

Complete and Efficient DRAT Proof Checking

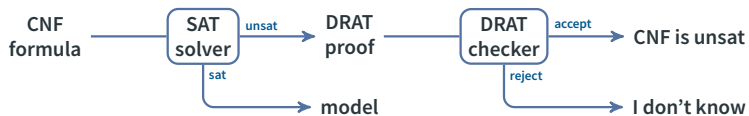
Adrián Rebola-Pardo, Luís Cruz-Filipe

TU Wien, University of Southern Denmark

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SAT solving and DRAT proofs



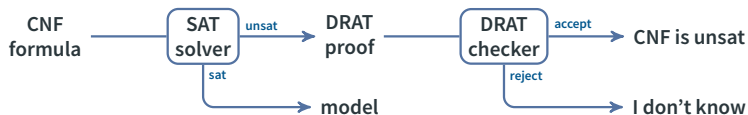
SAT solving and DRAT proofs



DRAT proof sequence of clause introductions and deletions

- i: C C must be a RUP or RAT clause
- d: C always allowed
- i: \square finishes the proof

SAT solving and DRAT proofs



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RUP / RAT introduction and clause deletion are **satisfiability-preserving**

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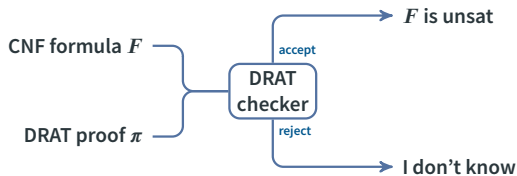
RUP / RAT introduction and clause deletion are **satisfiability-preserving**
if \square is derived, then the input formula is **unsatisfiable**

What I talk about when I talk about checking

DRAT checker checks that each inference is correct

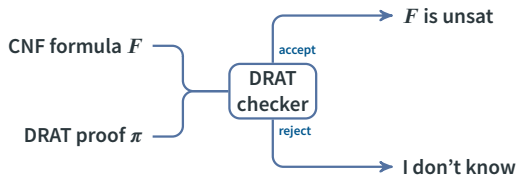
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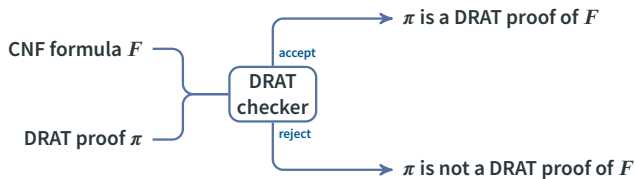
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This criterion is problematic: F unsat, $\pi = \text{covfefe}$ \Rightarrow accept

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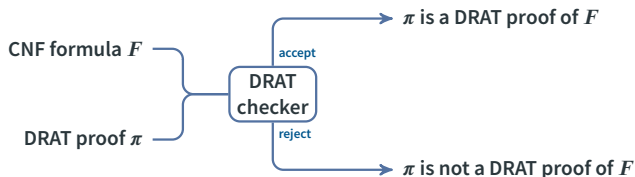
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Problem state-of-the-art DRAT checkers decide something slightly different from DRAT correctness

Proof system specification of *correct* refutations

Two flavors of DRAT

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Sound proof system if a correct refutation of F exists, then F is unsatisfiable

Refutations are correct **with respect to a proof system**

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specified DRAT



[Wetzler, Heule, Hunt '14]

operational DRAT



drat-trim, gratgen

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Discrepancies exist [Rebola-Pardo, Biere '18] sDRAT-correct proofs that are oDRAT-incorrect, and oDRAT-correct proofs that are sDRAT-incorrect

Why operational DRAT? The methods used in state-of-the-art DRAT checkers do not work when **unit clause deletions** occur in the input proof
ignore unit clause deletions

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RAT introduction depends on the absence of clauses.

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Contributions

- Can we check sDRAT as efficiently as oDRAT?
- How often do discrepancies occur in practice?

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- How often do discrepancies occur in practice?

