### Selected files

#### 9 printable files

```
ycbcr.py
huffman.py
fft.py
complex.py
arithmetic_coding.py
encoder/utils.py
encoder/huffman_jpeg.py
encoder/encoder.py
encoder/comparator.py
```

#### ycbcr.py

```
# Module transforming RGB images into YCbCr
2
   import numpy as np
3
   import numpy.linalg as alg
4
5
   mat = np.array(
   6
7
   )
8
9
   col = np.array([[16, 128, 128]])
10
11
12
   def rgb_to_ycbcr(rgb: tuple) -> tuple:
13
      a = np.asarray(rgb)
14
      b = mat.dot(a)
15
      return tuple(b + col)
16
17
18
   def ycbcr_to_rgb(t: tuple) -> tuple:
19
      a = np.asarray(t)
20
      b = alg.inv(mat)
21
      c = a - col
22
      d = b.dot(c[0])
23
      return tuple(d)
24
```

# huffman.py

```
# Module computing Huffman compression

from collections import Counter, namedtuple
from heapq import heapify, heappop, heappush

# Node in a Huffman Tree
Node = namedtuple("Node", ["char", "freq"])
```

```
11
   class HuffmanCompressor:
        """Huffman compression implementation"""
12
        def __init__(self):
13
14
            self.encoding_table = {}
            self.decoding table = {}
15
16
17
        def build_tables(self, s: str):
18
            """create both the encodingn and decoding tables of a given string
19
20
        parameters
21
        _____
22
            -s : string used to build the tables
23
24
        return
25
        _____
26
            - fill both the encoding and decoding table of the given class instance"""
27
28
            freq_table = Counter(s)
29
30
            # create a heap of the nodes in the tree
31
32
            for char, freq in freq_table.items():
33
                heap.append(Node(char, freq))
34
            heapify(heap)
35
36
            # create the Huffman tree
37
            while len(heap) > 1:
                left_node = heappop(heap)
38
39
                right_node = heappop(heap)
40
                combined_node = Node(None, left_node.freq + right_node.freq)
                heappush(heap, combined_node)
41
42
            def build_encoding_table(node, code=''):
43
                if node.char is not None:
44
45
                    # if the node is a leaf, add it to the encoding table
                    self.encoding table[node.char] = code
46
47
                    return
48
                # if the node is not a leaf, recursively build the encoding table
                build encoding table(node.left, code + '0')
49
50
                build_encoding_table(node.right, code + '1')
51
52
            build_encoding_table(heap[0])
53
54
55
            def build_decoding_table(node, code=''):
                if node.char is not None:
56
57
                    # if the node is a leaf, add it to the decoding table
                    self.decoding_table[code] = node.char
58
59
                    return
                # if the node is not a leaf, recursively build the decoding table
60
                build_decoding_table(node.left, code + "0")
61
62
                build_decoding_table(node.right, code + "1")
63
            build_decoding_table(heap[0])
64
65
66
        def compress(self, s: str) -> str:
67
            """compress the inputed string
```

```
parameters
_____
    -s : string to be compressed
return
    - compressed string"""
    compressed = ""
    for char in s:
        compressed += self.encoding_table[char]
    return compressed
def decompress(self, compressed: str) -> str:
    """decompress the inputed string
parameters
   -s : string to be compressed
return
    - decompressed string"""
    decompressed = ""
    i = 0
   while i < len(compressed):</pre>
        for j in range(i+1, len(compressed)+1):
            if compressed[i:j] in self.decoding_table:
                decompressed += self.decoding_table[compressed[i:j]]
                break
    return decompressed
```

# fft.py

68 69

70

71

72 73

74 75

76

77

78 79

80 81

82

83 84

85

86 87 88

89 90

91 92

93 94

95

96 97 98

99 100

```
# fast-fourier transforms
1
 2
3 import complex as cpx
   from numpy import log2
4
   from cmath import pi, exp, cos
   from scipy.fftpack import dct, idct
6
7
8
9
   def FFT(vector:list) -> list:
       """calculate the fast fourier tranform of a vector
10
11
12
       parameters
13
        _____
14
            -vector : list of Complex object
15
```

```
16
        return
17
18
            1-D fast fourier transform of the vector"""
19
        n = len(vector)
20
        assert log2(n).is_integer(), "make sure that the length of the arguement is a
    power of 2"
21
        if n == 1:
22
            return vector
23
        poly_even, poly_odd = vector[::2] , vector[1::2]
24
        res_even, res_odd = FFT(poly_even), FFT(poly_odd)
25
        res = [cpx.Complex(0)] * n
26
        for j in range(n//2):
27
            w_j = cpx.exp_to_literal(-2*pi*j/n)
28
            product = w_j * res_odd[j]
29
            res[j] = res even[j] + product
30
            res[j + n//2] = res_even[j] - product
31
        return res
32
33
   def IFFT aux(vector:list) -> list:
34
        """auxiliary function that makes the recursive steps of the IFFT algorithm
35
        parameters
36
        _____
37
            -vector : list of Complex object
38
39
        return
40
41
            - partial inverse of the 1-D fast fourier transform of the vector (lack
    the division by n)"""
42
        n = len(vector)
43
        assert log2(n).is_integer(), "make sure that the length of the arguement is a
    power of 2"
        if n == 1:
44
45
            return vector
46
        poly_even, poly_odd = vector[::2] , vector[1::2]
        res_even, res_odd = IFFT_aux(poly_even), IFFT_aux(poly_odd)
47
48
        res = [cpx.Complex(0)] * n
49
        for j in range(n//2):
50
            w_j = cpx.exp_to_literal((2 * pi * j) / n)
51
            product = w_j * res_odd[j]
52
            res[j] = res even[j] + product
53
            res[j + n//2] = res_even[j] - product
54
        return res
55
56
   def IFFT(vector:list) -> list:
        """caclulate the inverse of the fast fourier tranform of a vector (in order to
57
   have ifft(fft(poly)) == poly)
58
59
        parameters
60
61
            -vector : list of Complex object
62
63
        return
64
65
            - inverse of the 1-D fast fourier transform of the vector"""
66
        n = len(vector)
67
        res = IFFT_aux(vector)
68
        for i in range(n):
69
            res[i] = res[i] / cpx.Complex(n)
70
        return res
```

```
72
     def DCT(vector:list, orthogonalize:bool =False, norm="forward"):
73
         """calculate the one-dimensional type-II discrete cosine tranform of a matrix
     (MAKHOUL) (using the FFT function previously defined)
74
75
         parameters
76
77
             - vector: list of Numerical Object
78
79
         return
80
         _____
81
             - discrete cosine tranform of the input"""
82
         N = len(vector)
83
         temp = vector[ : : 2] + vector[-1 - N % 2 : : -2]
84
         temp = FFT(temp)
85
         factor = - pi / (N * 2)
         result = [2 * (val * (cpx.exp_to_literal(i * factor))).re for (i, val) in
86
     enumerate(temp)]
87
         if orthogonalize:
88
              result[0] *= 2 ** (-1 / 2)
         if norm == "ortho":
89
90
              result[0] *= (N) **(-1 / 2)
              result[1::] = [(2 / N) ** (1 / 2) * result[i]  for i in range(1,
91
     len(result))]
92
         return result
93
     def IDCT(vector:list):
94
     """calculate the one-dimensional "inverse" type-III discrete cosine tranform of a matrix (MAKHOUL) (using the FFT function previously defined)
95
96
97
         parameters
98
         _____
99
             - vector: list of Numerical Object
100
101
         return
102
103
             - type-III discrete cosine tranform of the input"""
104
         N = len(vector)
         factor = - pi / (N * 2)
105
         temp = [(cpx.Complex(val) if i > 0 else (cpx.Complex(val) / cpx.Complex(2))) *
106
     cpx.exp_to_literal(i * factor) for (i, val) in enumerate(vector)]
         temp = FFT(temp)
107
         temp = [val.re for val in temp]
108
         result = [None] * N
109
110
         result[::2] = temp[: (N + 1) // 2]
         result[-1 - N % 2 : : -2] = temp[(N + 1) // 2 : ]
111
112
         return result
113
     if name == " main ":
114
115
         vectorCpx= [cpx.Complex(5), cpx.Complex(2), cpx.Complex(4), cpx.Complex(8)]
116
         vector = [5, 2, 4, 8]
         print("DCT : ", DCT(vectorCpx))
117
118
         print("inverse + DCT : ", IDCT((DCT(vectorCpx))))
119
         print("scipy dct :", dct(vector))
         print("scipy + inverse dct: ", dct(idct(vector)))
print("scipy dct (ortho) : ", dct(vector, norm = "ortho"))
120
121
         print("scipy inverse + dct (ortho) : ", idct(dct(vector, norm="ortho"),
122
     norm="ortho"))
```

