

Set:-

- i) Roster form / Tabular form
- ii) Set-builder form / Rule method / property method

i) Roster form:-

ex:- $\{1, 2, 3\}$

ii) Set-builder form:-

$\{1^2, 2^2, 3^2, 4^2\}$ ✓

$\{x: x = n^2, n \in \mathbb{N}, n \leq 4\}$ ✓

Types of set

i) Null set / empty set / void set:-

1) $\{ \}$ ✓ 2) $\{\emptyset\}$ X 3) \emptyset ✓

2) Singleton set:-

$\{\emptyset\}$ ✓, $\{1\}$ ✓

$\{0, 1, 2\}$ X

3) finite set:-

$\{0, 1, 2, \dots, n\}$ ✓

$n = 100$

4) infinite set:- $\{0, 1, 2, \dots, n\}$ ✓

cardinal number :-

$$A = \{1, 2, 3, 4\}$$

$$n(A) = 4$$

$$B = \{1, 1, 2, 2, 3, 5\}$$

$$n(B) = 4$$

universal set :-

$$A = \{1, 2, 3\}, B = \{5, 4, 2\}$$

$$C = \{1, 2, 3, 4, 5, 6, 7, 8\}$$

C is universal set of A & B

subset :-

$$A = \{0, 1, 2, 3\}$$

$$B = \{1, 2\}$$

$$B \subseteq A$$

* every set is subset of itself.

$$B = \{1, 2\} \rightarrow \text{set}$$

$$B = \{1, 2\} \rightarrow B \subseteq B \quad \checkmark$$

* empty set is subset of every set.

$$\emptyset \subseteq B = \{1, 2, 3\}$$

$$\emptyset \subseteq B$$

1) $A = \{1, 2, 3\}$
 \emptyset

$$A = \{1, 2, 3\}$$

$$A_1 = \{\{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\}, \{1, 2, 3\}, \emptyset, \{2, 3\}\}$$

* Total number of subset = $2^{n(A)}$

$n(A)$ = cardinal number of any set

→ $A = \{1, 2, 3\}$

$$\text{Total no. of subset} = 2^3$$

$$= 8$$

Q $A = \{1, 2, 2, 3, 4, 4\}$

$$\text{Total no. of subset} = 2^4$$

$$= 16$$

1) Union (\cup)

$$A = \{1, 2, 3, 4\}, B = \{5, 1, 3, 4\}$$

$$A \cup B = \{1, 2, 3, 4, 5\}$$

* $A = \{1, 1, 2, 2, 3\}, B = \{1, 2, 5, 5, 3\}$

$$A \cup B = \{1, 2, 3, 5\}$$

2) Intersection (\cap)

$$A = \{1, 2, 3, 4\}, \quad B = \{1, 1, 2, 4\}$$

$$A \cap B = \{1, 2, 4\}$$

3) difference (-)

$$1) \quad A = \{1, 2, 5, 3\}, \quad B = \{5, 2, 1, 1, 3, 4\}$$

1X 2X

$$A - B = \{ \}$$

$$B - A = \{4\}$$

$$2) \quad A = \{1, 2, 3, 4\}, \quad B = \{1, 5, 10, 3\}$$

$$A - B = \{2, 4\}$$

$$B - A = \{5, 10\}$$

complement of a set A :-

$$A' = \bar{A} = U - A$$

$U \Rightarrow$ universal set

$$1) \quad U = \{1, 2, 3, 4, 5\}$$

$$A = \{1, 3\}$$

$$A' = \{2, 4, 5\}$$

$$2) \quad A = \{1, 2, 3\} \quad A' = \text{Set of all real numbers except } \{1, 2, 3\}$$

- 1) $n(A-B) = n(A) - n(A \cap B)$
- 2) $n(B-A) = n(B) - n(A \cap B)$
- 3) $n(A \cup B) = n(A) + n(B) - n(A \cap B)$
- 4) $n(A') = n(U) - n(A)$

$$n(A-B) = n(A) - n(A \cap B)$$

$$A = \{1, 2, 3\}, B = \{2, 3\}$$

$$\rightarrow n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

Q $n(A) = 10, n(B) = 5, n(A \cup B) = 4$
 $n(A \cap B) = ?$

$$\begin{aligned} n(A \cup B) &= n(A) + n(B) - n(A \cap B) \\ 4 &= 10 + 5 - n(A \cap B) \\ n(A \cap B) &= 15 - 4 \\ &= 11 \end{aligned}$$

condition product =

$$A = \{1, 2, 3\}, B = \{10, 20, 4\}$$

$$A \times B = \{(1, 10), (1, 20), (1, 4), (2, 10), (2, 20), (2, 4), (3, 10), (3, 20), (3, 4)\}$$

$$B \times A = \{(10, 1), (10, 2), (10, 3), (20, 1), (20, 2), (20, 3), (4, 1), (4, 2), (4, 3)\}$$

Q If $A = \{1, 4\}$, $B = \{4, 5\}$, $C = \{5, 7\}$
 then determine $(A \times B) \cap (A \times C)$

$$(A \times B) \cap (A \times C)$$

$$(A \times B) = \{(1, 4), (1, 5), (4, 4), (4, 5)\}$$

$$(A \times C) = \{(1, 5), (1, 7), (4, 5), (4, 7)\}$$

$$(A \times B) \cap (A \times C) = \{(4, 5), (1, 5)\}$$

Q Let A, B, C be any three sets then
 prove that $A \times (B \cap C) = (A \times B) \cap (A \times C)$

Suppose $(x, y) \in A \times (B \cap C)$

Q-1. if $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$

$A = \{2, 3, 4, 5, 6\}$ & $B = \{4, 5, 6, 7, 8\}$ then

find—

(i) $n(A)$

(ii) $n(A \cap B)$

(iii) $n(A - B)$

(iv) $n(A \cup B)$

~~(v) $n(A)$ & $n(B)$~~