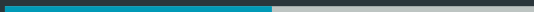
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Contributions

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- How often do discrepancies occur in practice? **Quite a lot**

Experimental evaluation



Questions

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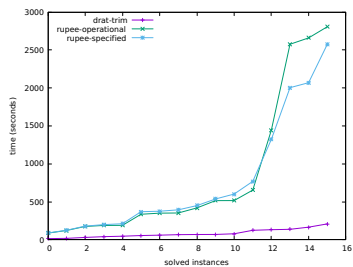
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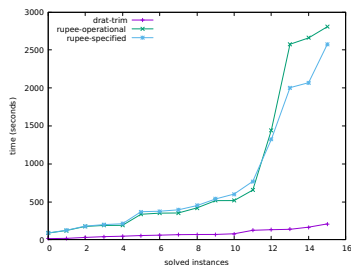
Benchmarks 11 instances from SAT Competition 2017

Solvers COMinisatPS_Pulsar, glucose-4.1, Maple_LCM_Dist, cadical-sc17

Experimental results

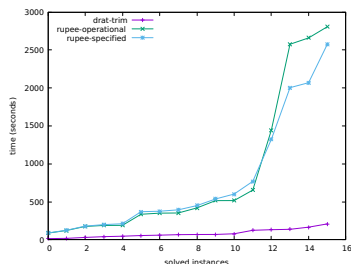


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rupee performs about an **order of magnitude worse** than drat-trim
probably due to code optimization and core-first propagation

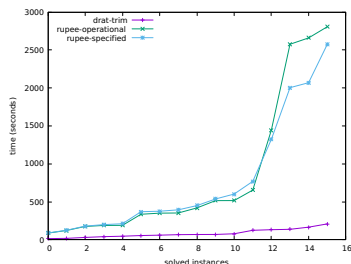
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no observable overhead due to unit clause deletion

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All proofs generated by cadical-sc17 are **correct** for both sDRAT and oDRAT. For the other 3 solvers, 8 out of 11 proofs were **incorrect** as sDRAT and correct as oDRAT.

probably due to the CDCL proof generation method inherited from minisat

Why are unit deletions ignored?



x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$
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$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$
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i: x_9

i: \square

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C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

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i: x_5 $\overline{x_5} x_1$

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i: x_5 $\overline{x_5} x_1 x_2$

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 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} \\
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 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp$$

$$i: x_9$$

$$i: \square$$

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$$\boxed{i: x_5} \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

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 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
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State-of-the-art DRAT checking

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$$i: x_9$$

$$i: \square$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9}$$

$$i: \square$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9} x_1$$

$$i: \square$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9} x_1 x_2$$

$$i: \square$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9} x_1 x_2 x_3$$

$$i: \square$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9} x_1 x_2 x_3 x_4$$

$$i: \square$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9} x_1 x_2 x_3 x_4 x_5$$

$$i: \square$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6$$

$$i: \square$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7$$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10}$$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp$$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$$

$$i: x_9 \quad \overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

i: x_5 $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

i: x_9 $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

i: x_5 $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

i: x_9 $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & x_9 \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$i: x_5 \quad \overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

$i: x_9 \quad \overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

$i: \square \quad x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

i: x_5 $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

i: x_9 $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

i: \square $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

i: x_5 $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

i: x_9 $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

i: \square $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$i: x_5$ $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

$i: x_9$ $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

$i: \square$ $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$i: x_5$ $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

$i: x_9$ $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

$i: \square$ $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$i: x_5$ $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

$i: x_9$ $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

$i: \square$ $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$i: x_5$ $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

$i: x_9$ $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

$i: \square$ $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$i: x_5$ $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

$i: x_9$ $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

$i: \square$ $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$i: x_5$ $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

$i: x_9$ $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

$i: \square$ $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$i: x_5$ $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

$i: x_9$ $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

$i: \square$ $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$i: x_5$ $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

$i: x_9$ $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

$i: \square$ $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$i: x_5$ $\overline{x_5} x_1 x_2 x_3 x_4 x_6 x_8 \perp \Rightarrow \text{RUP}$

$i: x_9$ $\overline{x_9} x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_{10} \perp \Rightarrow \text{RUP}$

$i: \square$ $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$

i: x_5

i: x_9

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$

$$x_1$$

$$i: x_5$$

$$i: x_9$$

$$i: \square$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{cccc}
 x_1 & x_5 \ x_6 & \overline{x_3} \ \overline{x_6} \ x_8 & \overline{x_4} \ \overline{x_9} \ x_{10} \\
 \overline{x_1} \ x_2 & \overline{x_2} \ \overline{x_5} \ x_7 & x_3 \ \overline{x_4} \ \overline{x_6} & x_9 \ \overline{x_{10}} \\
 \overline{x_1} \ \overline{x_2} \ x_3 & \overline{x_1} \ \overline{x_5} \ x_6 & x_5 \ \overline{x_8} & x_7 \ \overline{x_9} \\
 \overline{x_1} \ \overline{x_3} \ x_4 & x_4 \ \overline{x_5} \ \overline{x_6} & \overline{x_3} \ x_9 \ x_{10} & \overline{x_7} \ \overline{x_8} \ \overline{x_9} \ \overline{x_{10}}
 \end{array}$$

