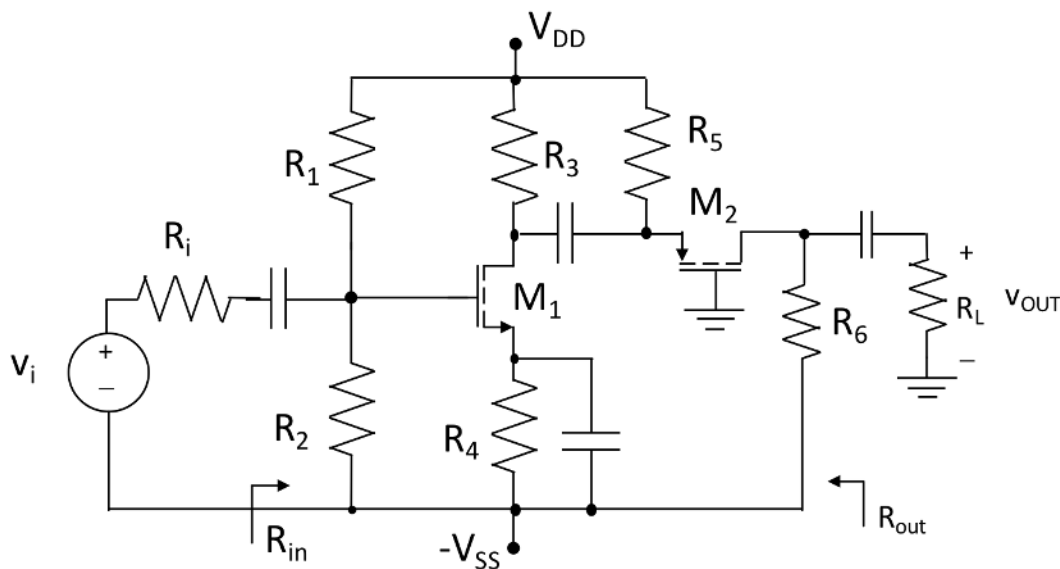


## PROBLEMA P1

Dato il circuito riportato nella figura sottostante, determinare:

- 1) il valore delle resistenze  $R_3, R_4, R_5, R_6$ , in modo che le correnti di drain di  $M_1$  e  $M_2$  valgano  $I_{D1} = 20 \text{ mA}$ ,  $V_{DS1} = 3 \text{ V}$ ;  $I_{D2} = 1 \text{ mA}$ ,  $V_{DS2} = -3 \text{ V}$
- 2) la potenza dissipata dai due MOSFETs  $M_1$  e  $M_2$  e la potenza dissipata dal circuito;
- 3) il guadagno di tensione ai piccoli segnali ac  $A_v = v_o/v_i$ ;
- 4) le resistenze di ingresso e uscita ai piccoli segnali ac  $R_{in}$  e  $R_{out}$ .



