

All programs should be written using MATLAB. MATLAB and its toolboxes are available in ME Computer Lab (MRDC2105). To save the image from the ME6406 website page, point the mouse cursor on the image and click on the mouse's right button. Choose <Save image as>.

Assignment #1: Due **September 8, 2016 (Thursday)**. Solutions must include m-files, results, and an explanation of your results in a document. All m-files must be submitted electronically in a zipped file through **T-square**. A confirmation email will be sent on receipt of submission.

1. Pin-hole optics

Consider a pin-hole projection area of radius R_1 scans across a bright circular landmark with radius R_2 . Let s denote the distance of the center of the pin-hole measured from the line joining the two intersection points. Let δA denote the area of the overlap region.

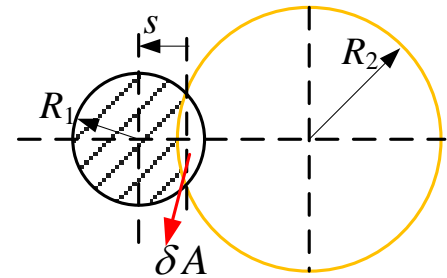


Figure 1. Pin-hole

(a) **Derive** an expression for $\delta A / \delta O$ in terms of $S=(s/R_1)$ and $\lambda=(R_2/R_1)$, where δO is the area of the pin-hole projection.

(b) **Plot** $\delta A / \delta O$ as a function of S , where $-1 \leq S \leq 1$ and $\lambda=3, 5, 10$.

2. Histogram equalization

(a) The sub-region of the pollen image shown in Fig. 2 is an 8-bit gray scale image matrix. Carry out histogram equalization by completing Table 1. Show the sub-region matrix after histogram equalization.

Table 1

Gray level	# of pixels	cdf	q_k	$\text{round}(q_k)$
117	1	1	5.313	5
\vdots	\vdots	\vdots	\vdots	\vdots
132	2	48	255	255

(b) Perform histogram equalization on an image by writing a Matlab script for the following:

- I. Read in and display the 'eyeball.png'.
- II. Compare by displaying the original and processed images and their histograms.

Suggested Matlab functions: rgb2gray, imshow, imhist or hist, histeq

3. Filtering masks

Sobel operator

(a) Use a 3x3 Sobel operator to calculate the *magnitude* and *direction* of the gradient at pixel (3, 2) in Fig. 2. Indicate the direction of the gradient on the pixel. (Note: Sobel operator is coordinate dependent. Be sure to use consistent coordinate systems on the sub-regions.)

(b) Write a Matlab script to compute the gradient of an image. For illustration, use the Sobel operator on the image "HeadCT.png" shown in Fig. 3(a). Display the gradient images (G_x , G_y , G). Suggested Matlab functions: edge.m

Gaussian operator

- (c) Use a Gaussian filter mask with different $\sigma (=1, 2, 5)$ to smooth the image 'salt_and_pepper_checker.png' (Fig. 3(b)). Use the proper mask size and compare the effect of σ on the smoothed image.

Suggested Matlab functions: `imfilter.m`

- (d) DoG is the difference between two Gaussians. Perform edge detections with DoG function on the image "HeadCT.png". (use $\sigma = 1$ and $\sigma = 2$)

4. Low-level information processing

This problem shows the process of obtaining some low-level information from an image (Fig. 4).

- (a) Read in and convert the image 'nut_and_shell.png' into a gray-scale image. Binarize the image using 3 different thresholds. Preferably one over-estimate, one under-estimate, one in between. (hint: look at histogram to get an idea of what thresholds to pick).
- (b) Obtain the area and centroid of the two objects (nut and shell) in the image with the appropriate threshold.
- (c) Find the outer boundaries of the nut and shell.

Suggested Matlab functions: `rgb2gray.m`, `im2bw.m`, `bwlabel.m`, `regionprops.m`, `bwboundaries.m`

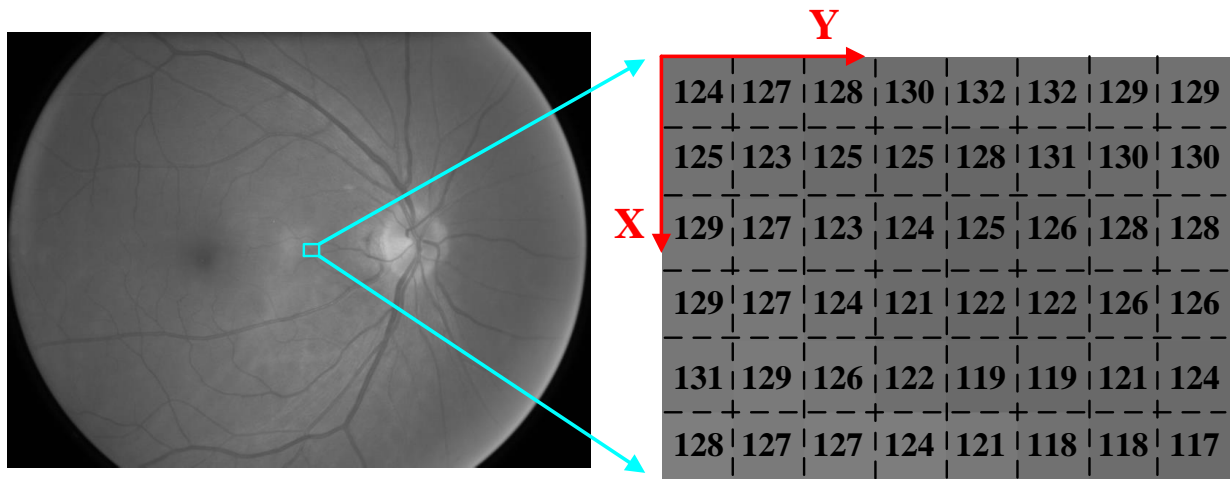


Figure 2. EyeBall.png



Figure 3(a).
HeadCT.png

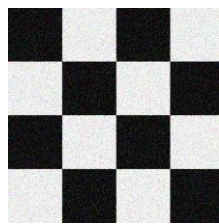


Figure 3(b).
salt_and_pepper_checker.png

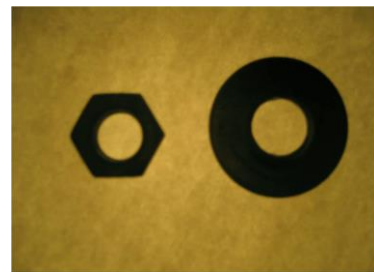


Figure 4. nut_and_shell.png