

In [696]:

```
1 %matplotlib inline
2 import pandas as pd
3 import numpy as np
4 import plotly.graph_objects as go
5 from statistics import mean
6 from pyquaternion import Quaternion
7 import matplotlib
8 from matplotlib import pyplot as plt
9 from matplotlib import animation, rc
10 from mpl_toolkits.mplot3d import Axes3D
11 from IPython.display import HTML
12 import math
13 from IPython.core.display import import display, HTML
14 display(HTML("<style>.container { width:100% !important; }</style>"))
15 matplotlib.rcParams['animation.embed_limit'] = 2**128
```

Read in Data and Preprocessing Data

In [697]:

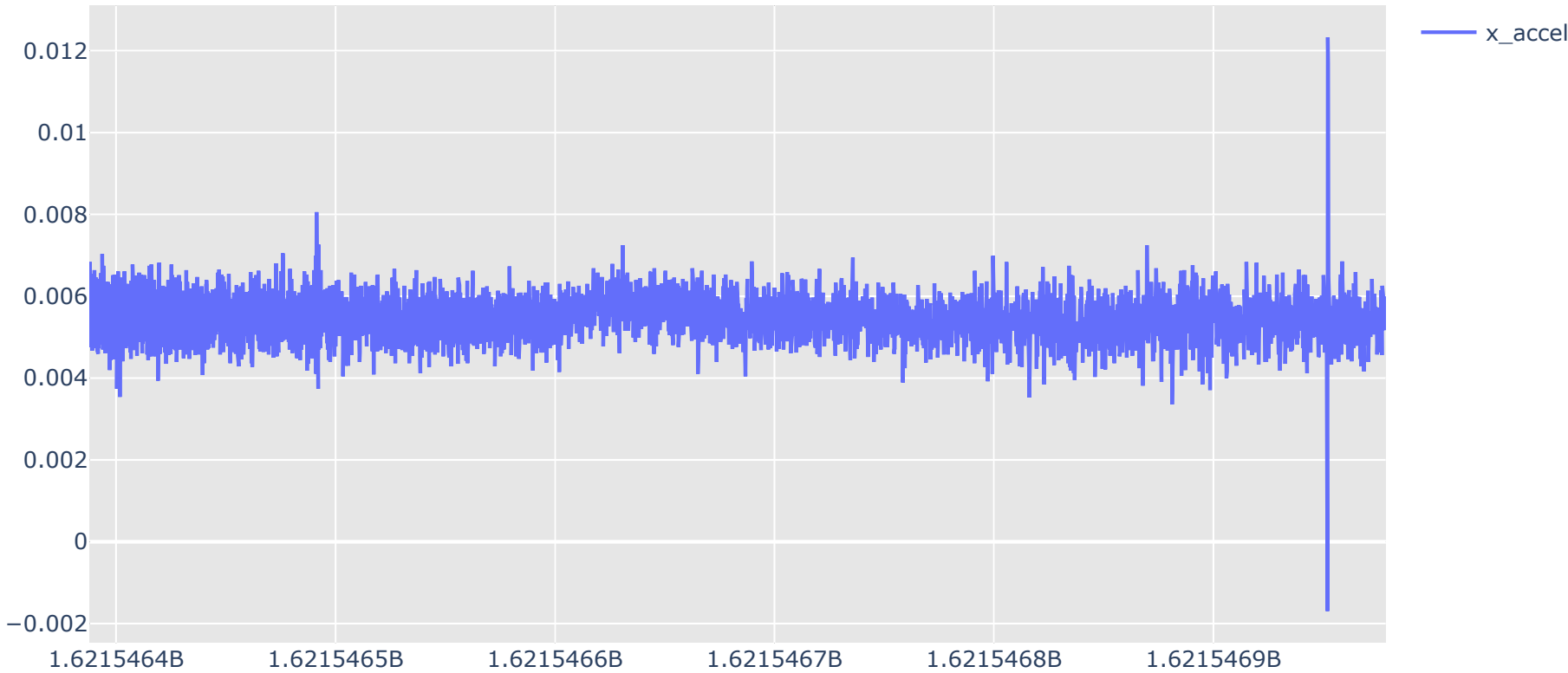
```
1 # ac2 = pd.read_csv('accel_file_1621445529.7862139.txt')
2 # gy2 = pd.read_csv('gyro_file_1621445529.81636.txt')
3
4 # ac2 = pd.read_csv('accel_file_1621471934.548843.txt')
5 # gy2 = pd.read_csv('gyro_file_1621471934.573803.txt')
6
7 ac2 = pd.read_csv('accel_file_1621546377.6777558.txt')
8 gy2 = pd.read_csv('gyro_file_1621546377.7080789.txt')
9
10 new_ac2 = ac2
11 if len(ac2) > len(gy2):
12     new_ac2 = ac2.iloc[0:len(ac2) - 1, 0:]
13
14 cut = len(new_ac2) % 1000 - 1
15 new_ac2 =new_ac2.iloc[cut:len(new_ac2)-0, 0:]
16 new_gy2 =gy2.iloc[cut:len(gy2)-0, 0:]
17
18 new_gy3 = new_gy2[["x","y","z"]]
19 new_ac3 = new_ac2[["x","y","z"]]
20 est_Ws = [] # gyro readings
21 est_local_As = [] # accelerometer readings
22 thresh_hold =100000 #0.06
23
24 for (g_row, g_values), (a_row , a_values) in zip(new_gy3.iterrows(), new_ac3.iterrows()):
25     g_s = [g_values[0] , g_values[1], g_values[2]]
26     a_s = [a_values[0] , a_values[1], a_values[2]]
27     if g_row == cut:
28         est_Ws.append(g_s)
29         est_local_As.append(a_s)
30     elif abs(g_s[0] - est_Ws[len(est_Ws) - 1][0]) > thresh_hold or abs(g_s[1] - est_Ws[len(est_Ws) - 1][1]) > thresh_hold or abs(g_s[2] - est_Ws[len(est_Ws) - 1][2]) > thresh_hold:
31         print("no add: ", g_row)
32
33     else:
34         est_Ws.append(g_s)
35         est_local_As.append(a_s)
```

