

Data structures and Algorithms

Complexity (Big O)

Complexity of an algorithm measures time and memory. How long does one algorithm takes to finish? How much memory does it use?

We measure these values in terms of the input size (Usually for the input size we use the letter n)

We can analyze algorithms in the Best case, Average case and Worst case.

Best case measures the quickest way for an algorithm to finish.

Average case measures what time does the algorithm need to finish on average.

Worst case measures the slowest time for an algorithm to finish.

General idea

1. Big O: $\mathcal{O}(n^2)$ - the algorithm takes **at most** n^2 steps to finish in the **WORST CASE**.
2. Little o: $o(n^2)$ - the algorithm takes **less than** n^2 steps to finish in the **WORST CASE**.
3. Big Omega: $\Omega(n^2)$ - the algorithm takes **at least** n^2 steps to finish in the **BEST CASE**.
4. Little Omega: $\omega(n^2)$ - the algorithm takes **more than** n^2 steps to finish in the **BEST CASE**.
5. Big Theta: $\Theta(n^2)$ - the combination of $\mathcal{O}(n^2)$ and $\Omega(n^2)$. Meaning the algorithm takes at least n^2 steps to finish and takes at most n^2 steps to finish, i.e. it always takes n^2 steps.

Comparison of orders of common functions

$$\mathcal{O}(1) < \mathcal{O}(\log\log(n)) < \mathcal{O}(\log(n)) < \mathcal{O}(\log^2(n)) < \mathcal{O}(\sqrt{n}) < \mathcal{O}(n) < \mathcal{O}(n\log(n)) < \mathcal{O}(n^2) < \mathcal{O}(n^3) < \mathcal{O}(2^n) < \mathcal{O}(3^n) < \mathcal{O}(n!) < \mathcal{O}(n^n) < \mathcal{O}(3^{n^2}) < \mathcal{O}(2^{n^3})$$

Big O cheat sheet

<https://www.bigocheatsheet.com/>

Formal definitions

$$\mathcal{O}(f(n)) = \{g(n) : \exists c > 0, \exists n_0 > 0 \mid 0 \leq g(n) \leq cf(n) \forall n \geq n_0\}$$

$$\Theta(f(n)) = \{g(n) : \exists c_1 > 0, \exists c_2 > 0, \exists n_0 > 0 \mid 0 \leq c_1 f(n) \leq g(n) \leq c_2 f(n) \forall n \geq n_0\}$$

$$\Omega(f(n)) = \{g(n) : \exists c > 0, \exists n_0 > 0 \mid 0 \leq cf(n) \leq g(n) \forall n \geq n_0\}$$

$$o(f(n)) = \{g(n) : \forall c > 0 \exists n_0 > 0 \mid 0 \leq g(n) < cf(n) \forall n \geq n_0\}$$

$$\omega(f(n)) = \{g(n) : \forall c > 0 \exists n_0 > 0 \mid 0 \leq cf(n) < g(n) \forall n \geq n_0\}$$