#### complex.py

```
# Module computing complex numbers
 2
   # disclaimer : this class is not made to deal with less than 1e-10 values
 3
4
5
   from numpy import arctan2, cos, pi, sin, sqrt
   from math import isclose
6
7
   from typing import Union, List
8
9
   class Complex:
10
        """Computing complex numbers"""
11
12
        def __init__(self, real=0., imaginary=0.):
                self.re = real # round(real, 15)
13
14
                self.im = imaginary # round(imaginary,15)
15
        def __str__(self) -> str:
            if self.im == 0.:
16
                string = f"{self.re}"
17
            elif self.re == 0:
18
                string = f"i({self.im})"
19
20
            else:
21
                string = f"{self.re} + i({self.im})"
22
            return string
23
        __repr__ = __str__
        def __eq__(self, other) -> bool:
24
25
            return bool(isclose(self.re, other.re) and isclose(self.im, other.im))
26
        def is_null(self):
27
            return isclose(self.re, 0) and isclose(self.im, 0)
28
        def is real(self):
29
            return isclose(self.im, 0)
30
        def is_imaginary(self):
31
            return isclose(self.re, 0)
32
        def arg(self):
            """return the argument of the complex number
33
            return None if 0"""
34
35
            if self.is null():
36
                arg = None
37
            elif isclose(self.re, 0) and self.im > 0:
38
                arg = pi / 2
39
            elif isclose(self.re, 0) and self.im < 0:</pre>
40
                arg = - pi / 2
41
            else:
42
                arg = round(arctan2(self.im, self.re), 15)
43
            return arg
        def module(self):
44
            """return the module of the complex number"""
45
46
            return round(sqrt(self.re**2 + self.im**2), 15)
47
        def conjuagate(self):
48
            return (Complex(self.re, -self.im))
49
        #arithmetic
50
        def __add__(self, other):
51
            return Complex(self.re + other.re, self.im + other.im)
52
        def __sub__(self, other):
53
            return Complex(self.re - other.re, self.im - other.im)
54
        def __mul__(self, other):
55
            real = (self.re * other.re) - (self.im * other.im)
```

```
imaginary = (self.re * other.im) + (self.im * other.re)
57
             return Complex(real, imaginary)
58
         def __truediv__(self, other):
59
             if other.is_null():
                 raise ValueError("Error : dividing by 0")
60
61
             elif other.is real():
62
                 return Complex(self.re / other.re, self.im / other.re)
63
             else:
64
                 denominator = (other.re ** 2) + (other.im ** 2)
65
                 real = ((self.re * other.re) + (self.im * other.im)) / denominator
                 imaginary = ((self.im * other.re) - (self.re * other.im)) /
66
    denominator
67
                 return Complex(real, imaginary)
68
69
    Num = Union[int, float]
70
    def addition(*complexes:Complex) -> Complex: #partially depreciated (can still be
71
    usefull for more iterable arguments)
72
         """calculate the sum of complex numbers
73
74
         parameters
75
         ______
76
             - *complexes : iterable type of Complex
77
78
         return
79
80
             - sum of the complex numbers"""
81
         res = Complex(0)
82
83
         for number in complexes:
84
             res.re += number.re
85
             res.im += number.im
86
         return res
87
88
    def difference(cpx1:Complex, cpx2:Complex = Complex(0)): #fully depreciated
     (replaced by __sub__ Complex methods)
         """calculate the difference of two complex numbers
89
90
91
         parameters
92
93
             - cpx1 : Complex number
             - cpx2 : Complex number to subtract to cpx1 (=Complex(0) by default)
94
95
96
         return
97
98
                 difference of the two complex numbers"""
99
         res = Complex()
100
         res.re = cpx1.re - cpx2.re
101
         res.im = cpx1.im - cpx2.im
102
         return res
103
    def product(*complexes:Complex) -> Complex: #partially depreciated (can still be
104
    usefull for more iterable arguments)
105
         """calculate the product of complex numbers
106
107
         parameters
108
         _____
109
             - *complexes : iterable type of Complex
110
```

```
return
112
113
             - product of the complex numbers"""
114
         res = Complex(1)
115
         for number in complexes:
116
             re = res.re * number.re - res.im * number.im
117
             im = res.re * number.im + res.im * number.re
118
             res.re = re
119
             res.im = im
120
         return res
121
    def exp_to_literal(arg:float, module:float = 1.0) -> Complex:
122
123
         """ return the literal expression of a complex number defined by its argument
    and module
124
125
         parameters
126
         _____
127
             - arg : type(float) (should be between 0 and 2pi)
128
             - module : type(float) (must have a positive value)(=1 by default)
129
130
         return
131
132
             Complex number associated"""
         assert(module >= 0), "second-argument(module) must have a positive value"
133
         return Complex(module*cos(arg), module*sin(arg))
134
135
136
    def nth_root(n:int, cpx:Complex = Complex(1)) -> Complex:
         """calculate the nth root of a complex number
137
138
139
         parameters
140
         -----
141
             - n : type(int)
142
             complex : type(Complex) (=Complex(1) by default) (must not be
    Complex(0))
143
144
         return
145
146
             - list of the nth roots"""
         assert(cpx.re != 0 or cpx.im != 0), "second argument must be a non-zero
147
    complex number"
148
        module = cpx.module()
         arg = cpx.arg()
149
150
         if arg is not None:
151
             return exp to literal((arg/n), module**(1/n))
152
153
             return Complex(1) #Not used case but just here to ensure nth_root cannot
     return None
154
155
156
    def nth_roots_unity(n:int) -> list:
         """ calculate the n roots of unity
157
158
159
         parameter
160
         _____
161
             - n : type(int) : must be a positive integer
162
163
         return
164
             - a list of Complex containing the n roots of unity"""
165
```

```
roots = [Complex(1) for i in range(n)]
166
167
         for k in range(0,n):
168
             roots[k] = exp_to_literal((2*k*pi/n), 1.0)
169
         return roots
170
171
    def inverse_nth_roots_unity(n:int) -> list:
         """ calculate the inversed n roots of unity
172
173
174
         parameter
175
176
         - n : type(int) : must be a positive integer
177
178
         return
179
         _____
         - a list of Complex containing the inversed n roots of unity"""
180
         roots = [Complex(1) for i in range(n)]
181
182
         for k in range(0,n):
             roots[k] = exp_to_literal((-2*k*pi/n), 1.0)
183
184
         return roots
185
186
    def make_complex(values:List[Num]) -> List[Complex]:
187
         res = []
         for value in values:
188
189
             res.extend([Complex(value)])
190
         return res
191
192
    if __name__ == "__main__":
193
194
         pass
195
```

# arithmetic coding.py

```
def proba(data):
1
 2
3
        Créer le dictionnaire de probabilités d'apparition des différents caractères
4
5
        assert len(data) != 0
6
        d = \{\}
7
        for x in data:
8
            d[x] = d.get(x, 0) + (1 / len(data))
9
        return d
10
11
12
   def create_int(data):
13
        Créer le dictionnaire des intervalles des différents caractères connaissant
14
    les données
        0.000
15
16
        p = proba(data)
17
        d = \{\}
        n = 0.0
18
19
        for c, v in p.items():
20
            d[c] = (n, n + v)
            n += v
21
```

```
22
        return d
23
24
25
   def create_int2(p):
26
27
        Créer le dictionnaire des intervalles des différents caractères connaissant
    les probas des différents caractères
28
29
        d = \{\}
30
        n = 0.0
31
        for c, v in p.items():
32
            d[c] = (n, n + v)
33
            n += v
        return d
34
35
36
37
   def encode(data):
38
39
        effectue l'encodage des données
40
41
        int = create_int(data)
42
        value = (0.0, 1.0)
        for x in data:
43
            d = value[1] - value[0]
44
45
            sup = value[0] + d * int[x][1]
46
            inf = value[0] + d * int[x][0]
47
            value = (inf, sup)
        return (value[0] + value[1]) / 2
48
49
50
51
    def appartient(x, int):
52
53
        teste l'appartenance de x à un intervalle fermé à gauche et ouvert à droite
54
55
        assert len(int) == 2
        return x >= int[0] and x < int[1]
56
57
58
59
   def inverse(dic):
60
61
        renvoie le dictionnaire où les clés et valeurs sont inversées
        0.00
62
63
        d = \{ \}
64
        for c, v in dic.items():
65
            d[v] = c
66
        return d
67
68
69
    def decode(n, p, nbr_carac):
70
        d = inverse(create_int2(p))
71
        res = []
72
        i = n
73
        while len(res) < nbr_carac:</pre>
74
            for c, v in d.items():
75
                 if appartient(i, c):
76
                     res.append(v)
77
                     i = (i - c[0]) / (c[1] - c[0])
78
                     break
79
        return res
```

```
80
81
82
    # Examples
83
    if __name__ == "__main__":
84
85
         print(encode("WIKI"))
         print(decode(0.171875, {"W": 0.25, "I": 0.5, "K": 0.25}, 4))
86
87
         print(encode("AAABBCCCCC"))
88
         print(decode(0.010783125000000005, {"A": 0.3, "B": 0.2, "C": 0.5}, 10))
89
         print(encode([1, 2, 3, 4, 5, 6, 7, 8, 9, 10]))
90
         print(
91
             decode(
92
                 encode([1, 2, 3, 4, 5, 6, 7, 8, 9, 10]),
93
94
                      1: 0.1,
95
                      2: 0.1,
                      3: 0.1,
96
97
                      4: 0.1,
98
                      5: 0.1,
99
                      6: 0.1,
                      7: 0.1,
100
101
                      8: 0.1,
102
                      9: 0.1,
                      10: 0.1,
103
104
                 },
                 10,
105
106
             )
         )
107
108
```

