

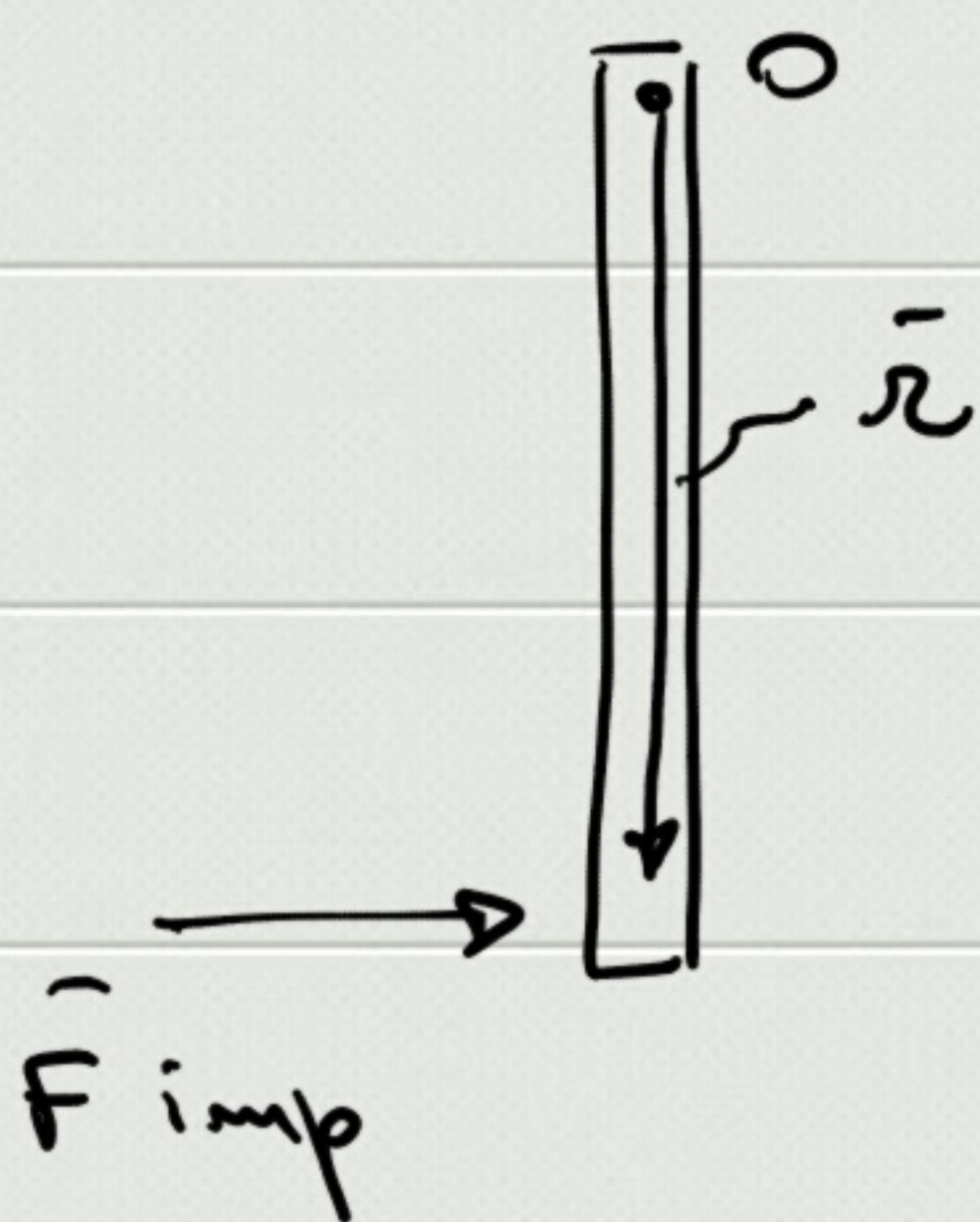
$$\vec{F} = \frac{d\vec{p}}{dt}$$

$$\vec{J} = \int \vec{F} dt = \int d\vec{p} = \Delta\vec{p}$$

$$\vec{M}_O^E = \frac{d\vec{L}_O}{dt}$$

$$\int_{t_0}^t \vec{M}_O^E dt = \int_{\vec{L}_O(t_0)}^{\vec{L}_O(t)} d\vec{L}_O = \vec{L}_O(t) - \vec{L}_O(t_0) = \Delta\vec{L}$$

Teorema del impulso del momento  
(impulso angular)



$$\vec{M}_O = \vec{r} \times \vec{F}$$

$$\vec{r} \approx \text{const}$$

$$\underline{\underline{\int \vec{M}_O dt = \int \vec{r} \times \vec{F} dt = \vec{r} \times \int \vec{F} dt = \underline{\underline{\vec{r} \times \vec{J}}}}}$$

