

$$\vec{R}^E = m \vec{a}_{CM}$$

$$\vec{M}_{pole}^E = \vec{I}_{CM} \alpha$$

$$\vec{M}_O = \vec{r} \times \vec{F}$$

$$\vec{F} + m\vec{g} + \vec{N} + \vec{f} = m \vec{a}_{CM}$$

$$pole \equiv CM \Rightarrow \vec{R} \times \vec{f} = \vec{I}_{CM} \alpha$$

$$\Rightarrow \begin{cases} F - f = m a_{CM} \\ N - mg = 0 \\ Rf = I_{CM} \alpha \\ a_{CM} = \alpha R \end{cases} \Rightarrow N = mg$$

$$\Rightarrow Rf = I_{CM} \alpha = I_{CM} \frac{a_{CM}}{R} \Rightarrow f = \frac{I_{CM}}{R^2} a_{CM}$$

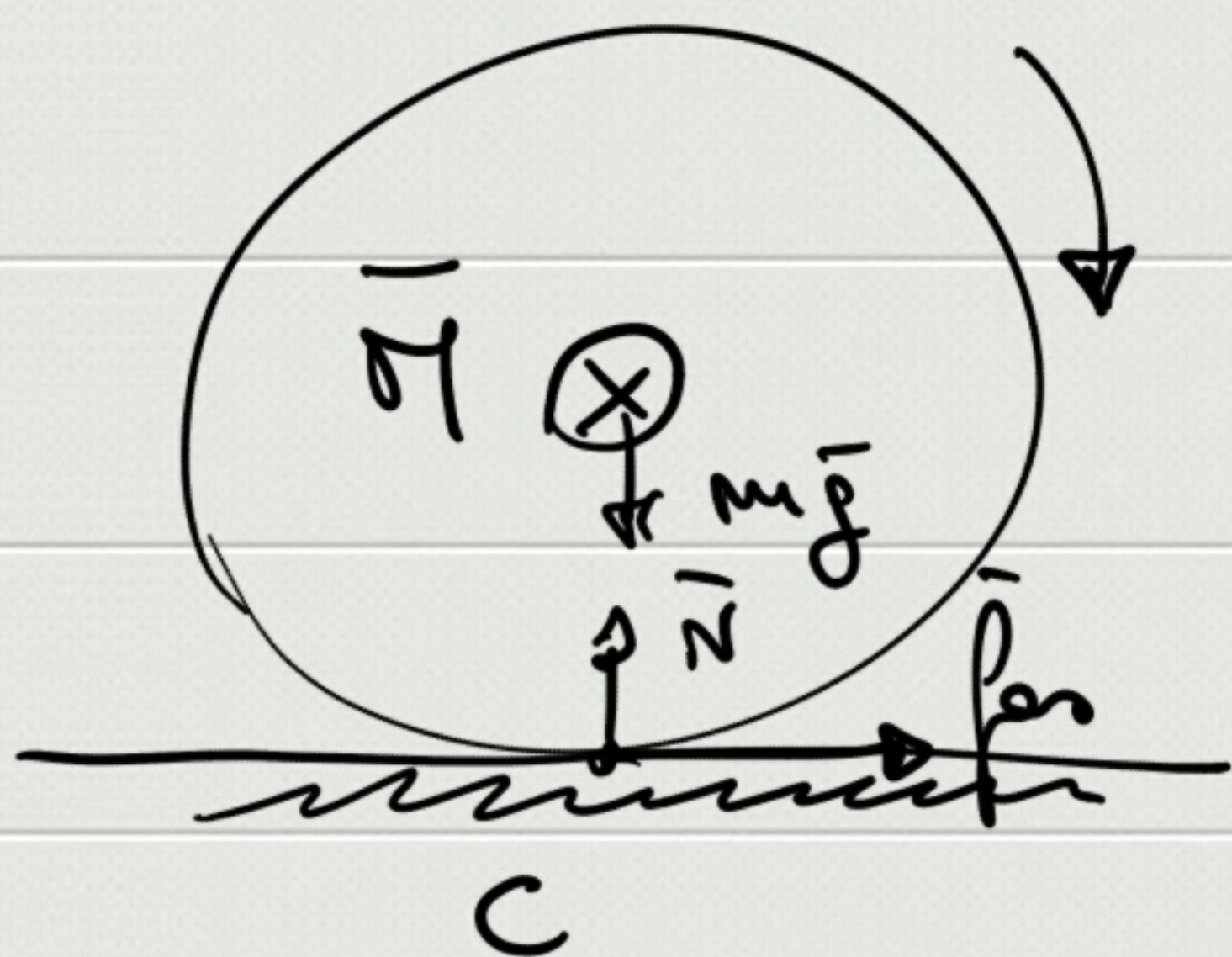
$$\Rightarrow F - \frac{I_{CM}}{R^2} a_{CM} = m a_{CM} \Rightarrow a_{CM} = \frac{F/m}{1 + \frac{I_{CM}}{m R^2}}$$