$$V_{DD} = V_{SS} = 15 \text{ V},$$

$$R_1 = 600 \text{ k}\Omega,$$

$$R_2 = 400 \text{ k}\Omega,$$

$$R_L = 48 \text{ k}\Omega,$$

$$R_i = 500 \Omega,$$

$$M_1:$$

$$k_n = 10 \text{ mA/V}^2,$$

$$V_{TN} = 3 \text{ V},$$

$$\lambda_p = 0 \text{ V}^{-1};$$

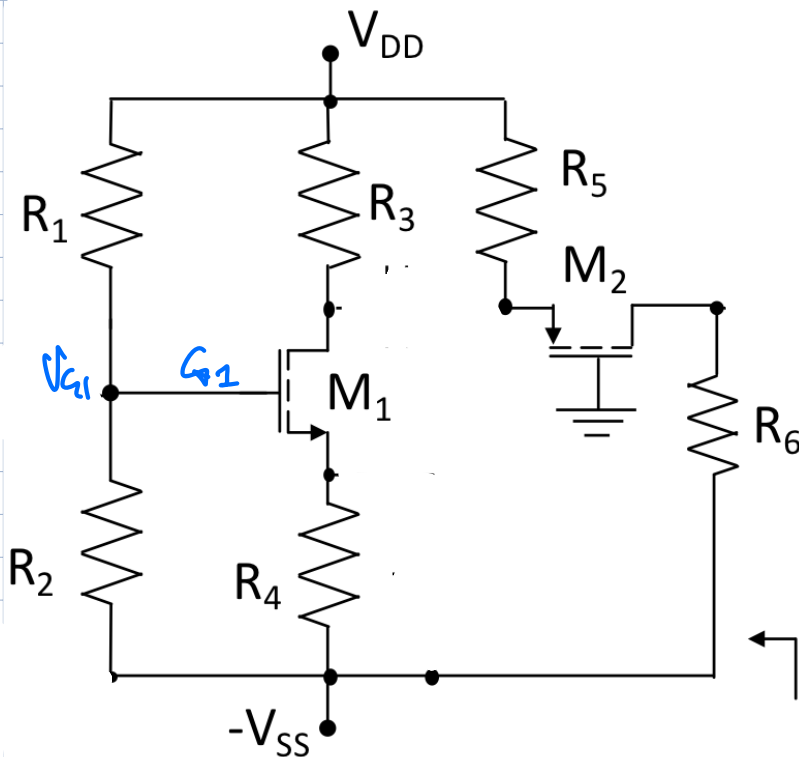
$$M_2:$$

$$k_p = 2 \text{ mA/V}^2,$$

$$V_{TP} = -3 \text{ V},$$

$$\lambda_p = 0 \text{ V}^{-1};$$

## ANALISI DC



$$V_{G1} = V_{DD} \cdot \frac{R_2}{R_1 + R_2} + (-V_{SS}) \cdot \frac{R_1}{R_1 + R_2}$$

$$= -3 \text{ V}$$

$$V_{GS1} = V_{TN} + \sqrt{\frac{2I_{D1}}{K_{M1}}} = 5 \text{ V}$$

$$\Rightarrow V_{S1} = V_{G1} - V_{GS1} = -8 \text{ V}$$

$$\Rightarrow R_4 = \frac{V_{S1} - (-V_{SS})}{I_{D1}}$$

$$= 350 \Omega$$

$$V_{D1} = V_{S1} + V_{DS1} = -5 \text{ V}$$

$$\Rightarrow R_3 = \frac{V_{DD} - V_{D1}}{I_{D1}} = 1 \text{ k}\Omega$$

$$V_{DS1} = 3 \text{ V} > V_{GS1} - V_{TN} = 2 \text{ V} \quad \text{OK } M_1 \text{ IN SATURATION}$$

$$V_{GS2} = V_{TP} - \sqrt{\frac{2I_{D2}}{K_{P2}}} = -4 \text{ V}$$

$$\Rightarrow V_{S2} = -V_{GS2} = 4 \text{ V}$$

$$R_5 = \frac{V_{DD} - V_{S2}}{I_{D2}} = 11 \text{ k}\Omega$$

$$V_{D2} = V_{S2} + V_{DS2} = 1 \text{ V}$$

$$R_6 = \frac{V_{D2} - (-V_{SS})}{I_{D2}} = 16 \text{ k}\Omega$$

$$V_{DS2} = -3 \text{ V} < V_{GS2} - V_{TP2} = -1 \text{ V}$$

OK  $M_2$  IN SAT.