## encoder/utils.py

```
import numpy as np
 2
   import math
 3
    import cv2
    from io import BytesI0
 4
 5
 6
 7
    # DCT block size
 8
    BH, BW = 8, 8
 9
10
11
    class MARKER:
12
        SOI = b"\xff\xd8"
13
        APP0 = b" \xff \xe0"
        APPn = (b'')xff'xe1'', b'')xff'xef'') # n=1\sim15
14
15
        DOT = b" \setminus xff \setminus xdb"
16
        SOF0 = b"\xff\xc0"
17
        DHT = b"\xff\xc4"
18
        DRI = b"\xff\xdd"
19
        SOS = b"\xff\xda"
20
        EOI = b"\xff\xd9"
21
22
```

```
def __init__(self, id_, horizontal, vertical, qt_id, dc_ht_id, ac_ht_id):
24
25
            self.id_ = id_
26
            self.horizontal = horizontal
27
            self.vertical = vertical
28
            self.qt_id = qt_id
29
            self.dc_ht_id = dc_ht_id
            self.ac_ht_id = ac_ht_id
30
31
32
        @classmethod
        def default(cls):
33
            return cls.__init__(*[0 for _ in range(6)])
34
35
36
        def encode SOS info(self):
37
            return int2bytes(self.id_, 1) + int2bytes(
                (self.dc_ht_id << 4) + self.ac_ht_id, 1
38
39
            )
40
        def encode_SOF0_info(self):
41
42
            return (
43
                int2bytes(self.id_, 1)
44
                + int2bytes((self.horizontal << 4) + self.vertical, 1)</pre>
45
                + int2bytes(self.qt_id, 1)
46
            )
47
48
        def __repr__(self):
49
            return (
                f"{self.id_}: qt-{self.qt_id}, ht-(dc-{self.dc_ht_id}, "
50
51
                f"ac-{self.ac_ht_id}), sample-{self.vertical, self.horizontal} "
52
53
54
55
   class BitStreamReader:
        """simulate bitwise read"""
56
57
58
        def __init__(self, bytes_: bytes):
59
            self.bits = np.unpackbits(np.frombuffer(bytes , dtype=np.uint8))
            self.index = 0
60
61
62
        def read bit(self):
63
            if self.index >= self.bits.size:
                raise EOFError("Ran out of element")
64
65
            self.index += 1
            return self.bits[self.index - 1]
66
67
68
        def read_int(self, length):
69
            result = 0
70
            for _ in range(length):
                result = result * 2 + self.read_bit()
71
72
            return result
73
74
        def __repr__(self):
75
            return f"[{self.index}, {self.bits.size}]"
76
77
   class BitStreamWriter:
78
79
        """simulate bitwise write"""
80
```