Accelerometer: Raw Data 5 + Minutes Still

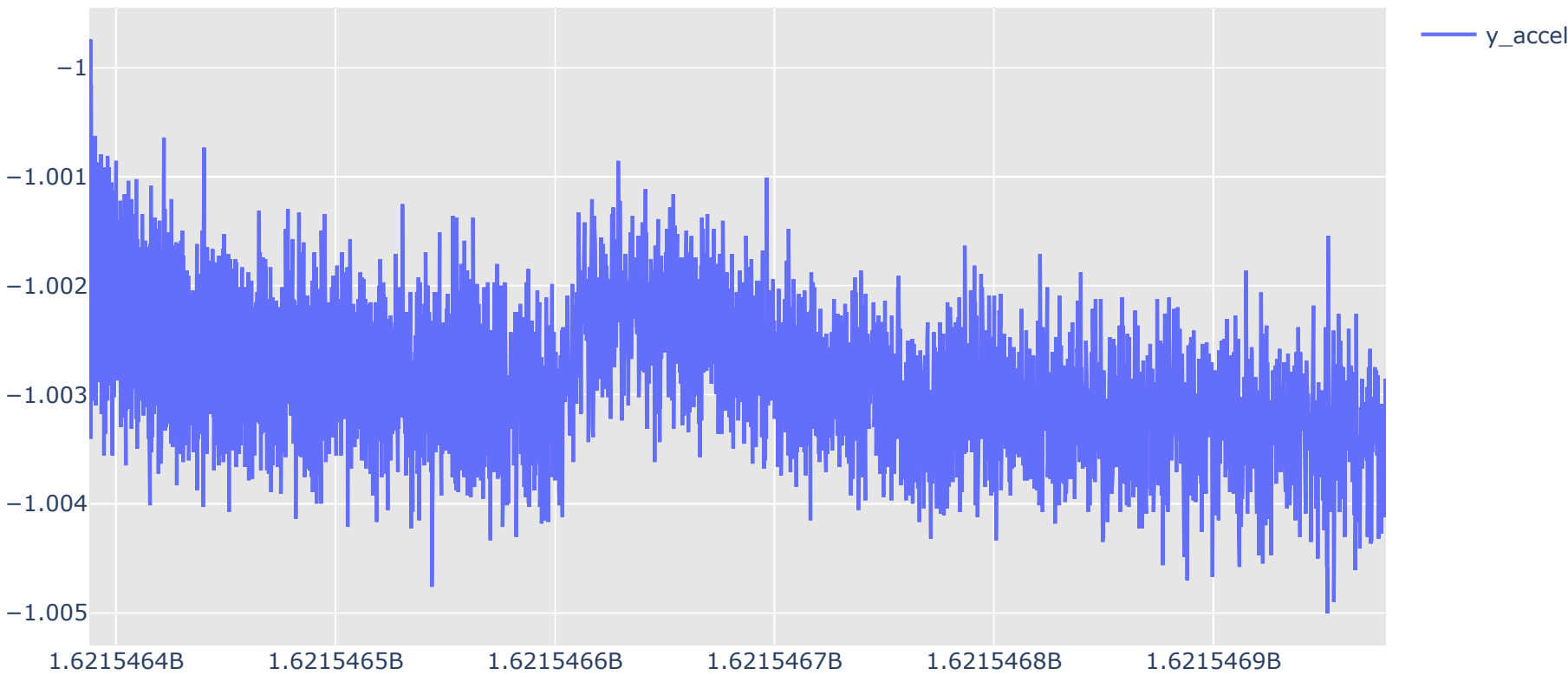
In [698]:

```
1 fig_ac2_x = go.Figure(go.Scatter(x = new_ac2['ts'], y = new_ac2['x'], name='x_accel'))
2 fig_ac2_x.update_layout(title='x_accel vs time', plot_bgcolor='rgb(230, 230,230)', showlegend=True)
3 fig_ac2_y = go.Figure(go.Scatter(x = new_ac2['ts'], y = new_ac2['y'], name='y_accel'))
4 fig_ac2_y.update_layout(title='y_accel vs time', plot_bgcolor='rgb(230, 230,230)', showlegend=True)
5 fig_ac2_z = go.Figure(go.Scatter(x = new_ac2['ts'], y = new_ac2['z'], name='z_accel'))
6 fig_ac2_z.update_layout(title='z_accel vs time', plot_bgcolor='rgb(230, 230,230)', showlegend=True)
7
8
9 fig_ac2_x.show()
10 fig_ac2_y.show()
11 fig_ac2_z.show()
```