$$x_1 \ x_2$$

i: x_5

i: x_9

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{cccc}
 x_1 & x_5 \ x_6 & \overline{x_3} \ \overline{x_6} \ x_8 & \overline{x_4} \ \overline{x_9} \ x_{10} \\
 \overline{x_1} \ x_2 & \overline{x_2} \ \overline{x_5} \ x_7 & x_3 \ \overline{x_4} \ \overline{x_6} & x_9 \ \overline{x_{10}} \\
 \overline{x_1} \ \overline{x_2} \ x_3 & \overline{x_1} \ \overline{x_5} \ x_6 & x_5 \ \overline{x_8} & x_7 \ \overline{x_9} \\
 \overline{x_1} \ \overline{x_3} \ x_4 & x_4 \ \overline{x_5} \ \overline{x_6} & \overline{x_3} \ x_9 \ x_{10} & \overline{x_7} \ \overline{x_8} \ \overline{x_9} \ \overline{x_{10}}
 \end{array}$$

$$x_1 \ x_2 \ x_3$$

i: x_5

i: x_9

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{cccc}
 x_1 & x_5 \ x_6 & \overline{x_3} \ \overline{x_6} \ x_8 & \overline{x_4} \ \overline{x_9} \ x_{10} \\
 \overline{x_1} \ x_2 & \overline{x_2} \ \overline{x_5} \ x_7 & x_3 \ \overline{x_4} \ \overline{x_6} & x_9 \ \overline{x_{10}} \\
 \overline{x_1} \ \overline{x_2} \ x_3 & \overline{x_1} \ \overline{x_5} \ x_6 & x_5 \ \overline{x_8} & x_7 \ \overline{x_9} \\
 \overline{x_1} \ \overline{x_3} \ x_4 & x_4 \ \overline{x_5} \ \overline{x_6} & \overline{x_3} \ x_9 \ x_{10} & \overline{x_7} \ \overline{x_8} \ \overline{x_9} \ \overline{x_{10}}
 \end{array}$$

$$x_1 \ x_2 \ x_3 \ x_4$$

i: x_5

i: x_9

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 \ x_2 \ x_3 \ x_4$$

i: x_5

i: x_9

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4$$

i: x_9

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5$$

i: x_9

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{ccccc}
 x_1 & x_5 \ x_6 & \overline{x_3} \ \overline{x_6} \ x_8 & \overline{x_4} \ \overline{x_9} \ x_{10} & x_5 \\
 \overline{x_1} \ x_2 & \overline{x_2} \ \overline{x_5} \ x_7 & x_3 \ \overline{x_4} \ \overline{x_6} & x_9 \ \overline{x_{10}} & \\
 \overline{x_1} \ \overline{x_2} \ x_3 & \overline{x_1} \ \overline{x_5} \ x_6 & x_5 \ \overline{x_8} & x_7 \ \overline{x_9} & \\
 \overline{x_1} \ \overline{x_3} \ x_4 & x_4 \ \overline{x_5} \ \overline{x_6} & \overline{x_3} \ x_9 \ x_{10} & \overline{x_7} \ \overline{x_8} \ \overline{x_9} \ \overline{x_{10}} &
 \end{array}$$

$$x_1 \ x_2 \ x_3 \ x_4$$

i: x_5

$$x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6$$

i: x_9

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7$$

i: x_9

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{ccccc}
 x_1 & x_5 \ x_6 & \overline{x_3} \ \overline{x_6} \ x_8 & \overline{x_4} \ \overline{x_9} \ x_{10} & x_5 \\
 \overline{x_1} \ x_2 & \overline{x_2} \ \overline{x_5} \ x_7 & x_3 \ \overline{x_4} \ \overline{x_6} & x_9 \ \overline{x_{10}} & x_9 \\
 \overline{x_1} \ \overline{x_2} \ x_3 & \overline{x_1} \ \overline{x_5} \ x_6 & x_5 \ \overline{x_8} & x_7 \ \overline{x_9} & \\
 \overline{x_1} \ \overline{x_3} \ x_4 & x_4 \ \overline{x_5} \ \overline{x_6} & \overline{x_3} \ x_9 \ x_{10} & \overline{x_7} \ \overline{x_8} \ \overline{x_9} \ \overline{x_{10}} &
 \end{array}$$

