

# DINAMICA DEI FLUIDI PER L'INGEGNERIA BIOMEDICA ①

## TEMI D'ESAME

### IDROSTATICA

ESERCIZIO 1: /

ESERCIZIO 2: /

ESERCIZIO 3: /

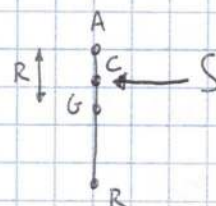
ESERCIZIO 4: /

ESERCIZIO 5: /

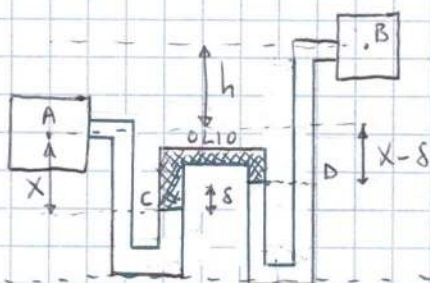
ESERCIZIO 6

$$M_{\text{EXT}} = \int (y_c - y_v) = \frac{\int y I_x}{S} = 1,06 \gamma_{\text{acciaio}} \times \frac{R^4}{4}$$

$$R = \sqrt[4]{\frac{4 M_{\text{EXT}}}{1,06 \gamma_{\text{acciaio}} \times}} = \sqrt[4]{\frac{4 \cdot 4 \cdot 10^{-4} \text{ Nm}}{1,06 \cdot 9810 \text{ N/m}^3 \cdot \times}} = 0,01488 \text{ m} = 1,488 \text{ cm}$$



ESERCIZIO 7



$$P_A = P_C - \gamma_{H_2O} X$$

$$P_C = P_D + \gamma_0 s$$

$$P_B = P_D - \gamma_{H_2O} (h + X - s)$$

$$P_A - P_B = P_C - \gamma_{H_2O} X - (P_D - \gamma_{H_2O} (h + X - s)) = \cancel{P_D} + \gamma_0 s - \cancel{\gamma_{H_2O} X} - \cancel{P_D} + \gamma_{H_2O} h + \cancel{\gamma_{H_2O} X} - \gamma_{H_2O} s = 1200 P_a$$

$$h = \frac{1200 P_a - \gamma_0 s + \gamma_{H_2O} s}{\gamma_{H_2O}} = \frac{1200 P_a - 0,8 \gamma_{H_2O} s + \gamma_{H_2O} s}{\gamma_{H_2O}} = \text{scribbled out}$$

$$= \frac{1200 P_a - 0,8 \cdot 9810 \text{ N/m}^3 \cdot 0,1 \text{ m} + 9810 \text{ N/m}^3 \cdot 0,1 \text{ m}}{9810 \text{ N/m}^3} = 0,142 \text{ m}$$

ESERCIZIO 8

$$S = S_{\overline{AB}} - S_{\overline{BC}} = S_{\overline{AB}} + G - (F_{\text{ARCHIMEDE}} - S_{\overline{AB}}) = 2 S_{\overline{AB}} - \cancel{G} - \cancel{F_{\text{ARCHIMEDE}}} = 2 P_h A = 2 (p_t + \gamma h) \underline{b} \cdot b = (p_t + \gamma h) b^2$$

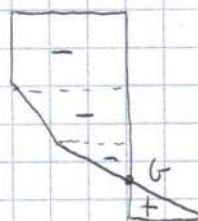


$$\gamma = \frac{\frac{S}{b^2} - P_t}{h} = \frac{\frac{35 \text{ N}}{(0,1)^2} - 1000 \text{ Pa}}{0,3 \text{ m}} = 8333,333 \text{ N/m}^3$$

ESERCIZIO 9

$$P_G = 0 = P_{\text{atm}} + \gamma_1 h_1 + \gamma_2 0,3 \text{ m}$$

$$h_1 = \frac{-P_{\text{atm}} - \gamma_2 0,3 \text{ m}}{\gamma_1} = \frac{-(-5 \text{ kPa}) - 10 \text{ kN/m}^3 \cdot 0,3 \text{ m}}{8 \text{ kN/m}^3} = 0,25 \text{ m}$$



## DINAMICA

ESERCIZIO 1:

ESERCIZIO 2:

ESERCIZIO 3:

ESERCIZIO 4:

ESERCIZIO 5:

ESERCIZIO 6:

