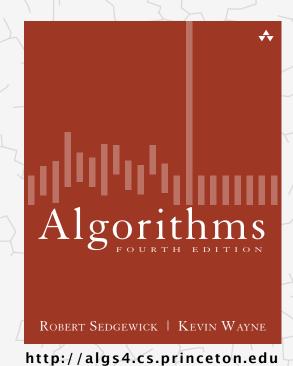
# Algorithms



## 3.5 SYMBOL TABLE APPLICATIONS

- > sets
- dictionary clients
- indexing clients
- sparse vectors

- ▶ sets
- dictionary clients
- indexing clients
- sparse vectors

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#### Set API

Mathematical set. A collection of distinct keys.

<pre>public class SET<key comparable<key="" extends="">&gt;</key></pre>			
	SET()	create an empty set	
void	add(Key key)	add the key to the set	
boolean	<pre>contains(Key key)</pre>	is the key in the set?	
void	remove(Key key)	remove the key from the set	
int	size()	return the number of keys in the set	
Iterator <key></key>	iterator()	iterator through keys in the set	

## Q. How to implement?

#### **Exception filter**

- Read in a list of words from one file.
- Print out all words from standard input that are { in, not in } the list.



## **Exception filter applications**

- · Read in a list of words from one file.
- Print out all words from standard input that are { in, not in } the list.

application	purpose	key	in list
spell checker	identify misspelled words	word	dictionary words
browser	mark visited pages	URL	visited pages
parental controls	block sites	URL	bad sites
chess	detect draw	board	positions
spam filter	eliminate spam	IP address	spam addresses
credit cards	check for stolen cards	number	stolen cards

## Exception filter: Java implementation

- Read in a list of words from one file.
- Print out all words from standard input that are in the list.

```
public class WhiteList
   public static void main(String[] args)
                                                           create empty set of strings
      SET<String> set = new SET<String>();
      In in = new In(args[0]);
      while (!in.isEmpty())
                                                           read in whitelist
         set.add(in.readString());
      while (!StdIn.isEmpty())
         String word = StdIn.readString();
                                                            print words not in list
         if (set.contains(word))
             StdOut.println(word);
```

#### Exception filter: Java implementation

- Read in a list of words from one file.
- Print out all words from standard input that are not in the list.

```
public class BlackList
   public static void main(String[] args)
                                                           create empty set of strings
      SET<String> set = new SET<String>();
      In in = new In(args[0]);
      while (!in.isEmpty())
                                                           read in whitelist
         set.add(in.readString());
      while (!StdIn.isEmpty())
         String word = StdIn.readString();
                                                            print words not in list
         if (!set.contains(word))
             StdOut.println(word);
```

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#### Dictionary lookup

#### Command-line arguments.

- A comma-separated value (CSV) file.
- Key field.
- Value field.

#### Ex 1. DNS lookup.

domain name is key IP is value % java LookupCSV ip.csv 0 1 adobe.com 192.150.18.60 www.princeton.edu 128.112.128.15 domain name ebay.edu IP is kev is value Not found % java LookupCSV ip.csv 1 0 128.112.128.15 www.princeton.edu 999.999.999.99 Not found

```
% more ip.csv
www.princeton.edu,128.112.128.15
www.cs.princeton.edu,128.112.136.35
www.math.princeton.edu,128.112.18.11
www.cs.harvard.edu,140.247.50.127
www.harvard.edu,128.103.60.24
www.yale.edu,130.132.51.8
www.econ.yale.edu,128.36.236.74
www.cs.yale.edu,128.36.229.30
espn.com,199.181.135.201
yahoo.com,66.94.234.13
msn.com,207.68.172.246
google.com,64.233.167.99
baidu.com, 202.108.22.33
yahoo.co.jp,202.93.91.141
sina.com.cn,202.108.33.32
ebay.com,66.135.192.87
adobe.com, 192.150.18.60
163.com, 220.181.29.154
passport.net,65.54.179.226
tom.com,61.135.158.237
nate.com, 203.226.253.11
cnn.com,64.236.16.20
daum.net,211.115.77.211
blogger.com, 66.102.15.100
fastclick.com, 205.180.86.4
wikipedia.org, 66.230.200.100
rakuten.co.jp,202.72.51.22
```

## Dictionary lookup

#### Command-line arguments.

- A comma-separated value (CSV) file.
- Key field.
- Value field.

