

# Solution to analysis in Home Assignment 1

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# 1 Analysis

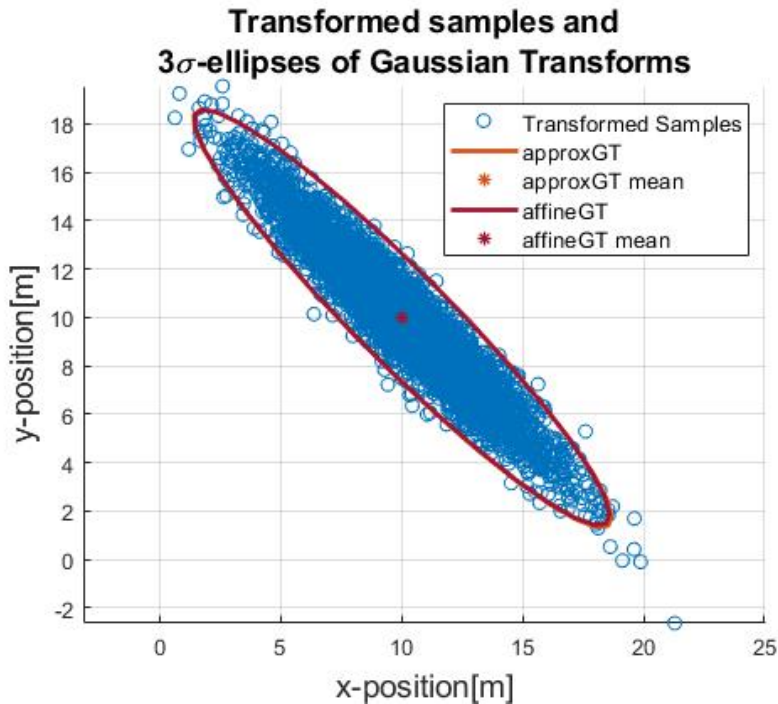
In this report I will present my independent analysis of the questions related to home assignment 1. I have discussed the solution with Karthik Nagaraj and Oskar Begic Johansson but I swear that the analysis written here are my own.

## 2 Transformation of Gaussian random variables

### 2.1 Task (a)

By using both the approxGaussianTransform and the affineGaussianTransform the mean and covariance of the transformed density is calculated.

The plot of the transformed samples from approxGaussianTransform together with mean and 3sigma ellipse is given below:

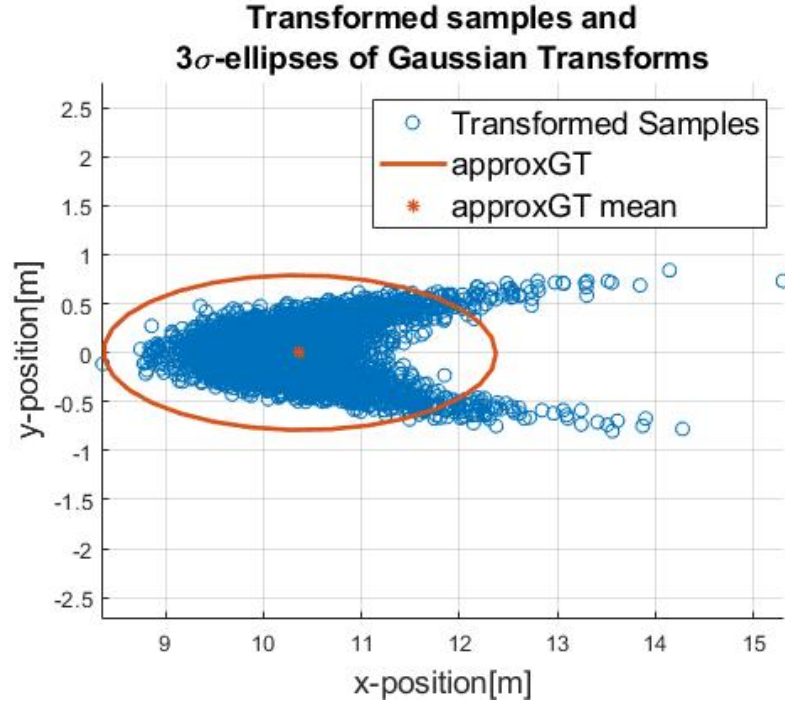


**Figure 1:** plot of the transformed samples with mean and 3sigma ellipse

yes, the ellipses match the sample points well because If  $X$  is the point set of an affine space, then every affine transformation on  $X$  can be represented as the composition of a linear transformation on  $X$  and a translation of  $X$ . Unlike a purely linear transformation, an affine transformation need not preserve the origin of the affine space.