ESERCIZIO 7

$$P_U = \gamma Q H_P \Rightarrow H_P = \frac{P_U}{\gamma Q} = \frac{0,07 \text{ W}}{10,4 \text{ kN/m}^3 \cdot \frac{1,2 \cdot 10^{-3} \text{ m}^3}{60 \text{ s}}} = 0,337 \text{ m}$$

$$\rho = \frac{\gamma}{g} = \frac{10,4 \text{ kN/m}^3}{g} = 1060,14 \text{ kg/m}^3$$

$$\nu = \frac{\mu}{\rho} = \frac{0,004 \text{ kg/(m s)}}{1060,14 \text{ kg/m}^3} = 3,77 \cdot 10^{-6} \text{ m}^2/\text{s}$$

$$V_{AB} = \frac{Q}{A_{AB}} = \frac{1,2 \cdot 10^{-3} \text{ m}^3 / 60 \text{ s}}{\pi \frac{(0,5 \cdot 10^{-2})^2}{4}} = 1,02 \text{ m/s}$$

$$V_{BA} = \frac{Q}{A_{BA}} = \frac{1,2 \cdot 10^{-3} \text{ m}^3 / 60 \text{ s}}{\pi \frac{(0,75 \cdot 10^{-2})^2}{4}} = 0,45 \text{ m/s}$$



$$Re_{AB} = \frac{V_{AB} d_{AB}}{\nu} = \frac{1,02 \text{ m/s} \cdot 0,005 \text{ m}}{3,77 \cdot 10^{-6} \text{ m}^2/\text{s}} = 1352 \quad \text{MOTO LAMINARE}$$

$$Re_{BA} = \frac{V_{BA} d_{BA}}{\nu} = \frac{0,45 \text{ m/s} \cdot 0,0075 \text{ m}}{3,77 \cdot 10^{-6} \text{ m}^2/\text{s}} = 895 \quad \text{MOTO LAMINARE}$$

$$H_{PA} - E_{AB}^{\text{CONTINUO}} - E_{AB}^{\text{LOCALIZZATO}} + H_{PB} - E_{BA}^{\text{CONTINUO}} = 0$$



$$H_{PA} - \frac{64}{Re_{AB} d_{AB}} \frac{V_{AB}^2 L_{AB}}{2g} + H_{PB} - \frac{64}{Re_{BA} d_{BA}} \frac{V_{BA}^2 L_{BA}}{2g} = 0$$

$$\sum \left( H_{PA} - \frac{64}{Re_{AB} d_{AB}} \frac{V_{AB}^2 L_{AB}}{2g} + H_{PB} - \frac{64}{Re_{BA} d_{BA}} \frac{V_{BA}^2 L_{BA}}{2g} \right) \frac{2g}{V_{AB}^2} =$$

$$= \left( 0,337 \text{ m} - \frac{64}{1352 \cdot 0,005 \text{ m}} \frac{(1,02 \text{ m/s})^2 \cdot 0,6 \text{ m}}{2g} + 0,337 \text{ m} - \frac{64}{895 \cdot 0,0075 \text{ m}} \frac{(0,45 \text{ m/s})^2 \cdot 0,4 \text{ m}}{2g} \right) \frac{2g}{(1,02 \text{ m/s})^2} = 6,312$$

$$\frac{\Delta P_{12}}{\gamma} = E_{AB}^{\text{LOCALIZZATO}} = \sum \frac{V_{AB}^2}{2g} = \frac{6,312 \cdot (1,02 \text{ m/s})^2}{2g} = 0,333 \text{ m}$$

$$\Delta P_{12} = 0,333 \text{ m} \cdot \gamma = 0,333 \text{ m} \cdot 10,4 \text{ kN/m}^3 = 3458,822 \text{ Pa}$$

Esercizio 8

$$V = \frac{Q}{\pi \frac{d^2}{4}} = \frac{3,5 \cdot 10^{-3} \text{ m}^3/\text{s}}{\pi \frac{(0,06 \text{ m})^2}{4}} = 1,24 \text{ m/s}$$

$$Re = \frac{\rho V d}{\mu} = \frac{1000 \text{ kg/m}^3 \cdot 1,24 \text{ m/s} \cdot 0,06 \text{ m}}{10^{-3} \text{ kg/(m s)}} = 74400 \quad \text{MOTO TURBOLENTA}$$