class ComponentInfo:

```
def __init__(self, length=10000):
81
82
             self.index = 0
83
             self.bits = np.zeros(length, dtype=np.uint8)
84
85
         def write_bitstring(self, bitstring):
             length = len(bitstring)
86
87
             if length + self.index > self.bits.size * 8:
                 arr = np.zeros((length + self.index) // 8 * 2, dtype=np.uint8)
88
                 arr[: self.bits.size] = self.bits
89
90
                 self.bits = arr
91
             for bit in bitstring:
                 self.bits[self.index // 8] |= int(bit) << (7 - self.index % 8)</pre>
92
93
                 self.index += 1
94
95
         def to_bytes(self):
96
             return self.bits[: math.ceil(self.index / 8)].tobytes()
97
98
         def to hex(self):
99
             length = math.ceil(self.index / 8) * 8
100
             for i in range(self.index, length):
101
                 self.bits[i] = 1
102
             bytes_ = np.packbits(self.bits[:length])
             return " ".join(f"{b:2x}" for b in bytes_)
103
104
105
106
    class BytesWriter(BytesI0):
         def init (self, *args, **kwargs):
107
             super(BytesWriter, self).__init__(*args, **kwargs)
108
109
110
         def add_bytes(self, *args):
111
             self.write(b"".join(args))
112
113
114
    def bytes2int(bytes_, byteorder="big"):
115
         return int.from_bytes(bytes_, byteorder)
116
117
118
    def int2bytes(int_: int, length):
119
         return int_.to_bytes(length, byteorder="big")
120
121
122
    def decode_2s_complement(complement, length) -> int:
123
         if length == 0:
124
             return 0
125
         if complement >> (length - 1) == 1: # sign bit equal to one
126
             number = complement
127
         else: # sign bit equal to zero
             number = 1 - 2**length + complement
128
129
         return number
130
131
132
    def encode_2s_complement(number) -> str:
         """return the 2's complement representation as string"""
133
134
         if number == 0:
             return ""
135
136
         if number > 0:
137
             complement = bin(number)[2:]
138
         else:
```

```
139
              length = int(np.log2(-number)) + 1
140
              complement = bin(number - (1 - 2**length))[2:].zfill(length)
141
         return complement
142
143
144
     def load_quantization_table(quality, component):
145
         # the below two tables was processed by zigzag encoding
146
         # in JPEG bit stream, the table is also stored in this order
         if component == "lum":
147
148
              q = np.array(
149
                  Γ
150
                      16,
151
                      11,
152
                      12,
153
                      14,
154
                      12,
155
                      10,
156
                      16,
157
                      14,
158
                      13,
159
                      14,
160
                      18,
161
                      17,
162
                      16,
163
                      19,
164
                      24,
165
                      40,
                      26,
166
                      24,
167
                      22,
168
169
                      22,
170
                      24,
171
                      49,
172
                      35,
173
                      37,
174
                      29,
175
                      40,
176
                      58,
177
                      51,
178
                      61,
179
                      60,
                      57,
180
181
                      51,
182
                      56,
183
                      55,
184
                      64,
185
                      72,
                      92,
186
187
                      78,
188
                      64,
189
                      68,
190
                      87,
191
                      69,
192
                      55,
193
                      56,
194
                      80,
195
                      109,
196
                      81,
```

```
197
                        87,
198
                        95,
199
                        98,
200
                        103,
201
                        104,
202
                        103,
203
                        62,
                        77,
204
205
                        113,
206
                        121,
207
                        112,
                        100,
208
209
                        120,
210
                        92,
211
                        101,
212
                        103,
213
                        99,
214
                    ],
215
                   dtype=np.int32,
216
               )
217
          elif component == "chr":
218
               q = np.array(
219
                    220
                        17,
221
                        18,
222
                        18,
223
                        24,
224
                        21,
225
                        24,
                        47,
226
227
                        26,
                        26,
228
229
                        47,
230
                        99,
231
                        66,
232
                        56,
233
                        66,
234
                        99,
235
                        99,
236
                        99,
237
                        99,
238
                        99,
239
                        99,
                        99,
240
241
                        99,
242
                        99,
243
                        99,
244
                        99,
245
                        99,
246
                        99,
247
                        99,
248
                        99,
                        99,
249
250
                        99,
251
                        99,
252
                        99,
253
                        99,
254
                        99,
```

```
99,
255
256
                      99,
257
                      99,
258
                      99,
259
                      99,
260
                      99,
261
                      99,
262
                      99,
263
                      99,
264
                      99,
265
                      99,
                      99,
266
267
                      99,
268
                      99,
269
                      99,
270
                      99,
271
                      99,
272
                      99,
273
                      99,
274
                      99,
275
                      99,
276
                      99,
277
                      99,
278
                      99,
279
                      99,
280
                      99,
281
                      99,
282
                      99,
283
                      99,
284
                  ],
285
                  dtype=np.int32,
286
287
         else:
              raise ValueError(
288
289
                  (
290
                      f"component should be either 'lum' or 'chr', "
                      f"but '{component}' was found."
291
292
                  )
293
              )
294
         if 0 < quality < 50:
295
              q = np.minimum(np.floor(50 / quality * q + 0.5), 255)
296
         elif 50 <= quality <= 100:
297
              q = np.maximum(np.floor((2 - quality / 50) * q + 0.5), 1)
298
         else:
299
              raise ValueError("quality should belong to (0, 100].")
300
         return q.astype(np.int32)
301
302
303
     def zigzag_points(rows, cols):
304
         # constants for directions
305
         UP, DOWN, RIGHT, LEFT, UP_RIGHT, DOWN_LEFT = range(6)
306
307
         move_func = {
308
              UP: lambda p: (p[0] - 1, p[1]),
              DOWN: lambda p: (p[0] + 1, p[1]),
309
310
              LEFT: lambda p: (p[0], p[1] - 1),
311
              RIGHT: lambda p: (p[0], p[1] + 1),
              UP_RIGHT: lambda p: move(UP, move(RIGHT, p)),
312
```

```
DOWN_LEFT: lambda p: move(DOWN, move(LEFT, p)),
313
314
         }
315
316
         # move the point in different directions
         def move(direction, point):
317
             return move func[direction](point)
318
319
320
         # return true if point is inside the block bounds
321
         def inbounds(p):
322
             return 0 \ll p[0] \ll rows and 0 \ll p[1] \ll rows
323
324
         # start in the top-left cell
325
         now = (0, 0)
326
327
         # True when moving up-right, False when moving down-left
328
         move_up = True
329
         trace = []
330
         for i in range(rows * cols):
331
332
             trace.append(now)
333
             if move_up:
334
                 if inbounds(move(UP_RIGHT, now)):
335
                      now = move(UP_RIGHT, now)
336
                 else:
337
                     move up = False
338
                      if inbounds(move(RIGHT, now)):
339
                          now = move(RIGHT, now)
340
                      else:
341
                          now = move(DOWN, now)
342
343
                 if inbounds(move(DOWN_LEFT, now)):
344
                      now = move(DOWN_LEFT, now)
345
                 else:
346
                     move_up = True
347
                      if inbounds(move(DOWN, now)):
348
                          now = move(DOWN, now)
349
                      else:
350
                          now = move(RIGHT, now)
         0.00
351
         for rows = cols = 8, the actual 1-D index:
352
             0, 1, 8, 16, 9, 2, 3, 10, 17, 24, 32, 25, 18, 11, 4, 5,
353
354
             12, 19, 26, 33, 40, 48, 41, 34, 27, 20, 13, 6, 7, 14, 21, 28,
             35, 42, 49, 56, 57, 50, 43, 36, 29, 22, 15, 23, 30, 37, 44, 51,
355
             58, 59, 52, 45, 38, 31, 39, 46, 53, 60, 61, 54, 47, 55, 62, 63
356
357
358
         return trace
359
360
361
     def RGB2YCbCr(im):
362
         im = im.astype(np.float32)
363
         im = cv2.cvtColor(im, cv2.COLOR_RGB2YCrCb)
364
365
         RGB [0, 255]
366
         opency uses the following equations to conduct color conversion in float32
             Y = 0.299 * R + 0.587 * G + 0.114 * B
367
368
             Cb = (B - Y) * 0.564 + 0.5
             Cr = (R - Y) * 0.713 + 0.5
369
370
         Y [0, 255], Cb, Cr [-128, 127]
```

```
371
372
         # convert YCrCb to YCbCr
373
         Y, Cr, Cb = np.split(im, 3, axis=-1)
374
         im = np.concatenate([Y, Cb, Cr], axis=-1)
375
         return im
376
377
378
     def YCbCr2RGB(im):
379
         im = im.astype(np.float32)
380
         Y, Cb, Cr = np.split(im, 3, axis=-1)
381
         im = np.concatenate([Y, Cr, Cb], axis=-1)
         im = cv2.cvtColor(im, cv2.COLOR_YCrCb2RGB)
382
383
384
         Y [0, 255], Cb, Cr [-128, 127]
385
         conversion equation (float32):
             B = (Cb - 0.5) / 0.564 + Y
386
387
             R = (Cr - 0.5) / 0.713 + Y
             G = (Y - 0.299 * R - 0.114 * B) / 0.587
388
         RGB [0, 255]
389
         0.00
390
391
         return im
392
393
394
     def bits_required(n):
395
         n = abs(n)
396
         result = 0
         while n > 0:
397
             n >>= 1
398
399
             result += 1
400
         return result
401
402
403
     def divide_blocks(im, mh, mw):
404
         h, w = im.shape[:2]
405
         return im.reshape(h // mh, mh, w // mw, mw).swapaxes(1, 2).reshape(-1, mh, mw)
406
407
408
     def restore_image(block, nh, nw):
409
         bh, bw = block.shape[1:]
410
         return block.reshape(nh, nw, bh, bw).swapaxes(1, 2).reshape(nh * bh, nw * bw)
411
412
413
     def flatten(lst):
414
         return [item for sublist in lst for item in sublist]
415
416
417
     def averageMatrix(
418
         arrayMatrix,
419
         # given an array of 2D-array, return the average (coef by coef) 2D array
         avgMatrix = np.zeros_like(arrayMatrix[0])
420
421
         for i in range(avgMatrix.shape[0]):
422
             for j in range(avgMatrix.shape[1]):
423
                 avgMatrix[i, j] = np.average(arrayMatrix[:, i, j])
424
         return avgMatrix
425
426
427
     if __name__ == "__main__":
428
         arrMatrix = np.array([[[1, 2], [3, 4]], [[5, 2], [3, 4]]])
```

```
429 print(averageMatrix(arrMatrix))
430
```