$$x_1 \ x_2 \ x_3 \ x_4$$

i: x_5

$$x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7 \ x_8$$

i: x_9

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & x_9 \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & x_9 \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9$$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & x_9 \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10}$$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

$$\begin{array}{ccccc}
 x_1 & x_5 \ x_6 & \overline{x_3} \ \overline{x_6} \ x_8 & \overline{x_4} \ \overline{x_9} \ x_{10} & x_5 \\
 \overline{x_1} \ x_2 & \overline{x_2} \ \overline{x_5} \ x_7 & x_3 \ \overline{x_4} \ \overline{x_6} & x_9 \ \overline{x_{10}} & x_9 \\
 \overline{x_1} \ \overline{x_2} \ x_3 & \overline{x_1} \ \overline{x_5} \ x_6 & x_5 \ \overline{x_8} & x_7 \ \overline{x_9} & \\
 \overline{x_1} \ \overline{x_3} \ x_4 & x_4 \ \overline{x_5} \ \overline{x_6} & \overline{x_3} \ x_9 \ x_{10} & \overline{x_7} \ \overline{x_8} \ \overline{x_9} \ \overline{x_{10}} &
 \end{array}$$

$$x_1 \ x_2 \ x_3 \ x_4$$

i: x_5

$$x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7 \ x_8$$

i: x_9

$$x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7 \ x_8 \ x_9 \ x_{10} \ \perp$$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$x_1 x_2 x_3 x_4$

i: x_5

$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$

i: x_9

$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$x_1 x_2 x_3 x_4$

i: x_5

$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$

i: x_9

$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	x_9
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$x_1 x_2 x_3 x_4$

i: x_5

$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$

i: x_9

$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & x_9 \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & x_9 \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$$

i: \square

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & x_9 \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$$

$$i: \square \quad x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & x_9 \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$$

$$\boxed{i: \square} \quad x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \quad \Rightarrow \text{RUP}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$$

i: \square

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$$

i: \square

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 \overline{x_9}$$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$$

i: \square

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9 $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 \overline{x_9} x_{10} \perp$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$$

i: \square $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9 $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 \overline{x_9} x_{10} \perp \Rightarrow \text{RUP}$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$$

i: \square $x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

$$i: x_9 \quad x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 \overline{x_9} x_{10} \perp \Rightarrow \text{RUP}$$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$$

$$i: \square \quad x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{cccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

$$i: x_5$$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

$$i: x_9$$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 \overline{x_9} x_{10} \perp \Rightarrow \text{RUP}$$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp$$

$$i: \square$$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp \Rightarrow \text{RUP}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{cccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}
 \end{array}$$

$$\begin{array}{lcl}
 \text{i: } x_5 & x_1 x_2 x_3 x_4 & \\
 \text{i: } x_9 & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 \overline{x_9} x_{10} \perp & \Rightarrow \text{RUP} \\
 \text{i: } \square & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp & \Rightarrow \text{RUP}
 \end{array}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{cccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}
 \end{array}$$

$$\begin{array}{lcl}
 \text{i: } x_5 & x_1 x_2 x_3 x_4 \overline{x_5} & \\
 \text{i: } x_9 & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 \overline{x_9} x_{10} \perp & \Rightarrow \text{RUP} \\
 \text{i: } \square & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp & \Rightarrow \text{RUP}
 \end{array}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{cccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}
 \end{array}$$

$$\begin{array}{lcl}
 & x_1 x_2 x_3 x_4 & \\
 \textcircled{i: x_5} & x_1 x_2 x_3 x_4 \overline{x_5} x_6 x_8 \perp & \\
 & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 & \\
 \textcircled{i: x_9} & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 \overline{x_9} x_{10} \perp & \Rightarrow \text{RUP} \\
 & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp & \\
 \textcircled{i: \square} & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp & \Rightarrow \text{RUP}
 \end{array}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{cccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}
 \end{array}$$

$$\begin{array}{lcl}
 \text{i: } x_5 & x_1 x_2 x_3 x_4 \overline{x_5} x_6 x_8 \perp & \Rightarrow \text{RUP} \\
 \text{i: } x_9 & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 \overline{x_9} x_{10} \perp & \Rightarrow \text{RUP} \\
 \text{i: } \square & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp & \Rightarrow \text{RUP}
 \end{array}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

