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Lab Course Scientific Computing

Worksheet 1

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In this worksheet, we study some numerical aspects of the classical two-player game rock-paper-scissors, using MATLAB. In particular, we focus on simple strategies that, in the long run, could benefit both the computer and the human player. The provided files are:

- game.fig contains the graphical user interface and should not be modified
- game.m contains the initialization of the game and the rest of the logic (e.g. handling events) related to the GUI. It may be modified
- mchoice.m contains the "brain" of the game. It may be modified
- gen_human_move.m is a function that generates moves for the human player. It can be used to run a user-defined number of rounds automatically. For the purposes of this worksheet, it should not be modified

The GUI contains a button Save data that permits you to create a .mat file containing the last transition matrix of the game and the results after each round.

- a) In mchoice.m, fill in the implementation of predict1 such that
 - i) it takes two input arguments, j the previous move of the human player, and transm the current predicted transition matrix for the human player
 - ii) it prints the input parameter transm
 - iii) it uses two global variables $param_a$, $param_b$ representing probabilities satisfying $0 < param_a < param_b < 1$
 - iv) it computes the variable *hnext*, representing the *predicted next move of the human player*, using the following algorithm
 - 1) generate a uniform random variable using the built-in function rand
 - 2) remembering that $0 \leq param_a \leq param_b \leq 1$, compute hnext as

$$\label{eq:mod_probability} \begin{aligned} \text{hnext} &= \begin{cases} \text{mod}(j,3) + 1) \quad \text{with probability param_a} \\ \text{mod}(j+1,3) + 1) \quad \text{with probability param_b} - \quad \text{param_a} \\ j \quad \text{with probability } 1 - \text{param_b} \\ \end{aligned}$$

(1)

using the generated uniform random variable to decide which branch to follow

- \mathbf{v}) it returns the variable next = winchoice(hnext)
- b) Analyze the three prediction policy functions (the one implemented in a) and the two existing ones, found in mchoice.m) and fill in the entries of the following table with yes/no:

Property Method	Deterministic	With memory
predict1	Yes	No
predict2	No	Yes
predict3	No	Yes

c) Find (experimentally) the convergence limit of the transition matrix *transm* using the *predict2* policy and the default strategy (implemented in gen_human_move.m) for the human player

Hint: Perform simulations with an increasing number of rounds

- d) Using the functions initmchoice, updatesamplem, and updatetransm, implement the matrices samplem2 and transm2 corresponding to the sample matrix and transmition matrix of the computer player, respectively. Print the computed transm2 matrix at the end of mchoice. Additionally, add transm2 to the list of variables saved to file in game.m.
 - **Hint**: use the last two moves of the computer player saved in the *history* array as additional parameters of the mchoice function.
- e) Similarly to c), find (experimentally) the convergence limit of the transition matrix transm2 using predict3 policy and the default strategy provided by the GUI for the human player
- f) Fill in the matrices below with the results from c) and e)

With Prediction Policy 2
$$transm o \begin{bmatrix} 0.0030 & 0.9911 & 0.0059 \\ 0.0030 & 0.0030 & 0.9940 \\ 0.9940 & 0.0030 & 0.0030 \end{bmatrix}$$
 $transm2 o \begin{bmatrix} 0.0030 & 0.9940 & 0.0030 \\ 0.0059 & 0.0089 & 0.9852 \\ 0.9940 & 0.0030 & 0.0030 \end{bmatrix}$

Questions:

- 1) What is the type of the transition matrix of the game? What properties does it posses?
- 2) Related to exercise **c**): For which of the three prediction strategies of the computer player can it be (intuitively) guaranteed that, in the long run (i.e. an infinite number of rounds), a winning strategy for the human player can be found?