

$$|\vec{F}_{el}| \propto |\vec{r} - \vec{r}_c|$$

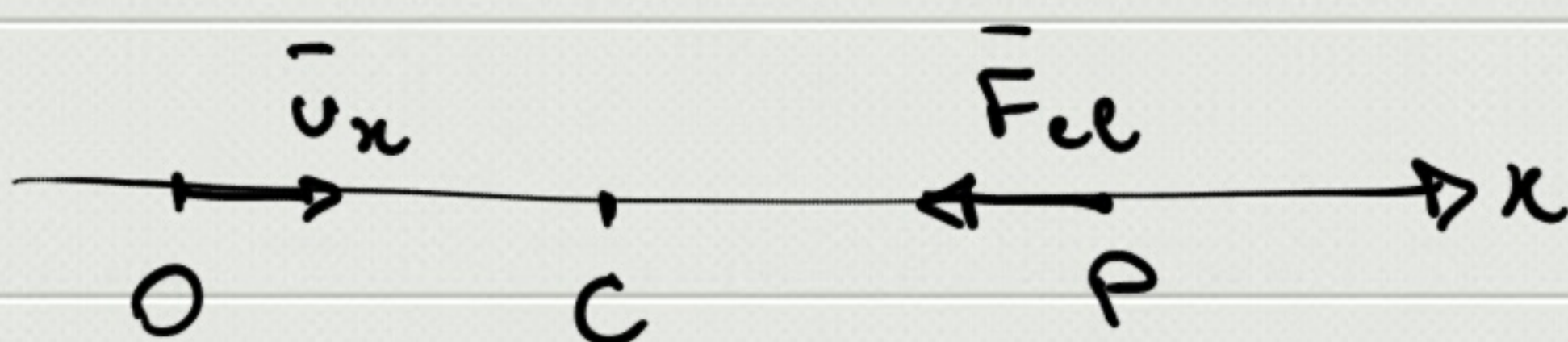
C: centro della forza

$$\vec{r} - \vec{r}_c = \vec{u}_c$$

$$\boxed{\vec{F}_{el} = -k (\vec{r} - \vec{r}_c)} = -k |\vec{r} - \vec{r}_c| \vec{u}_c$$