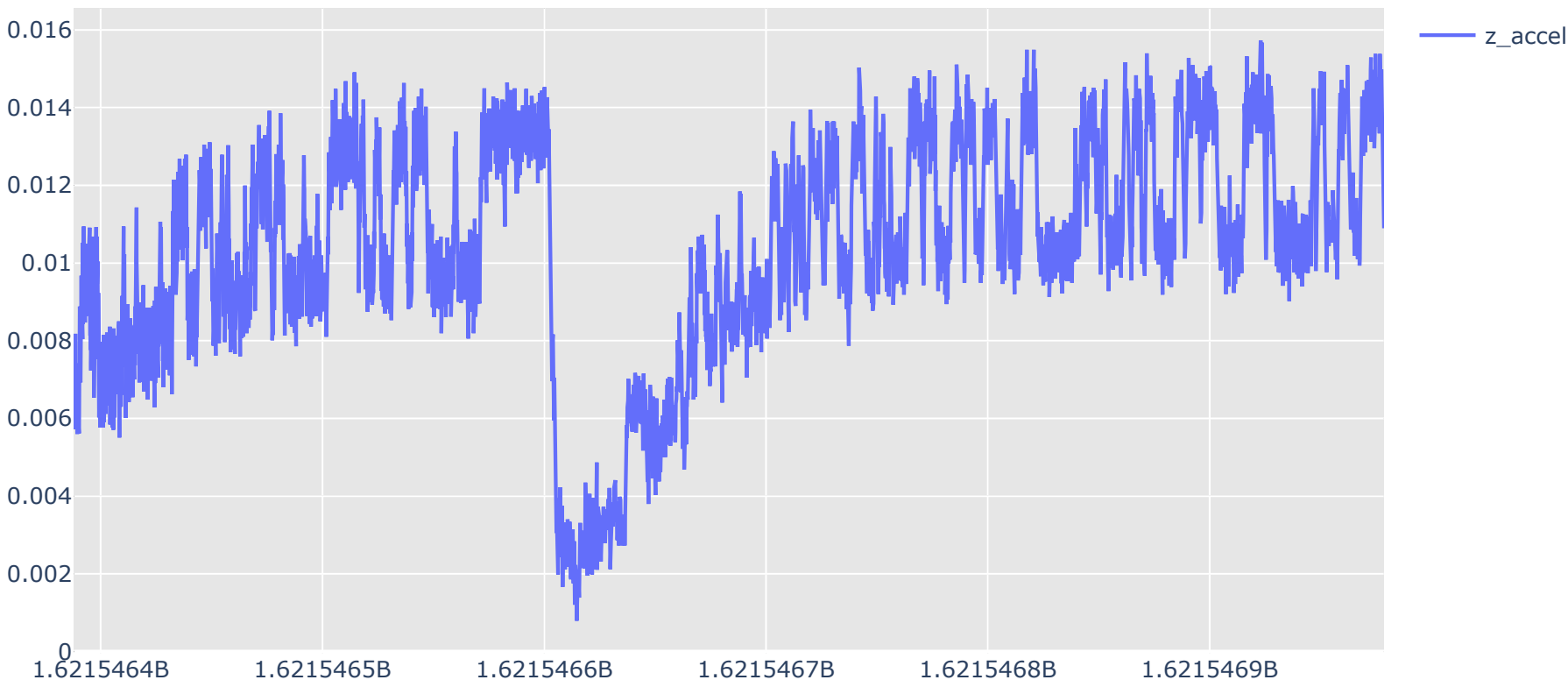
x_accel vs time



y_accel vs time



z_accel vs time



Accelerometer: Axis Bias

In [699]:

```
1 ac2_x_avg = mean(new_ac2['x'])
2 ac2_y_avg = mean(new_ac2['y'])
3 ac2_z_avg = mean(new_ac2['z'])
4 print("x accel bias:",ac2_x_avg,", y accel bias:",ac2_y_avg,", z accel bias:",ac2_z_avg)
```

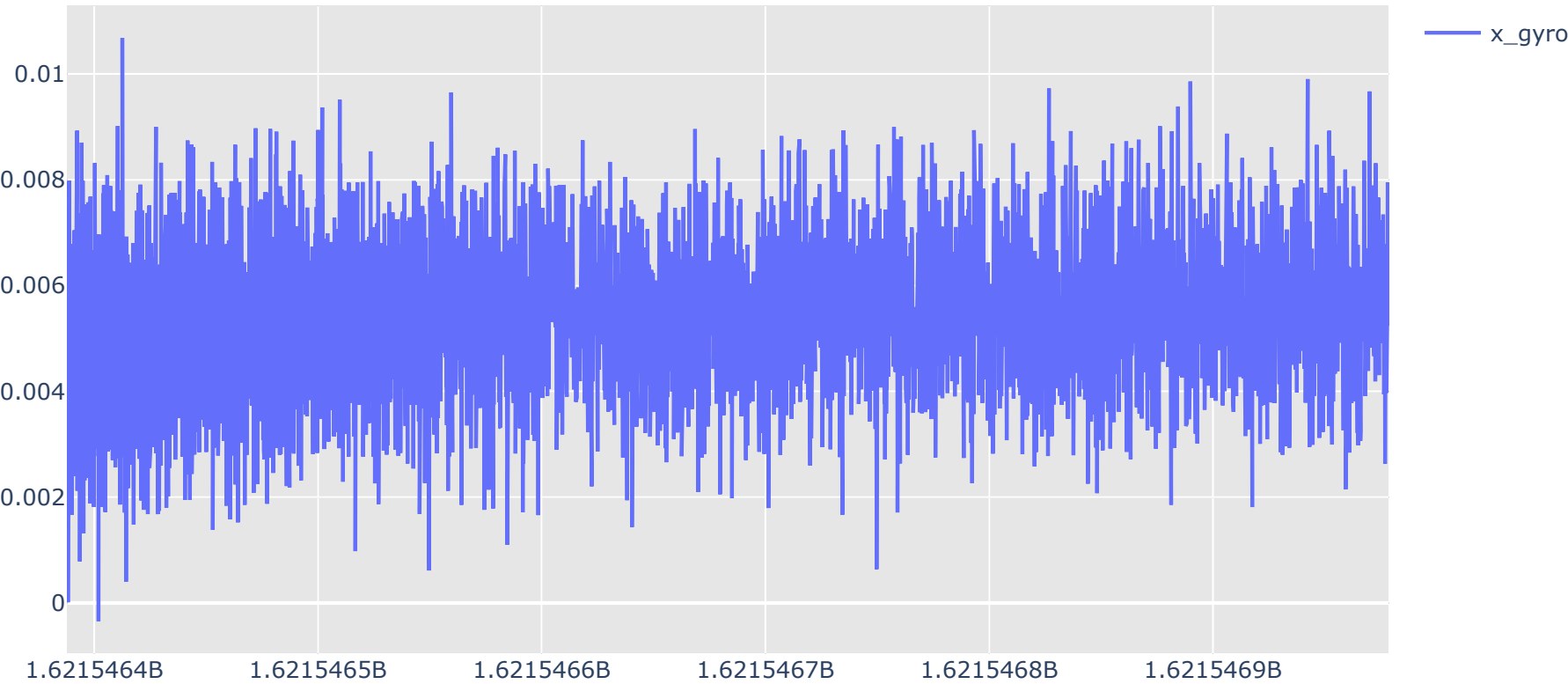
x accel bias: 0.005467154705172836 , y accel bias: -1.0027479983194532 , z accel bias: 0.010190491119318655

