



$$m_1 = 0.23 \text{ kg}$$

$$N_{01} = N_{02} = 0$$

Vertikal compl. ausl.

$$m_2 = 0.51 \text{ kg}$$

$$k = 150 \text{ N/m}$$

$$\Delta x_{\max} = 0.068 \text{ m}$$

$$N_1 = \sqrt{2gh / \sin \theta} \quad a = g \sin \theta \quad * \quad v_f^2 = v_i^2 + 2a \Delta l$$

~~$m_1 gh = m_1 N_1$~~

$$m_1 gh = \frac{1}{2} m_1 N_1^2 \quad * \quad \Rightarrow N_1 = \sqrt{2gh}$$

~~$m_1 gh = \frac{1}{2} (m_1 + m_2) N_1^2$~~

$$\bar{P} = \text{cost} \Rightarrow m_1 N_1 = (m_1 + m_2) N$$

$$\Rightarrow N = \frac{m_1}{m_1 + m_2} \sqrt{2gh}$$

$$\frac{1}{2} k \Delta x^2 = \frac{1}{2} m_2 N^2$$

~~$$0 = v^2 + 2 \alpha \Delta x$$~~

$$\alpha = - \frac{k \Delta x}{m_1 + m_2}$$

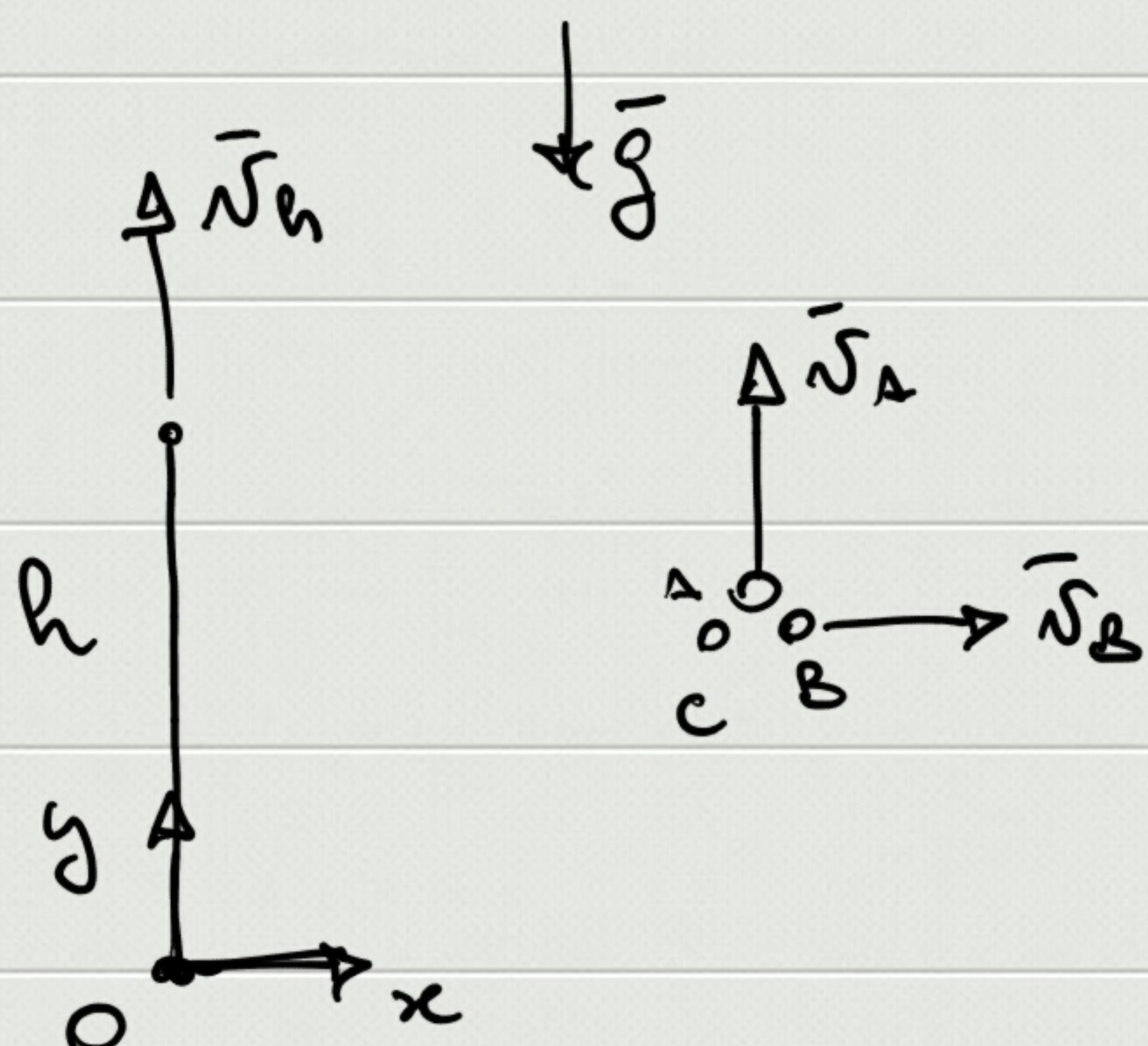
~~$$\frac{1}{2} k \Delta x^2 = m_1 g h$$~~