# encoder/huffman\_jpeg.py

```
1
   import numpy as np
2
 3
   MAX_CLEN = 32 # assumed maximum initial code length
4
5
6
   def getFreq(data):
7
        freq = [0] * 257
8
        for elem in data:
9
            freq[elem] += 1
        freq[256] = 1
10
11
        return freq
12
13
14
   def jpegGenerateOptimalTable(freq):
15
        bits = [0] * (MAX_CLEN + 1)
16
        bitPos = [0] * (MAX_CLEN + 1)
17
        codesize = [0] * 257
18
        nzIndex = [0] * 257
19
        others = [-1] * 257
20
21
22
        numNzSymbols = 0
23
        for i in range(257):
24
            if freq[i]:
25
                nzIndex[numNzSymbols] = i
26
                freq[numNzSymbols] = freq[i]
27
                numNzSymbols += 1
28
29
        huffval = [0] * (numNzSymbols - 1)
30
31
        while True:
32
            c1 = -1
33
            c2 = -1
34
            V = 1000000000
            v2 = 10000000000
35
36
            for i in range(numNzSymbols):
37
                if freq[i] <= v2:
38
                     if freq[i] <= v:
39
                         c2 = c1
                         v2 = v
40
                         v = freq[i]
41
42
                         c1 = i
43
                     else:
44
                         v2 = freq[i]
45
                         c2 = i
46
47
            if c2 < 0:
48
                break
49
```

```
50
             freq[c1] += freq[c2]
51
             freq[c2] = 1000000001
52
53
             codesize[c1] += 1
             while others[c1] >= 0:
54
55
                 c1 = others[c1]
                 codesize[c1] += 1
56
57
58
             others[c1] = c2
59
             codesize[c2] += 1
60
61
             while others[c2] >= 0:
62
                 c2 = others[c2]
63
                 codesize[c2] += 1
64
65
         for i in range(numNzSymbols):
66
             bits[codesize[i]] += 1
67
68
69
         for i in range(1, MAX_CLEN + 1):
70
             bitPos[i] = p
71
             p += bits[i]
72
73
         for i in range(MAX_CLEN, 16, -1):
74
             while bits[i] > 0:
75
                 j = i - 2
76
                 while bits[j] == 0:
77
                      j -= 1
78
                 bits[i] -= 2
                 bits[i - 1] += 1
79
                 bits[j + 1] += 2
80
81
                 bits[j] -= 1
82
83
         i = MAX_CLEN
         while bits[i] == 0:
84
85
             i -= 1
         bits[i] -= 1
86
87
88
         for i in range(numNzSymbols - 1):
89
             huffval[bitPos[codesize[i]]] = nzIndex[i]
90
             bitPos[codesize[i]] += 1
91
92
         return bits, huffval
93
94
95
    def jpegGenerateHuffmanTable(bits, huffval):
96
         huffsize = [0] * 257
         huffcode = [0] * 257
97
98
99
         p = 0
100
         for l in range(1, 17):
             i = bits[l]
101
             while i:
102
                 huffsize[p] = l
103
                 p += 1
104
105
                 i -= 1
106
107
         huffsize[p] = 0
```

```
108
         lastp = p
109
110
         code = 0
111
         si = huffsize[0]
112
         p = 0
113
         while huffsize[p]:
114
             while huffsize[p] == si:
                 huffcode[p] = code
115
                 code += 1
116
117
                 p += 1
118
             code <<= 1
             si += 1
119
120
         ehufco = [0] * 257
121
122
         ehufsi = [0] * 257
123
124
         for p in range(lastp):
125
             i = huffval[p]
126
             ehufco[i] = huffcode[p]
127
             ehufsi[i] = huffsize[p]
128
129
         return ehufsi, ehufco
130
131
132
    def jpegTransformTable(ehufsi, ehufco):
133
         table = \{\}
134
         for i in range(len(ehufco)):
             if ehufsi[i] != 0:
135
136
                 endCode = bin(ehufco[i])[2:]
                 nbZeros = ehufsi[i] - len(endCode)
137
138
                 table[i] = "0" * nbZeros + endCode
139
         return table
140
141
142
    def jpegCreateHuffmanTable(arr):
143
         freq = getFreq(arr)
144
         bits, huffval = jpegGenerateOptimalTable(freg)
145
         ehufsi, ehufco = jpegGenerateHuffmanTable(bits, huffval)
146
         table = jpegTransformTable(ehufsi, ehufco)
         return table
147
148
149
150
    def convert_huffman_table(table):
         """convert huffman table to count and weigh"""
151
152
         # table[int] = string
153
         pairs = sorted(table.items(), key=lambda x: (len(x[1]), x[1]))
154
         weigh, codes = zip(*pairs)
155
         weigh = np.array(weigh, dtype=np.uint8)
         # count[i]: there are count[i] codes of length i+1
156
157
         count = np.zeros(16, dtype=np.uint8)
         for c in codes:
158
             count[len(c) - 1] += 1
159
160
         return count, weigh
161
162
163
    def read_huffman_code(table, stream):
164
         prefix = ""
165
         while prefix not in table:
```

```
166
             prefix += str(stream.read_bit())
167
         return table[prefix]
168
169
170
     def reverse(table):
171
         return {v: k for k, v in table.items()}
172
173
174
    # 4 recommended huffman tables in JPEG standard
175
    # luminance DC
176
    RM_Y_DC = {
177
         "00": 0,
178
         "010": 1,
179
         "011": 2,
180
         "100": 3,
         "101": 4,
181
         "110": 5,
182
         "1110": 6,
183
         "11110": 7,
184
185
         "111110": 8,
186
         "1111110": 9,
         "11111110": 10,
187
188
         "111111110": 11,
189
     }
190
191
    # luminance AC
    RM Y AC = {
192
         "00": 1,
193
         "01": 2,
194
         "100": 3,
195
196
         "1010": 0,
197
         "1011": 4,
198
         "1100": 17,
         "11010": 5,
199
200
         "11011": 18,
201
         "11100": 33,
         "111010": 49,
202
203
         "111011": 65,
204
         "1111000": 6,
205
         "1111001": 19,
         "1111010": 81,
206
207
         "1111011": 97,
208
         "11111000": 7,
209
         "11111001": 34,
         "11111010": 113,
210
211
         "111110110": 20,
212
         "111110111": 50,
213
         "111111000": 129,
214
         "111111001": 145,
         "111111010": 161,
215
         "1111110110": 8,
216
         "1111110111": 35,
217
218
         "11111111000": 66,
219
         "1111111001": 177,
         "11111111010": 193,
220
221
         "111111110110": 21,
222
         "111111110111": 82,
223
         "111111111000": 209,
```

```
"11111111001": 240,
224
225
         "1111111110100": 36,
226
         "1111111110101": 51,
227
         "1111111110110": 98,
228
         "1111111110111": 114,
229
         "1111111111000000": 130,
230
         "11111111110000010": 9,
231
         "11111111110000011": 10,
232
         "11111111110000100": 22,
233
         "11111111110000101": 23,
234
         "11111111110000110": 24,
         "111111111100001111": 25,
235
         "11111111110001000": 26,
236
237
         "11111111110001001": 37,
238
         "11111111110001010": 38,
239
         "11111111110001011": 39,
         "1111111110001100": 40,
240
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241
         "1111111110001110": 42,
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244
         "11111111110010000": 53,
245
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         "1111111110010010": 55,
246
247
         "11111111110010011": 56,
248
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249
         "11111111110010101": 58,
250
         "11111111110010110": 67,
251
         "111111111100101111": 68,
252
         "11111111110011000": 69,
         "11111111110011001": 70,
253
254
         "11111111110011010": 71,
255
         "11111111110011011": 72,
         "11111111110011100": 73,
256
         "11111111110011101": 74,
257
258
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259
         "1111111110011111": 84,
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260
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261
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262
         "11111111110100011": 88,
263
         "11111111110100100": 89,
264
265
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         "11111111110100110": 99,
266
         "111111111101001111": 100,
267
268
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269
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270
         "11111111110101010": 103,
         "11111111101010111": 104,
271
272
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273
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274
         "111111111101011110": 115,
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275
276
         "11111111110110000": 117,
         "11111111110110001": 118,
277
         "11111111110110010": 119,
278
279
         "11111111110110011": 120,
280
         "11111111110110100": 121,
281
         "11111111110110101": 122,
```

```
"11111111110110110": 131,
282
283
         "11111111110110111": 132,
284
         "111111111110111000": 133,
285
         "11111111110111001": 134,
         "11111111110111010": 135,
286
         "11111111110111011": 136,
287
288
         "111111111111100": 137,
         "11111111110111101": 138,
289
290
         "11111111110111110": 146,
291
         "11111111110111111": 147,
292
         "111111111110000000": 148,
293
         "11111111111000001": 149,
         "11111111111000010": 150,
294
295
         "11111111111000011": 151,
         "11111111111000100": 152,
296
297
         "11111111111000101": 153,
298
         "11111111111000110": 154,
         "11111111111000111": 162,
299
         "11111111111001000": 163,
300
301
         "11111111111001001": 164,
302
         "11111111111001010": 165,
         "11111111111001011": 166,
303
304
         "11111111111001100": 167,
         "11111111111001101": 168,
305
         "11111111111001110": 169,
306
         "1111111111001111": 170,
307
308
         "11111111111010000": 178,
         "11111111111010001": 179,
309
         "11111111111010010": 180,
310
         "11111111111010011": 181,
311
312
         "11111111111010100": 182,
313
         "11111111111010101": 183,
314
         "11111111111010110": 184,
315
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339
         "11111111111101111": 229,
```

```
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341
         "11111111111110001": 231,
342
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343
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344
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347
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350
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         "11111111111111011": 247,
351
         "1111111111111100": 248,
352
353
         "1111111111111101": 249,
354
         "1111111111111110": 250,
355
     }
356
357
     # chroma DC
     RM_C_DC = {
358
359
         "00": 0,
360
         "01": 1,
361
         "10": 2,
362
         "110": 3,
         "1110": 4,
363
364
         "11110": 5,
365
         "111110": 6,
         "1111110": 7,
366
         "11111110": 8,
367
368
         "111111110": 9,
369
         "1111111110": 10,
370
         "11111111110": 11,
371
     }
372
373
     # chroma AC
374
     RM_C_AC = {
375
         "00": 0,
         "01": 1,
376
         "100": 2,
377
         "1010": 3,
378
         "1011": 17,
379
         "11000": 4,
380
         "11001": 5,
381
382
         "11010": 33,
383
         "11011": 49,
384
         "111000": 6,
385
         "111001": 18,
386
         "111010": 65,
         "111011": 81,
387
         "1111000": 7,
388
         "1111001": 97,
389
         "1111010": 113,
390
         "11110110": 19,
391
392
         "11110111": 34,
393
         "11111000": 50,
         "11111001": 129,
394
395
         "111110100": 8,
396
         "111110101": 20,
397
         "111110110": 66,
```

```
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399
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400
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401
          "111111010": 193,
402
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408
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         "111111111000": 114,
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413
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416
417
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420
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         "11111111110001101": 39,
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430
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432
         "11111111110010110": 58,
433
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         "11111111110011000": 68,
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435
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         "11111111110011010": 70,
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         "11111111110011101": 73,
440
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         "11111111110100101": 89,
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449
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450
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451
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479
         "11111111111000101": 151,
480
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         "11111111111000111": 153,
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483
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486
         "11111111111001100": 165,
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         "11111111111001101": 166,
488
         "11111111111001110": 167,
489
         "111111111110011111": 168,
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502
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         "11111111111011101": 196,
503
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507
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508
         "11111111111100010": 201,
509
         "11111111111100011": 202,
         "11111111111100100": 210,
510
511
         "11111111111100101": 211,
512
         "11111111111100110": 212,
513
         "11111111111100111": 213,
```

```
515
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516
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517
         "11111111111101011": 217,
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528
         "11111111111110110": 242,
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530
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532
533
         "11111111111111011": 247,
534
         "11111111111111100": 248,
         "1111111111111101": 249,
535
536
         "1111111111111110": 250,
537
     }
538
     if __name__ == "__main__":
539
540
         arr = np.array([np.random.randint(-127, 128) for _ in range(64)])
541
         table = jpegCreateHuffmanTable(arr)
542
         print(table)
543
```