#### Ex 2. Amino acids.

#### codon is key name is value

```
% java LookupCSV amino.csv 0 3
ACT
Threonine
TAG
Stop
CAT
Histidine
```

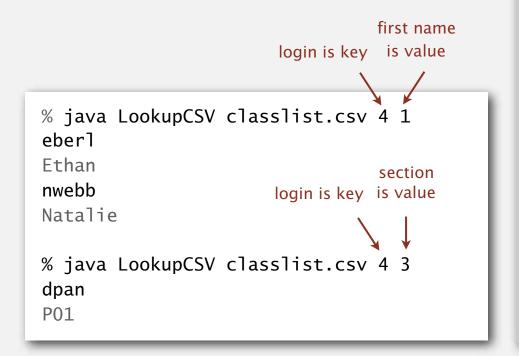
```
% more amino.csv
TTT, Phe, F, Phenylalanine
TTC, Phe, F, Phenylalanine
TTA, Leu, L, Leucine
TTG, Leu, L, Leucine
TCT, Ser, S, Serine
TCC, Ser, S, Serine
TCA, Ser, S, Serine
TCG, Ser, S, Serine
TAT, Tyr, Y, Tyrosine
TAC, Tyr, Y, Tyrosine
TAA, Stop, Stop, Stop
TAG, Stop, Stop, Stop
TGT, Cys, C, Cysteine
TGC, Cys, C, Cysteine
TGA, Stop, Stop, Stop
TGG, Trp, W, Tryptophan
CTT, Leu, L, Leucine
CTC, Leu, L, Leucine
CTA, Leu, L, Leucine
CTG, Leu, L, Leucine
CCT, Pro, P, Proline
CCC, Pro, P, Proline
CCA, Pro, P, Proline
CCG, Pro, P, Proline
CAT, His, H, Histidine
CAC, His, H, Histidine
CAA, Gln, Q, Glutamine
CAG, Gln, Q, Glutamine
CGT, Arg, R, Arginine
CGC, Arg, R, Arginine
```

## Dictionary lookup

#### Command-line arguments.

- A comma-separated value (CSV) file.
- Key field.
- Value field.

#### Ex 3. Class list.



```
% more classlist.csv
13, Berl, Ethan Michael, P01, eberl
12, Cao, Phillips Minghua, P01, pcao
11, Chehoud, Christel, P01, cchehoud
10, Douglas, Malia Morioka, P01, malia
12, Haddock, Sara Lynn, P01, shaddock
12, Hantman, Nicole Samantha, PO1, nhantman
11, Hesterberg, Adam Classen, PO1, ahesterb
13, Hwang, Roland Lee, P01, rhwang
13, Hyde, Gregory Thomas, P01, ghyde
13, Kim, Hyunmoon, P01, hktwo
12, Korac, Damjan, P01, dkorac
11, MacDonald, Graham David, P01, gmacdona
10, Michal, Brian Thomas, PO1, bmichal
12, Nam, Seung Hyeon, P01, seungnam
11, Nastasescu, Maria Monica, PO1, mnastase
11, Pan, Di, P01, dpan
12, Partridge, Brenton Alan, P01, bpartrid
13, Rilee, Alexander, P01, arilee
13, Roopakalu, Ajay, P01, aroopaka
11, Sheng, Ben C, P01, bsheng
12, Webb, Natalie Sue, PO1, nwebb
```

## Dictionary lookup: Java implementation

```
public class LookupCSV
   public static void main(String[] args)
      In in = new In(args[0]);
                                                                         process input file
      int keyField = Integer.parseInt(args[1]);
      int valField = Integer.parseInt(args[2]);
      ST<String, String> st = new ST<String, String>();
      while (!in.isEmpty())
         String line = in.readLine();
         String[] tokens = line.split(",");
                                                                         build symbol table
         String key = tokens[keyField];
         String val = tokens[valField];
         st.put(key, val);
      while (!StdIn.isEmpty())
                                                                         process lookups
         String s = StdIn.readString();
                                                                         with standard I/O
         if (!st.contains(s)) StdOut.println("Not found");
                               StdOut.println(st.get(s));
         else
   }
```

sets

dictionary clients

indexing clients

sparse vectors

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sets

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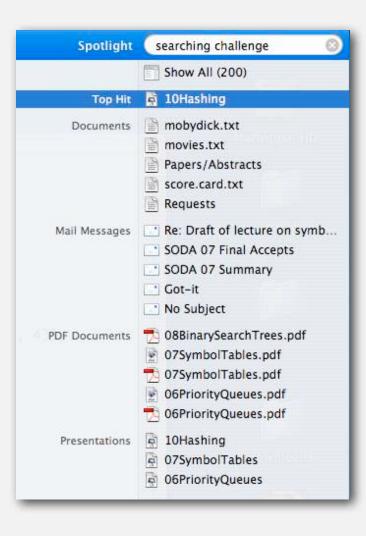
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## File indexing

Goal. Index a PC (or the web).



