Bernoulli example

■ Define the working directory and load CmdStan.m

```
In[30]:= (* Linux *)
     SetDirectory["~/GitHub/MathematicaStan/Examples/Bernoulli"]
     (* Windows *)
     (* SetDirectory["C:\\Users\\USER_NAME\\Documents\\Mathematica\\STAN\\Examples\\Bernoulli"] *)
     Needs["CmdStan`"]
Out[30]= /ISO06139/home/pix/GitHub/MathematicaStan/Examples/Bernoulli
   ■ Generate the Bernoulli Stan code and compile it
In[32]:= stanCode="data {
       int<lower=0> N;
       int<lower=0,upper=1> y[N];
     }
     parameters {
      real<lower=0,upper=1> theta;
     model {
       theta \sim beta(1,1);
       for (n in 1:N)
        y[n] ~ bernoulli(theta);
     StanCodeExport["bernoulli",stanCode]
     (* Compile your code.
      * Caveat: this can take some time
     StanCompile["bernoulli"]
Out[33]= bernoulli.stan
Generate some data and save them (RDump file)
ln[35] := n = 1000;
     y=Table[Random[BernoulliDistribution[0.2016]],{i,1,n}];
     RDumpExport["bernoulli",{{"N",n},{"y",y}}];
   ■ Run Stan and get result
In[38]:= StanRunSample ["bernoulli"]
     output = StanImport [ "output.csv"];
Out[38]= method = sample (Default)
        num_samples = 1000 (Default)
        num_warmup = 1000 (Default)
```

```
save_warmup = 0 (Default)
    thin = 1 (Default)
    adapt
      engaged = 1 (Default)
      delta = 0.800000000000000000004 (Default)
      kappa = 0.75 (Default)
      t0 = 10 (Default)
      init_buffer = 75 (Default)
      term_buffer = 50 (Default)
      window = 25 (Default)
    algorithm = hmc (Default)
      hmc
        engine = nuts (Default)
         nuts
            max_depth = 10 (Default)
        metric = diag_e (Default)
        stepsize = 1 (Default)
        stepsize_jitter = 0 (Default)
id = 0 (Default)
data
  file = /IS006139/home/pix/GitHub/MathematicaStan/Examples/Bernoulli/bernoulli.data.R
init = 2 (Default)
random
  seed = 3382355977
output
  file = /IS006139/home/pix/GitHub/MathematicaStan/Examples/Bernoulli/output.csv
  diagnostic_file = (Default)
  refresh = 100 (Default)
Gradient evaluation took 7.7e-05 seconds
1000 transitions using 10 leapfrog steps per transition would take 0.77 seconds.
Adjust your expectations accordingly!
Iteration:
             1 / 2000 [ 0%]
                               (Warmup)
Iteration: 100 / 2000 [ 5%]
                               (Warmup)
Iteration: 200 / 2000 [ 10%]
                               (Warmup)
Iteration: 300 / 2000 [ 15%]
                               (Warmup)
Iteration: 400 / 2000 [ 20%]
                               (Warmup)
Iteration: 500 / 2000 [ 25%]
                               (Warmup)
Iteration: 600 / 2000 [ 30%]
                               (Warmup)
Iteration: 700 / 2000 [ 35%]
                               (Warmup)
Iteration: 800 / 2000 [ 40%]
                               (Warmup)
Iteration: 900 / 2000 [ 45%]
                               (Warmup)
Iteration: 1000 / 2000 [ 50%]
                               (Warmup)
Iteration: 1001 / 2000 [ 50%]
                               (Sampling)
Iteration: 1100 / 2000 [ 55%]
                               (Sampling)
Iteration: 1200 / 2000 [ 60%]
                               (Sampling)
Iteration: 1300 / 2000 [ 65%]
                               (Sampling)
Iteration: 1400 / 2000 [ 70%]
                               (Sampling)
Iteration: 1500 / 2000 [ 75%]
                               (Sampling)
Iteration: 1600 / 2000 [ 80%]
                               (Sampling)
Iteration: 1700 / 2000 [ 85%]
                               (Sampling)
Iteration: 1800 / 2000 [ 90%]
                               (Sampling)
Iteration: 1900 / 2000 [ 95%]
                              (Sampling)
```

```
Iteration: 2000 / 2000 [100%] (Sampling)
        Elapsed Time: 0.226371 seconds (Warm-up)
                         0.298571 seconds (Sampling)
                         0.524942 seconds (Total)
    Use the results
    ■ List Header
In[40]:= StanImportHeader[output]
\label{eq:condition} \mbox{Out}[40] = \{\{\mbox{lp\_, 1}\}, \{\mbox{accept\_stat\_\_, 2}\}, \{\mbox{stepsize\_\_, 3}\}, \{\mbox{treedepth\_\_, 4}\}, \\
        {n_{p, 0}, 5}, {divergent_, 6}, {energy_, 7}, {theta, 8}
```