$$f_{\text{as}} = \frac{I_{\text{cm}}}{R^2} \frac{F/m}{1 + \frac{I_{\text{cm}}}{mR^2}} = \frac{F}{1 + \frac{mR^2}{I_{\text{cm}}}}$$

$$f_{\text{as}} \leq f_{\text{as, max}} = \mu_s N$$

$$\Rightarrow f_{\text{as}} = \frac{F}{1 + \frac{mR^2}{I_{\text{cm}}}} \leq \mu_s mg \Rightarrow$$

$$\Rightarrow F \leq F_{\text{max}} = \mu_s mg \left(1 + \frac{mR^2}{I_{\text{cm}}} \right)$$



$$\begin{cases} m\vec{g} + \vec{N} + \vec{f}_{es} = m\vec{a}_{cm} \\ \vec{r} \times \vec{f}_{es} + \vec{M} = \vec{I}_{cm} \vec{\alpha} \end{cases}$$

$$\Rightarrow \begin{cases} f_{es} = m a_{cm} \\ -R f_{es} + M = I_{cm} \alpha = I_{cm} \frac{a_{cm}}{R} \end{cases} \quad N = mg$$

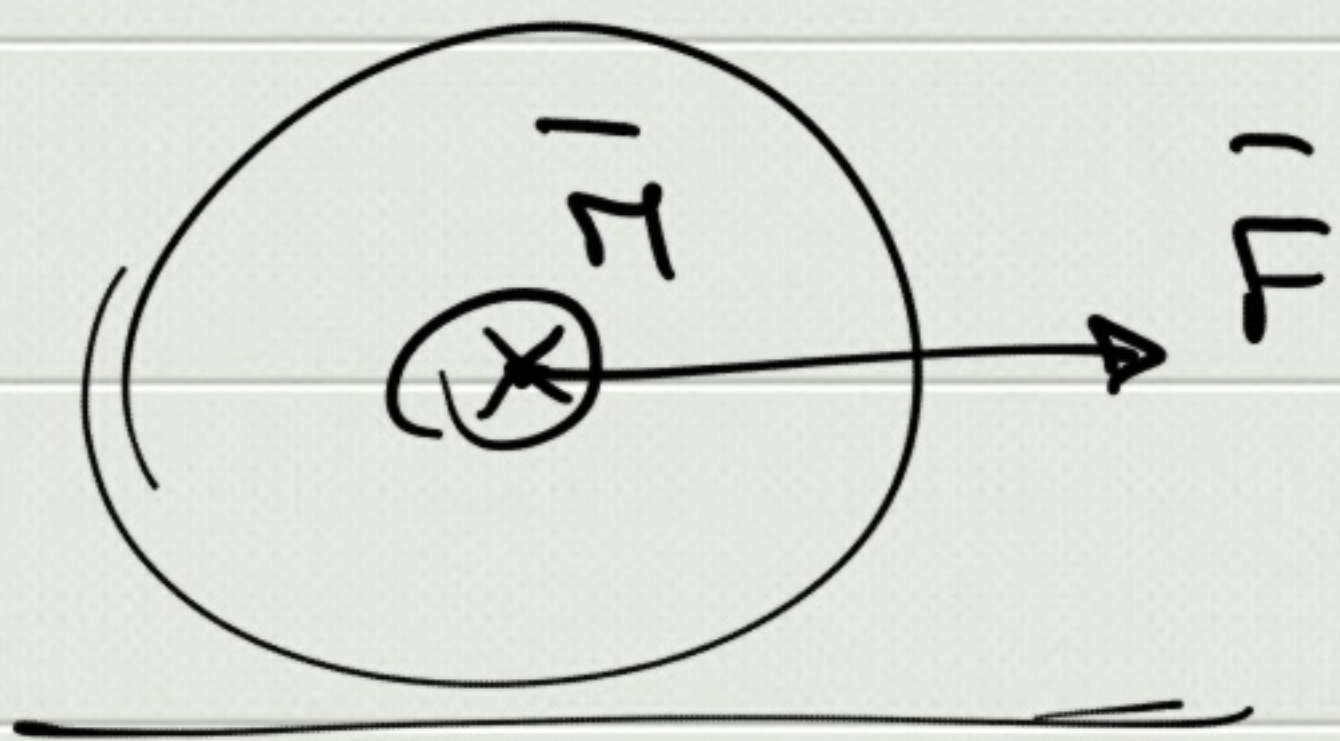
$$\Rightarrow M - mR a_{cm} = I_{cm} \frac{a_{cm}}{R}$$