Examples

$$\mathcal{O}(34n^4 + 5) = n^4$$

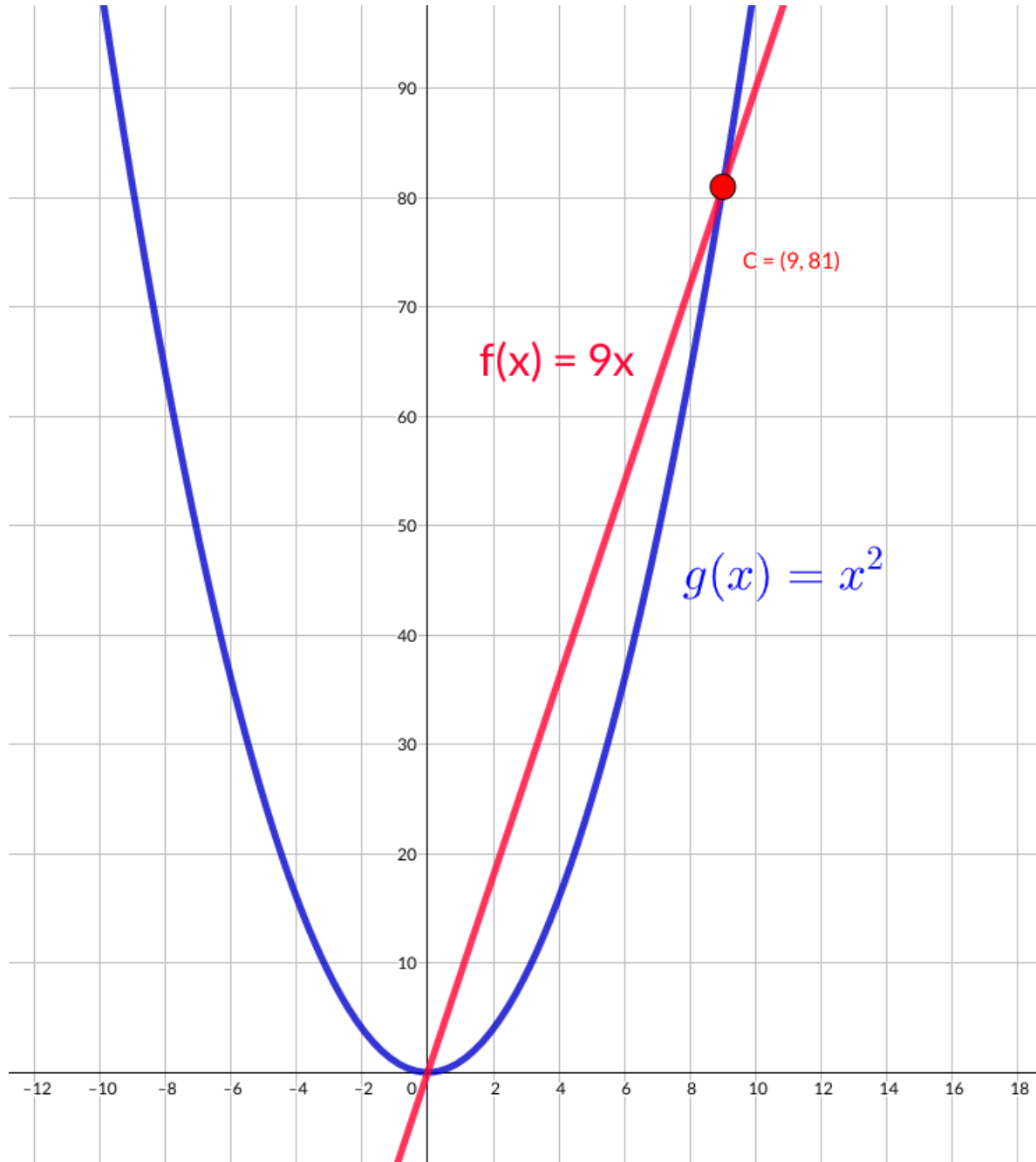
$$\mathcal{O}(2^n + n^{1024} + \log(n)) = 2^n$$

$$\mathcal{O}(5N + \frac{1}{2}M) = N + M$$

$\mathcal{O}(n^2)$ means that if our algorithm takes input of 10 elements it will need 100 steps to finish in the worst case. If the input is of 100 elements it will need 10000 steps to finish in the worst case.

Constants and Big O

Usually we discard constants when using Big O, but in some cases the constant can be meaningful for small input sizes. In the following example $\mathcal{O}(n^2)$ is faster than $\mathcal{O}(n)$ because our complexities are n^2 and $9n$ so for $n < 9$ the n^2 algorithm is faster than the $9n$ one.



Sorting

Sorting means ordering a set of elements in a sequence.

We can sort a set of elements whose elements are in partial order. Partial order is a relation with the following properties:

1. Antisymmetry - For every 2 elements in the set (A, B), if $A \leq B$ and $B \leq A$ then $A = B$.
2. Transitivity - For every 3 elements in the set (A, B, C), if $A \leq B$ and $B \leq C$ then $A \leq C$.
3. Reflexivity - For every element in the set A, $A \leq A$.

Sorting properties

Stable sort

A sorting algorithm is stable if two equal objects appear in the same order in the ordered output as they appeared in the unsorted input.

Example input: 1, 2, 3_a, 8, 5, 3_b. Here 3_a and 3_b are simply a 3 but we have marked them to follow what happens with them after the sorting.

Example output: 1, 2, 3_a, 3_b, 5, 8

Unstable sort output: 1, 2, 3_b, 3_a, 5, 8

In place sort

Uses only a small constant amount of extra memory. In place sort means the elements are swapped around. Out of place means we use another extra array to swap items around.

Number of comparisons

How many times do we need to compare 2 elements. For most sorts this represents the time complexity.

Adaptive sort

Determines whether the sorting algorithm runs faster for inputs that are partially or fully sorted. If an algorithm is unadaptive it runs for the same time on sorted and unsorted input. If an algorithm is adaptive it runs faster on sorted input than on unsorted input.

Online sort

Determines if an algorithm needs all the items from the input to start sorting. If an algorithm is online it can start sorting input that is given in parts. If an algorithm is offline it can start sorting only after it has the whole input.

External sort

Allows sorting data which cannot fit into memory. Such algorithms are designed to sort massive amounts of data (Gigabytes, Terabytes, etc.)

Parallel sort

An algorithm which can be ran on multiple threads at the same time, speeding the running time.

Locality

An algorithm which heavily uses the processor cache to speed up its execution. The data processed needs to be sequentially located.

