

$$v_{0x} = v_0 \quad v_{0y} = 0 \quad (t_0 = 0)$$

$$x_0 = 0 \quad y_0 = h$$

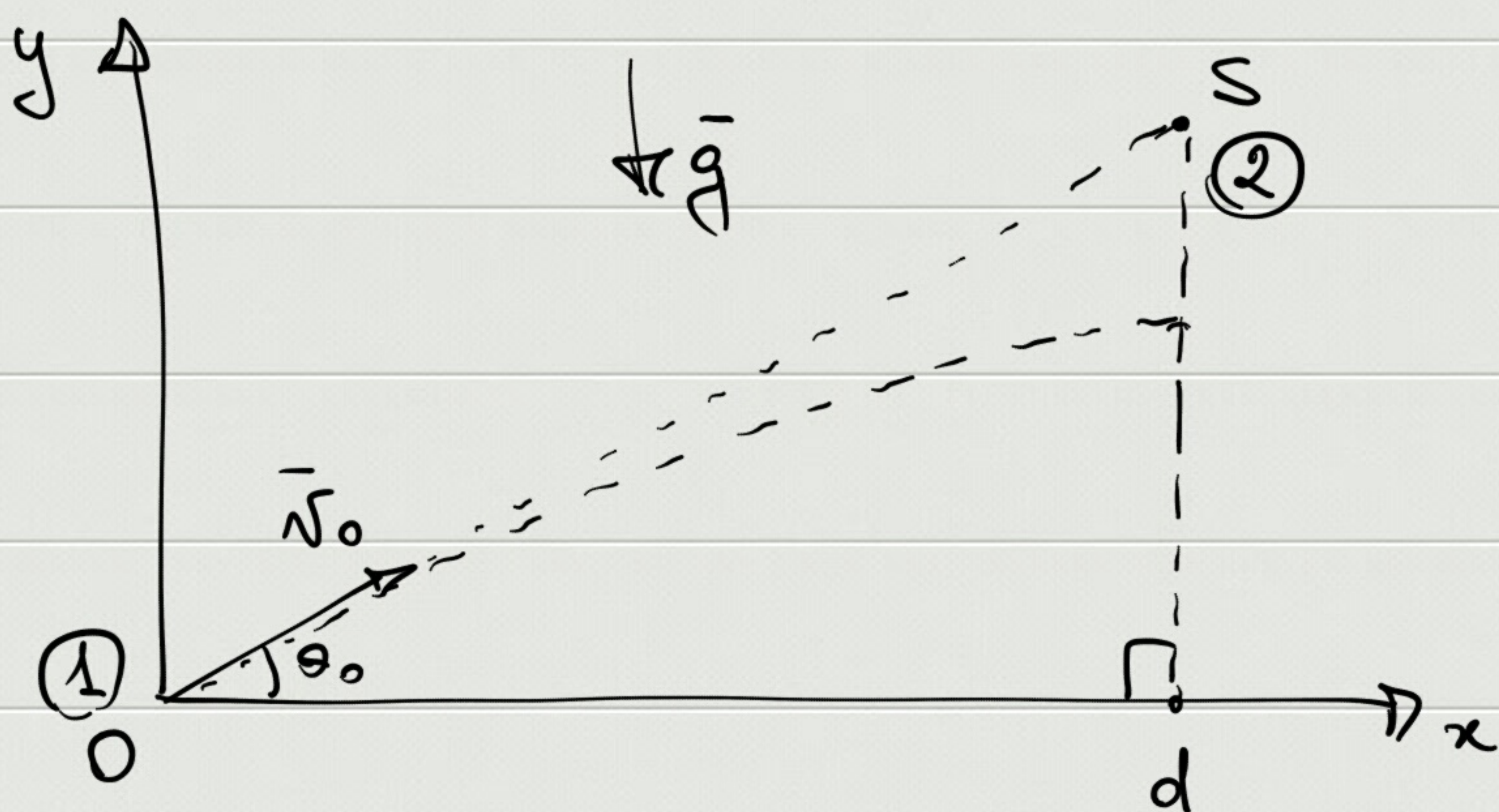
$$\begin{cases} v_x(t) = v_0 \\ v_y(t) = -gt \end{cases}$$

$$\begin{cases} x(t) = v_0 t \\ y(t) = h - \frac{1}{2} g t^2 \end{cases}$$

$$y(t_G) = 0 \Rightarrow \boxed{t_G = \sqrt{\frac{2h}{g}}} \Rightarrow \boxed{x_G = v_0 \sqrt{\frac{2h}{g}}}$$

$$\begin{aligned} v(t_G) &= \sqrt{v_x^2(t_G) + v_y^2(t_G)} = \\ &= \sqrt{v_0^2 + 2gh} \end{aligned}$$





$$1: \begin{cases} x_1(t) = v_0 \cos \theta_0 \cdot t \\ y_1(t) = v_0 \sin \theta_0 \cdot t - \frac{1}{2} g t^2 \end{cases}$$

$$2: \begin{cases} x_2(t) = d \\ y_2(t) = d \tan \theta_0 - \frac{1}{2} g t^2 \end{cases}$$

$$x_1(t^*) = d = v_0 \cos \theta_0 \cdot t^* \Rightarrow t^* = \frac{d}{v_0 \cos \theta_0}$$

$$y_1(t^*) = v_0 \sin \theta_0 \cdot \frac{d}{v_0 \cos \theta_0} - \frac{1}{2} g \frac{d^2}{v_0^2 \cos^2 \theta_0} =$$

$$= d \tan \theta_0 - \frac{g d^2}{2 v_0^2 \cos^2 \theta_0}$$

$$y_2(t^*) = d \tan \theta_0 - \frac{1}{2} g \frac{d^2}{v_0^2 \cos^2 \theta_0}$$

$$y_1(t^*) = y_2(t^*)$$