The approximated ellipse's fit to the analytically calculated ellipse because both the mean and covariance of approxGaussianTransform and the affineGaussianTransform we got is perfectly match.

## 2.2 Task (b)



**Figure 2:** plot of the transformed samples with mean and 3sigma ellipse

yeah, the ellipse almost match with the sample points only some of the points are lying outside. The approximated ellipse's fit to true distribution change with number of samples because the approximated mean depends on the samples propagated through f.

## 3 Snow depth in Norway

### 3.1 Task (a)

The plot of  $3\sigma$  -ellipsoid of  $p(x; y)$  for the snow depth at Hafjell and Kvitfjell.

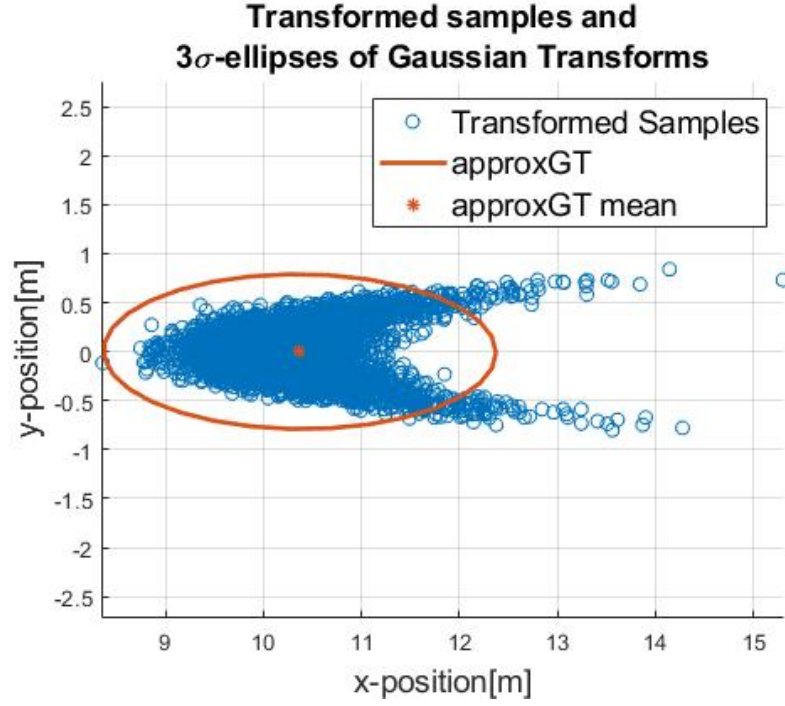


Figure 3: plot of  $3\sigma$  ellipse for Hafjell

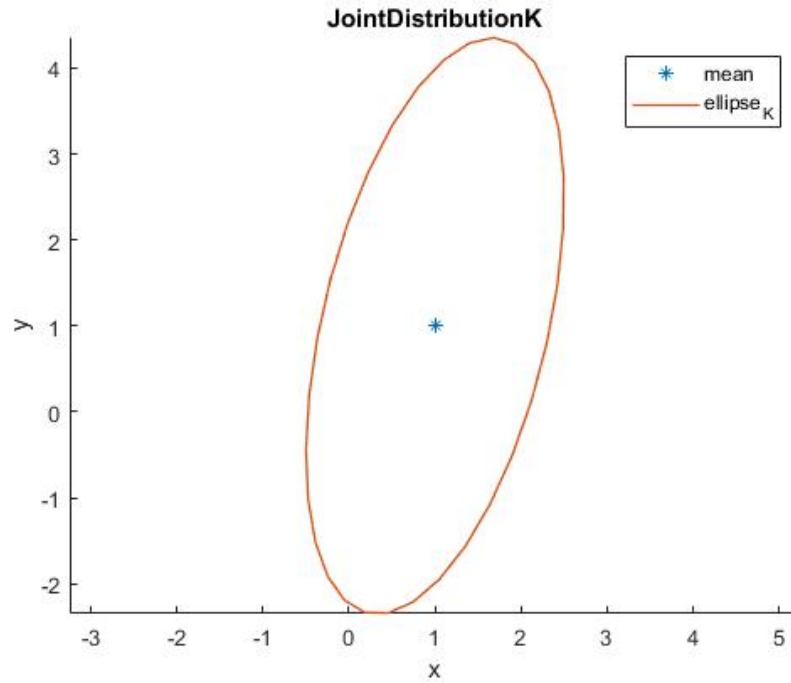
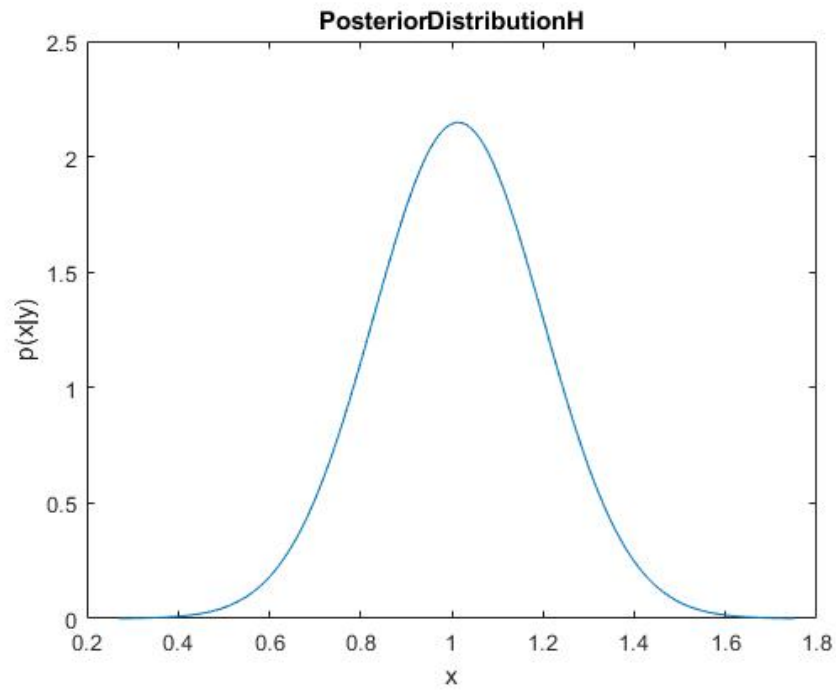