### PARAMETRI AL PICCOLO SEGNALE

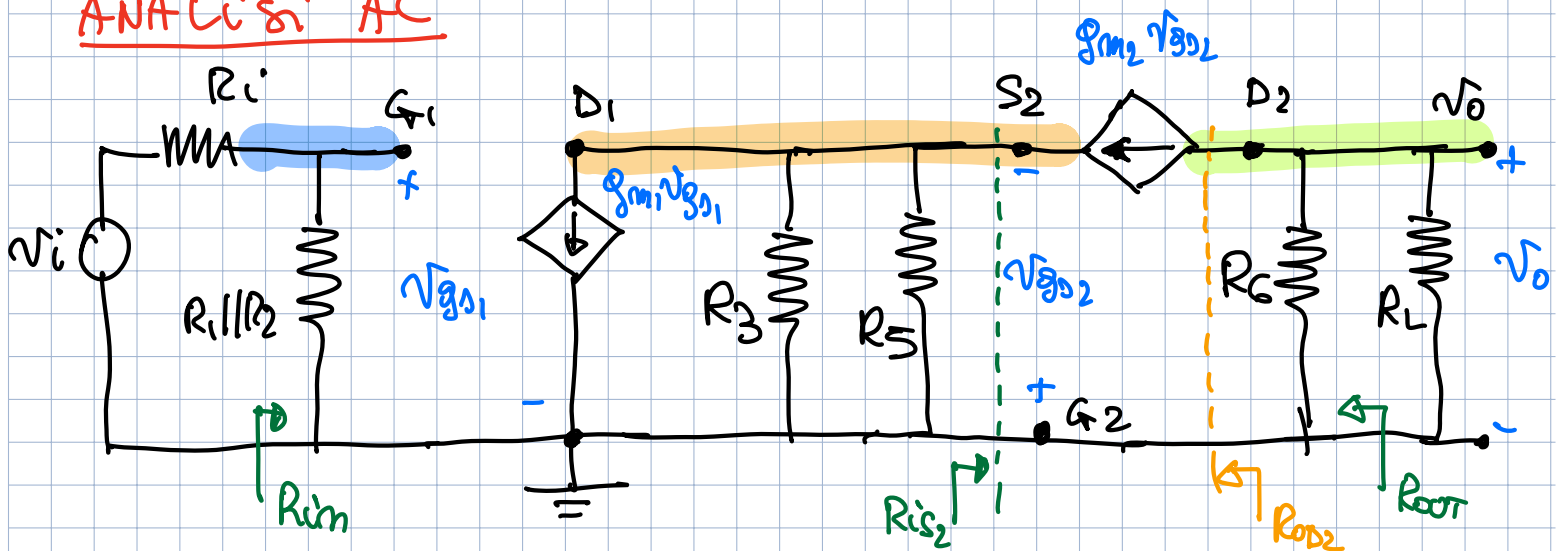
$$g_{m1} = \frac{2I_{D1}}{V_{GS1} - V_{TN}} = 20 \text{ mS}$$

$$r_{o1} = \infty$$

$$g_{m2} = \frac{2I_{D2}}{|V_{GS2} - V_{TP}|} = 2 \text{ mS}$$

$$r_{o2} = \infty$$

# ANALISI AC

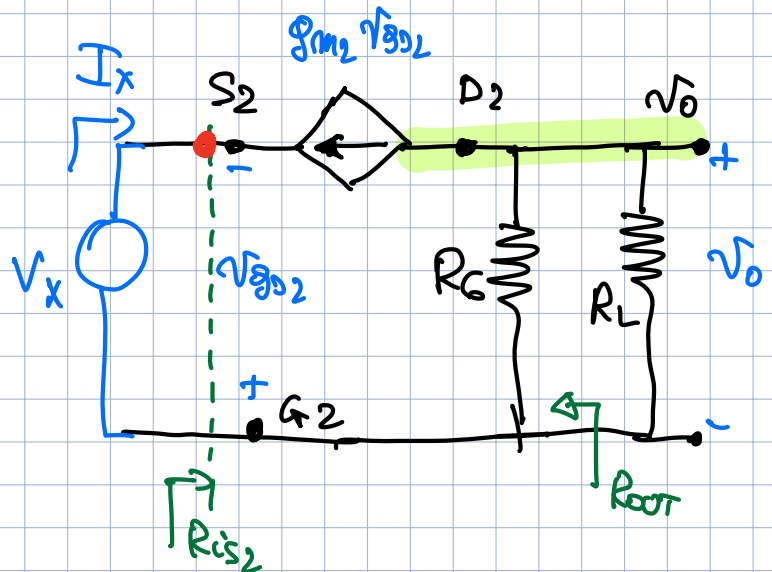


$R_{is2} = ?$

$$I_x = -g_{m2} v_{gs2}$$

$$V_x = -v_{gs2}$$

$$\Rightarrow R_{is2} = \frac{V_x}{I_x} = \frac{1}{g_{m2}}$$



$$R_{L1} = R_3 // R_5 // R_{is2} = R_3 // R_5 // \frac{1}{g_{m2}} = 323,5 \Omega$$

