

#### Technische Universität Berlin

#### Master's Thesis

## Fast Sparse Light Field Reconstruction with Shearlet-based Inpainting

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#### Erklärung

Hiermit erkläre ich, dass ich die vorliegende Arbeit selbstständig und eigenhändig sowie ohne unerlaubte fremde Hilfe und ausschließlich unter Verwendung der aufgeführten Quellen und Hilfsmittel angefertigt habe.

Die selbständige und eigenständige Anfertigung versichert an Eides statt: Berlin, den

4. August 2017

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## Zusammenfassung in deutscher Sprache

# Schnelle Rekonstruktion für Dünne Lichtfelder mit Shearlet-basierten Einfärbungen

Diese These ist angewendete

A Natasha y los años que nos quedan juntos A mi madre Julieta y Padre Héctor sin los cuales nada de esto hubiera pasado A Patricia, Sara y Cristina, por enseñarme cada día lo que es una familia

You don't understand anything until you learn it more than one way.  $Marvin\ Minsky$ 

# Acknowledgements

To my mom. To all of you, thank you very much.

Berlin, September 2017

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## Introduction

Introduction template.

## Light Field Photography

The propagation of the light rays in the 3D space can be completely described by a 7D continuous function  $R(\theta, \phi, \lambda, \tau, V_x, V_y, V_z)$ , where  $(V_x, V_y, V_z)$  is a location in the 3D space,  $(\theta, \phi)$  are propagation angles,  $\lambda$  is the wavelength and  $\tau$  the time; this function is known as the plenoptic function and describes the amount of light flowing in every direction through every point in space an any time, the magnitude of R is known as the radiance. In an 1846 lecture entitled "Thoughts on Ray Vibrations" Michael Faraday proposed for the first time that light could be interpreted as a field, inspired by his work on magnetic fields; but the idea of a plenoptic function representing the spectral radiance distribution of rays was first proposed by Adelson and Bergen [4].

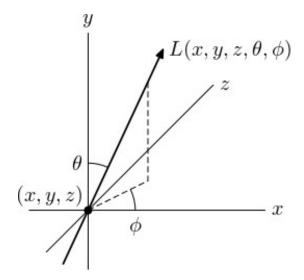


FIGURE 2.1: Spatio-angular parametrization of the plenoptic function for fixed  $\tau$  and  $\lambda$ . Figure taken from Wikipedia (https://en.wikipedia.org/wiki/Light\_field)

In a more practical approach the plenoptic function can be simplified to a 4D version, called 4D Light Field or simply Light Field (abbreviated from now on as LF), denoted as the function L. The LF quantifies the intensity of static and monochromatic light rays propagating in half space, though this seems like an important reduction of information, this constraint does not substantially limit us in the accurate 3D description of the scene from where the light rays come from.

There exists three tipical forms of this 4D approximation:

- 1. The LF rays positions are indexed by their Cartesian coordinates on two parallel planes, also called the two-plane parametrization L(u, v, s, t).
- 2. The LF rays positions are indexed by their Cartesian coordinates on a plane and the directional angles leaving each point,  $L(u, v, \phi, \theta)$ .

3. Pairs of points on the surface of a sphere  $L(\phi_1, \theta_1, \phi_2, \theta_2)$ .

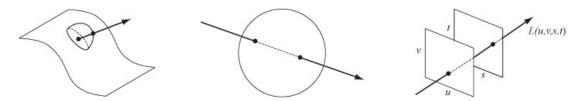


FIGURE 2.2: Three different representations of 4D LF. Left:  $L(u,v,\phi,\theta)$ . Center:  $L(\phi_1,\theta_1,\phi_2,\theta_2)$ . Right: L(u,v,s,t). Figure taken from Wikipedia (https://en.wikipedia.org/wiki/Light\_field)

In this work we will centered our attention in the two plane parametrization L(u, v, s, t), if you are interested in the other descriptions we recommend to see [5]. In order to understand deeply this way of LF description, lets consider a camera with image plane coordinates (u, v) and the focal distance f moving along the (s, t) plane.

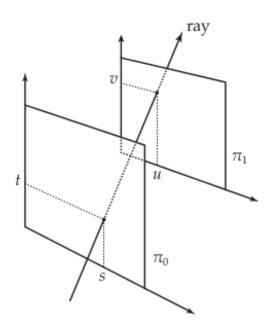


FIGURE 2.3: Graphic representation of the two plane parametrization of a single ray on the LF which is parametrized by the intersection (s,t) and (u,v) with planes  $\pi_0$  and  $\pi_1$ , respectively. Figure taken from [6] p.21

For simplicity one can constrain the vertical camera motion by fixing  $s = s_0$  and moving the camera along the t-axes in an straight light motion, in the section 2.2 we will see that this constraint leads to an elegant geometric 3D representation of the scene called Epipolar Geometry, this multiview aquisition is referred as parallax only (HPO). Under this constraint, images captured by successive camera positions  $t_1, t_2,...$  can be stacked together, and one can also interpret each camera position as a time step.

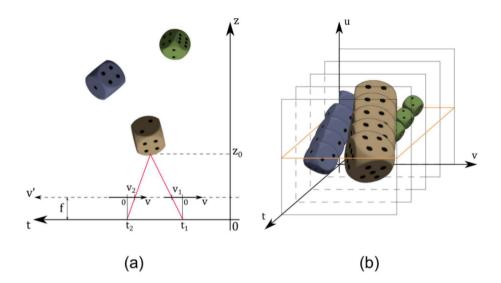


FIGURE 2.4: Stacked captured images represented in (b) from the scene setup (a). Figure taken from [3] p. 2

- 2.1 Light Field Photography in the History
- 2.2 Epipolar Geometry, Stereo Vision and Image rectifictation
- 2.3 Sparse aquisition of Epipolar-plane
- 2.4 Typical applications for the Light Field Theory

## Shearlets

#### Sample of Chapter 3

- 3.1 Shearlets as Frames
- 3.2 Generalization of Shearlets to Alpha Particles
- 3.3 Linear Shearlets and its relation with ridgelets
- 3.4 Image inpainting using Shearlets
- 3.5 Epipolar-plane representation with linear Shearlets

# Inpainting Sparse Sampled Epipolar-plane

Sample of Chapter 4

- 4.1 Using linear Shearlets to inpaint sparse sampled Epipolarplane
- 4.2 Iterative thresholding with constant velocity
- 4.3 Iterative thresholding with vaiable velocity

## Conclusion and outlook

Template of Conclusion, [1]

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