"11111111111101000": 214,

514

# encoder/encoder.py

```
from math import ceil
 2
   import cv2
 3
   import numpy as np
   from PIL import Image
 5
   from pathlib import Path
6
7
   from utils import *
8
   from huffman_jpeg import *
9
10
11
   def padding(im, mh, mw):
12
13
        pad use boundary pixels so that its height and width are
        the multiple of the height and width of MCUs, respectively
14
15
16
        h, w, d = im.shape
        if h % mh == 0 and w % mw == 0:
17
18
            return im
19
        hh, ww = ceil(h / mh) * mh, ceil(w / mw) * mw
20
        im_ex = np.zeros_like(im, shape=(hh, ww, d))
21
        im_ex[:h, :w] = im
```

```
22
        im_ex[:, w:] = im_ex[:, w - 1 : w]
23
        im_ex[h:, :] = im_ex[h - 1 : h, :]
24
        return im_ex
25
26
27
   mcu_sizes = {
        "4:2:0": (BH * 2, BW * 2),
28
29
        "4:1:1": (BH * 2, BW * 2),
30
        "4:2:2": (BH, BW * 2),
31
        "4:4:4": (BH, BW),
32
   }
33
34
35
   def scan blocks(mcu, mh, mw):
36
        scan MCU to blocks for DPCM, for 4:2:0, the scan order is as follows:
37
38
39
        | 0 | 1 | | 4 | 5 |
40
        -----
41
        | 2 | 3 | | | 6 | 7 |
42
        0.000
43
44
        blocks = (
45
            mcu.reshape(-1, mh // BH, BH, mw // BW, BW).swapaxes(2, 3).reshape(-1, BH,
    BW)
46
47
        return blocks
48
49
50
   def DCT(blocks):
51
        dct = np.zeros_like(blocks)
52
        for i in range(blocks.shape[0]):
53
            dct[i] = cv2.dct(blocks[i])
54
        return dct
55
56
57
   def zigzag_encode(dct):
58
        trace = zigzag_points(BH, BW)
59
        zz = np.zeros_like(dct).reshape(-1, BH * BW)
        for i, p in enumerate(trace):
60
            zz[:, i] = dct[:, p[0], p[1]]
61
62
        return zz
63
64
65
   def quantization(dct, table):
        ret = dct / table[None]
66
67
        return np.round(ret).astype(np.int32)
68
69
70
   def DPCM(dct):
71
72
        encode the DC differences
        0.00
73
74
        dc_pred = dct.copy()
75
        dc_pred[1:, 0] = dct[1:, 0] - dct[:-1, 0]
76
        return dc_pred
77
78
79
   def run_length_encode(arr):
```

```
80
         # determine where the sequence is ending prematurely
81
         last_nonzero = -1
82
         for i, elem in enumerate(arr):
83
             if elem != 0:
84
                 last nonzero = i
85
         rss, values = [], []
86
         run_length = 0
87
         for i, elem in enumerate(arr):
88
             if i > last_nonzero:
89
                 rss.append(0)
90
                 values.append(0)
91
                 break
92
             elif elem == 0 and run_length < 15:</pre>
93
                 run length += 1
94
             else:
95
                 size = bits_required(elem)
96
                 rss.append((run_length << 4) + size)</pre>
97
                 values.append(elem)
98
                 run_length = 0
99
         return rss, values
100
101
    def encode_header(qts, hts, cop_infos, height, width):
102
         writer = BytesWriter()
103
104
         add bytes = writer.add bytes
105
         add_bytes(
106
             MARKER.SOI,
107
             MARKER.APP0,
             b"\x00\x10", # length = 16
108
                          # identifier = JFIF0
             b"JFIF\x00",
109
110
             b"\x01\x01", # version
111
             b"\x00", # unit
112
             b"\x00\x01", # x density
113
             b"\x00\x01", # y density
114
             b"\x00\x00", # thumbnail data
115
116
         for id_, qt in enumerate(qts):
117
             add_bytes(
118
                 MARKER.DQT,
                 b"\x00C", # length = 67
119
                 # precision (8 bits), table id, = 0, id_
120
121
                 int2bytes(id_, 1),
122
                 qt.astype(np.uint8).tobytes(),
123
             )
         cop_num = len(cop_infos)
124
125
         add_bytes(
126
             MARKER.SOF0,
             int2bytes(8 + 3 * cop_num, 2), # length
127
128
             int2bytes(8, 1), # 8 bit precision
             int2bytes(height, 2),
129
130
             int2bytes(width, 2),
131
             int2bytes(cop_num, 1),
132
         )
133
         add_bytes(*[info.encode_SOFO_info() for info in cop_infos])
134
135
         # type << 4 + id, (type 0: DC, 1 : AC)
136
         type_ids = [b"\x00", b"\x10", b"\x01", b"\x11"]
137
         for type_id, ht in zip(type_ids, hts):
```

```
count, weigh = convert_huffman_table(ht)
138
139
             ht_bytes = count.tobytes() + weigh.tobytes()
140
             add_bytes(
141
                 MARKER.DHT,
142
                 int2bytes(len(ht_bytes) + 3, 2), # length
143
144
                 ht_bytes,
145
             )
146
147
         add_bytes(
148
             MARKER.SOS,
             int2bytes(6 + cop_num * 2, 2), # length
149
150
             int2bytes(cop_num, 1),
151
         )
152
         add_bytes(*[info.encode_SOS_info() for info in cop_infos])
153
         add_bytes(b"\x00\x3f\x00")
154
         return writer
155
156
157
    def encode_mcu(mcu, hts):
        bit stream = BitStreamWriter()
158
159
         for cur in mcu:
             for dct, (dc_ht, ac_ht) in zip(cur, hts):
160
                 dc code = encode 2s complement(dct[0])
161
                 container = [dc_ht[len(dc_code)], dc_code]
162
163
                 rss, values = run_length_encode(dct[1:])
                 for rs, v in zip(rss, values):
164
                     container.append(ac_ht[rs])
165
                     container.append(encode_2s_complement(v))
166
                 bitstring = "".join(container)
167
168
                 bit_stream.write_bitstring(bitstring)
169
         return bit_stream.to_bytes()
170
171
    def encode_jpeg(im, quality=95, subsample="4:2:0", use_rm_ht=True):
172
173
         im = np.expand_dims(im, axis=-1) if im.ndim == 2 else im
         height, width, depth = im.shape
174
175
176
         mh, mw = mcu_sizes[subsample] if depth == 3 else (BH, BW)
177
         im = padding(im, mh, mw)
178
         im = RGB2YCbCr(im) if depth == 3 else im
179
180
        # DC level shift for luminance,
         # the shift of chroma was completed by color conversion
181
182
        Y_{im} = im[:, :, 0] - 128
183
        # divide image into MCUs
         mcu = divide blocks(Y im, mh, mw)
184
         # MCU to blocks, for luminance there are more than one blocks in each MCU
185
        Y = scan_blocks(mcu, mh, mw)
186
187
         Y dct = DCT(Y)
         # the quantization table was already processed by zigzag scan,
188
         # so we apply zigzag encoding to DCT block first
189
190
         Y_z = zigzag_encode(Y_dct)
191
         qt_y = load_quantization_table(quality, "lum")
192
         Y_q = quantization(Y_z, qt_y)
193
        Y_p = DPCM(Y_q)
        # whether to use recommended huffman table
194
195
         if use_rm_ht:
```

```
Y_dc_ht, Y_ac_ht = reverse(RM_Y_DC), reverse(RM_Y_AC)
196
197
         else:
198
             Y_dc_ht = jpegCreateHuffmanTable(np.vectorize(bits_required)(Y_p[:, 0]))
199
             Y_ac_ht = jpegCreateHuffmanTable(
                 flatten(run_length_encode(Y_p[i, 1:])[0] for i in range(Y_p.shape[0]))
200
201
             )
         qts, hts = [qt_y], [Y_dc_ht, Y_ac_ht]
202
203
         cop_infos = [ComponentInfo(\mathbf{1}, mw // BW, mh // BH, \mathbf{0}, \mathbf{0}, \mathbf{0})]
         # the number of Y DCT blocks in an MCU
204
205
         num = (mw // BW) * (mh // BH)
206
         mcu_hts = [(Y_dc_ht, Y_ac_ht) for _ in range(num)]
         # assign DCT blocks to MCUs
207
208
         mcu_ = Y_p.reshape(-1, num, BH * BW)
209
210
         if depth == 3:
211
             # chroma subsample
212
             ch = im[:: mh // BH, :: mw // BW, 1:]
             Cb = divide_blocks(ch[:, :, 0], BH, BW)
213
             Cr = divide_blocks(ch[:, :, 1], BH, BW)
214
215
             Cb_dct, Cr_dct = DCT(Cb), DCT(Cr)
             Cb_z, Cr_z = zigzag_encode(Cb_dct), zigzag_encode(Cr_dct)
216
217
             qt_c = load_quantization_table(quality, "chr")
218
             Cb_q, Cr_q = quantization(Cb_z, qt_c), quantization(Cr_z, qt_c)
219
             Cb_p, Cr_p = DPCM(Cb_q), DPCM(Cr_q)
220
             if use rm ht:
                 C_dc_ht, C_ac_ht = reverse(RM_C_DC), reverse(RM_C_AC)
221
222
             else:
                 ch_ = np.concatenate([Cb_p, Cr_p], axis=0)
223
224
                 C_dc_ht = jpegCreateHuffmanTable(np.vectorize(bits_required)(ch_[:,
     0]))
225
                 C_ac_ht = jpegCreateHuffmanTable(
                     flatten(run_length_encode(ch_[i, 1:])[0] for i in
226
     range(ch_.shape[0]))
227
             qts.append(qt_c), hts.extend([C_dc_ht, C_ac_ht])
228
229
             cop_infos.extend(
230
                 [ComponentInfo(2, 1, 1, 1, 1, 1), ComponentInfo(3, 1, 1, 1, 1, 1)]
231
             mcu_hts.extend((C_dc_ht, C_ac_ht) for _ in range(2))
232
233
             mcu_ = np.concatenate([mcu_, Cb_p[:, None], Cr_p[:, None]], axis=1)
234
235
         writer = encode_header(qts, hts, cop_infos, height, width)
236
         bytes_ = encode_mcu(mcu_, mcu_hts)
         writer.write(bytes_.replace(b"\xff", b"\xff\x00"))
237
238
         writer.write(MARKER.E0I)
239
         return writer.getvalue()
240
241
    def write_jpeg(filename, im, quality=95, subsample="4:2:0", use_rm_ht=True):
242
243
         bytes_ = encode_jpeg(im, quality, subsample, use_rm_ht)
244
         Path(filename).write_bytes(bytes_)
245
246
247
    def main():
         im = Image.open("./data/villeLyon.jpg")
248
         write_jpeg("data/villeLyonLow.jpg", np.array(im), 5, "4:1:1", False)
249
250
251
252 if __name__ == "__main__":
```

```
253 main()
254
```

