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EE298 HW1

1. How to use:

run:

>> \$ python arriesgado_HW1_EE298.py <your_image.jpg>

The output will be saved in a file named "output.jpg" located in the same directory as the python script

2. Brief notes on the solution

The projective distoriton is of the form $\hat{b} = Hb$, where H is the transformation matrix. This can be rewritten as,

$$\begin{bmatrix} \widetilde{x} \\ \widetilde{y} \\ \widetilde{z} \end{bmatrix} = \begin{bmatrix} p_{11} p_{12} p_{13} \\ p_{21} p_{22} p_{23} \\ p_{31} p_{32} p_{33} \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} \quad \text{where} \quad \begin{bmatrix} \widetilde{x} \\ \widetilde{y} \\ \widetilde{z} \end{bmatrix} \quad \text{and} \quad \begin{bmatrix} x \\ y \\ z \end{bmatrix} \quad \text{are the homogenous coordinates of} \quad \begin{bmatrix} \hat{x} \\ \hat{y} \end{bmatrix} \quad \text{and} \quad \begin{bmatrix} x \\ y \end{bmatrix}$$
 respectively.

$$\widetilde{x} = p_{11}x + p_{12}y + p_{13}z$$

 $\widetilde{y} = p_{21}x + p_{22}y + p_{23}z$
 $\widetilde{z} = p_{31}x + p_{32}y + p_{33}z$

But since,
$$\hat{x} = \frac{\widetilde{x}}{\widetilde{z}}$$
 and $\hat{y} = \frac{\widetilde{y}}{\widetilde{z}}$

$$\hat{x} = \frac{p_{11}x + p_{12}y + p_{13}z}{p_{31}x + p_{32}y + p_{33}z} \text{ and } \hat{y} = \frac{p_{21}x + p_{22}y + p_{23}z}{p_{31}x + p_{32}y + p_{33}z}$$

Rearranging we have,

$$\begin{array}{l} p_{11}x + p_{12}y + p_{13}z - p_{31}x\hat{x} - p_{32}y\hat{x} - p_{33}z\hat{x} = 0 \\ p_{21}x + p_{22}y + p_{23}z - p_{31}x\hat{y} - p_{32}y\hat{y} - p_{33}z\hat{y} = 0 \\ \text{for each pair of point} \quad & (x^{(i)}, y^{(i)}) \land (x^{(i)}, y^{(i)}) \end{array}.$$

With z = 1, this can be written as a 8x9 matrix,

$$\begin{bmatrix} x^{(1)} & y^{(1)} & 1 & 0 & 0 & 0 & -x^{(1)}x^{\hat{1}} & -y^{(1)}x^{\hat{1}} & -x^{\hat{1}} \\ 0 & 0 & 0 & x^{(1)} & y^{(1)} & 1 & -x^{(1)}y^{\hat{1}} & -y^{(1)}y^{\hat{1}} & -y^{\hat{1}} \end{bmatrix} \begin{bmatrix} p_{11} \\ p_{12} \\ p_{13} \\ \vdots \\ p_{33} \end{bmatrix} = 0$$

This is a homogenous system of equations Ax = 0.

The elements of A are known. To determine the values of x, singular value decomposition can be used, i.e. determine the basis of the nullspace of A.

The elements of vector x will be the elements of the tranformation matrix H.

3. Sample transformations