Helper code

```
// swap the values of two variables
void swap(int & a, int & b) {
    int tmp = a;
    a = b;
    b = tmp;
}
```

Bubble sort

Bubble sort	n = input size
Time complexity	$\mathcal{O}(n^2)$
Space complexity	$\mathcal{O}(1)$
Adaptive	Yes
Stable	Yes
Number of comparisons	$\mathcal{O}(n^2)$
Number of swaps	$\mathcal{O}(n^2)$
Online	No
In place	Yes

Honorable mention - Cocktail shaker sort, similar to bubble and selection sort. It's like the Online version of bubble sort.

Clean code

```
void bubbleSort(int * array, int length) {
    for (int bubbleStartIndex = 0; bubbleStartIndex < length;
        bubbleStartIndex++) {
        for (int bubbleMovedIndex = 0; bubbleMovedIndex < length - 1;
            bubbleMovedIndex++) {
            if (array[bubbleMovedIndex] > array[bubbleMovedIndex+1]) {
                swap(array[bubbleMovedIndex], array[bubbleMovedIndex+1]);
            }
        }
    }
}
```

Short code

```
void bubbleSort(int * array, int length) {
    for (int i = 0; i < length; i++) {
        for (int k = 0; k < length - 1; k++) {
            if (array[k] > array[k+1]) {
                swap(array[k], array[k+1]);
            }
        }
    }
}
```

Optimization 1 - make it faster

```

void bubbleSort(int * array, int length) {
    for (int i = 0; i < length; i++) {
        for (int k = 0; k < length - 1 - i; k++) { // length - 1 - i = 2x less
iterations
            if (array[k] > array[k+1]) {
                swap(array[k], array[k+1]);
            }
        }
    }
}

```

Optimization 2 - make it adaptive

```

void bubbleSort(int * array, int length) {
    for (int i = 0; i < length; i++) {
        bool swappedAtLeastOnce = false; // add a flag to check if a swap has
occurred

        for (int k = 0; k < length - 1 - i; k++) {
            if (array[k] > array[k+1]) {
                swap(array[k], array[k+1]);
                swappedAtLeastOnce = true;
            }
        }

        if (!swappedAtLeastOnce) { // if there were no swaps, it's ordered
            break;
        }
    }
}

```

Selection sort

Selection sort	n = input size
Time complexity	$\mathcal{O}(n^2)$
Space complexity	$\mathcal{O}(1)$
Adaptive	No
Stable	No
Number of comparisons	$\mathcal{O}(n^2)$
Number of swaps	$\mathcal{O}(n)$
Online	No
In place	Yes

Key points

1. It's better than bubble sort in cases we need to sort items which are very large in size because it has $\mathcal{O}(n)$ swaps.

Clean code

```
void selectionSort(int * array, int length) {
    for (int currentIndex = 0; currentIndex < length; currentIndex++) {
        int smallestNumberIndex = currentIndex;

        for (int potentialSmallerNumberIndex = currentIndex + 1;
             potentialSmallerNumberIndex < length;
             potentialSmallerNumberIndex++) {
            if (array[potentialSmallerNumberIndex] < array[smallestNumberIndex])
            {
                smallestNumberIndex = potentialSmallerNumberIndex;
            }
        }

        swap(array[currentIndex], array[smallestNumberIndex]);
    }
}
```

Short code

```
void selectionSort(int * array, int length) {
    for (int i = 0; i < length; i++) {
        int index = i;

        for (int k = i + 1; k < length; k++) {
            if (array[k] < array[index]) {
                index = k;
            }
        }

        swap(array[i], array[index]);
    }
}
```

Insertion sort

Insertion sort	n = input size
Time complexity	$\mathcal{O}(n^2)$
Space complexity	$\mathcal{O}(1)$
Adaptive	Yes
Stable	Yes
Number of comparisons	$\mathcal{O}(n^2)$
Number of swaps	$\mathcal{O}(n^2)$
Online	Yes
In place	Yes

Key points

1. The best algorithm for sorting small arrays.
2. Often combined with other algorithms for optimal runtime.

Clean code

```
void insertionSort(int * array, int length) {
    for (int nextItemToSortIndex = 1; nextItemToSortIndex < length;
nextItemToSortIndex++) {
        for (int potentiallyBiggerItemIndex = nextItemToSortIndex;
            potentiallyBiggerItemIndex > 0 &&
            array[potentiallyBiggerItemIndex] <
array[potentiallyBiggerItemIndex - 1];
            potentiallyBiggerItemIndex--) {
            swap(array[potentiallyBiggerItemIndex],
array[potentiallyBiggerItemIndex-1]);
        }
    }
}
```

Short code

```
void insertionSort(int * array, int length) {
    for (int i = 1; i < length; i++) {
        for (int k = i; k > 0 && array[k] < array[k - 1]; k--) {
            swap(array[k], array[k-1]);
        }
    }
}
```

Merge sort

Merge sort	n = input size
Time complexity	$\mathcal{O}(n * \log(n))$
Space complexity	$\mathcal{O}(n)$
Adaptive	No
Stable	Yes
Number of comparisons	$\mathcal{O}(n * \log(n))$
External	Yes
Parallel	Yes
Online	No
In place	No