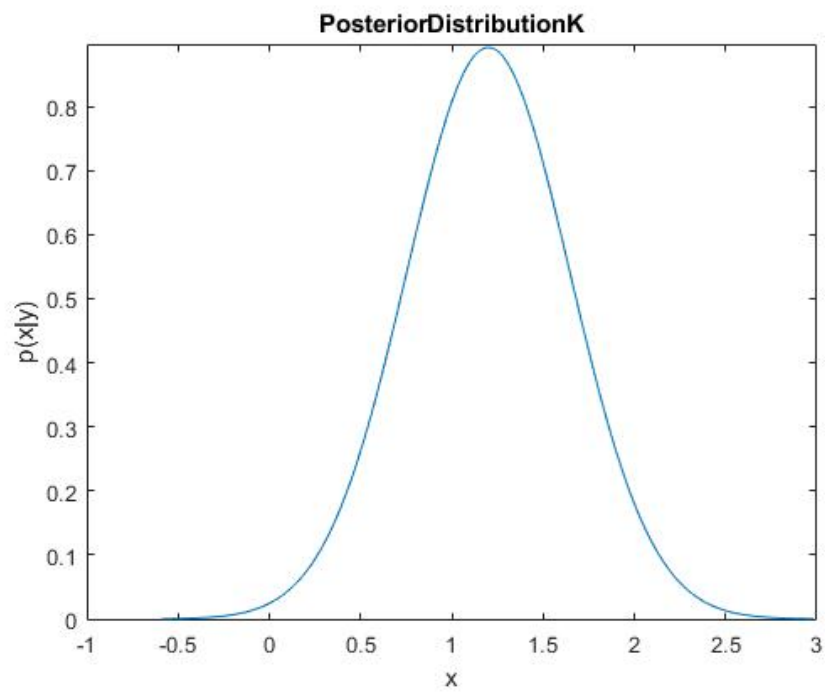
Figure 4: plot of  $3\sigma$  ellipse for Kvitfjell

The slope is randomly picked  $x = 2, 2.5$ . The major axis in Hafjell is high because the depth of hafjell is 1.1 which is high compared to Kvitfjell

### 3.2 Task (b)



**Figure 5:** plot of Posterior distribution for hafjell



**Figure 6:** plot of Posterior distribution for Kvitfjell

since the mean of both the distribution is equal to the mean of both case of ellipse. we can easily identify in the posterior distribution.

### 3.3 task (c)

Based on his decision by maximizing expected snow depth he will choose Hafjell since the chances of getting snow in Hafjell is low compared to Kvitfjell.