## File indexing

Goal. Given a list of files specified, create an index so that you can efficiently find all files containing a given query string.

```
% ls *.txt
aesop.txt magna.txt moby.txt
sawyer.txt tale.txt

% java FileIndex *.txt

freedom
magna.txt moby.txt tale.txt

whale
moby.txt

lamb
sawyer.txt aesop.txt
```

```
% ls *.java
BlackList.java Concordance.java
DeDup.java FileIndex.java ST.java
SET.java WhiteList.java

% java FileIndex *.java

import
FileIndex.java SET.java ST.java

Comparator
null
```

Solution. Key = query string; value = set of files containing that string.

## File indexing

```
import java.io.File;
public class FileIndex
   public static void main(String[] args)
                                                                           symbol table
      ST<String, SET<File>> st = new ST<String, SET<File>>();
      for (String filename : args) {
                                                                           list of file names
         File file = new File(filename);
                                                                           from command line
         In in = new In(file);
         while (!in.isEmpty())
                                                                           for each word in file.
             String key = in.readString();
                                                                           add file to
             if (!st.contains(key))
                                                                           corresponding set
                st.put(key, new SET<File>());
             SET<File> set = st.get(key);
             set.add(file);
      while (!StdIn.isEmpty())
         String query = StdIn.readString();
                                                                           process queries
         StdOut.println(st.get(query));
   }
```

#### **Book index**

#### Goal. Index for an e-book.

#### Index

Abstract data type (ADT), 127abstract classes, 163 classes, 129-136 collections of items, 137-139 creating, 157-164 defined, 128 duplicate items, 173-176 equivalence-relations, 159-162 FIFO queues, 165-171 first-class, 177-186 generic operations, 273 index items, 177 insert/remove operations, 138modular programming, 135 polynomial, 188-192 priority queues, 375-376 pushdown stack, 138-156 stubs, 135 symbol table, 497-506 ADT interfaces array (myArray), 274 complex number (Complex), 181 existence table (ET), 663 full priority queue (PQfull), indirect priority queue (PQi), itcm (myItem), 273, 498 key (myKey), 498 polynomial (Poly), 189 point (Point), 134 priority queue (PQ), 375 queue of int (intQueue), 166

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Balanced tree, 238, 555-598 595-598 randomized, 559-564 red-black, 577-585 skip lists, 587-594 splay, 566-571

#### Concordance

Goal. Preprocess a text corpus to support concordance queries: given a word, find all occurrences with their immediate contexts.

# % java Concordance tale.txt cities tongues of the two \*cities\* that were blended in majesty their turnkeys and the \*majesty\* of the law fired me treason against the \*majesty\* of the people in of his most gracious \*majesty\* king george the third princeton no matches

#### Concordance

```
public class Concordance
   public static void main(String[] args)
      In in = new In(args[0]);
      String[] words = in.readAllStrings();
      ST<String, SET<Integer>> st = new ST<String, SET<Integer>>();
      for (int i = 0; i < words.length; <math>i++)
                                                                              read text and
      {
                                                                               build index
         String s = words[i];
         if (!st.contains(s))
            st.put(s, new SET<Integer>());
         SET<Integer> set = st.get(s);
         set.add(i);
      while (!StdIn.isEmpty())
                                                                             process queries
         String query = StdIn.readString();
                                                                               and print
         SET<Integer> set = st.get(query);
                                                                              concordances
         for (int k : set)
             // print words[k-4] to words[k+4]
```

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## Matrix-vector multiplication (standard implementation)

```
      a[][]
      x[]
      b[]

      0 .90 0 0 0 0
      0.05
      .036

      0 0 .36 .36 .18
      .04
      .297

      0 0 0 .90 0
      .36
      =
      .333

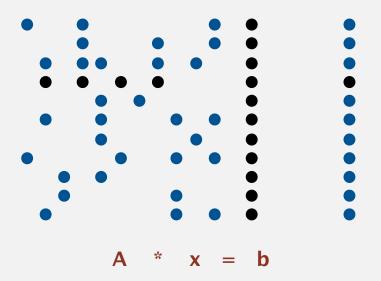
      .90 0 0 0 0 0
      .37
      .045

      .47 0 .47 0 0
      .19
      .1927
```

## Sparse matrix-vector multiplication

Problem. Sparse matrix-vector multiplication.