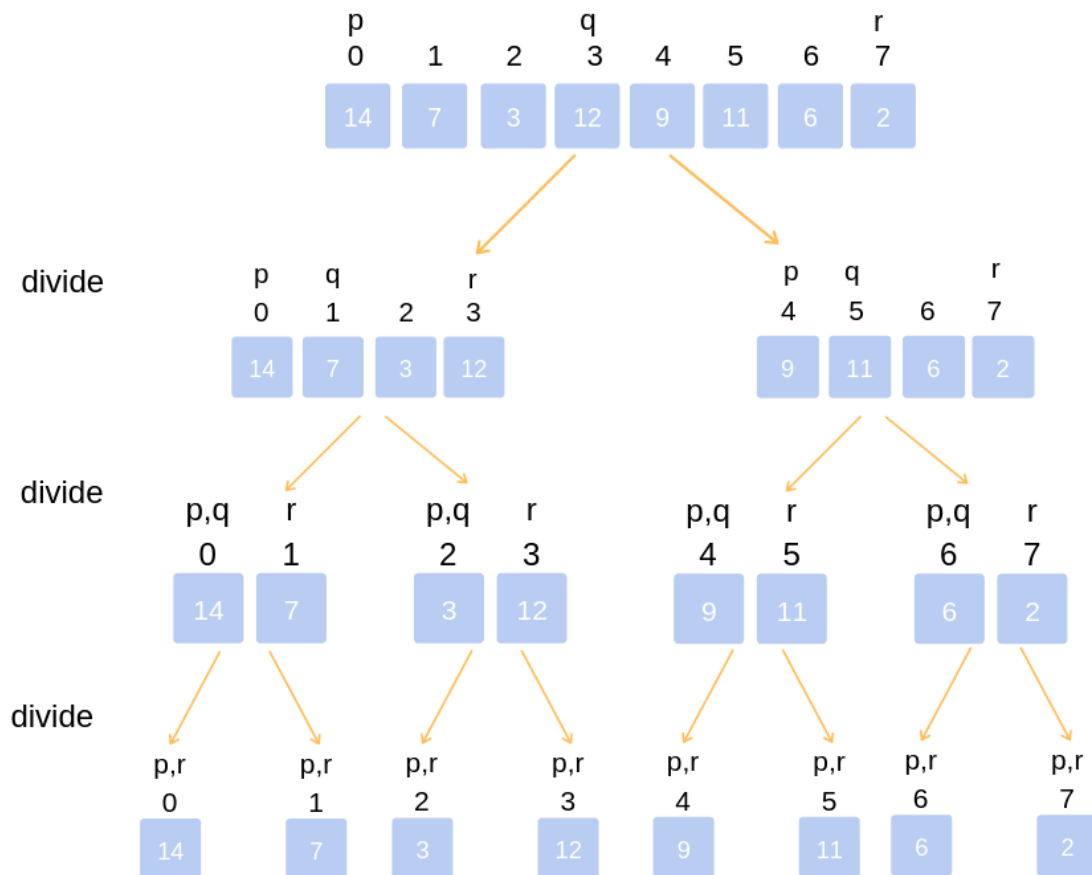
Key points

1. Every array of 0 or 1 elements is sorted.
2. Merging requires additional memory.
3. Splitting the array in 2 every time gives us $\log(n)$ levels.

4. On each level we have $\mathcal{O}(n)$ for the merging operation.

Honorable mention - Ford-Johnson aka Merge-insertion sort. Cool idea, but not practical enough.

Important algorithm: Timsort - Absolute beast.



Clean code

```
void merge(int * originalArray, int * mergeArray, int start, int mid, int end) {
    int leftIndex = start;
    int rightIndex = mid + 1;
    int sortedIndex = start;

    while (leftIndex <= mid && rightIndex <= end) {
        if (originalArray[leftIndex] <= originalArray[rightIndex]) {
            mergeArray[sortedIndex] = originalArray[leftIndex];
            leftIndex++;
        } else {
            mergeArray[sortedIndex] = originalArray[rightIndex];
            rightIndex++;
        }

        sortedIndex++;
    }

    while (leftIndex <= mid) {
        mergeArray[sortedIndex] = originalArray[leftIndex];
        leftIndex++;
    }

    while (rightIndex <= end) {
        mergeArray[sortedIndex] = originalArray[rightIndex];
        rightIndex++;
    }
}
```



```

    }

    for (int i = start; i <= end; i++) {
        originalArray[i] = mergeArray[i];
    }
}

void mergeSortRecursive(int * original, int * mergeArray, int start, int end) {
    if (start < end) {
        int mid = (start + end) / 2;

        mergeSortRecursive(original, mergeArray, start, mid);
        mergeSortRecursive(original, mergeArray, mid + 1, end);

        merge(original, mergeArray, start, mid, end);
    }
}

void mergeSort(int * array, int length) {
    int * mergeArray = new int[length];
    mergeSortRecursive(array, mergeArray, 0, length - 1);
    delete[] mergeArray;
}