## 4 MMSE and MAP estimates for Gaussian mixture posteriors

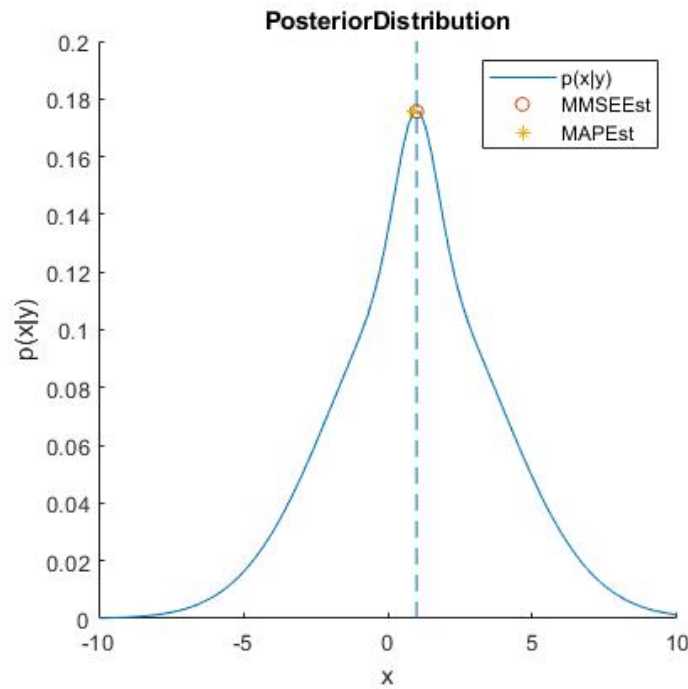


Figure 7: plot a)

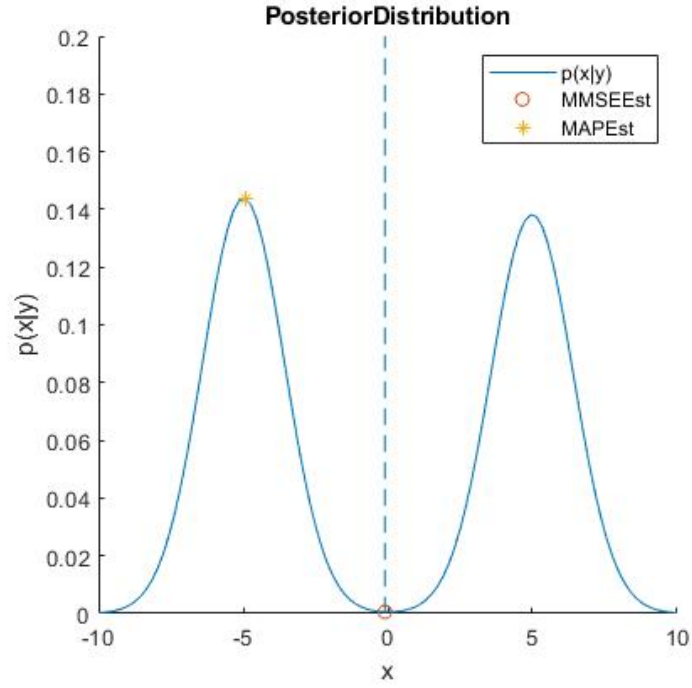


Figure 8: plot b)

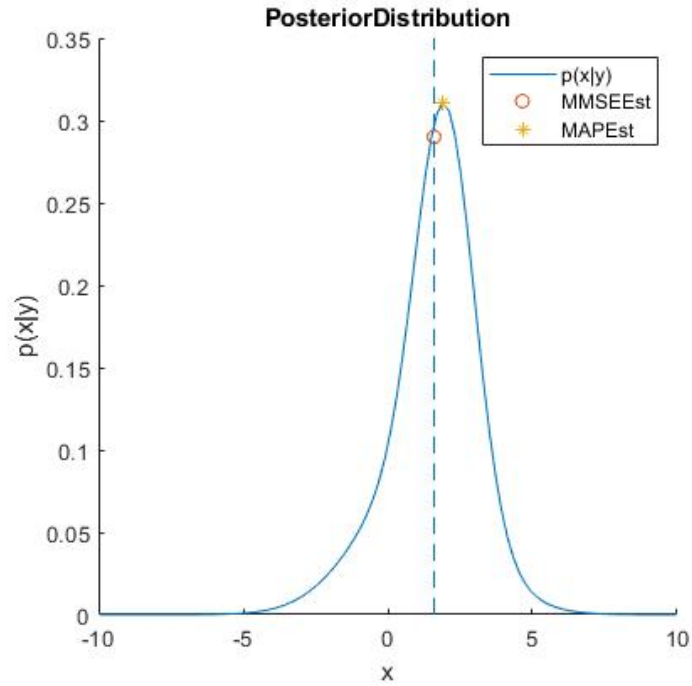


Figure 9: plot c)

(MAP) estimator aims to find and use the sparsest representation, the minimum mean-squared-error (MMSE) estimator a common measure of estimator quality, of the fitted values



of a dependent variable. In some case, the MMSE estimator is given by the posterior mean of the parameter to be estimated. yes if the MAP estimate is ambiguous, it is enough to mark one MAP estimate.