~~$$\frac{1}{2} k \Delta x^2 = \frac{1}{2} (m_1 + m_2) N^2$$~~

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$$k \Delta x^2 = (m_1 + m_2) \frac{m_1^2}{(m_1 + m_2)^2} 2gh$$

$$\Rightarrow h = \frac{m_1 + m_2}{m_1^2} \frac{k \Delta x^2}{2g} = 0.495 \text{ m}$$



$$h = 1000 \text{ m}$$

$$v_h = 250 \text{ m/s}$$

$$m_A = m_C = m$$

$$m_B = 2 \text{ m}$$

$$v_A = 450 \text{ m/s}$$

$$v_B = 240 \text{ m/s}$$

$$\bar{v}_c = ? \quad \bar{r}_{cm}(t_1=2s) = ?$$

$$\bar{P} = \text{cost}$$

~~$$\bar{v}_c = \bar{v}_h - \bar{v}_A - \bar{v}_B$$~~

~~$$\frac{1}{2} (4m) \bar{v}_h^2 = \frac{1}{2} m_A \bar{v}_A^2 + \frac{1}{2} m_B \bar{v}_B^2 + \frac{1}{2} m_C \bar{v}_C^2$$~~

$$4 \cancel{m} \bar{v}_h = \cancel{m} \bar{v}_A + 2 \cancel{m} \bar{v}_B + \cancel{m} \bar{v}_C \quad *$$

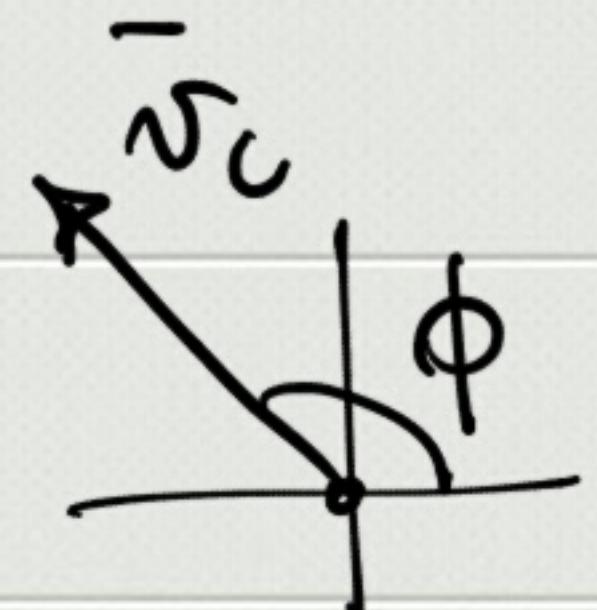
~~$$4 m \bar{v}_h = m \cancel{\bar{v}_A} + 2 m \bar{v}_B + m \bar{v}_C$$~~

$$x: \left\{ \begin{array}{l} 0 = 2 \bar{v}_B + \bar{v}_{Cx} \Rightarrow \bar{v}_{Cx} = -2 \bar{v}_B = -480 \text{ m/s} \end{array} \right.$$