```

Short code

```

void merge(int * originalArray, int * mergeArray, int start, int mid, int end) {
    int left = start;
    int right = mid + 1;

    for (int i = start; i <= end; i++) {
        if (left <= mid && (right > end || originalArray[left] <=
originalArray[right])) {
            mergeArray[i] = originalArray[left];
            left++;
        } else {
            mergeArray[i] = originalArray[right];
            right++;
        }
    }

    for (int i = start; i <= end; i++) {
        originalArray[i] = mergeArray[i];
    }
}

void mergeSortRecursive(int * originalArray, int * mergeArray, int start, int
end) {
    if (start < end) {
        int mid = (start + end) / 2;

        mergeSortRecursive(originalArray, mergeArray, start, mid);
        mergeSortRecursive(originalArray, mergeArray, mid + 1, end);

        merge(originalArray, mergeArray, start, mid, end);
    }
}

```

```

void mergeSort(int * array, int length) {
    int * mergeArray = new int[length];
    mergeSortRecursive(array, mergeArray, 0, length - 1);
    delete[] mergeArray;
}

```

Quick sort

Quick sort	n = input size
Time complexity (Worst case)	$O(n^2)$
Time complexity (Average case)	$O(n * \log(n))$
Space complexity	$O(\log(n))$
Adaptive	No
Anti-Adaptive	Yes (the more randomness, the better)
Stable	No
Number of comparisons	$O(n * \log(n))$
Parallel	Yes
Online	No
In place	Yes
Locality	Yes

Key points

1. Quick sort adores chaos. That's why a common strategy is to shuffle the array before sorting it.

C++ STL sorting algorithm is Introsort, which is a hybrid between quicksort and heapsort.

Quick sort optimization for arrays with many equal numbers - three-way partitioning, aka Dutch national flag.

Quick sort can also be optimized with picking 2 pivots instead of 1 - multi-pivot quicksort.

Uses apart from sorting

1. Find k-th biggest/smallest element

Clean code using Lomuto partitioning

```

int partition(int * array, int startIndex, int endIndex) {
    int pivot = array[endIndex];
    int pivotIndex = startIndex;

    for (int i = startIndex; i <= endIndex; i++) {
        if (array[i] < pivot) {
            swap(array[i], array[pivotIndex]);
            pivotIndex++;
        }
    }
}

```

```

    }

    swap(array[endIndex], array[pivotIndex]);
    return pivotIndex;
}

void _quickSort(int * array, int startIndex, int endIndex) {
    if (startIndex < endIndex) {
        int pivot = partition(array, startIndex, endIndex);
        _quickSort(array, startIndex, pivot - 1);
        _quickSort(array, pivot + 1, endIndex);
    }
}

void quickSort(int * array, int length) {
    _quickSort(array, 0, length - 1);
}

```

Short code using Lomuto partitioning

```

int partition(int * array, int start, int end) {
    int pivot = array[end];
    int pivotIndex = start;
    for (int i = start; i <= end; i++) {
        if (array[i] < pivot) {
            swap(array[i], array[pivotIndex]);
            pivotIndex++;
        }
    }
    swap(array[end], array[pivotIndex]);
    return pivotIndex;
}

void _quickSort(int * array, int start, int end) {
    if (start < end) {
        int pivot = partition(array, start, end);
        _quickSort(array, start, pivot - 1);
        _quickSort(array, pivot + 1, end);
    }
}

void quickSort(int * array, int length) {
    _quickSort(array, 0, length - 1);
}

```

Optimization 1 - pivot is random number

```

#include <random>

int generateRandomNumber(int from, int to) {
    std::random_device dev;
    std::mt19937 rng(dev());
    std::uniform_int_distribution<std::mt19937::result_type> dist6(from, to);

    return dist6(rng);
}

```

```

int partition(int * array, int start, int end) {
    int randomIndex = generateRandomNumber(start, end);
    swap(array[end], array[randomIndex]);

    int pivot = array[end];
    int pivotIndex = start;
    for (int i = start; i <= end; i++) {
        if (array[i] < pivot) {
            swap(array[i], array[pivotIndex]);
            pivotIndex++;
        }
    }
    swap(array[end], array[pivotIndex]);
    return pivotIndex;
}

void _quickSort(int * array, int start, int end) {
    if (start < end) {
        int pivot = partition(array, start, end);
        _quickSort(array, start, pivot - 1);
        _quickSort(array, pivot + 1, end);
    }
}

void quickSort(int * array, int length) {
    _quickSort(array, 0, length - 1);
}