$$R_{L2} = R_6 // R_L = 12 \text{ k}\Omega$$

N.B.  $v_o \equiv v_{o2}$ ;  $v_{o1} \equiv v_{s2}$

$$A_v = \frac{v_o}{v_i} = \frac{v_o}{v_{s2}} \cdot \frac{v_{s2}}{v_{G1}} \cdot \frac{v_{G1}}{v_i} = \frac{v_{o2}}{v_{s2}} \cdot \frac{v_{o1}}{v_{G1}} \cdot \frac{v_{G1}}{v_i} =$$

$$\Rightarrow A_v = A_{vE}^{CG} \cdot A_{vE}^{CS} \cdot \frac{v_{G1}}{v_i}$$

$$A_{vE}^{CG} = g_{m2} R_{L2} = 24$$

$$\begin{cases} v_{o2} = -g_{m2} v_{gs2} R_6 // R_L \\ v_{gs2} = -v_{s2} \end{cases}$$

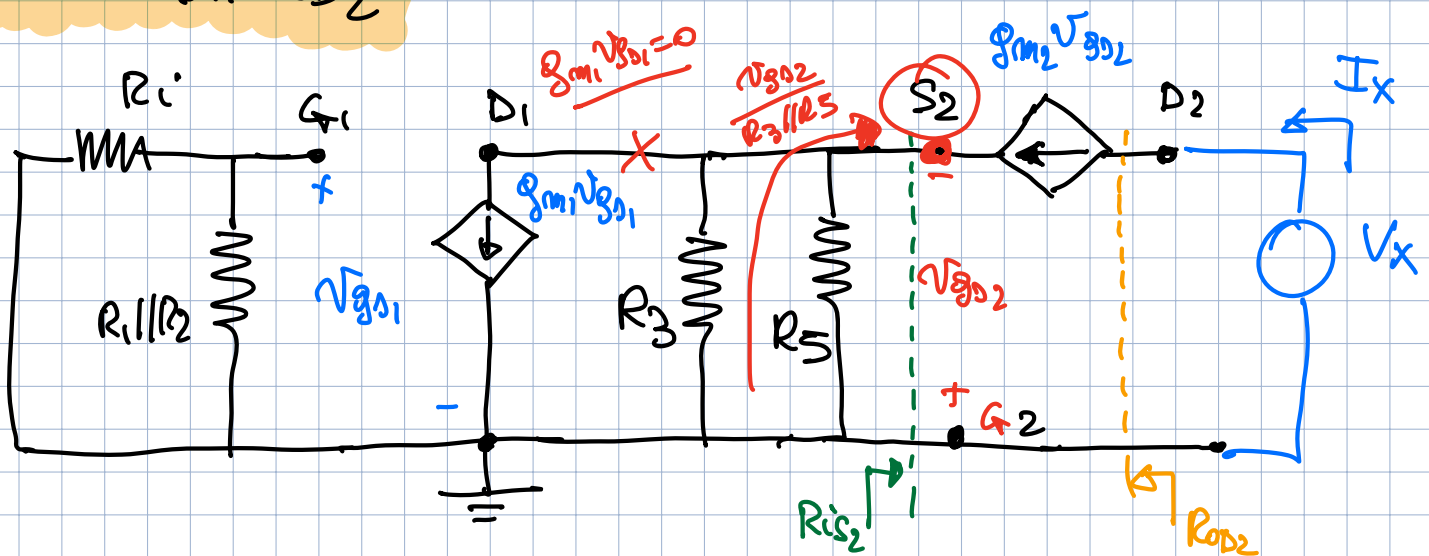
$$A_{vt}^{CS} = -g_{m1} R_{L1} = -6,47 \quad \left( \begin{array}{l} v_{D1} = -g_{m1} v_{gs1} R_{L1} \\ v_{G1} = v_{gs1} \end{array} \right)$$