#### encoder/comparator.py

```
1
   import numpy as np
   import encoder
 3
   import sys, os
 4
   from pathlib import Path
 5
   from PIL import Image
 6
   import cv2
 7
   import pandas as pd
8
   import time as t
9
   import shutil
    import utils
10
11
    import matplotlib.pyplot as plt
12
    from encoder import DCT, padding
13
    from scipy.fftpack import dct
14
   import random as rd
15
16
   LIM = 2 # number of files to test to
17
18
19
   def compare(
20
        qualities=None,
21
        dataDirectory=None,
22
        outputDirectory=None,
23
        subsamples=None,
24
        useStdHuffmanTable=None,
25
        DeleteFilesAfterward=True,
26
    ):
27
        if qualities is None:
28
            qualities = [np.random.randint(0, 101)]
29
        if subsamples is None:
            subsamples = ["4:2:2"]
30
31
        if dataDirectory is None:
32
            dataDirectory = "./data/datasetBmp"
33
        if useStdHuffmanTable is None:
34
            useStdHuffmanTable = [False]
35
        stat = np.zeros(
36
            (LIM * len(qualities) * len(subsamples) * len(useStdHuffmanTable), 6),
37
            dtype=object,
38
          # dim 0 : quality factor, dim 1 : subsample method, dim 2 : usage of std Hf
   Tables, dim 3 : size before compression, dim 4 : size after compression, dim 5 :
    time to compress
39
        i = 0
40
        i_max = LIM * len(qualities) * len(subsamples) * len(useStdHuffmanTable)
41
        filesTreated = rd.choices(os.listdir(dataDirectory), k=LIM)
42
        for quality in qualities:
43
            for subsample in subsamples:
44
                for hfTables in useStdHuffmanTable:
                    outputDirectory = f"./data/treated/quality{quality}-
45
    subsample{subsample}-stdHf{hfTables}"
46
                    for filename in filesTreated:
47
                        f = os.path.join(dataDirectory, filename)
```

```
48
                          if not os.path.exists(outputDirectory):
49
                               os.makedirs(outputDirectory)
50
                          f_out = os.path.join(outputDirectory, filename + ".jpg")
51
                           if os.path.isfile(f):
                               previousSize = os.stat(f).st size
52
53
                               image = Image.open(f)
54
                               time = t.time()
55
                               encoder.write ipeq(
56
                                   f out, np.array(image), quality, subsample, hfTables
57
58
                               time = t.time() - time
59
                               newSize = os.stat(f_out).st_size
60
                               stat[i][0] = quality
61
                               stat[i][1] = subsample
62
                               stat[i][2] = hfTables
63
                               stat[i][3] = previousSize
64
                               stat[i][4] = newSize
65
                               stat[i][5] = time
66
67
                           print(f"{i}/{i_max}", end="\r")
                      if DeleteFilesAfterward:
68
69
                           shutil.rmtree(outputDirectory)
70
         return stat
71
72
     def write_stat(statFile, stat, quality, subsample, standHuffTables):
73
         with open(statFile, "a+") as f:
74
75
             f.write("\n" * 2)
76
             f.write("New sample \n")
77
             f.write(f"Size of sample : {LIM} images \n")
78
             f.write(
     f"Parameters of compression : (quality) {quality}, (subsample)
{subsample}, (usage of standard HuffTables) {'Yes' if standHuffTables else 'No'}
79
     n'
80
             avgPreviousSize = np.average(stat[:, 0])
81
82
             avgNewSize = np.average(stat[:, 1])
83
             f.write(
                  f"Average size of image before compression : {avgPreviousSize} bytes
84
     \n"
85
             f.write(f"Average size of images after compression : {avgNewSize} bytes
86
     \n")
87
             f.write(f"Ratio is {avgPreviousSize / avgNewSize:.2f}")
88
89
90
     def write_stat_csv(output, stat):
91
         if os.path.isfile(output):
92
             pd.DataFrame(stat).to_csv(output, mode="a", index=False, header=False)
93
         else:
94
             pd.DataFrame(stat).to csv(
95
                  output,
                  index=False,
96
97
                  header=[
98
                      "quality",
                      "subsample",
99
                      "stdHuffmanTables",
100
101
                      "oldSize".
                      "newSize",
102
```

```
],
105
             )
106
107
108
    def csv_to_stat(csvFile):
109
         stat = pd.read_csv(csvFile)
110
         return stat
111
112
113
    def dataInterpreation(dataFrame):
114
         df = dataFrame
         qualities = df["quality"].unique()
115
116
         qualitySize = {}
117
         qualityTime = {}
118
         for quality in qualities:
119
             qualitySize[quality] = int(df[df["quality"] == quality]["newSize"].mean())
             qualityTime[quality] = round(df[df["quality"] == quality]["time"].mean(),
120
     3)
         stdSize = int(df[df["stdHuffmanTables"] == True]["newSize"].mean())
121
122
         stdTime = round(df[df["stdHuffmanTables"] == True]["time"].mean(), 3)
         nonStdSize = int(df[df["stdHuffmanTables"] == False]["newSize"].mean())
123
         nonStdTime = round(df[df["stdHuffmanTables"] == False]["time"].mean(), 3)
124
125
126
         plt.rcParams["figure.figsize"] = [10, 5]
127
128
         fig, (ax1, ax3) = plt.subplots(1, 2)
129
         ax2 = ax1.twinx()
130
131
         fig.suptitle("Comparaison des compressions en fonction du facteur de qualité")
132
133
         width = 0.25
134
135
         initialSize = 786486
136
         xaxis = list(qualitySize.keys())
137
         yaxisSize = np.array(list(qualitySize.values()))
138
         yaxisTime = np.array(list(qualityTime.values()))
139
         yaxisRatio = (initialSize - yaxisSize) / yaxisTime
140
141
         color1 = "tab:red"
         color2 = "tab:blue"
142
143
         color3 = "tab:green"
144
145
         ax1.bar(
146
             np.arange(len(qualitySize)) - width,
147
             yaxisSize,
148
             width,
149
             tick_label=xaxis,
150
             color=color1,
151
             label="Taille après compression",
         )
152
153
         ax2.bar(
154
             np.arange(len(qualityTime)),
155
             yaxisTime,
156
             width,
             tick_label=xaxis,
157
158
             color=color2,
159
             label="Temps de compression",
160
         )
```