```

Optimization 2 - shuffle before picking pivot

```

#include <random>

int generateRandomNumber(int from, int to) {
    std::random_device dev;
    std::mt19937 rng(dev());
    std::uniform_int_distribution<std::mt19937::result_type> dist6(from, to);

    return dist6(rng);
}

void shuffle(int * arr, int length) {
    for (int i = 0; i < length - 1; i++) {
        int swapCurrentWith = generateRandomNumber(i, length - 1);
        swap(arr[i], arr[swapCurrentWith]);
    }
}

int partition(int * array, int start, int end) {
    shuffle(array + start, end - start);

    int pivot = array[end];
    int pivotIndex = start;
    for (int i = start; i <= end; i++) {
        if (array[i] < pivot) {
            swap(array[i], array[pivotIndex]);
            pivotIndex++;
        }
    }
}

```

```

    }
    swap(array[end], array[pivotIndex]);
    return pivotIndex;
}

void _quickSort(int * array, int start, int end) {
    if (start < end) {
        int pivot = partition(array, start, end);
        _quickSort(array, start, pivot - 1);
        _quickSort(array, pivot + 1, end);
    }
}

void quickSort(int * array, int length) {
    _quickSort(array, 0, length - 1);
}

```

Short code using Hoare partitioning

```

int partition(int * array, int start, int end) {
    int pivot = array[(start + end) / 2];
    int left = start;
    int right = end;

    while (true) {
        while (array[left] < pivot) {
            left++;
        }
        while (array[right] > pivot) {
            right--;
        }

        if (left >= right) {
            return right;
        }

        swap(array[left], array[right]);
    }
}

void _quickSort(int * array, int start, int end) {
    if (start < end) {
        int pivot = partition(array, start, end);
        _quickSort(array, start, pivot - 1);
        _quickSort(array, pivot + 1, end);
    }
}

void quickSort(int * array, int length) {
    _quickSort(array, 0, length - 1);
}

```

Counting sort

Counting sort	n = input size, k = max number
Time complexity (Worst case)	$\mathcal{O}(n + k)$
Time complexity (Best case)	$\mathcal{O}(n)$
Space complexity	$\mathcal{O}(k)$

Key points

1. Not a comparison sort.
2. Very efficient for an array of integers with many repeating integers with small difference between the biggest and smallest integer.

Uses apart from sorting

1. Counting inversions

Counting sort for positive numbers

```
void countingSort(int * array, int length) {
    int maxNumber = 0;
    for (int i = 0; i < length; i++) {
        if (array[i] > maxNumber) {
            maxNumber = array[i];
        }
    }

    int * countingArray = new int[maxNumber + 1];
    for (int i = 0; i < maxNumber + 1; i++) {
        countingArray[i] = 0;
    }

    for (int i = 0; i < length; i++) {
        countingArray[array[i]]++;
    }

    int sortedIndex = 0;
    for (int i = 0; i < length; i++) {
        while (countingArray[sortedIndex] == 0) {
            sortedIndex++;
        }

        array[i] = sortedIndex;
        countingArray[sortedIndex]--;
    }

    delete[] countingArray;
}
```

Bucket sort

Bucket sort	n = input size, k = number of buckets
Time complexity (Worst case)	$\mathcal{O}(n^2)$
Time complexity (Average case)	$\mathcal{O}(n + \frac{n^2}{k} + k)$
Space complexity	$\mathcal{O}(nk)$

Key points

1. It's a distribution sort, not a comparison sort.
2. Very situational sort.
3. The bellow code is a sample implementation for floats between 0 and 1.

Code

```
#include <iostream>
#include <vector>
#include <algorithm>
void bucketSort(double *array, int length) {
    std::vector<double> buckets[length];

    for(int i = 0; i < length; i++) {
        buckets[int(length * array[i])].push_back(array[i]);
    }

    for(int i = 0; i < length; i++) {
        sort(buckets[i].begin(), buckets[i].end());
    }

    int index = 0;
    for(int i = 0; i < length; i++) {
        while(!buckets[i].empty()) {
            array[index] = buckets[i][0];
            index++;
            buckets[i].erase(buckets[i].begin());
        }
    }
}
```

Radix sort

Radix sort	n = input size
Time complexity (Worst case)	$\mathcal{O}(n^2)$
Time complexity (Average case)	$\mathcal{O}(n + \frac{n^2}{k} + k)$
Space complexity	$\mathcal{O}(nk)$

Key points

1. Good on multi-threaded machines.

Code

```

#include <iostream>
#include <cmath>
#include <list>

int abs(int a) {
    return a >= 0 ? a : -a;
}

void radixSort(int * array, int length) {
    int maxNumber = 0;
    for (int i = 0; i < length; i++) {
        if (abs(array[i]) > maxNumber) {
            maxNumber = abs(array[i]);
        }
    }

    int maxDigits = log10(maxNumber) + 1;

    std::list<int> pocket[10];

    for(int i = 0; i < maxDigits; i++) {
        int m = pow(10, i + 1);
        int p = pow(10, i);

        for(int j = 0; j < length; j++) {
            int temp = array[j] % m;
            int index = temp / p;
            pocket[index].push_back(array[j]);
        }

        int count = 0;
        for(int j = 0; j < 10; j++) {
            while(!pocket[j].empty()) {
                array[count] = *(pocket[j].begin());
                pocket[j].erase(pocket[j].begin());
                count++;
            }
        }
    }
}

```

Searching

Linear search

Linear search	n = input size
Time complexity	$\mathcal{O}(n)$
Space complexity	$\mathcal{O}(1)$

Algorithm idea

Iterate every element in order and check if it is the element we are looking for.