$$\frac{v_{G1}}{v_i} = \frac{R_1 // R_2}{R_i + R_1 // R_2} = 0,888$$

$$\Rightarrow A_v = -154,97$$

$$\left[ \begin{array}{l} R_{in} = R_1 // R_2 = 240 \text{ K}\Omega \text{ (OVVIO)} \\ R_{out} = R_6 = 16 \text{ K}\Omega \text{ (VEDI SOTTO)} \end{array} \right]$$

$$R_{out} = R_6 // R_{od2}$$



$$v_{G1} = 0 \text{ V} \Rightarrow v_{gs1} = 0 \text{ V}$$

$$\Rightarrow \underline{g_{m1} v_{gs1}} = 0 \text{ A} \Rightarrow$$

AL NODO  $S_2$ :

$$\frac{v_{gs2}}{R_3 // R_5} + g_{m2} v_{gs2} = 0$$

$$\Rightarrow v_{gs2} = 0 \text{ V}$$

$$\Rightarrow g_{m2} v_{gs2} = 0$$

$$\Rightarrow i_x = 0$$

$$R_{od2} = \frac{v_x}{i_x} = \infty$$

$$R_{out} = R_6 // R_{od2} = R_6$$

## Esercizio 1

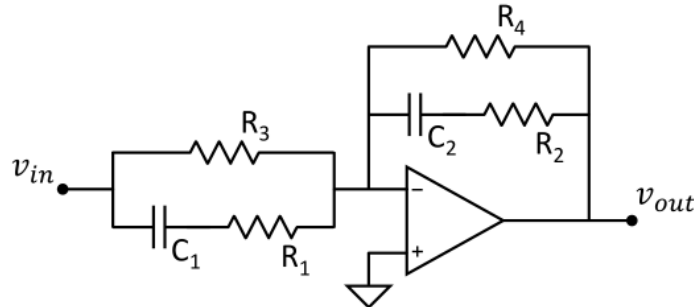
Sia dato il circuito in figura realizzato con un amplificatore operazionale ideale. Sappiamo che  $C_1 = 1 \text{ nF}$  e  $C_2 = 100 \text{ nF}$ ,  $R_1 = 1 \text{ k}\Omega$ ,  $R_2 = 10 \text{ k}\Omega$ ,  $R_3 = 99 \text{ k}\Omega$  e  $R_4 = 990 \text{ k}\Omega$

- 1) Calcolare il guadagno per  $\omega = 0$ .
- 2) Calcolare la funzione di trasferimento  $W(\omega)$  e tracciare il diagramma di Bode asintotico del modulo e della fase
- 3) Dato il segnale di ingresso:

$$v_{i(t)} = V_{s1} \cdot \sin(\omega_1 t + \pi) + V_{s2} \cdot \sin\left(\omega_2 t + \frac{\pi}{2}\right)$$

$$V_{s1} = 10 \text{ mV}, \omega_1 = 10^4 \text{ rad/s}, V_{s2} = 5 \text{ mV}, \omega_2 = 10^6 \text{ rad/s},$$

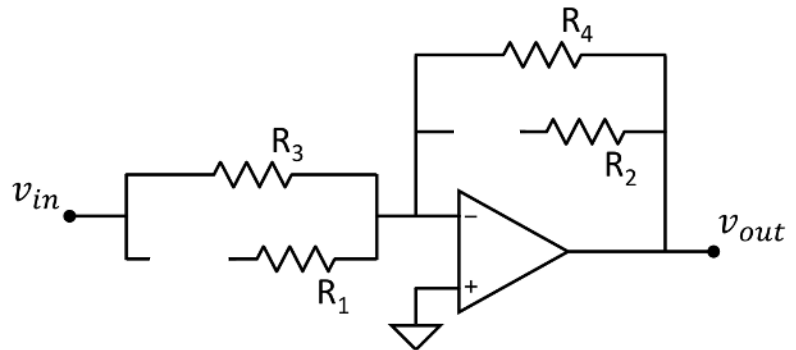
calcolare il segnale di uscita usando i diagrammi di Bode disegnati al punto 2).