Gyro: Raw Data 5 + Minutes Still

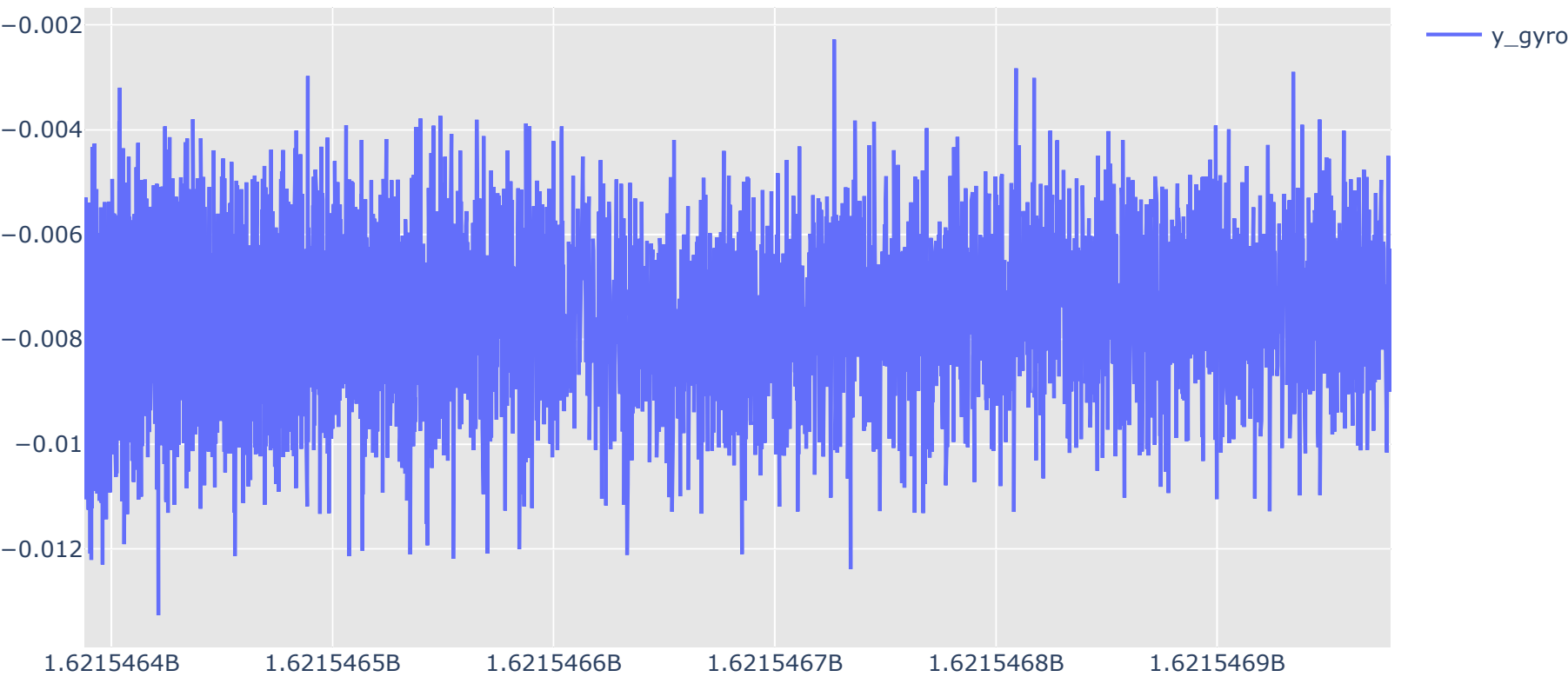
In [700]:

```
1 fig_gy2_x = go.Figure(go.Scatter(x = new_gy2['ts'], y = new_gy2['x'], name='x_gyro'))
2 fig_gy2_x.update_layout(title='x_gyro vs time', plot_bgcolor=rgb(230, 230,230)', showlegend=True)
3 fig_gy2_y = go.Figure(go.Scatter(x = new_gy2['ts'], y = new_gy2['y'], name='y_gyro'))
4 fig_gy2_y.update_layout(title='y_gyro vs time', plot_bgcolor=rgb(230, 230,230)', showlegend=True)
5 fig_gy2_z = go.Figure(go.Scatter(x = new_gy2['ts'], y = new_gy2['z'], name='z_gyro'))
6 fig_gy2_z.update_layout(title='z_gyro vs time', plot_bgcolor=rgb(230, 230,230)', showlegend=True)
7
8
9 fig_gy2_x.show()
10 fig_gy2_y.show()
11 fig_gy2_z.show()
```