$$y: \left\{ \begin{array}{l} 4 \bar{v}_h = \bar{v}_A + \bar{v}_{Cy} \Rightarrow \bar{v}_{Cy} = 4 \bar{v}_h - \bar{v}_A = 550 \text{ m/s} \end{array} \right.$$

$$v_c = \sqrt{\bar{v}_{Cx}^2 + \bar{v}_{Cy}^2} = 730 \text{ m/s}$$

$$\tan \phi = \frac{\bar{v}_{Cy}}{\bar{v}_{Cx}} \Rightarrow \phi = 131^\circ$$



$$\bar{r}_{cm} = \frac{\sum_i^3 (\cancel{r_{0,i}} + \frac{1}{2} \bar{g} t_i^2) m_i}{\sum_i m_i}$$

$$\bar{r}_{cm} = \frac{\sum_i (\bar{r}_{0,i} + \bar{v}_{0,i} t_i + \frac{1}{2} \bar{g} t_i^2) m_i}{\sum_i m_i} *$$

$$y_{cm} = \cancel{h} \cancel{x_{cm}} = 0$$

$$y_{cm} = h + \sqrt{h} t_i - \frac{1}{2} \bar{g} t_i^2 \quad x_{cm} = 0 \quad *$$

$$\bar{r}_{cm} = \frac{\sum_i m_i \bar{r}_i}{\sum_i m_i} \quad \bar{R}^E = M_{TOT} \bar{a}_{cm}$$

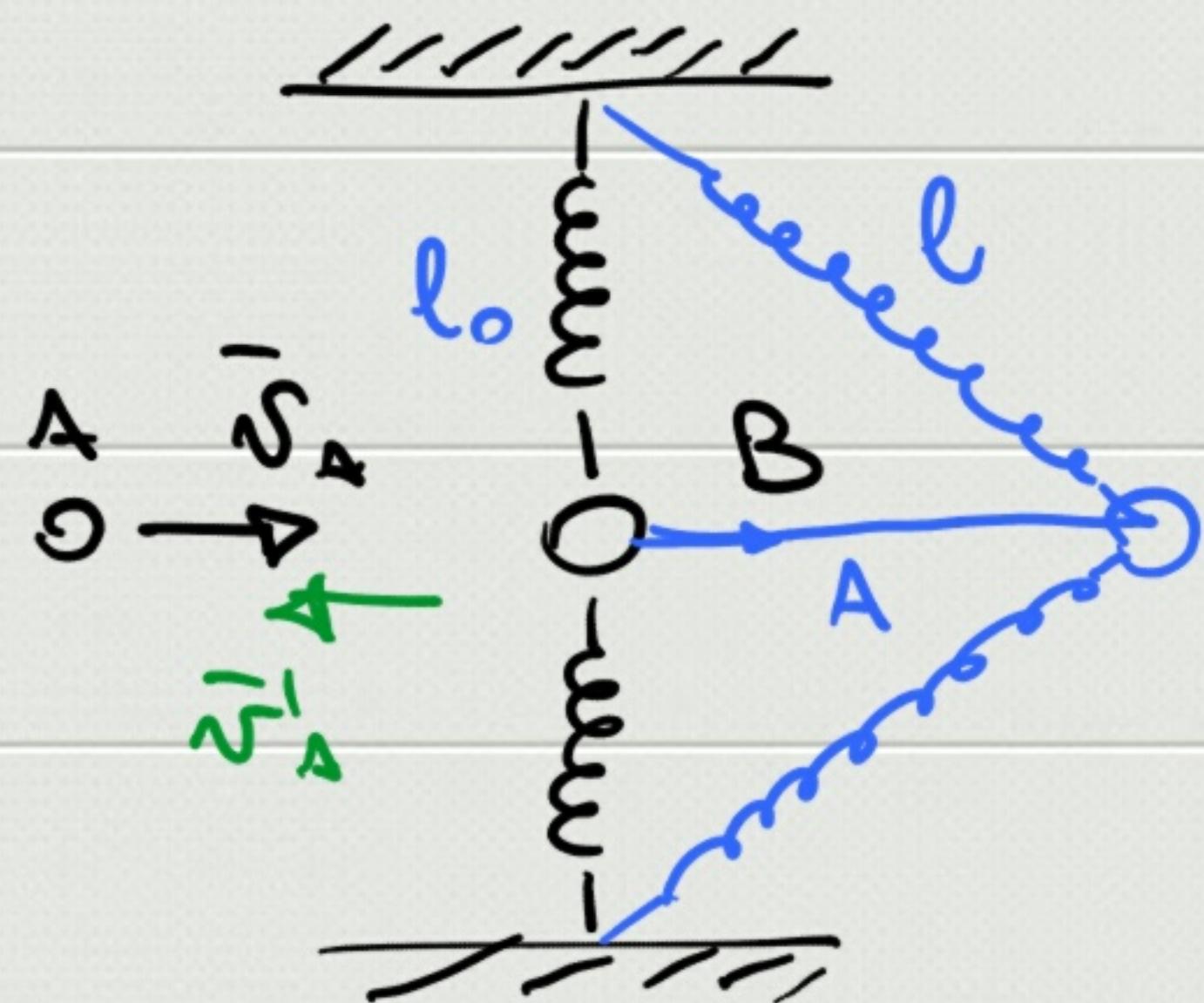
$$4m\bar{g} = M_{TOT} \bar{a}_{cm} \Rightarrow \boxed{\bar{a}_{cm} = \bar{g}}$$

