}
Indexes:  0    1    2    3    4    5    6
```

```
low = 0, high = 6, pivot = arr[h] = 70
Initialize index of smaller element, i = -1
```

Traverse elements from j = low to high-1

**j = 0** : Since arr[j] <= pivot, do i++ and swap(arr[i], arr[j])

**i = 0**

arr[] = {10, 80, 30, 90, 40, 50, 70} // No change as i and j

// are same

**j = 1** : Since arr[j] > pivot, do nothing  
// No change in i and arr[]

**j = 2** : Since arr[j] <= pivot, do i++ and swap(arr[i], arr[j])

**i = 1**

arr[] = {10, 30, 80, 90, 40, 50, 70} // We swap 80 and 30

**j = 3** : Since arr[j] > pivot, do nothing  
// No change in i and arr[]

**j = 4** : Since arr[j] <= pivot, do i++ and swap(arr[i], arr[j])

**i = 2**

```
arr[] = {10, 30, 40, 90, 80, 50, 70} // 80 and 40
Swapped
j = 5 : Since arr[j] <= pivot, do i++ and swap
arr[i] with arr[j]
i = 3
arr[] = {10, 30, 40, 50, 80, 90, 70} // 90 and 50
Swapped
```

We come out of loop because j is now equal to high-1.

**Finally we place pivot at correct position by swapping**

**arr[i+1] and arr[high] (or pivot)**

```
arr[] = {10, 30, 40, 50, 70, 90, 80} // 80 and 70
Swapped
```

Now 70 is at its correct place. All elements smaller than 70 are before it and all elements greater than 70 are after it.

### Implementation:

Following are C++, Java and Python implementations of QuickSort.

- C/C++
- Java
- Python

### C/C++

```
#include<stdio.h>

void swap(int* a, int* b)
```

```
{

    int t = *a;

    *a = *b;

    *b = t;

}

int partition (int arr[], int low, int high)
{

    int pivot = arr[high];

    int i = (low - 1);

    for (int j = low; j <= high- 1; j++)
    {

        if (arr[j] <= pivot)
        {

            i++;

            swap(&arr[i], &arr[j]);

        }

    }

    swap(&arr[i + 1], &arr[high]);

    return (i + 1);

}

void quickSort(int arr[], int low, int high)
{

    if (low < high)
    {
```

```
        int pi = partition(arr, low, high);
        quickSort(arr, low, pi - 1);
        quickSort(arr, pi + 1, high);
    }
}

void printArray(int arr[], int size)
{
    int i;
    for (i=0; i < size; i++)
        printf("%d ", arr[i]);
    printf("\n");
}

int main()
{
    int arr[] = {10, 7, 8, 9, 1, 5};
    int n = sizeof(arr)/sizeof(arr[0]);
    quickSort(arr, 0, n-1);
    printf("Sorted array: n");
    printArray(arr, n);
    return 0;
}
```

## Java

```
class QuickSort
```

```
{

int partition(int arr[], int low, int high)
{
    int pivot = arr[high];
    int i = (low-1);
    for (int j=low; j<high; j++)
    {
        if (arr[j] <= pivot)
        {
            i++;

            int temp = arr[i];
            arr[i] = arr[j];
            arr[j] = temp;
        }
    }

    int temp = arr[i+1];
    arr[i+1] = arr[high];
    arr[high] = temp;
    return i+1;
}

void sort(int arr[], int low, int high)
{
    if (low < high)
    {
```



```
        int pi = partition(arr, low, high);
        sort(arr, low, pi-1);
        sort(arr, pi+1, high);
    }
}

static void printArray(int arr[])
{
    int n = arr.length;
    for (int i=0; i<n; ++i)
        System.out.print(arr[i]+" ");
    System.out.println();
}

public static void main(String args[])
{
    int arr[] = {10, 7, 8, 9, 1, 5};
    int n = arr.length;
    QuickSort ob = new QuickSort();
    ob.sort(arr, 0, n-1);
    System.out.println("sorted array");
    printArray(arr);
}
}
```

## Python