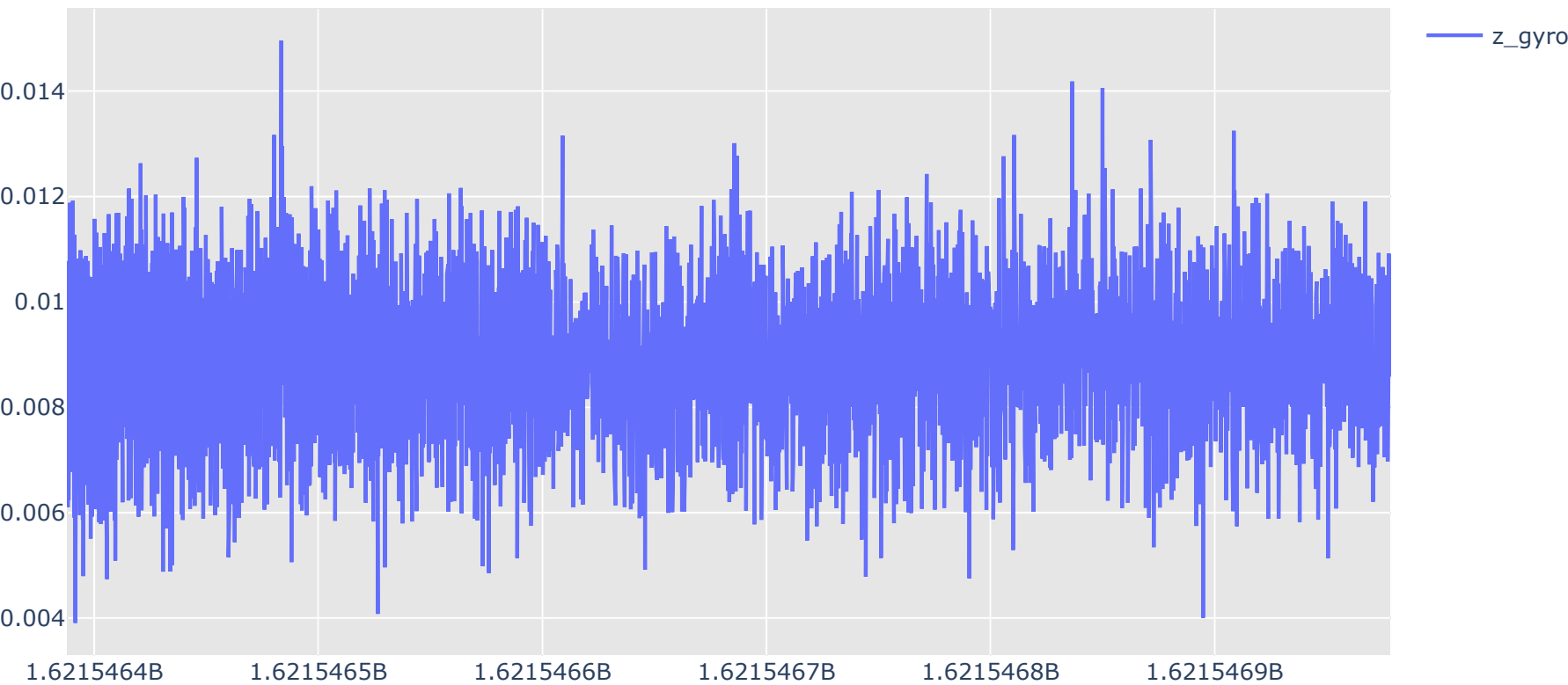
x_gyro vs time



y_gyro vs time



z_gyro vs time



Gyro: Axis Bias

In [701]:

```
1 gy2_x_avg = mean(new_gy2['x'])
2 gy2_y_avg = mean(new_gy2['y'])
3 gy2_z_avg = mean(new_gy2['z'])
4 print("x gyro bias:", gy2_x_avg, ", y gyro bias:", gy2_y_avg, ", z gyro bias:", gy2_z_avg)
```

x gyro bias: 0.005307499035239443 , y gyro bias: -0.0076071045342757816 , z gyro bias: 0.008861463428024074

Gyro

In [702]:

```
1 def w_to_q_0 (w, q_0, group_size, offSets = [-gy2_x_avg, -gy2_y_avg, -gy2_z_avg], sample_rate = 100):
2     """sample_rates = 100 # sensor sample Frequency (Hz)"""
3     delta_t = (1.0 / sample_rates) # time intervals
4     better_w = []
5     better_w.append(w[0] + offSets[0])
6     better_w.append(w[1] + offSets[1])
7     better_w.append(w[2] + offSets[2])
8     l = np.linalg.norm(better_w) # current rate of rotaion (rad/sec)
9     theta = l * delta_t #* group_size # current angle
10    # if (abs(theta) < 0.00005):
11    #     theta = 0
12    v = np.array([(1 / l) * better_w[0], (1 / l) * better_w[1], (1 / l) * better_w[2]]) # current axis of rotation
13    q_w = Quaternion(axis = v, angle = theta)# current angular velocity quarternion
14    next_q_0 = (q_0 * q_w)#.normalised
15    return next_q_0, q_w, theta
16
```