Uses

Searching in unordered data, when we have very few queries. If we have many requests it's better to sort the array and use faster searching for the queries.

Binary search

Binary search	n = input size
Time complexity	$\mathcal{O}(\log(n))$
Space complexity	$\mathcal{O}(1)$

Works only on sorted array-like structures, which support $\mathcal{O}(1)$ access to elements.

The algorithm uses $\mathcal{O}(\log(n))$ space if written recursively, but can be written iteratively to have $\mathcal{O}(1)$ space as well.

Algorithm idea

1. Check the middle element, if it's the element we are looking for - we are done
2. If the element is bigger than the one we are looking for - recurse into the left sub-array (the sub-array with smaller elements).
3. If the element is smaller than the one we are looking for - recurse into the right sub-array (the sub-array with bigger elements).

Uses

Fast searching in ordered data.

Guess and check algorithms.

Ternary search

Ternary search	n = input size
Time complexity	$\mathcal{O}(\log(n))$
Space complexity	$\mathcal{O}(1)$

Algorithm idea

The same idea as binary search but we split the array in 3 parts. On each step we decide which one part to discard and recurse into the other 2.

Uses

Finding min/max in a sorted array.

Exponential search

Exponential search	n = input size
Time complexity	$\mathcal{O}(\log(n))$
Space complexity	$\mathcal{O}(1)$

Algorithm idea

This is the binary search algorithm applied for ordered data of unknown size. We don't have a mid point so we start from the beginning and double our guessed index each time. e.g for guessed index: 1, 2, 4, 8, 16, 32... If we overshoot the end of the data we go back using binary search because we now have an end index. e.g for array with 27 elements we do a jump to element 32 which doesn't exist and then use binary search on elements 16 - 32.

Uses

Binary search on streams, which are ordered and other ordered data of unknown size.

Jump search

Jump search	n = input size
Time complexity	$\mathcal{O}(\log(n))$
Space complexity	$\mathcal{O}(1)$

Algorithm idea

We decide on a jump step and check elements on each step. e.g for step 32 we will check elements 0, 32, 64, etc.

Optimal jump step is \sqrt{n} .

Uses

Because it's worse than Binary search, it's useful when the data structure we are searching in has very slow jump back, aka it's slow to go back to index $i - 10$ from i .

Interpolation search

Interpolation search	n = input size
Time complexity for evenly distributed data	$\mathcal{O}(\log(\log(n)))$
Time complexity for badly distributed data	$\mathcal{O}(n)$
Space complexity	$\mathcal{O}(1)$

Algorithm idea

If we have well distributed data we can approximate where we will find the element with the following formula

$$jumpToIndex = startIndex + \left(\frac{endIndex - startIndex}{array[endIndex] - array[startIndex]} \right) \times (target - array[startIndex])$$

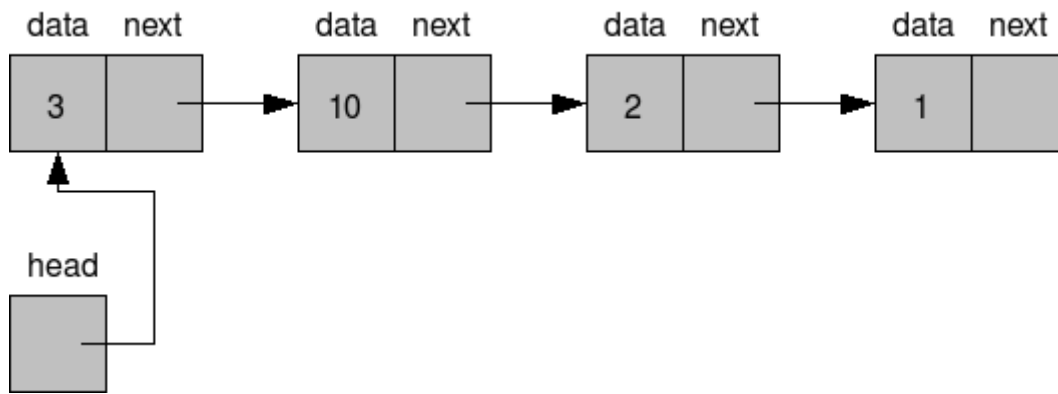
Example for well distributed data: 1, 2, 3, 4, 5, 6 99, 100

Example for badly distributed data: 1, 1, 1, 1.... 1, 1, 100

Uses

Very situational, when we have data which is very well distributed.

Linked lists



Linked list stores its data in separate Nodes. Each node points the next node in the list. The last node points NULL.