```
def partition(arr, low, high) :  
    i = ( low-1 )  
    pivot = arr[high]  
    for j in range(low , high):  
        if arr[j] <= pivot:  
            i = i+1  
            arr[i],arr[j] = arr[j],arr[i]  
    arr[i+1],arr[high] = arr[high],arr[i+1]  
    return ( i+1 )  
  
def quickSort(arr, low, high) :  
    if low < high:  
        pi = partition(arr, low, high)  
        quickSort(arr, low, pi-1)  
        quickSort(arr, pi+1, high)  
  
arr = [10, 7, 8, 9, 1, 5]  
n = len(arr)  
quickSort(arr, 0, n-1)  
print ("Sorted array is:")  
for i in range(n):  
    print ("%d" %arr[i]),
```

### Output:

Sorted array:

1 5 7 8 9 10

### Analysis of QuickSort

Time taken by QuickSort in general can be written as following.

$$T(n) = T(k) + T(n-k-1) + \theta(n)$$

The first two terms are for two recursive calls, the last term is for the partition process.  $k$  is the number of elements which are smaller than pivot.

The time taken by QuickSort depends upon the input array and partition strategy. Following are three cases.

**Worst Case:** The worst case occurs when the partition process always picks greatest or smallest element as pivot. If we consider above partition strategy where last element is always picked as pivot, the worst case would occur when the array is already sorted in increasing or decreasing order. Following is recurrence for worst case.

$$T(n) = T(0) + T(n-1) + \theta(n)$$

which is equivalent to

$$T(n) = T(n-1) + \theta(n)$$

The solution of above recurrence is  $\theta(n^2)$ .

**Best Case:** The best case occurs when the partition process always picks the middle element as pivot. Following is recurrence for best case.

$$T(n) = 2T(n/2) + \theta(n)$$

The solution of above recurrence is  $\theta(n \log n)$ . It can be solved using case 2 of [Master Theorem](#).

**Average Case:**

To do average case analysis, we need to [consider all possible permutation of array and calculate time taken by every permutation which doesn't look easy](#).

We can get an idea of average case by considering the case when partition puts  $O(n/9)$  elements in one set and  $O(9n/10)$  elements in other set. Following is recurrence for this case.

$$T(n) = T(n/9) + T(9n/10) + \theta(n)$$

Solution of above recurrence is also  $O(n \log n)$

Although the worst case time complexity of QuickSort is  $O(n^2)$  which is more than many other sorting algorithms like [Merge Sort](#) and [Heap Sort](#), QuickSort is faster in practice, because its inner loop can be efficiently implemented on most architectures, and in most real-world data. QuickSort can be implemented in different ways by changing the choice of pivot, so that the worst case rarely occurs for a given type of data. However, merge sort is generally considered better when data is huge and stored in external storage.

### What is 3-Way QuickSort?

In simple QuickSort algorithm, we select an element as pivot, partition the array around pivot and recur for subarrays on left and right of pivot.

Consider an array which has many redundant elements. For example, {1, 4, 2, 4, 2, 4, 1, 2, 4, 1, 2, 2, 2, 2, 4, 1, 4, 4, 4}. If 4 is picked as pivot in Simple QuickSort, we fix only one 4 and recursively process remaining occurrences. In 3 Way QuickSort, an array `arr[l..r]` is divided in 3 parts:

- a) `arr[l..i]` elements less than pivot.
- b) `arr[i+1..j-1]` elements equal to pivot.
- c) `arr[j..r]` elements greater than pivot.

See [this](#) for implementation.

### How to implement QuickSort for Linked Lists?

[QuickSort on Singly Linked List](#)

[QuickSort on Doubly Linked List](#)

### Can we implement QuickSort Iteratively?

Yes, please refer [Iterative Quick Sort](#).

### Why Quick Sort is preferred over MergeSort for sorting Arrays

Quick Sort in its general form is an in-place sort (i.e. it doesn't require any extra storage) whereas merge sort requires  $O(N)$  extra storage,  $N$  denoting the array size which may be quite expensive.

Allocating and de-allocating the extra space used for merge sort increases the running time of the algorithm. Comparing average complexity we find that both type of sorts have  $O(N \log N)$  average complexity but the constants differ. For arrays, merge sort loses due to the use of extra  $O(N)$  storage space.