1) GUADAGNO PER  $\omega = 0$

$$V_{out} = V_{in} \left( -\frac{R_4}{R_3} \right)$$

$$\Rightarrow A_v = \frac{V_{out}}{V_{in}} = -\frac{R_4}{R_3} = -10$$



2)  $W(s)$

$$Z_1 = R_1 + \frac{1}{sC_1} = \frac{1 + sC_1 R_1}{sC_1}$$

$$Z_2 = \frac{1 + sC_2 R_2}{sC_2}$$

$$Z_{in} = R_3 \parallel Z_1 = \frac{R_3 \cdot \frac{1 + sC_1 R_1}{sC_1}}{R_3 + \frac{1 + sC_1 R_1}{sC_1}} = \frac{R_3 (1 + sC_1 R_1)}{1 + sC_1 (R_1 + R_3)}$$

$$Z_F = R_4 \parallel Z_2 = \frac{R_4 (1 + sC_2 R_2)}{1 + sC_2 (R_2 + R_4)}$$

$$\begin{aligned} W(s) &= -\frac{Z_F}{Z_{in}} = -\frac{R_4 (1 + sC_2 R_2)}{1 + sC_2 (R_2 + R_4)} \cdot \frac{1 + sC_1 (R_1 + R_3)}{R_3 (1 + sC_1 R_1)} \\ &= -\frac{R_4}{R_3} \cdot \frac{(1 + sC_2 R_2) [1 + sC_1 (R_1 + R_3)]}{(1 + sC_1 R_1) [1 + sC_2 (R_2 + R_4)]} \end{aligned}$$

