

# Multirate Signal Processing

## Seminar 3

To be presented:

even week – 17.06.21

odd week – 24.06.21

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# Homework assignment

Improve the filters from Homework 2 (everything else stays the same as in HW2):

- a) **Design a new window** (using optimization) to achieve optimal attenuation and transition band (number of taps = 32 )  
Hint: use 32 random coefficients as starting point of your optimization routine, define error function which has to be minimized.
- b) Plot frequency and impuls responses of your window
- c) Use ideal impulse response (sinc) for filter implementation
- d) Using Modulation method with modulation function  
$$N(n) = \cos\left(n \frac{\pi}{N} (k + 0.5)\right)$$
 to implement LP, BP1, BP2, HP filters  
(The band pass filters should be such that all subbands have the same bandwidth)
- e) Plot corresponding frequency and impuls responses VS previous filters to evaluate your improvement.

# Homework assignment

- Listen to the downsampled subband 0
- Listen to the reconstructed signal
- Plot frequency responses of the original and reconstructed signals to see the difference (alias components?)

## Hints:

- Please refer to Lecture slides #6, page 17 “Conclusion”

# Optimization Example

```
import numpy as np
import scipy.optimize as optimize
```

*#Example for 2 unknowns, args: function-name, starting point, method:*

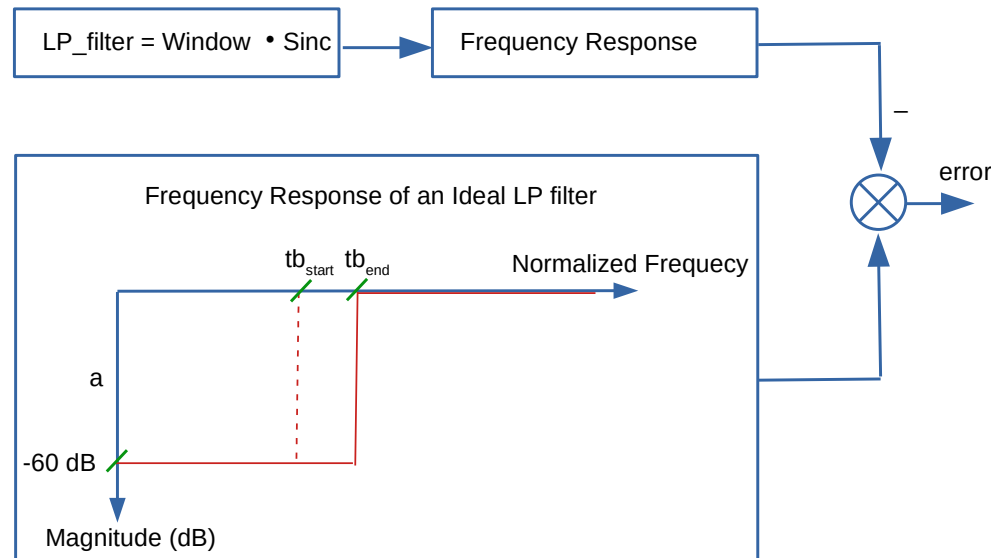
```
def functionexamp(x):
    #x: array with 2 variables

    y=np.sin(x[0])+np.cos(x[1])
    return y
```

```
xmin=optimize.minimize(functionexamp,[-1.0,-3.0], method='CG')
```

```
#Alternative solution: scipy.fminbound
print xmin
```

# Optimization Structure Tips



Optimize (find) coefficients for the *Window* function in such a way that:

1. Attenuation factor as smaller as possible:  $a < -60\ dB$
2. Transition band as smaller as possible:  $tb_{end} - tb_{start} \rightarrow 0$
3. Cut off frequency, which starts from  $tb_{end}$ , has to be defined according to your Downsampling factor
4. The difference between Ideal LP filter and your resulting  $LP\_filter$  has to be as smaller as possible:  $error \rightarrow 0$

***All aforementioned parameters have to be implemented in the code!!!***