"time",

103

```
161
         ax3.bar(
162
             np.arange(len(qualitySize)),
163
             yaxisRatio,
164
             width,
165
             tick label=xaxis,
166
             color=color3,
167
             label="Octets gagnés par seconde",
         )
168
169
170
         ax1.legend(loc="upper left")
         ax2.legend(loc="upper left", bbox_to_anchor=(0, 0.9))
171
         ax3.legend(loc="upper right")
172
173
174
         ax3.yaxis.tick right()
175
         ax1.set_xlabel("Facteur de qualité")
176
177
         ax1.set_ylabel("Taille (en octets)", color=color1)
         ax2.set ylabel("Temps (en secondes)", color=color2)
178
179
         ax3.set_xlabel("Facteur de qualité")
         ax3.set_ylabel("Taille gagné par unité de temps (octets.Hz)", color=color3)
180
181
         ax3.yaxis.set_label_position("right")
182
183
         plt.savefig("./data/treated/compressionComparaison", transparent=True)
184
185
         plt.rcParams["figure.figsize"] = [7, 5]
186
         plt.clf()
187
         fig = plt.figure()
188
189
         ax1 = fig.add_subplot(111)
         ax2 = ax1.twinx()
190
191
192
         fig.suptitle(
193
             "Comparaison des compressions en fonction des tables de Huffman utilisées"
194
         )
195
196
         yaxisSize = [stdSize, nonStdSize]
         yaxisTime = [stdTime, nonStdTime]
197
198
         labels = ["Tables Standards", "Tables Optimales"]
199
200
         ax1.bar(
201
             np.arange(2) - width / 2,
202
             yaxisSize,
203
             width,
204
             tick label=labels,
205
             color=color1,
206
             label="Taille après compression",
207
         )
         ax2.bar(
208
209
             np.arange(2) + width / 2,
210
             vaxisTime,
211
             width,
             tick_label=labels,
212
213
             color=color2,
214
             label="Temps de compression",
215
         )
216
217
         ax1.legend(loc="upper center", bbox_to_anchor=(0.45, 1))
218
         ax2.legend(loc="upper center", bbox_to_anchor=(0.45, 0.9))
```

```
220
         ax1.set_ylabel("Taille (en octets)", color=color1)
         ax2.set_ylabel("Temps (en secondes)", color=color2)
221
222
         plt.savefig("./data/treated/compressionComparaison2", transparent=True)
223
224
225
226
    def energyCompaction(imgPath):
227
         img = cv2.imread(imgPath)
228
229
         imgYCrCB = cv2.cvtColor(
230
             img, cv2.C0L0R_RGB2YCrCb
         ) # Convert RGB to YCrCb (Cb applies V, and Cr applies U).
231
232
233
         Y, Cr, Cb = cv2.split(padding(imgYCrCB, 8, 8))
         Y = Y.astype("int") - 128
234
235
         blocks_Y = utils.divide_blocks(Y, 8, 8)
236
         dctBlocks Y = np.zeros like(blocks Y)
237
         for i in range(len(blocks_Y)):
238
             dctBlocks_Y[i] = dct(
239
                 dct(blocks_Y[i], axis=0, norm="ortho"), axis=1, norm="ortho"
240
         avg_Y = utils.averageMatrix(blocks_Y)
241
242
         avgDct_Y = utils.averageMatrix(dctBlocks_Y)
243
244
         x = np.random.randint(blocks_Y.shape[0])
245
         arr1 = blocks Y[x]
246
         arr2 = dctBlocks Y[x]
247
248
         fig, (ax1, ax2) = plt.subplots(1, 2)
249
250
         valueMax, valueMin = max(np.max(arr1), np.max(arr2)), min(
251
             np.min(arr1), np.min(arr2)
252
         # fig.suptitle('Matrice de la luminance de "villeLyon.jpg"')
253
254
         ax1.matshow(arr1, cmap="cool", vmin=valueMin, vmax=valueMax)
255
256
         ax1.set_title("avant DCT")
257
         ax2.matshow(arr2, cmap="cool", vmin=valueMin, vmax=valueMax)
258
259
         ax2.set_title("après DCT")
260
261
         for i in range(arr1.shape[0]):
             for j in range(arr1.shape[1]):
262
                 cNormal = int(arr1[i, j])
263
264
                 cDct = int(arr2[i, j])
265
                 ax1.text(i, j, str(cNormal), va="center", ha="center")
                 ax2.text(i, j, str(cDct), va="center", ha="center")
266
267
         plt.savefig("./data/energyCompaction.png", transparent=True)
268
269
270
    def rgbToYCbCr_channel_bis():
         img = cv2.imread("./data/villeLyon.jpg") # Read input image in BGR format
271
272
273
         imgYCrCB = cv2.cvtColor(
274
             img, cv2.COLOR_BGR2YCrCb
275
         ) # Convert RGB to YCrCb (Cb applies V, and Cr applies U).
276
```

```
277
         Y, Cr, Cb = cv2.split(imgYCrCB)
278
         # Fill Y and Cb with 128 (Y level is middle gray, and Cb is "neutralized").
279
280
         onlyCr = imgYCrCB.copy()
281
         onlyCr[:, :, 0] = 128
         onlyCr[:, :, 2] = 128
282
283
         onlyCr_as_bgr = cv2.cvtColor(
284
             onlyCr, cv2.COLOR_YCrCb2BGR
285
            # Convert to BGR - used for display as false color
286
         # Fill Y and Cr with 128 (Y level is middle gray, and Cr is "neutralized").
287
         onlyCb = imgYCrCB.copy()
288
         onlyCb[:, :, 0] = 128
289
290
         onlyCb[:, :, 1] = 128
         onlyCb_as_bgr = cv2.cvtColor(
291
             onlyCb, cv2.COLOR_YCrCb2BGR
292
           # Convert to BGR - used for display as false color
293
294
295
         cv2.imshow("img", img)
296
         cv2.imshow("Y", Y)
         cv2.imshow("onlyCb_as_bgr", onlyCb_as_bgr)
297
         cv2.imshow("onlyCr_as_bgr", onlyCr_as_bgr)
298
299
         cv2.waitKey()
300
         cv2.destroyAllWindows()
301
302
         cv2.imwrite("./data/treated/villeLyon_Y.jpg", Y)
         cv2.imwrite("./data/treated/villeLyon_Cb.jpg", onlyCb_as_bgr)
303
         cv2.imwrite("./data/treated/villeLyon_Cr.jpg", onlyCr_as_bgr)
304
305
306
     if __name__ == "__main__":
307
         # compare()
308
309
         # rgbToYCbCr_channel_bis()
         # energyCompaction("./data/villeLyon.jpg")
310
         \# test = np.array([[93, 90, 83, 68, 61, 61, 46, 21],
311
312
         #
                           [102, 92, 95, 77, 65, 60, 49, 32],
313
         #
                           [69, 55, 47, 57, 65, 60, 72, 65],
         #
                           [55, 55, 40, 42, 23, 1, 11, 38],
314
                           [55, 57, 47, 53, 35, 59, -2, 26],
315
         #
         #
                           [64, 41, 42, 55, 60, 57, 25, -8],
316
                           [77, 87, 58, -2, -5, 14, -10, -35],
317
         #
318
         #
                           [38, 14, 33, 33, -21, -23, -43, -34]])
         # print(dct(dct(test, axis=0, norm="ortho"), axis=1, norm='ortho'))
319
320
         # stat = compare(qualities = list(range(1, 101, 10)), subsamples=['4:4:4',
321
              '4:1:1', '4:2:2'], useStdHuffmanTable=[True, False],
     DeleteFilesAfterward=True)
         # write_stat_csv("./data/treated/stat.csv", stat)
322
         stat = csv to stat("./data/treated/stat.csv")
323
324
         dataInterpreation(stat)
```