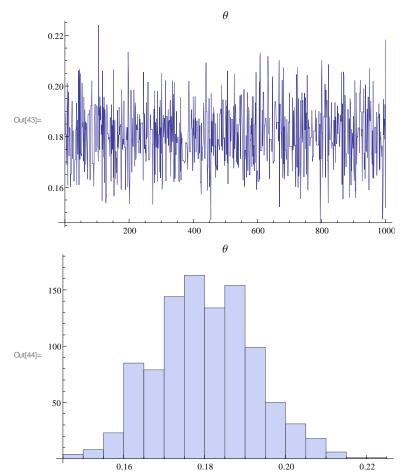
■ Show sample matrix

In[41]:= Dimensions[StanImportData[output]]

```
Take[StanImportData[output],3]
Out[41]= \{1000, 8\}
\text{Out}[42] = \; \left\{ \left. \left\{ -473.55 \,,\, 0.505272 \,,\, 1.80506 \,,\, 1. \,,\, 1. \,,\, 0. \,,\, 475.647 \,,\, 0.189243 \right\} \,, \right. \right. \\
           \{-473.305, 1., 1.80506, 1., 1., 0., 473.39, 0.180792\},
```

 $\{-473.305, 0.83586, 1.80506, 1., 1., 0., 473.499, 0.180792\}\}$

■ Plot θ sample and histogram



■ Maximimize likelihood with StanRunOptimize

```
In[45]:= StanRunOptimize["bernoulli"]
Out[45]= method = optimize
       optimize
         algorithm = lbfgs (Default)
           lbfgs
             init_alpha = 0.001 (Default)
             tol_obj = 9.99999999999998e-13 (Default)
             tol_rel_obj = 10000 (Default)
             tol_grad = 1e-08 (Default)
             tol_rel_grad = 10000000 (Default)
             tol_param = 1e-08 (Default)
             history_size = 5 (Default)
         iter = 2000 (Default)
         save_iterations = 0 (Default)
     id = 0 (Default)
       file = /IS006139/home/pix/GitHub/MathematicaStan/Examples/Bernoulli/bernoulli.data.R
     init = 2 (Default)
     random
       seed = 3382357427
     output
       file = /IS006139/home/pix/GitHub/MathematicaStan/Examples/Bernoulli/output.csv
       diagnostic_file = (Default)
       refresh = 100 (Default)
     initial log joint probability = -1711.06
         Iter
                   log prob
                                                               alpha
                                                                          alpha0 # evals Notes
                                   ||dx||
                                               ||grad||
            6
                   -471.393 0.000508262 0.000274025
                                                                  1
                                                                              1
                                                                                        7
     Optimization terminated normally:
       Convergence detected: relative gradient magnitude is below tolerance
    ■ Options manipulation
In[46]:= StanOptionOptimize[]
                                                                       (* list current options *)
      StanSetOptionOptimize["iter",100];
                                                                       (* modify the "iter" option *)
      StanSetOptionOptimize["output file","output_optimize.csv"];
                                                                       (* and the "output file" one *)
     StanOptionOptimize[]
Out[46]= { }
Out[47]= {{iter, 100}, {output file, output_optimize.csv}}
```

Out[51]= { }

■ New run with the new options

```
In[48]:= StanRunOptimize["bernoulli"]
Out[48]= method = optimize
       optimize
         algorithm = lbfgs (Default)
            lbfgs
             init_alpha = 0.001 (Default)
             tol_obj = 9.99999999999998e-13 (Default)
             tol_rel_obj = 10000 (Default)
             tol_grad = 1e-08 (Default)
             tol_rel_grad = 10000000 (Default)
              tol_param = 1e-08 (Default)
             history_size = 5 (Default)
          iter = 100
         save_iterations = 0 (Default)
     id = 0 (Default)
       file = /IS006139/home/pix/GitHub/MathematicaStan/Examples/Bernoulli/bernoulli.data.R
     init = 2 (Default)
     random
       seed = 3382357496
     output
       file = output_optimize.csv
       diagnostic_file = (Default)
       refresh = 100 (Default)
      initial log joint probability = -1724.21
          Iter
                    log prob
                                    ||dx||
                                                 ||grad||
                                                                alpha
                                                                           alpha0 # evals Notes
             6
                    -471.393
                              0.000480461
                                            0.000248854
                                                                                1
     Optimization terminated normally:
       Convergence detected: relative gradient magnitude is below tolerance
    ■ Overwrite and/or reset option
In[49]:= StanSetOptionOptimize["iter",100]
     StanSetOptionOptimize["iter",10]
      StanResetOptionOptimize[]
Out[49]= {{iter, 100}, {output file, output_optimize.csv}}
Out[50]= {{iter, 10}, {output file, output_optimize.csv}}
```