Most practical implementations of Quick Sort use randomized version. The randomized version has expected time complexity of  $O(n \log n)$ . The worst case is possible in randomized version also, but worst case doesn't occur for a particular pattern (like sorted array) and randomized Quick Sort works well in practice.

Quick Sort is also a cache friendly sorting algorithm as it has good locality of reference when used for arrays.

Quick Sort is also tail recursive, therefore tail call optimizations is done.

### **Why MergeSort is preferred over QuickSort for Linked Lists?**

In case of linked lists the case is different mainly due to difference in memory allocation of arrays and linked lists. Unlike arrays, linked list nodes may not be adjacent in memory. Unlike array, in linked list, we can insert items in the middle in  $O(1)$  extra space and  $O(1)$  time. Therefore merge operation of merge sort can be implemented without extra space for linked lists.

In arrays, we can do random access as elements are continuous in memory. Let us say we have an integer (4-byte) array A and let the address of  $A[0]$  be x then to access  $A[i]$ , we can directly access the memory at  $(x + i * 4)$ . Unlike arrays, we can not do random access in linked list. Quick Sort requires a lot of this kind of access. In linked list to access i'th index, we have to travel each and every node from the head to i'th node as we don't have continuous block of memory. Therefore, the overhead increases for quick sort. Merge sort accesses data sequentially and the need of random access is low.

### **How to optimize QuickSort so that it takes $O(\log n)$ extra space in worst case?**

Please see [QuickSort Tail Call Optimization \(Reducing worst case space to  \$\log n\$ \)](https://www.geeksforgeeks.org/quick-sort/)

## Snapshots:

**Partition**

10 80 30 90 40 50 70

Counter variables  
I: Index of smaller element  
J: Loop variable

We start the loop with initial values.

Pivot

| Test condition      | Actions | Value of variables  |
|---------------------|---------|---------------------|
| $arr[J] \leq pivot$ |         | $I = -1$<br>$J = 0$ |

**Partition**

10 80 30 90 40 50 70

Counter variables  
I: Index of smaller element  
J: Loop variable

Pass 2

Pivot

| Test condition                            | Actions   | Value of variables |
|---|-----------|--------------------|
| $arr[J] \leq pivot$<br>$80 < 70$<br>False | No action | $I = 0$<br>$J = 1$ |

**Partition**

10 30 80 90 40 50 70

Counter variables  
I: Index of smaller element  
J: Loop variable

Pivot

| Test condition                           | Actions                              | Value of variables |
|--|--------------------------------------|--------------------|
| $arr[J] \leq pivot$<br>$30 < 70$<br>True | $I++$<br>Swap( $arr[I]$ , $arr[J]$ ) | $I = 1$<br>$J = 2$ |

**Partition**

10 30 40 90 80 50 70

Counter variables  
I: Index of smaller element  
J: Loop variable

Pass 5

Pivot

| Test condition                           | Actions                              | Value of variables |
|--|--------------------------------------|--------------------|
| $arr[J] \leq pivot$<br>$40 < 70$<br>True | $I++$<br>Swap( $arr[I]$ , $arr[J]$ ) | $I = 2$<br>$J = 4$ |

### Partition

10 30 40 50 80 90 70

Counter variables  
I: Index of smaller element  
J: Loop variable

Before Pass 7, J becomes 6 so we come out of the loop.

| Test condition      | Actions | Value of variables |
|---------------------|---------|--------------------|
| $arr[J] \leq pivot$ |         | I = 3<br>J = 6     |

### Partition

10 30 40 50 70 90 80

Counter variables  
I: Index of smaller element  
J: Loop variable

We know swap  $arr[i+1]$  and pivot.

I = 3

### Quick sort left

10 30 40 50 70 90 80

Since quick sort is a recursion function, we call the Partition function again.

First 50 is the pivot.

As it is already at its correct position we call the quicksort function again on the left part.

### Quick sort Right

10 30 40 50 70 80 90

80 is the Pivot.

80 and 90 are swapped to bring pivot to correct position.

- [Quiz on QuickSort](#)
- [Recent Articles on QuickSort](#)
- [Coding practice for sorting.](#)

### References:

<http://en.wikipedia.org/wiki/Quicksort>

**Other Sorting Algorithms on GeeksforGeeks/GeeksQuiz:**

[Selection Sort](#), [Bubble Sort](#), [Insertion Sort](#), [Merge Sort](#), [Heap Sort](#), [QuickSort](#), [Radix Sort](#), [Counting Sort](#), [Bucket Sort](#), [ShellSort](#), [Comb Sort](#), [Pigeonhole Sort](#)

Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above.