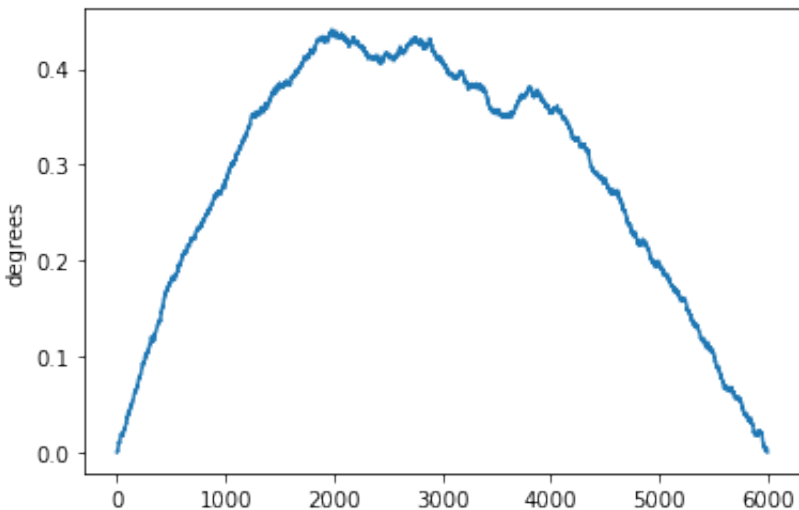
In [741]:

```
1 group_size = 20
2 q_ws = [] # axis-angle representation for estimated angular velocity
3 q_0s = [Quaternion()] # axis-angle representation for estimated orientaion
4 # ^q[0] identity quarterninan
5 # unit Quarterninan (this is a null quaternion
6 # (has no effect on the rotated vector).
7 # For the purposes of quaternion multiplication,
8 # this is a unit quaternion (has no effect when multiplying)
9 # thetas = [] # angles over time
10
11 for est_w, q in zip(est_ws, q_0s):
12     q_0, q_w, _ = w_to_q_0 (est_w, q, group_size)
13     # thetas.append(theta)
14     q_ws.append(q_w)
15     q_0s.append(q_0)
```

Graph: Gyro 5+ min corrected

In [742]:

```
1 # graph tilt error
2 up = [0, 1, 0]
3 gyro_tilt_errors = []
4 for q_0 in q_0s:
5     next_pos = q_0.rotate(up)
6     gyro_tilt_errors.append(math.degrees(np.arccos(np.dot(next_pos, up)/(np.linalg.norm(next_pos) * np.linalg.norm(up)))))
7
8 plt.plot(gyro_tilt_errors)
9 plt.ylabel('degrees')
10 plt.show()
```



Accelerometer

In [743]:

```
1 def a_to_global_a (a, offSets=[-ac2_x_avg, -(ac2_y_avg + 1), -ac2_z_avg], q=Quaternion(), up= [0.0, 1.0, 0.0], g = [0.0, -1.0, 0.0]):
2     better_a = []
3     better_a.append(a[0] + offSets[0])
4     better_a.append(a[1] + offSets[1])
5     better_a.append(a[2] + offSets[2])
6     q_a = Quaternion(axis=np.array(better_a) , radians = np.pi) # For quaternion-vector multiplication,
7     # we assume the vector is converted to a
8     # quaternion as (0, wx , wy , wz )
9
10    # set current estimated global acceloration
11    if(better_a != g):
12        q_G_A = (q.inverse * q_a * q).normalised # ^a = q^(-1) * ~a * q
13        # I think these q's should be the orientaion quarternians derived from the angular velocity
14        # not sure what else they could be
15        # q - an arbitraty orientaion
16
17    else:
18        q_G_A = q_l_A
19
20    a_G = q_G_A.rotate(up) # ^a
21    return a_G
```

In [744]:

```
1 def group_avg(group):
2     group_avg = []
3     for a in group:
4         group_avg.append(minu_g(a))
5     group_avg = abs(np.mean(np.array(group_avg), axis = 0))
6     return group_avg
```

In [745]:

```
1 def minu_g (a, g = [0.0, -1.0, 0.0]):
2     return np.subtract(a, g)
```

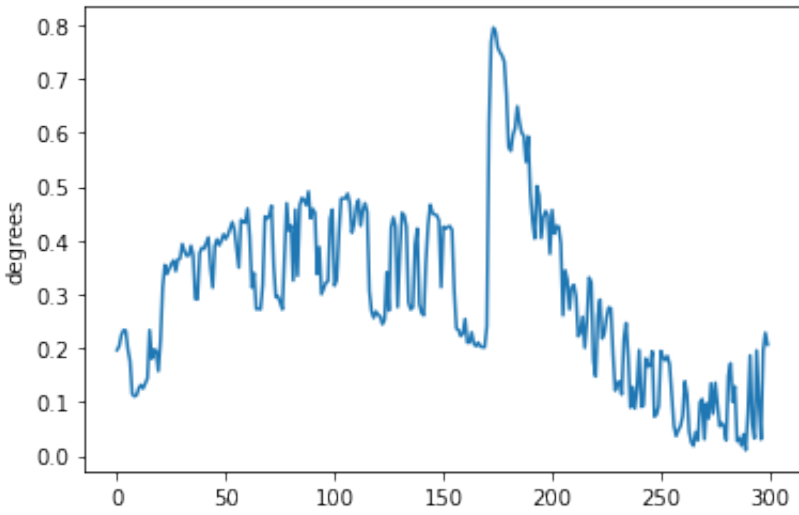
In [746]:

```
1 t = [] # tilt Axies
2 phi_s=[] # tilt error
3 est_global_As = [] # estimated global acceleration
4 aHats = []
5 avg_global_As = [] # we cannot trust accelerometer
6                       # data in the short term.
7                       # However, averaged over a long period of time,
8                       # accelerometer output (in the global frame)
9                       # produces a good estimate for the direction of gravity
10
11 for est_local_A, b_q in zip(est_local_As, q_0s):
12     a_G = a_to_global_a (est_local_A, q = b_q) # try pluggin in the q complementary filter & try doing a constant avg
13     est_global_As.append(a_G)
14
15 G_A_groups = zip(*(iter(est_global_As),) * group_size)
16 for group in G_A_groups:
17     aHat = group_avg(group)
18     t = [aHat[2], 0, -aHat[0]]
19     phi = math.degrees(np.arccos(np.dot(aHat, up)/(np.linalg.norm(aHat) * np.linalg.norm(up))))
20     phi_s.append(phi)
21     for i in range(group_size):
22         avg_global_As.append(aHat)
23
```