$$E_A = E_{AB}^{\text{CONTINUO}} + E_{AB}^{\text{LOCALIZZATO}} + E_B$$

$$h_A = \frac{f}{d} \frac{V^2 L}{2g} + \frac{V^2}{2g} \left( 1 + \frac{1}{2} \right) + h_B \Rightarrow f = \left( h_A - h_B - \frac{V^2}{2g} \frac{3}{2} \right) \frac{2g d}{V^2 L} = \left( 0,6 \text{ m} - 0,2 \text{ m} - \frac{(1,24 \text{ m/s})^2}{2g} \frac{3}{2} \right) \frac{2g \cdot 0,06 \text{ m}}{(1,24 \text{ m/s})^2} = 0,03676$$



$$\frac{1}{\sqrt{f}} = -2 \log_{10} \left( \frac{e/d}{3,71} + \frac{2,52}{Re \sqrt{f}} \right) \Rightarrow e = \left( 10^{-\frac{1}{2\sqrt{f}}} - \frac{2,52}{Re \sqrt{f}} \right) 3,71 d =$$

$$= \left( 10^{-\frac{1}{2\sqrt{0,03616}}} - \frac{2,52}{74400 \sqrt{0,03616}} \right) 3,71 \cdot 0,06 \text{ m} = 4,85 \cdot 10^{-4} \text{ m} = 0,485 \text{ mm}$$

$$\frac{1}{\sqrt{f}} = -2 \log_{10} \left( \frac{e/d}{3,71} \right) \Rightarrow f = \left( -2 \log_{10} \left( \frac{e/d}{3,71} \right) \right)^{-2} = \left( -2 \log_{10} \left( \frac{4,85 \cdot 10^{-4} \text{ m}}{0,06 \text{ m}} \right) \right)^{-2} =$$

$$= 0,03528 \neq 0,03616 \quad \text{NOTO NON È SU PARALLELO IDRAULICAMENTE SCABRO}$$

ESEMPIO 9

$$\rho = \frac{3 \gamma_{\text{acqua}}}{g} = \frac{3 \cdot 9810 \text{ N/m}^3}{g} = 3000 \text{ kg/m}^3$$

$$\mu = \rho 2 \nu_{\text{acqua}} = 3000 \text{ kg/m}^3 \cdot 2 \cdot 10^{-6} \text{ m}^2/\text{s} = 6 \cdot 10^{-3} \text{ kg/(m s)}$$

$$\left\{ \begin{aligned} \tau &= \frac{\gamma_i r}{2} \Rightarrow i = \frac{2\tau}{8r} = \frac{2 \cdot 10 \text{ Pa}}{3 \cdot 9810 \text{ N/m}^3 \cdot 1,012 \cdot 10^{-3} \text{ m}} = 0,6778 \end{aligned} \right.$$

$$\left\{ \begin{aligned} Q &= \gamma_i \frac{\pi r^4}{8\mu} = \frac{\gamma_i \tau}{4\mu} \frac{\pi r^4}{8\mu} \Rightarrow r = \sqrt[3]{\frac{Q 4\mu}{\tau \pi}} = \sqrt[3]{\frac{5 \cdot 10^{-3} \text{ m}^3 / 60^2 \text{ s} \cdot 4 \cdot 6 \cdot 10^{-3} \text{ kg/(m s)}}{10 \text{ Pa} \cdot \pi}} = 1,012 \cdot 10^{-3} \text{ m} \\ &= 1,012 \text{ mm} \end{aligned} \right.$$

$$V = \frac{Q}{A} = \frac{5 \cdot 10^{-3} \text{ m}^3 / 60^2 \text{ s}}{\pi (1,012 \cdot 10^{-3} \text{ m})^2} = 0,43 \text{ m/s}$$

$$Re = \frac{Vd}{2\nu_{\text{acqua}}} = \frac{0,43 \text{ m/s} \cdot 2 \cdot 1,012 \cdot 10^{-3} \text{ m}}{2 \cdot 10^{-6} \text{ m}^2/\text{s}} = 435 \text{ NOTO LAMINARE}$$

$$E_A = E_{AB}^{\text{convuls}} + E_B \Leftrightarrow h_A + \frac{\alpha V^2}{2g} = \frac{64}{Re d} \frac{V^2}{2g} L + h_B$$

$$h_B = h_A + \frac{\alpha V^2}{2g} - \frac{64}{Re d} \frac{V^2}{2g} L = 0,4 \text{ m} + \frac{2(0,43 \text{ m/s})^2}{2g} - \frac{64 \cdot 16}{435 \cdot 2 \cdot 1,012 \cdot 10^{-3}} \frac{(0,43 \text{ m/s})^2}{2g} \cdot 0,5 \text{ m} = 0,0825 \text{ m}$$

$$Q = \pi \frac{\delta}{t} \Rightarrow t = \frac{\pi^2 \delta}{Q} = \frac{(0,1 \text{ m})^2 (0,03)}{5 \cdot 10^{-3} \text{ m}^3 / 60^2 \text{ s}} = 276 \text{ s}$$