State-of-the-art DRAT checking

$$\begin{array}{cccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}
 \end{array}$$

$$\begin{array}{lcl}
 \text{i: } x_5 & x_1 x_2 x_3 x_4 \overline{x_5} x_6 x_8 \perp & \Rightarrow \text{RUP} \\
 \text{i: } x_9 & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 \overline{x_9} x_{10} \perp & \Rightarrow \text{RUP} \\
 \text{i: } \square & x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 x_9 x_{10} \perp & \Rightarrow \text{RUP}
 \end{array}$$

C is a **reverse unit propagation (RUP)** clause in F whenever $F \wedge \overline{C}$ reaches a conflict by unit propagation

Optimizations trace preprocessing and backwards checking

Unit clause deletion breaks stuff

$$\begin{array}{cccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}
 \end{array}$$

i: x_5

d: $\overline{x_1} x_2$

i: x_9

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{cccc}
 x_1 & x_5 \ x_6 & \overline{x_3} \ \overline{x_6} \ x_8 & \overline{x_4} \ \overline{x_9} \ x_{10} \\
 \overline{x_1} \ x_2 & \overline{x_2} \ \overline{x_5} \ x_7 & x_3 \ \overline{x_4} \ \overline{x_6} & x_9 \ \overline{x_{10}} \\
 \overline{x_1} \ \overline{x_2} \ x_3 & \overline{x_1} \ \overline{x_5} \ x_6 & x_5 \ \overline{x_8} & x_7 \ \overline{x_9} \\
 \overline{x_1} \ \overline{x_3} \ x_4 & x_4 \ \overline{x_5} \ \overline{x_6} & \overline{x_3} \ x_9 \ x_{10} & \overline{x_7} \ \overline{x_8} \ \overline{x_9} \ \overline{x_{10}}
 \end{array}$$

$$x_1 \ x_2 \ x_3 \ x_4$$

i: x_5

d: $\overline{x_1} \ x_2$

i: x_9

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

d: $\overline{x_1} x_2$

i: x_9

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4$$

d: $\overline{x_1} x_2$

i: x_9

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

i: x_9

i: \square

Unit clause deletion breaks stuff

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
$\overline{x_1} x_2$	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

i: x_9

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_2} \overline{x_5} x_7 & \overline{x_3} \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

i: x_9

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_2} \overline{x_5} x_7 & \overline{x_3} \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

???

i: x_9

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_2} \overline{x_5} x_7 & \overline{x_3} \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

$$x_1 x_5 x_6 x_4 x_3 x_8$$

i: x_9

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_2} \overline{x_5} x_7 & \overline{x_3} \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

$$x_1 x_5 x_6 x_4 x_3 x_8$$

i: x_9

How do I find this?

How do I restore the trace
during backwards checking?

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_2} \overline{x_5} x_7 & \overline{x_3} \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

$$x_1 x_5 x_6 x_4 x_3 x_8$$

i: x_9

How do I find this?

How do I restore the trace
during backwards checking?

i: \square

Unit clause every literal but one is falsified by UP by the current formula
reason clauses are always unit clauses

How do we delete unit clauses



Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_1} x_2 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

i: x_9

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 \overline{x_2} \overline{x_5} x_7 & \overline{x_3} \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

i: x_9

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} \overline{x_6} & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

Remove all literals
propagated because of x_2

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} \overline{x_6} & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

i: x_9

Remove all literals
propagated because of x_2

i: \square

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} \overline{x_6} & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

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 \overline{x_2} \overline{x_5} x_7 & \overline{x_3} \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} \overline{x_6} & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} \overline{x_4} & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 \ x_2 \ x_3 \ x_4$$

i: x_5

$$x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7 \ x_8$$

d: $\overline{x_1} \ x_2$

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 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} \overline{x_6} & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
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Unit clause deletion breaks stuff

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 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} \overline{x_6} & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
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$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8 \quad x_2 x_3 x_4 x_7 x_8$$

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 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} \overline{x_6} & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

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d: $\overline{x_1} x_2$

$$x_1 x_5 x_6$$

$$x_2 x_3 x_4 x_7 x_8$$

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Remove all literals
propagated because of x_2

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Unit clause deletion breaks stuff

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$x_1 x_2 x_3 x_4$

i: x_5

$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$

d: $\overline{x_1} x_2$

$x_1 x_5 x_6$

$x_2 x_3 x_4 x_7 x_8$

i: x_9

Remove all literals
propagated because of x_2

i: \square

Check clauses with \overline{x}
for each removed x

Unit clause deletion breaks stuff

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
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i: x_5