Graph: Accelerometer 5+ min corrected

In [747]:

```
1 plt.plot(phi_s)
2 plt.ylabel('degrees')
3 plt.show()
```



Both Gyro and Accelerometer

In [748]:

```
1 def betterQ (t, phi, q_0, alpha):
2     return Quaternion(axis= np.array(t), radians = -alpha * phi).normalised * q_0.normalised
3
```

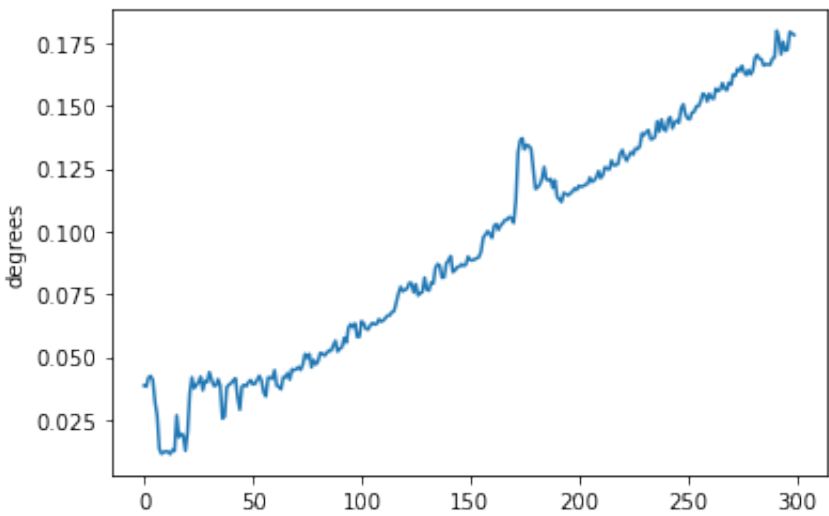
In [750]:

```
1 est_global_As = [] # estimated global acceleration
2 aHats = []
3 alpha = 0.2
4 better_q_0s = [Quaternion()]
5 tiltCorrectedAngle = []
6 avg_global_As = []
7 phi_s=[] # tilt error
8 for est_local_A in est_local_As:
9     a_G = a_to_global_a (est_local_A) # try pluggin in the q complementary filter & try doing a constant avg
10    est_global_As.append(a_G)
11
12 G_A_groups = zip(*(iter(est_global_As),) * group_size)
13 # print()
14 for group in G_A_groups:
15     aHat = group_avg(group)
16     avg_global_As.append(aHat)
17
18 est_Ws_concac = []
19 for i in range(int((len(est_Ws)-1)/group_size)):
20     est_Ws_concac.append(est_Ws[group_size*(i+1)-1])
21
22 # print(len(est_Ws_concac))
23 # print(len(avg_global_As))
24
25 for w, q, aHat in zip(est_Ws_concac, better_q_0s, avg_global_As):
26
27     t = [aHat[2], 0, -aHat[0]]
28     phi = np.arccos(np.dot(aHat, up)/(np.linalg.norm(aHat) * np.linalg.norm(up)))
29     q_0, q_w, _ = w_to_q_0 (est_w, q, group_size)
30     better_q_0 = betterQ(t, phi, q_0, alpha)
31     better_q_0s.append(q_0)
32     news = better_q_0.rotate(up)
33     tiltCorrectedAngle.append(math.degrees(np.arccos(np.dot(news, up)/(np.linalg.norm(news) * np.linalg.norm(up)))))
34
35
```

Graph: Complementary Filter 5+ min corrected

In [751]:

```
1 plt.plot(tiltCorrectedAngle)
2 plt.ylabel('degrees')
3 plt.show()
```