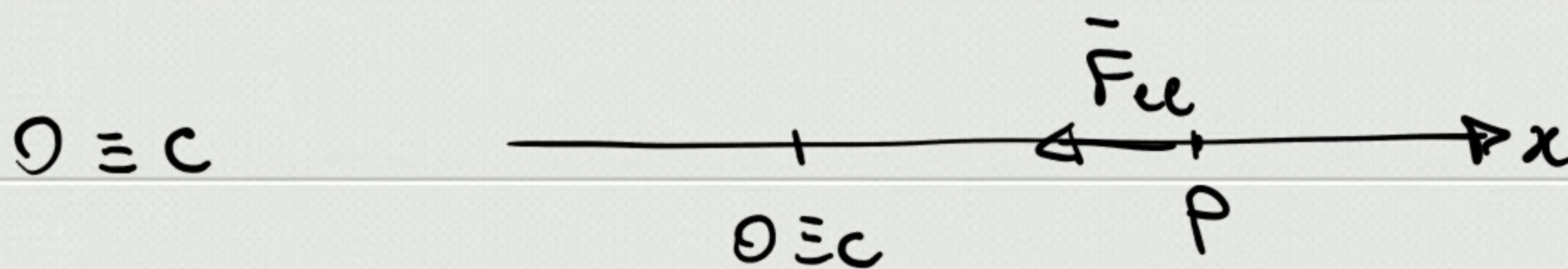
k: costante elastica

$$[k] = \left[ \frac{F}{r} \right] = N/m$$



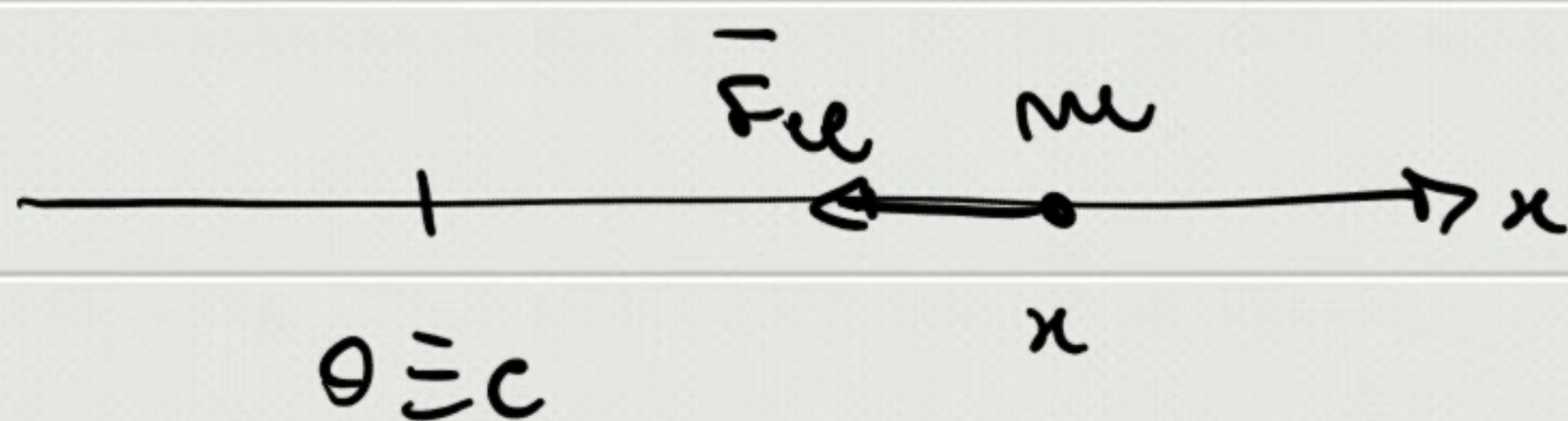
$$\vec{F}_{el} = -k (x - x_c) \vec{u}_x$$

$$\Rightarrow \boxed{F_{el} = -k (x - x_c) = -k \Delta x} *$$



$$\boxed{F_{el} = -k x}$$





$$F_{el} = ma \Rightarrow -kx = m \frac{d^2x}{dt^2}$$

$$\Rightarrow \frac{d^2x}{dt^2} + \frac{k}{m}x = 0 \quad \frac{k}{m} = \omega^2$$

$$\frac{d^2x}{dt^2} + \omega^2x = 0 \rightarrow \text{eq. } \underline{\text{moto armonico}}$$

