

Amir Arsalan Yavari HW6

Using the **partition theorem**, we will solve the problem. If a failure is covered (i.e., fault detected and using the spare component), since our spare component is **a hot spare** and works in synchronization with the primary, the reliability formula will be the same as the reliability of **a parallel system**.

$$R(T_{\text{sys}} | I=1) = R_p(t) + R_s(t) - R_p(t) * R_s(t)$$

If no fault is detected, then the system's reliability is equal to the reliability of the primary component.

$$R(T_{\text{sys}} | I=0) = R_p(t)$$

So the reliability of the entire system is equal to:

$$R(T_{\text{sys}}) = C * R(T_{\text{sys}} | I=1) + (1 - C) * R(T_{\text{sys}} | I=0)$$

Now I define the variables values based on the problem.

$\lambda := 50;$

$C_values := [seq(i, i=0 .. 1, 0.1)];$

$\lambda := 50$

$C_values := [0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0]$

(1)

$color_list := [cyan, yellow, purple, pink, brown, blue, orange, red, black, magenta, green];$

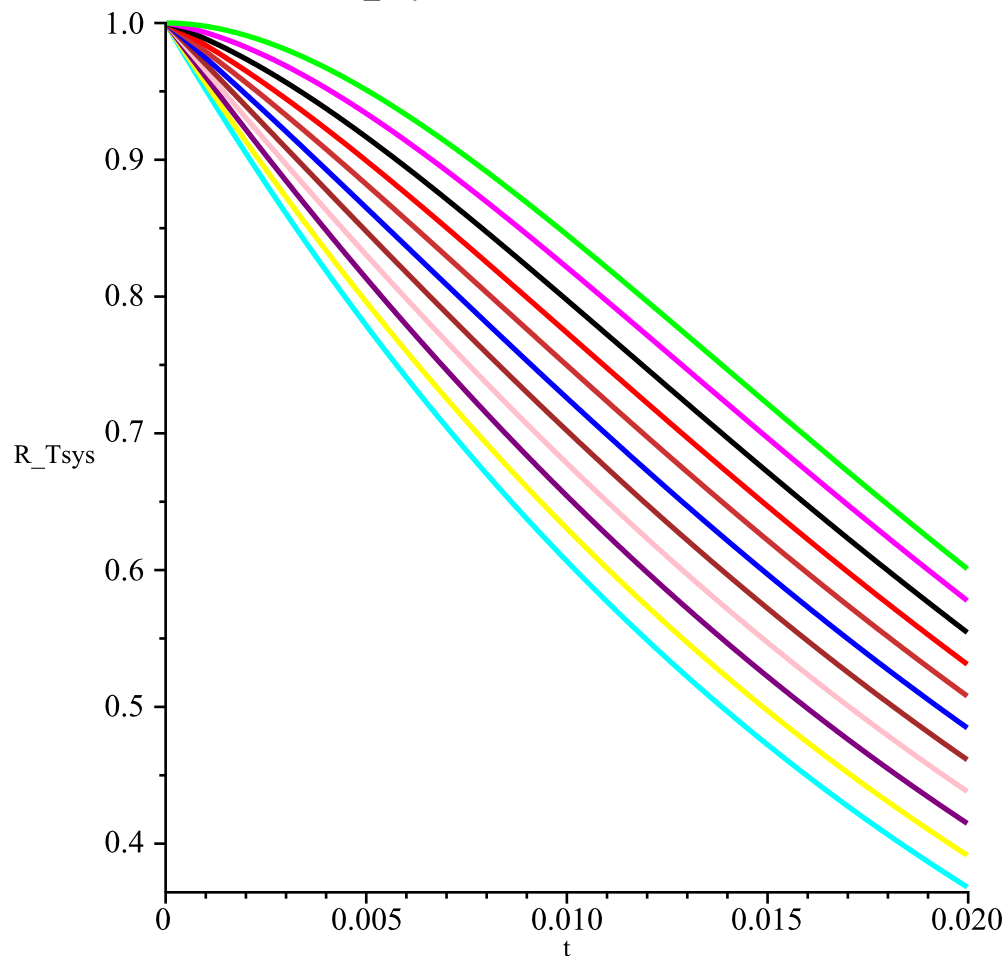
$R(Tsys) := (C, t) \rightarrow C * (2 * \exp(-\lambda * t) - \exp(-2 * \lambda * t)) + (1 - C) * \exp(-\lambda * t);$

$combined_plot := plot([seq(R(Tsys)(C, t), C = C_values)], t = 0 .. 0.02, title = "Plot of R_Tsys for Different Values of C", labels = ["t", "R_Tsys"], color = color_list, thickness = 2);$

$color_list := [cyan, yellow, purple, pink, brown, blue, orange, red, black, magenta, green]$

$R := Tsys \mapsto (C, t) \mapsto C \cdot (2 \cdot e^{-\lambda \cdot t} - e^{-2 \cdot \lambda \cdot t}) + (1 - C) \cdot e^{-\lambda \cdot t}$

Plot of R_Tsys for Different Values of C



I plot the chart in range 0 to 0.02 because of the lambda value is 50.