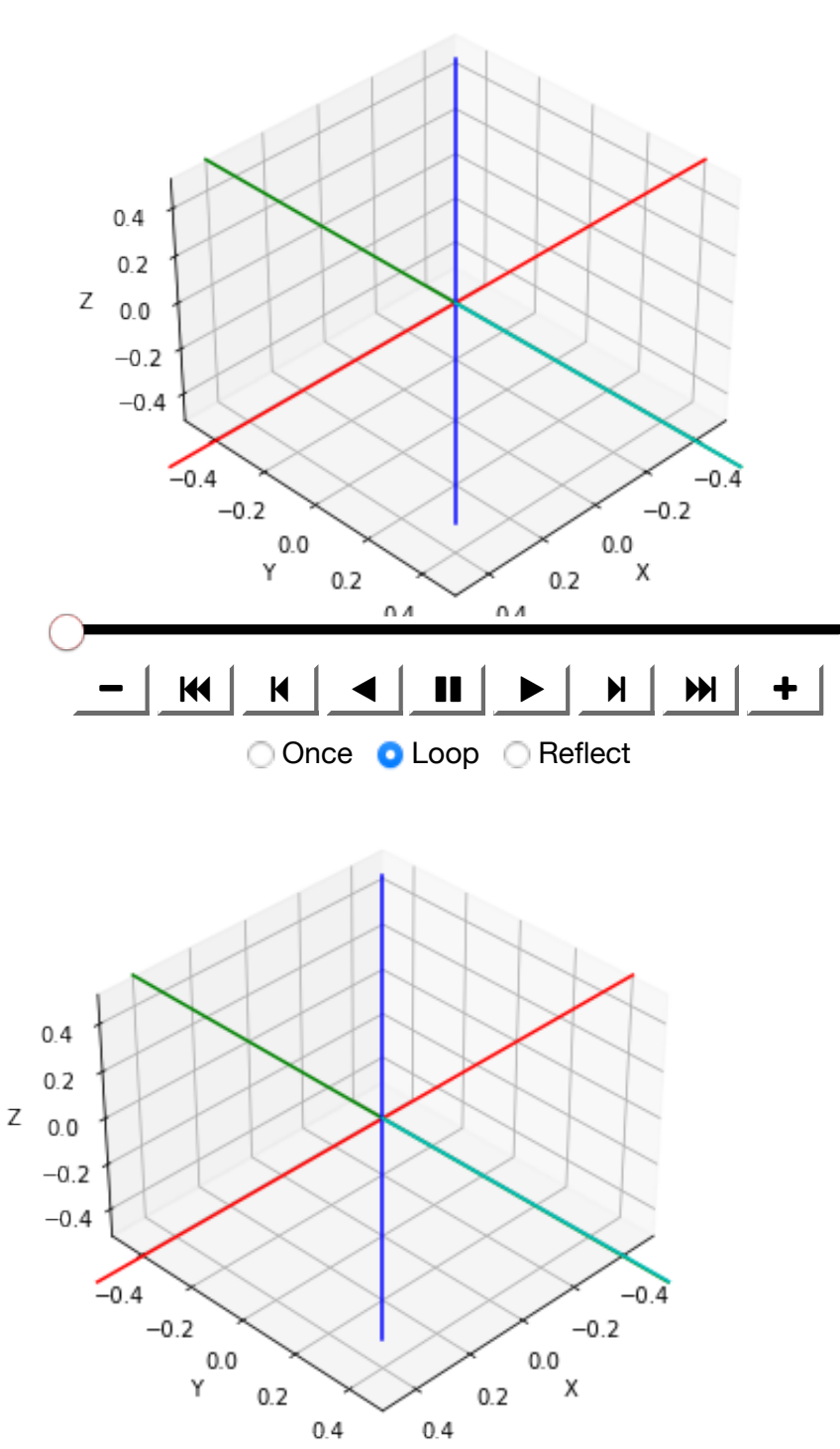
Complementary Filter Sim: No movement

light blue represent the phone very slight giter is visible

In [648]:

```
1 # Set up figure & 3D axis for animation
2 fig = plt.figure()
3 ax = fig.add_axes([0, 0, 1, 1], projection='3d')
4 ax.set_xlabel('X')
5 ax.set_ylabel('Y')
6 ax.set_zlabel('Z')
7 #ax.axis('off')
8
9 # use a different color for each axis
10 colors = ['r', 'g', 'b', 'c', 'm', 'y']
11
12 # set up lines and points
13 lines = sum([ax.plot([], [], [], c=c)
14             for c in colors], [])
15
16 startpoints = np.array([[ -1, 0, 0], [0, -1, 0], [0, 0, -1], [0, 0, 0], [0, 0, 0], [0, 0, 0]])
17 endpoints = np.array([[1, 0, 0], [0, 1, 0], [0, 0, 1], [0, 1, 0], [1, 0, 1], [1, 0, 1]])
18
19 # prepare the axes limits
20 ax.set_xlim((-0.5, 0.5))
21 ax.set_ylim((-0.5, 0.5))
22 ax.set_zlim((-0.5, 0.5))
23
24 # set point-of-view: specified by (altitude degrees, azimuth degrees)
25 ax.view_init(35, 45)
26
27
28 # initialization function: plot the background of each frame
29 def init():
30     for line in lines:
31         line.set_data(np.array([], np.array([]))
32         line.set_3d_properties(np.array([]))
33
34     lines[0].set_data(np.array([startpoints[0][0], endpoints[0][0]]), np.array([startpoints[0][1], endpoints[0][1]]))
35     lines[0].set_3d_properties(np.array([startpoints[0][2], endpoints[0][2]]))
36
37     lines[1].set_data(np.array([startpoints[1][0], endpoints[1][0]]), np.array([startpoints[1][1], endpoints[1][1]]))
38     lines[1].set_3d_properties(np.array([startpoints[1][2], endpoints[1][2]]))
39
40     lines[2].set_data(np.array([startpoints[2][0], endpoints[2][0]]), np.array([startpoints[2][1], endpoints[2][1]]))
41     lines[2].set_3d_properties(np.array([startpoints[2][2], endpoints[2][2]]))
42
43     return lines
44
45 # animation function. This will be called sequentially with the frame number
46 def animate(i):
47
48
49     q = better_q_0s[i]
50
51     start = q.rotate(startpoints[3])
52     end = q.rotate(endpoints[3])
53
54
55     lines[3].set_data(np.array([start[0], end[0]]), np.array([start[1], end[1]]))
56     lines[3].set_3d_properties(np.array([start[2], end[2]]))
57
58     return lines
59
60 # instantiate the animator.
61 anim1 = animation.FuncAnimation(fig, animate, init_func=init,
62                                frames=len(better_q_0s), interval=100, blit=True)
63
64 # Save as mp4. This requires mplayer or ffmpeg to be installed
65 #anim.save('lorentz_attractor.mp4', fps=15, extra_args=['-vcodec', 'libx264'])
66
67 # plt.show()
68 HTML(anim1.to_jshtml())
```

Out [648]:



In []:

```
1
```