$$x(t) = A \sin(\omega t + \phi) \quad *$$

$$v(t) = A\omega \cos(\omega t + \phi)$$

$$x(t=0) = x_0 \quad v(t=0) = 0$$

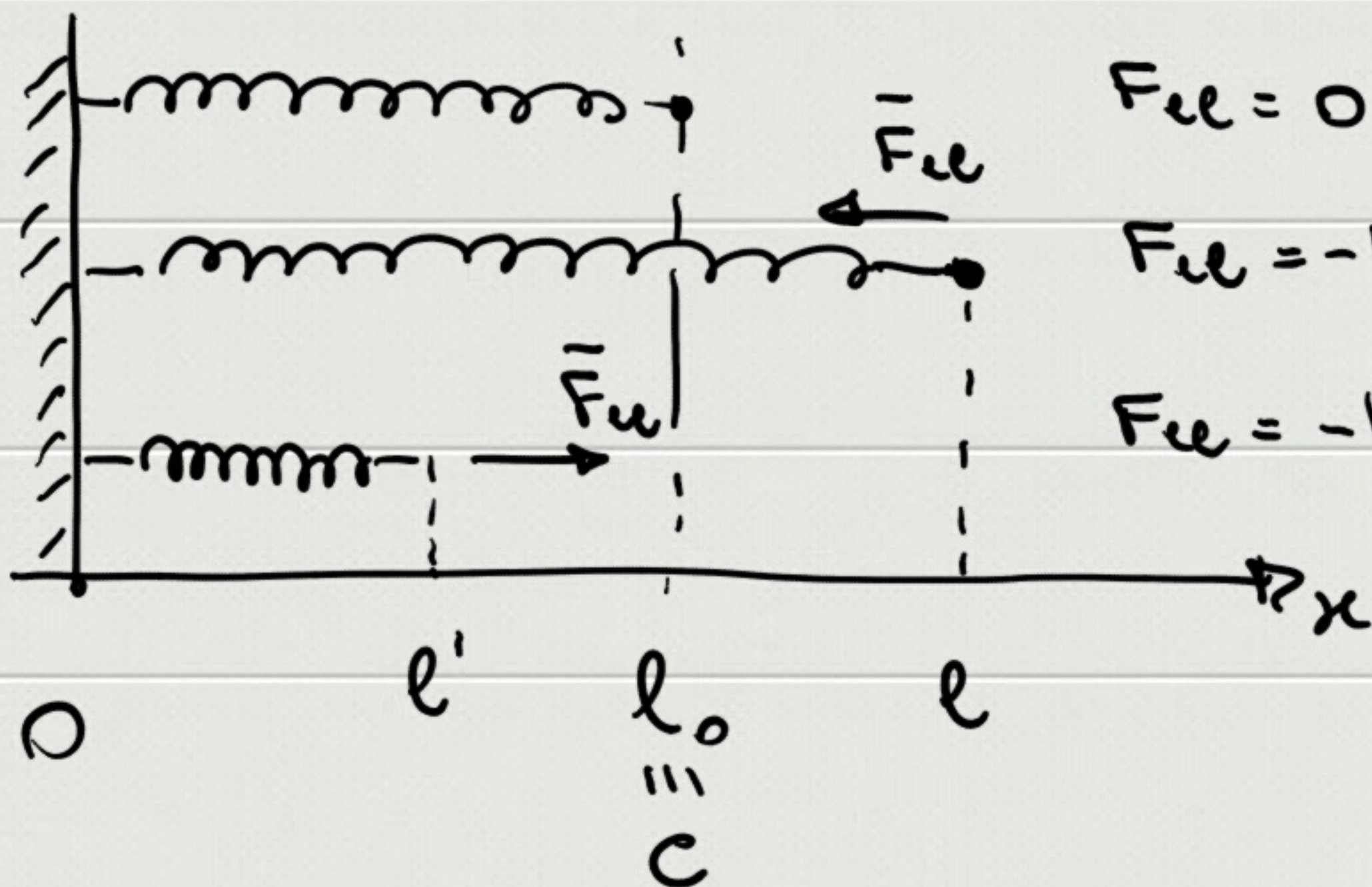
$$\Rightarrow v(0) = 0 = A\omega \cos \phi \Rightarrow \underline{\phi = \pi/2}$$