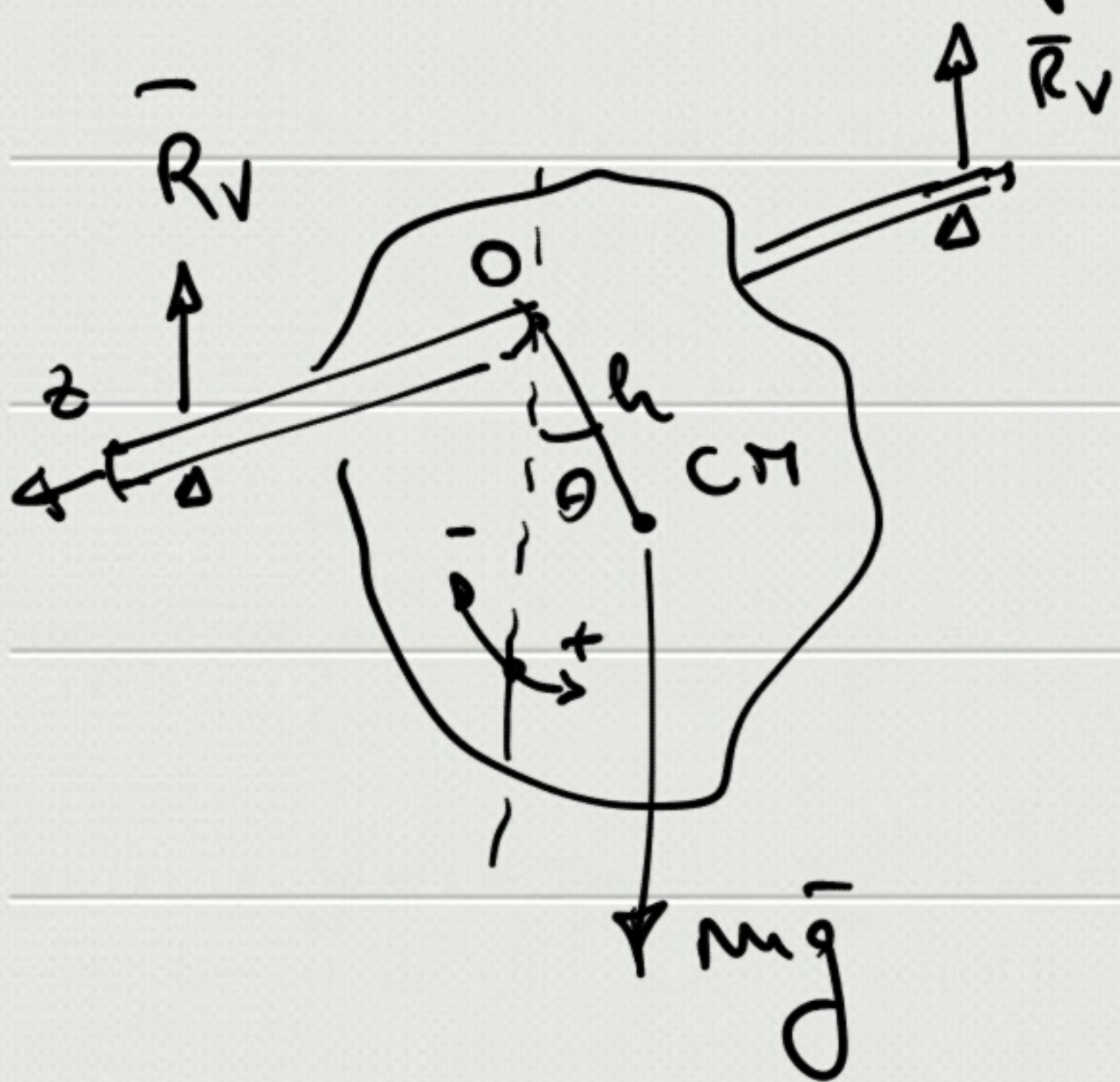


Impulso del momento = momento dell'impulso

Teorema del momento dell'impulso



# Pendolo composto



$$\vec{M}_O^E = I_z \vec{\alpha}$$

$$\begin{aligned} \vec{M}_{O, \text{peso}} &= \vec{h} \times m\vec{g} \\ &= h mg \sin \theta (-\vec{u}_z) \end{aligned}$$