$$\Rightarrow a_{cm} = \frac{M/mR}{1 + \frac{I_{cm}}{mR^2}}$$

$$\Rightarrow f_{es} = \frac{M/R}{1 + \frac{I_{cm}}{mR^2}}$$

$$\leq f_{es, \max} = \mu_s mg$$

$$\Rightarrow \mu \leq \mu_s mg R \left(1 + \frac{I_{cm}}{mR^2} \right)$$

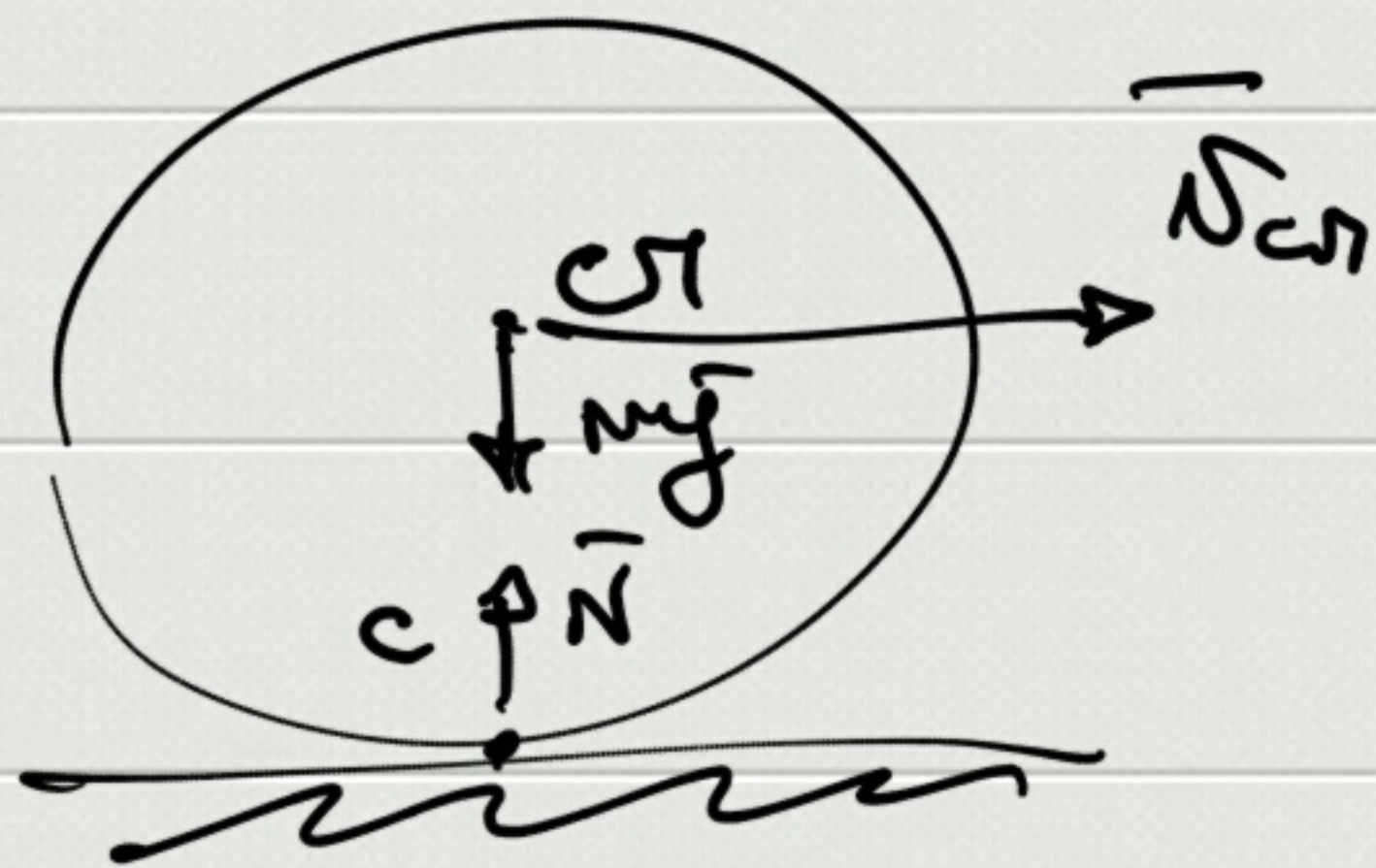


$$a_{cm} = \frac{1}{m} \frac{\tau/R + F}{1 + \frac{I_{cm}}{mR^2}}$$

