

## Heterogeneous Population

e.g., single cells

or

individual patients



## Generative Model for Individual ( $i$ )

$$\mathbf{y}^{(i)} = \mathcal{M}(\phi^{(i)})$$

## Model For Population

$$\phi^{(i)} = f(\beta, \mathbf{b}^{(i)}) \quad \text{e.g.,} \quad \phi^{(i)} = \beta + \mathbf{b}^{(i)}$$

with fixed effects  $\beta$

and random effects  $\mathbf{b}^{(i)} \sim p(\theta)$  e.g.,  $\mathbf{b}^{(i)} \sim N(0, \theta)$

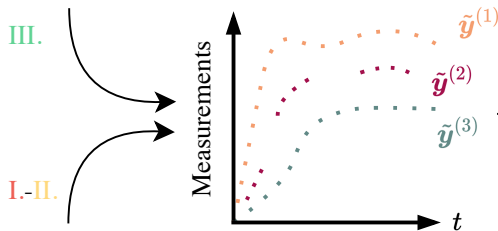
Real Data

$$\tilde{\mathbf{y}}_{\text{obs}}^{(i)} \sim p(\tilde{\mathbf{y}} | \phi^{(i)})$$

Neural Posterior Estimator

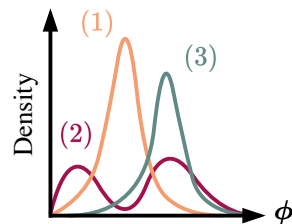
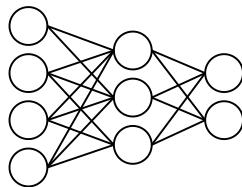
Individual-Specific Posteriors

$$\phi^{(i)} \sim p(\phi | \tilde{\mathbf{y}}_{\text{sim}}^{(i)} \text{ or } \tilde{\mathbf{y}}_{\text{obs}}^{(i)})$$



Simulations

$$\tilde{\mathbf{y}}_{\text{sim}}^{(i)} \sim \mathcal{M}(\phi^{(i)})$$



### I. Simulation Phase

Simulate training data with  
generative model  $\mathcal{M}(\phi)$



### II. Training Phase

Simulation-based training of a  
conditional normalizing flow



### III. Amortized Inference Phase

Efficiently infer population  
characteristics for any new data set