$$-mgh \sin \theta = I_z \alpha$$

piccole oscillazioni

$$\Rightarrow -mgh \theta = I_z \frac{d^2 \theta}{dt^2}$$

$$\Rightarrow \frac{d^2 \theta}{dt^2} + \frac{mgh}{I_z} \theta = 0$$

$$\Omega = \sqrt{\frac{mgh}{I_z}}$$

$$\Rightarrow \boxed{\theta(t) = \theta_0 \sin(\Omega t + \phi)}$$

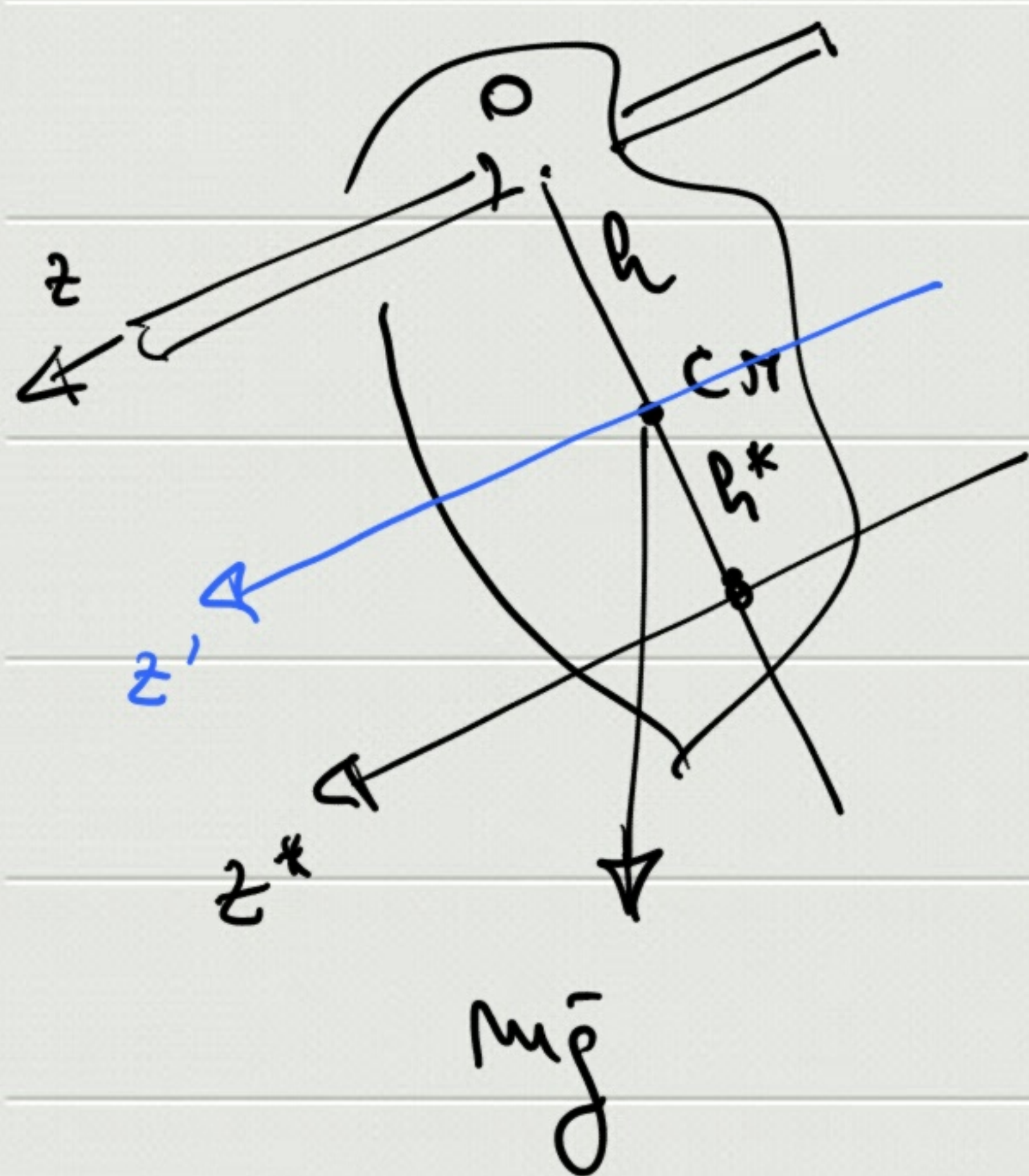
$$T = \frac{2\pi}{\Omega} = 2\pi \sqrt{\frac{I_z}{mgh}}$$

$$T = 2\pi \sqrt{\frac{l}{g}}$$



$$\boxed{l = \frac{I_z}{mh}}$$

lunghezza ridotta



$$\begin{aligned} l &= \frac{I_z}{mh} \stackrel{H-S}{=} \frac{I_{z'} + mh^2}{mh} = \\ &= \frac{I_{z'}}{mh} + h = \underline{\underline{h^* + h}} \end{aligned}$$

$$\Rightarrow \boxed{I_{z'} = mh h^*}$$

$$\Rightarrow l^* = \frac{I_{z^*}}{mh^*}$$

$$\underline{\underline{l^* = \frac{I_{z^*}}{mh^*} = \frac{I_{z'} + mh^{*2}}{mh^*} = \frac{I_{z'}}{mh^*} + h^* = \underline{\underline{h + h^*}}}}$$

$z$  e  $z^*$   $\rightarrow$  assi reciproci