$$x(0) = x_0 = \underline{A \sin \phi = A}$$

$$\Rightarrow \boxed{x(t) = x_0 \cos \omega t}$$



$l_0$ : lunghezza a riposo

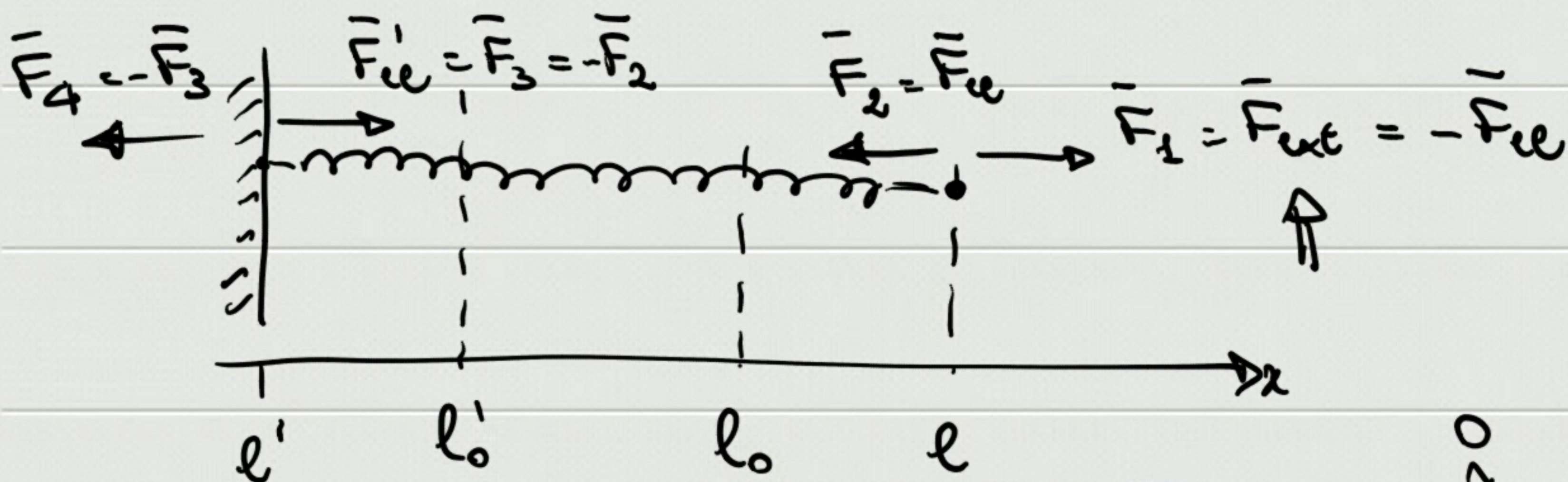


$$F_{el} = 0$$

$$F_{el} = -k(l - l_0) < 0 \quad \leftarrow \vec{F}_{el}$$

$$F_{el} = -k(l' - l_0) > 0 \quad \rightarrow \vec{F}_{el}$$

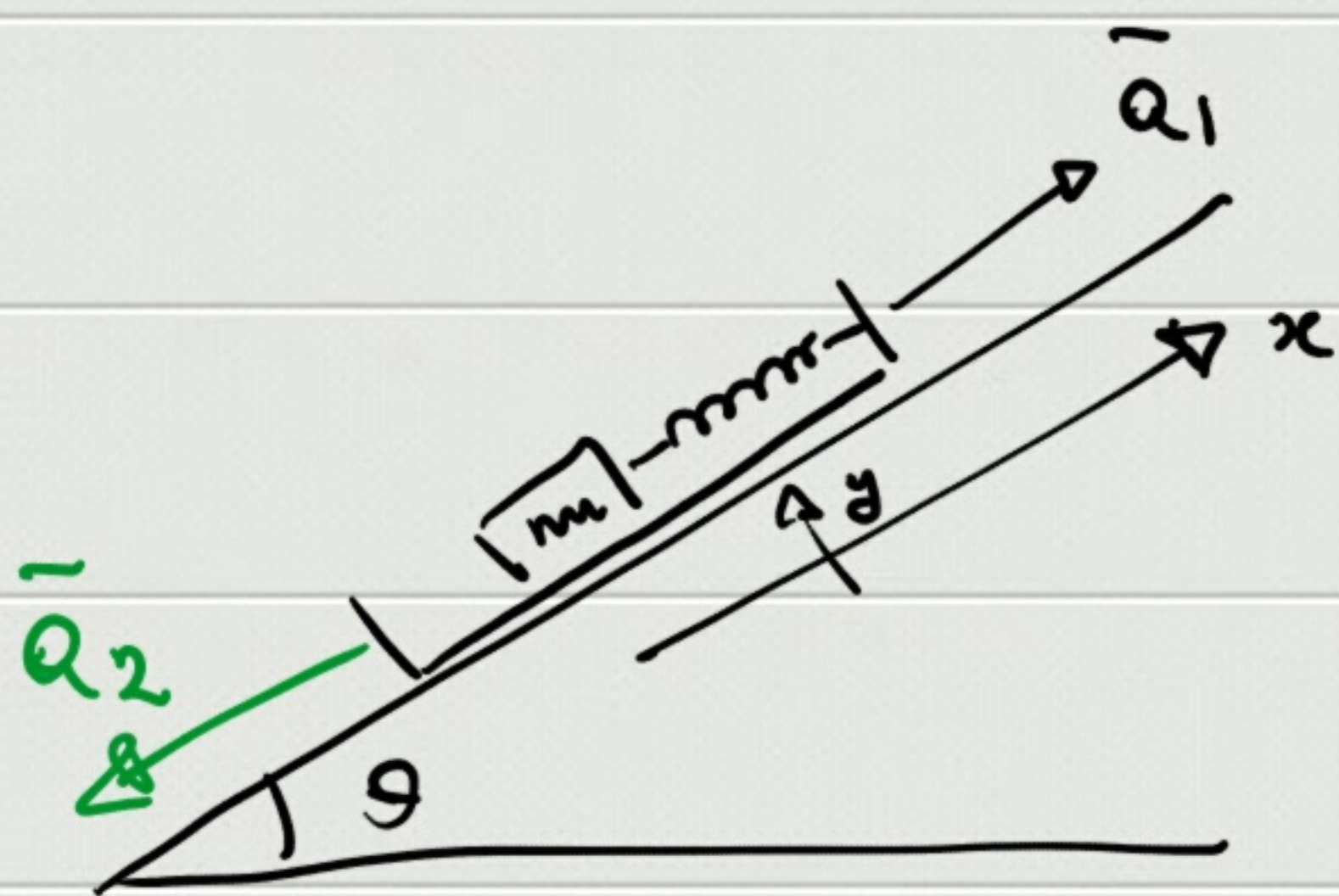
$$\boxed{F_{el} = -k \Delta x}$$