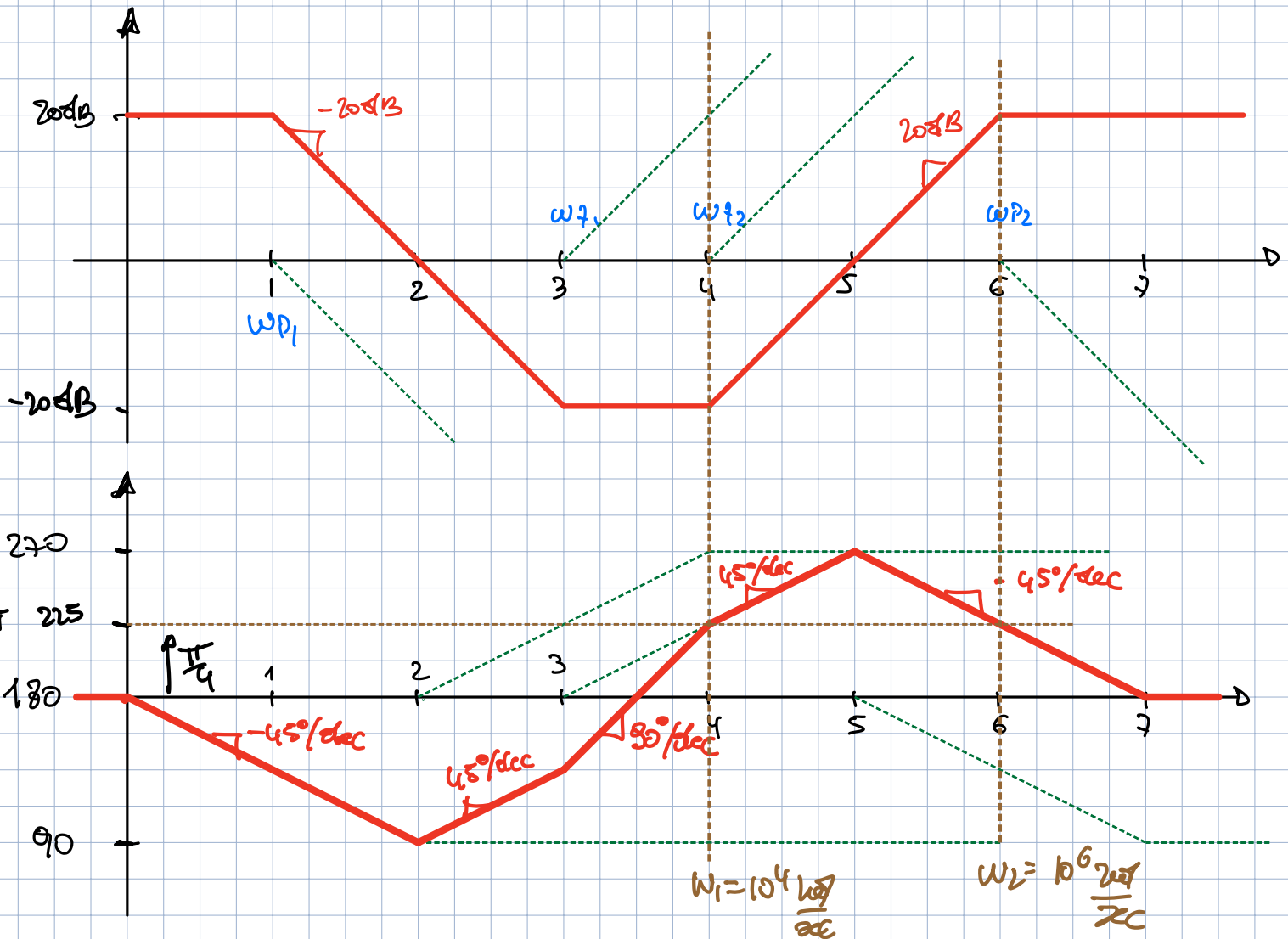
$$\omega_{p1} = \frac{1}{C_2 R_2} = 10^3 \text{ rad/sec}$$

$$\omega_{p2} = \frac{1}{C_1 (R_1 + R_3)} = 10^4 \text{ rad/sec}$$

$$\omega_{p1} = \frac{1}{C_2 (R_2 + R_4)} = 10^1 \text{ rad/sec}$$

$$\omega_{p2} = \frac{1}{R_1 C_1} = 10^6 \text{ rad/sec}$$

$$A_0 = -\frac{R_4}{R_3} = 10 = 20 \text{ dB}$$



$$\omega_1 = 10^4 \text{ rad/sec} \quad |W(j\omega_1)| = -20 \text{ dB} \cdot \sqrt{2} = 0,1 \cdot 1,414 = 0,1414$$

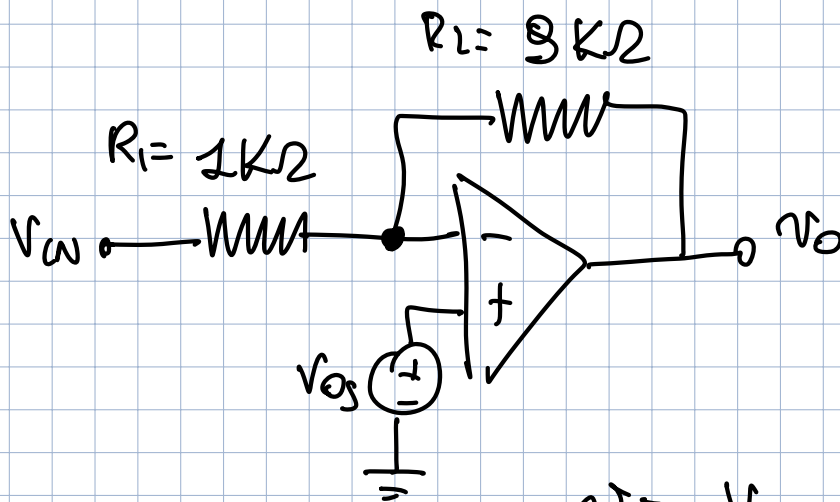
$$\angle W(j\omega_1) = 225^\circ$$

$$\omega_2 = 10^6 \text{ rad/sec} \quad |W(j\omega_2)| = +20 \text{ dB} \cdot \frac{1}{\sqrt{2}} = \frac{10}{1,414} = 7,05$$