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	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

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i: x_5

$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$

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 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 x_2 x_3 x_4$$

i: x_5

$$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$$

d: $\overline{x_1} x_2$

$$x_1 x_5 x_6 x_4$$

$$x_2 x_3 x_4 x_7 x_8$$

i: x_9

Remove all literals
propagated because of x_2

i: \square

Check clauses with \overline{x}
for each removed x

Propagate again

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 & \overline{x_2} \overline{x_5} x_7 & \textcolor{orange}{x_3} \textcolor{orange}{x_4} \textcolor{orange}{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
 \end{array}$$

$$x_1 \ x_2 \ x_3 \ x_4$$

i: x_5

$$x_1 \ x_2 \ x_3 \ x_4 \ x_5 \ x_6 \ x_7 \ x_8$$

d: $\overline{x_1} x_2$

$$x_1 \ x_5 \ x_6 \ x_4$$

$$\textcolor{teal}{x_2 \ x_3 \ x_4 \ x_7 \ x_8}$$

i: x_9

Remove all literals
propagated because of x_2

i: \square

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Propagate again

Unit clause deletion breaks stuff

$$\begin{array}{ccccc}
 x_1 & x_5 x_6 & \overline{x_3} \overline{x_6} x_8 & \overline{x_4} \overline{x_9} x_{10} & x_5 \\
 & \overline{x_2} \overline{x_5} x_7 & x_3 \overline{x_4} \overline{x_6} & x_9 \overline{x_{10}} & \\
 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
 \overline{x_1} \overline{x_3} x_4 & x_4 \overline{x_5} \overline{x_6} & \overline{x_3} x_9 x_{10} & \overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}} &
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 \overline{x_1} \overline{x_2} x_3 & \overline{x_1} \overline{x_5} x_6 & x_5 \overline{x_8} & x_7 \overline{x_9} & \\
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$$x_1 x_5 x_6 x_4 x_3 x_8$$

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Unit clause deletion breaks stuff

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
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$$x_1 x_2 x_3 x_4$$

i: x_5

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$$x_1 x_5 x_6 x_4 x_3 x_8$$

i: x_9

How do we reconstruct the trace during backwards checking?

i: \square

Unit clause deletion breaks stuff

x_1	$x_5 x_6$	$\overline{x_3} \overline{x_6} x_8$	$\overline{x_4} \overline{x_9} x_{10}$	x_5
	$\overline{x_2} \overline{x_5} x_7$	$x_3 \overline{x_4} \overline{x_6}$	$x_9 \overline{x_{10}}$	
$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
$\overline{x_1} \overline{x_3} x_4$	$x_4 \overline{x_5} \overline{x_6}$	$\overline{x_3} x_9 x_{10}$	$\overline{x_7} \overline{x_8} \overline{x_9} \overline{x_{10}}$	

$x_1 x_2 x_3 x_4$

i: x_5

$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$

d: $\overline{x_1} x_2$

$x_1 x_5 x_6 x_4 x_3 x_8$

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Unit clause deletion breaks stuff

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$\overline{x_1} \overline{x_2} x_3$	$\overline{x_1} \overline{x_5} x_6$	$x_5 \overline{x_8}$	$x_7 \overline{x_9}$	
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$x_1 x_2 x_3 x_4$

i: x_5

$x_1 x_2 x_3 x_4 x_5 x_6 x_7 x_8$

d: $\overline{x_1} x_2$

$x_1 x_5 x_6 x_4 x_3 x_8$

i: x_9

i: \square

How do we reconstruct the trace during backwards checking?

Just store it in memory

Are we done yet?

Are we done yet?

I'd wish.

Are we done yet?

I'd wish.

Two-watched literal schema makes unit propagation efficient

I'd wish.

Two-watched literal schema makes unit propagation efficient

Problem our procedure breaks the invariants that make it work

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Solution (kind of) restore the invariants clause by clause
overall, 85% of the time is spent on unit clause deletion

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- Efficient causal cone detection

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- Efficient causal cone detection
- Compress traces before storing them to memory
- Restore invariants only where really needed by exploiting other invariants

Result negligible overhead of unit clause deletion!

Conclusion

Contributions

- Can we check sDRAT as efficiently as oDRAT?
- How often do discrepancies occur in practice?

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We conjecture that proofs can be generated **according to the specification**, and that proofs can be checked under the specification with **similar performance** to that of state-of-the-art DRAT checkers.