$$F_2 = F_{el} = -k(l - l_0) < 0 \quad \leftarrow \vec{F}_{el}$$

$$F_3 = F_{el} = -k(l' - l_0) > 0 \quad \rightarrow \vec{F}_{el}$$





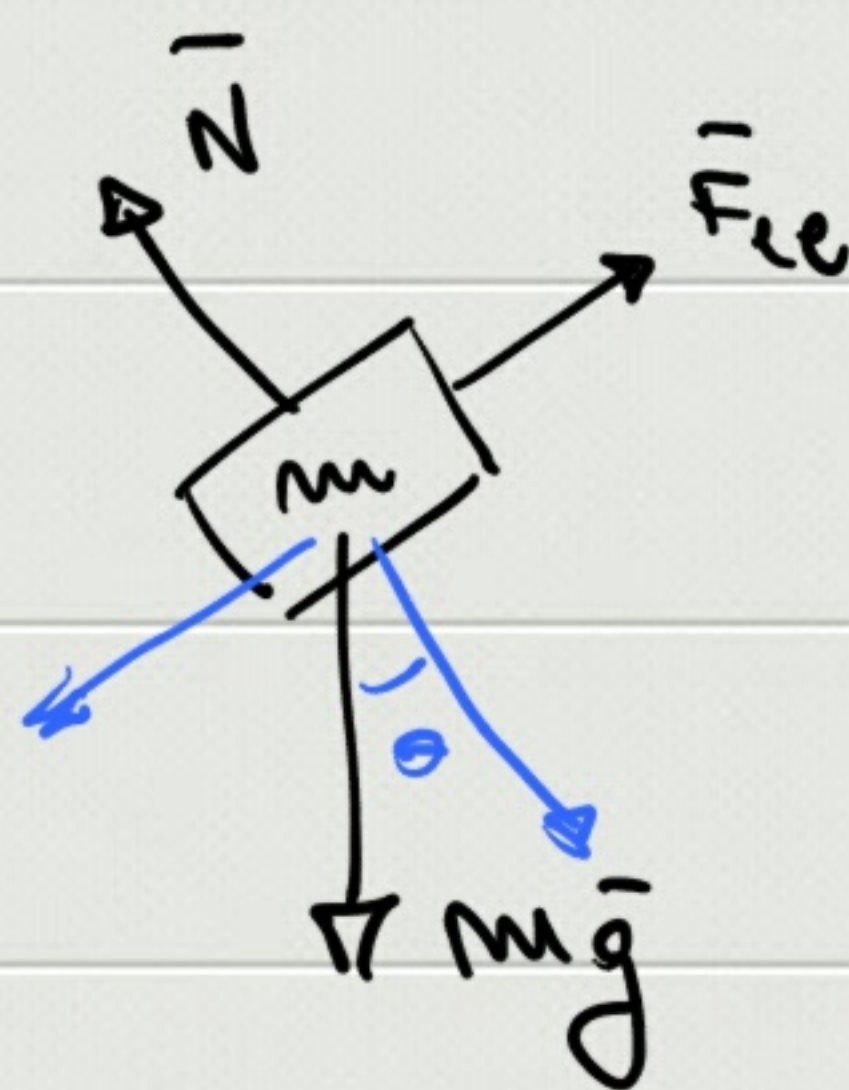
$$\theta = 29^\circ$$

$$a_1 = 1 \text{ m/s}^2$$

$$m = 0.5 \text{ kg}$$

$$k = 12 \text{ N/m}$$

$$\Delta x = ?$$



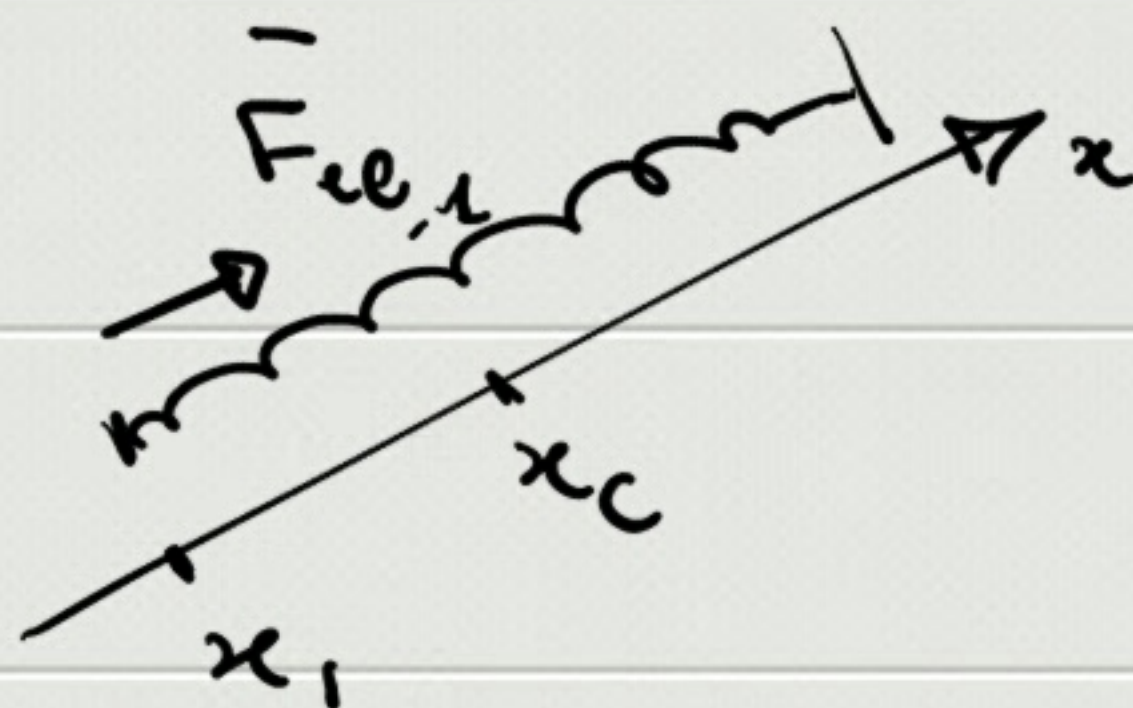
$$m\vec{g} + \vec{N} + \vec{F}_{el,1} = m\vec{a}_1$$

$$x: -mg \sin \theta - k \Delta x_1 = m a_1$$

$$\Rightarrow \Delta x_1 = -\frac{m}{k} (g \sin \theta + a_1) = -0.181 \text{ m}$$

$$| \Delta x_1 | = x_1 - x_c < 0$$

$$\vec{F}_{el,1} = -k \Delta x_1 > 0$$



$$Q_2 = 5 \text{ m/s}^2 \Rightarrow m\vec{g} + \vec{N} + \vec{F}_{el,2} = m\vec{a}_2$$

$$-mg \sin \theta - k \Delta x_2 = -m a_2$$

$$\Delta x_2 = \frac{m}{k} (a_2 - g \sin \theta) = 0.069 \text{ m} > 0$$

$$| \Delta x_2 | = x_2 - x_c$$