$$\angle W(j\omega_2) = 225^\circ$$

$$v_o(t) = 1,414 \text{ mV} \cdot \sin(\omega_1 t + \frac{\pi}{4}) + 35,35 \text{ mV} (\sin \omega_2 t - \frac{\pi}{4})$$

## PROBLEMA Q1



$$V_{OS} = 10\text{mV}$$

$$V_{IN} = 2\text{V}$$

$$V_{OUT} = ?$$

$$V_O = -V_{IN} \cdot \frac{R_2}{R_1} + V_{OS} \left( 1 + \frac{R_2}{R_1} \right)$$

$$= -18\text{V} + 0,1\text{V} = -17,9\text{V}$$

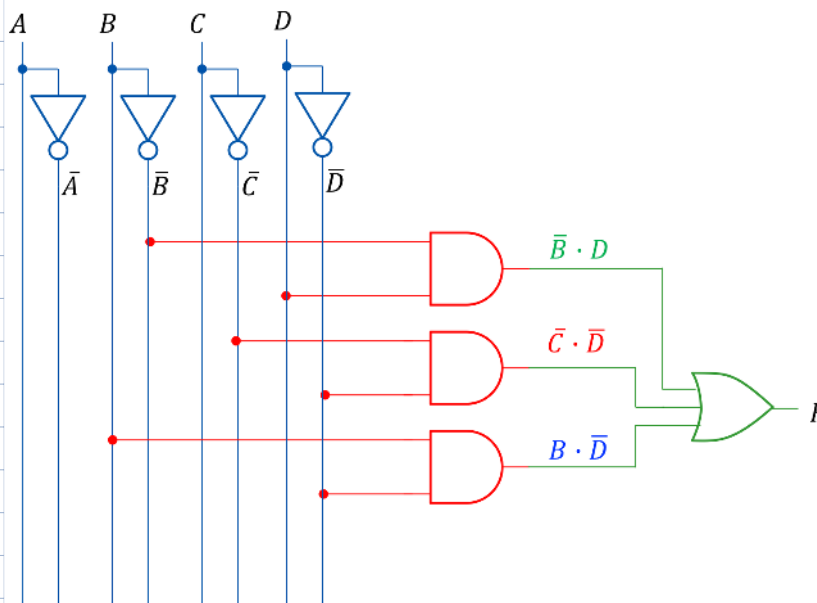
## PROBLEMA Q2

Data la seguente tabella della verità

- 1) Ricavare la mappa di Karnaugh corrispondente;
- 2) Trovare una F minimizzata
- 3) Disegnare la rete logica minimizzata tramite porte logiche fondamentali.

| CD \ AB | 00 | 01 | 11 | 10 |
|---------|----|----|----|----|
|         | 00 | 01 | 11 | 10 |
| 00      | 1  | 1  | 1  |    |
| 01      | 1  |    |    | 1  |
| 11      | 1  |    | X  | X  |
| 10      | X  | 1  | 1  |    |

$$\bar{B} \cdot D + \bar{C} \cdot \bar{D} + B \cdot \bar{D}$$



| A | B | C | D | F |
|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 1 |
| 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 1 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 |
| 0 | 1 | 0 | 0 | 1 |
| 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 | X |
| 1 | 0 | 0 | 1 | 1 |
| 1 | 0 | 1 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 |
| 1 | 1 | 0 | 0 | 1 |
| 1 | 1 | 0 | 1 | 0 |
| 1 | 1 | 1 | 0 | X |
| 1 | 1 | 1 | 1 | X |