$$f_{es} = \frac{\tau/R - \frac{I_{cm}}{mR^2} F}{1 + \frac{I_{cm}}{mR^2}}$$

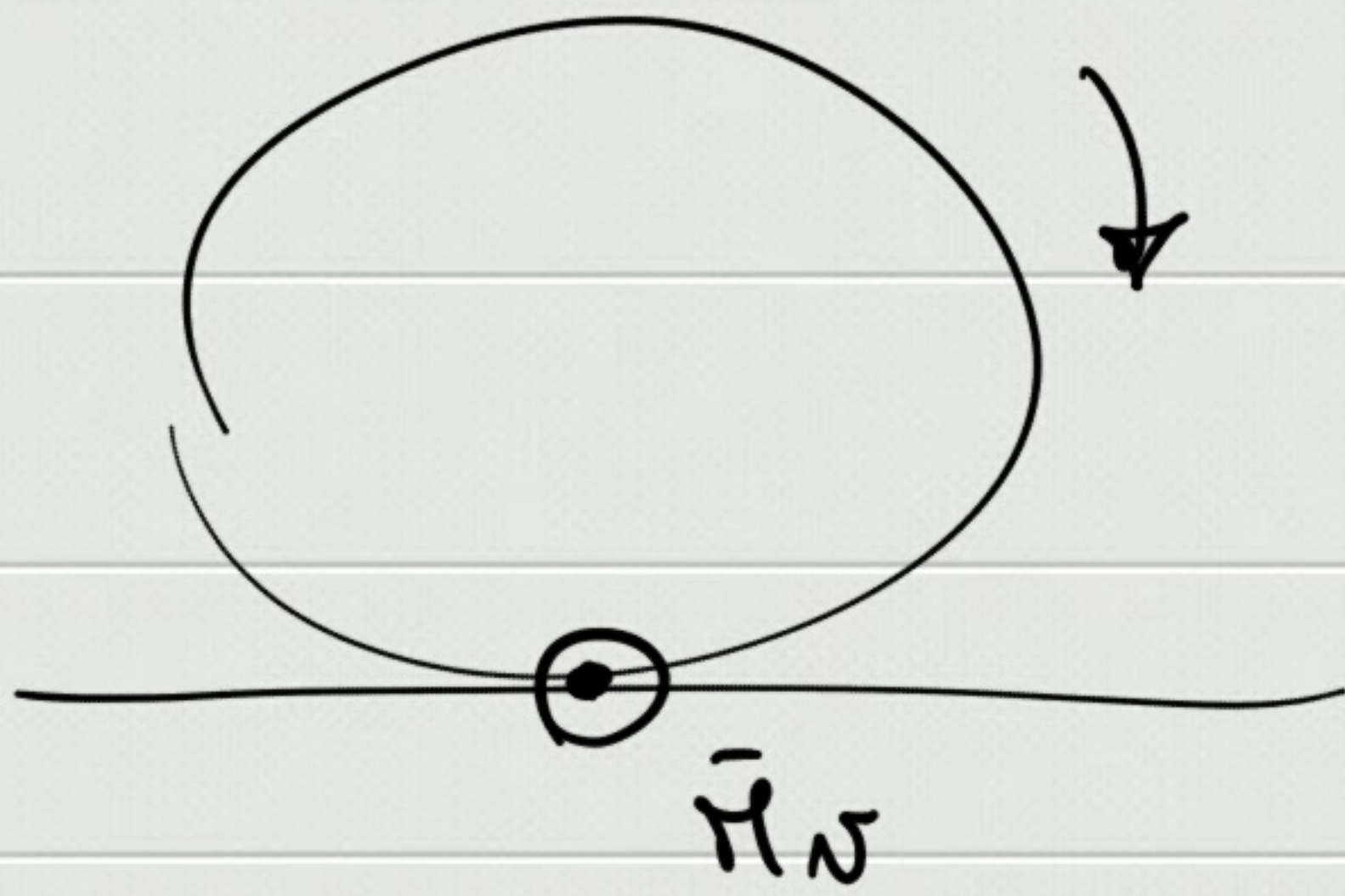
$$W_{tot} = \Delta E_k$$

$$W = \int \vec{F} \cdot d\vec{s}$$



$$\Rightarrow W_{f_{es}} = \int \vec{f}_{es} \cdot d\vec{s} = 0$$

Attivita' solvente



$$\bar{\pi}_s = -h N \bar{v}_w$$

✓
coeff. di attivita'
solvente

generalmente è trascurabile