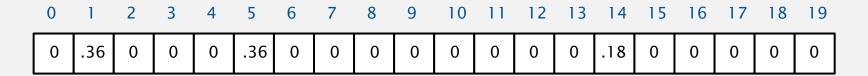
Assumptions. Matrix dimension is 10,000; average nonzeros per row ~ 10.



## Vector representations

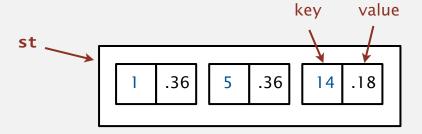
#### 1d array (standard) representation.

- Constant time access to elements.
- Space proportional to N.



#### Symbol table representation.

- Key = index, value = entry.
- Efficient iterator.
- Space proportional to number of nonzeros.



#### Sparse vector data type

```
public class SparseVector
                                                       HashST because order not important
   private HashST<Integer, Double> v;
   public SparseVector()
                                                       empty ST represents all 0s vector
   { v = new HashST<Integer, Double>();
   public void put(int i, double x)
                                                       a[i] = value
   { v.put(i, x); }
   public double get(int i)
      if (!v.contains(i)) return 0.0;
                                                       return a[i]
      else return v.get(i);
   public Iterable<Integer> indices()
      return v.keys(); }
   public double dot(double[] that)
                                                        dot product is constant
                                                       time for sparse vectors
       double sum = 0.0;
       for (int i : indices())
           sum += that[i]*this.get(i);
       return sum;
```

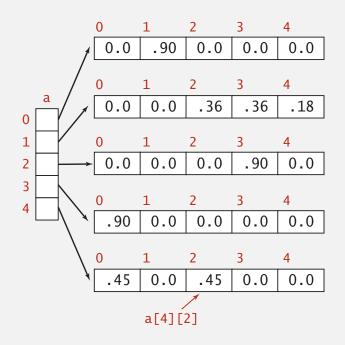
## Matrix representations

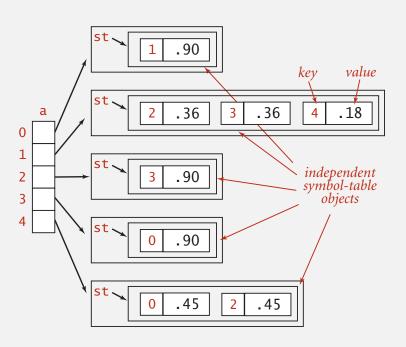
2D array (standard) matrix representation: Each row of matrix is an array.

- Constant time access to elements.
- Space proportional to N<sup>2</sup>.

Sparse matrix representation: Each row of matrix is a sparse vector.

- Efficient access to elements.
- Space proportional to number of nonzeros (plus N).





## Sparse matrix-vector multiplication

```
      a[][]
      x[]
      b[]

      0 .90 0 0 0 0
      0.05
      .036

      0 0 .36 .36 .18
      .04
      .297

      0 0 0 .90 0
      .36
      =

      .90 0 0 0 0
      .37
      .045

      .47 0 .47 0 0
      .19
      .1927
```

```
SparseVector[] a = new SparseVector[N];
double[] x = new double[N];
double[] b = new double[N];
...
// Initialize a[] and x[]
...
for (int i = 0; i < N; i++)
    b[i] = a[i].dot(x);

linear running time
for sparse matrix</pre>
```

sets

dictionary clients

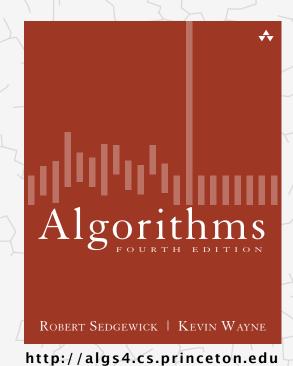
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