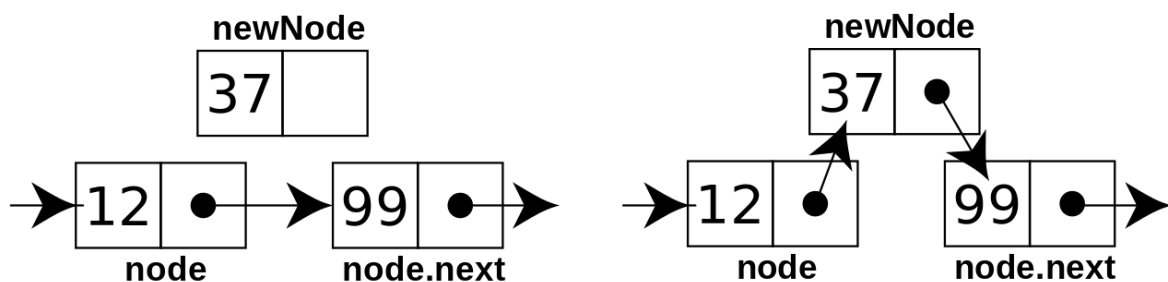
The most primitive linked list's node contains 2 fields - Data and Next pointer

```
struct Node {
    int data;
    Node* next;
};
```

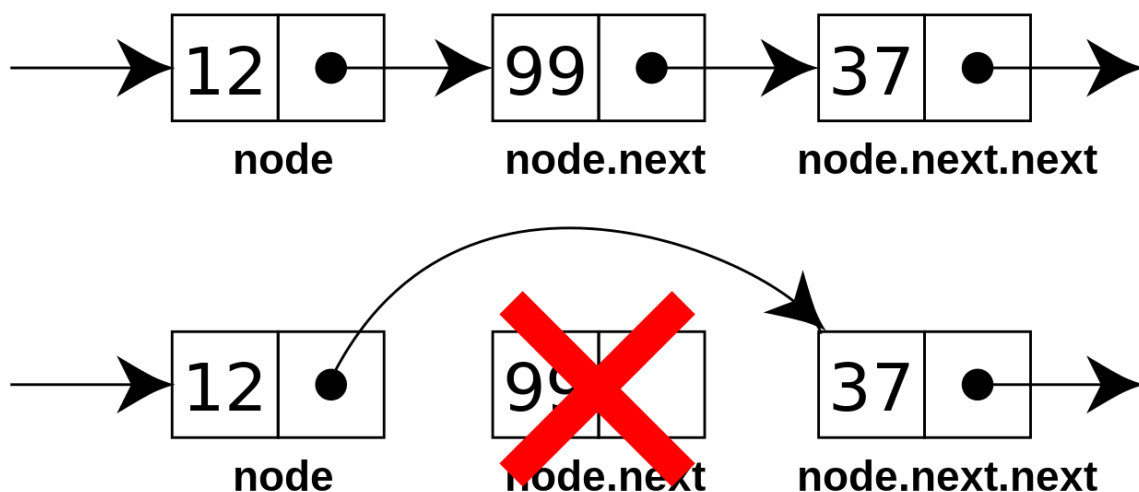
Use

Linked lists are useful if we don't know the input size (when getting data from streams).

Inserting a node



Removing a node



Singly linked list

Singly linked lists have only one pointer to the next Node.

```
struct Node {  
    int data;  
    Node* next;  
};
```

Doubly linked list

Doubly linked lists have two pointers, one to the previous item, one to the next.

```
struct Node {  
    int data;  
    Node* previous;  
    Node* next;  
};
```

Circular linked list

Circular linked lists can be implemented as singly or doubly linked list but the start and end nodes are connected. i.e the end node's next pointer is not NULL but points the first node instead.

XOR linked list

Unrolled linked list

Skip list

Dynamic arrays

Stack (LIFO)

Queue (FIFO)

Ring buffer

Okasaki Queue

Trees

Traversals

Preorder

Postorder

Inorder traversal

Level order

Morris order

Tree variations

Trie

Segment Tree

Merge Tree

K-D Tree

BSP Tree

Merkle Tree

Treap

Strict Binary Tree

Full Binary Tree

Complete Binary Tree

Binary Search Trees

BST

AVL Tree

Splay Tree

Scape Goat Tree

Red-black Tree

Heap

Heap sort

Disjoint Set

Hashes

Rolling hash

Bloom Filter

Graphs

Graph variations

Undirected Graph

Directed Graph

Weighted Graph

Connected Graph

Disconnected Graph

Trees

Complete Graph

Tournament Graph

Bipartite Graph

Representing Graphs

Edge List

Adjacency Matrix

Adjacency List

Exploring Graphs

Depth First Search

Breadth First Search

Topological Sorting

Minimum Spanning Tree

Prim

Kruskal

Shortest Path

Dijkstra

Bellman-Ford

A*

NP-problems