$$\bar{r}_{cm} = \bar{r}_0 + \bar{v}_0 t + \frac{1}{2} \bar{a}_{cm} t^2$$

↓      ↓      ↓  
 $(0, h)$      $(0, \sqrt{h})$      $(0, -g)$

$$x_{cm} = 0 \quad y_{cm} = h + \sqrt{h} t - \frac{1}{2} g t^2$$

$$\Rightarrow y_{cm}(t_1) = 1480 \text{ m}$$



$$m_A = 0.1 \text{ kg}$$

$$v_A = 1.5 \text{ m/s}$$

$$m_B = 1 \text{ kg} \quad v_{0B} = 0$$

$$l_0 = 1 \text{ m} \quad k = 0.5 \text{ N/m}$$

$$|v'_A| = 0.5 \text{ m/s}$$

$$v'_B = ?$$

~~$$\bar{v}_A = \bar{v}_A + \bar{v}'_B$$~~

~~$$m_A \bar{v}_A = -m_A \bar{v}_A + m_B \bar{v}'_B$$~~

$$\frac{1}{2} m_A v_A^2 = \frac{1}{2} m_A v_A'^2 + \frac{1}{2} m_B v_B'^2$$

$$m_A v_A = m_A v_A' + m_B v_B' \quad * \quad v_A' = -|v_A'|$$

$$\Rightarrow v_B' = \frac{m_A}{m_B} (v_A - v_A') = 0.2 \text{ m/s}$$

$$\Delta E_{\text{dim}} = |\Delta E_m| = |\Delta E_k| = |E_{k,\text{fin}} - E_{k,\text{ini}}| =$$

$$= \left| \left( \frac{1}{2} m_A v_A'^2 + \frac{1}{2} m_B v_B'^2 \right) - \frac{1}{2} m_A v_A^2 \right| = 0.08 \text{ J}$$

$$E_p = \frac{1}{2} k \Delta x^2$$

~~$$\frac{1}{2} m_B v_B'^2 = 2 \cdot \frac{1}{2} k l^2$$~~

~~$$0 = v_B'^2 + 2\alpha A \quad \alpha = \frac{kA}{m_B}$$~~

~~$$\frac{1}{2} m_B v_B'^2 = 2 \cdot \frac{1}{2} k (l - l_0)^2$$~~

~~$$\frac{1}{2} m_A v_A'^2 + \frac{1}{2} m_B v_B'^2 = 2 \cdot \frac{1}{2} k (l - l_0)^2$$~~

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$$l = l_0 + v_B' \sqrt{\frac{m_B}{2k}}$$

$$A = \sqrt{l^2 - l_0^2} = 0.66 \text{ m}$$