ESEMPIO 10

$$Re = \frac{vd}{\nu} \Rightarrow v = \frac{Re \nu}{d} = \frac{2 \cdot 10^5 \cdot 10^{-6} \text{ m}^2/\text{s}}{0,2 \text{ m}} = 1 \text{ m/s}$$

$$Q = vA = 1 \text{ m/s} \cdot \pi (0,2)^2 = 0,03 \text{ m}^3/\text{s}$$



$$H_P = f \frac{V^2}{d} L = \frac{0,04878}{0,2m} \frac{50m}{2g} = 0,62m$$

$$\frac{1}{\sqrt{f}} = -2 \log_{10} \left( \frac{e/d}{3,71} \right) \Rightarrow f = \left( -2 \log_{10} \left( \frac{e/d}{3,71} \right) \right)^{-2} = \left( -2 \log_{10} \left( \frac{0,004m}{3,71} \right) \right)^{-2} = 0,04858$$

$f_{TENT}$	$f_{CALC}$	$\frac{1}{\sqrt{f}} = -2 \log_{10} \left( \frac{e/d}{3,71} + \frac{2,52}{Re \sqrt{f}} \right) \Rightarrow f = \left( -2 \log_{10} \left( \frac{e/d}{3,71} + \frac{2,52}{Re \sqrt{f}} \right) \right)^{-2} =$
$0,04858 \neq 0,04878$		$= 0,04878$
$0,04878 = 0,04878$		

$$P_U = \gamma Q H_P = 9810 N/m^3 \cdot 0,03 m^3/s \cdot 0,62m = 182,47 W$$

$$E_A + H_P = E_B \Leftrightarrow h_A + H_P = \frac{p_{atm}}{\gamma} + h_B \Rightarrow h_B = h_A + H_P - \frac{p_{atm}}{\gamma} = 1m + 0,62m - \frac{9810 N/m^3}{9810 N/m^3} = 0,8m$$

#### 5-54 | ESEMPIO 5

$$Q_3 = Q_1 + Q_2 = Q_1 + 2Q_1 = 3Q_1 = 3 \cdot 0,035 \cdot 10^{-3} m^3/s = 1,05 \cdot 10^{-4} m^3/s$$

$$\begin{cases} E_A + H_{P1} = E_N \\ E_A + H_{P2} = E_N \\ E_N = E_{NB}^{CONTINUO} + E_B \end{cases} \Rightarrow H_{P1} = H_{P2} = H_P \Rightarrow E_A + H_P = E_{NB}^{CONTINUO} + E_B$$

$$V_1 = \frac{Q_1}{A} = \frac{0,035 \cdot 10^{-3} m^3/s}{\pi \frac{(0,01m)^2}{4}} = 0,45 m/s$$

$$Re_1 = \frac{V_1 d}{\nu} = \frac{0,45 m/s \cdot 0,01m}{2 \cdot 10^{-5} kg/(ms)} = 225 \text{ FLOTO LAMINARE}$$

$$V_2 = \frac{Q_2}{A} = \frac{2 \cdot 0,035 \cdot 10^{-3} m^3/s}{\pi \frac{(0,01m)^2}{4}} = 0,9 m/s$$

$$Re_2 = \frac{V_2 d}{\nu} = \frac{0,9 m/s \cdot 0,01m}{2 \cdot 10^{-5} kg/(ms)} = 450 \text{ FLOTO LAMINARE}$$

$$V_3 = \frac{Q_3}{A} = \frac{1,05 \cdot 10^{-4} m^3/s}{\pi \frac{(0,01m)^2}{4}} = 1,34 m/s$$

$$Re_3 = \frac{V_3 d}{\nu} = \frac{1,34 m/s \cdot 0,01m}{2 \cdot 10^{-5} kg/(ms)} = 670 \text{ FLOTO LAMINARE}$$



$$E_A = \alpha \frac{V^2}{2g} \quad E_{A1} = \alpha \frac{V_1^2}{2g} = 2 \cdot \frac{(0,45 \text{ m/s})^2}{2g} = 0,02 \text{ m}$$

$$E_{A2} = \alpha \frac{V_2^2}{2g} = 2 \cdot \frac{(0,9 \text{ m/s})^2}{2g} = 0,08 \text{ m}$$

$$E_{NB}^{\text{CONTINU}} = ; L_{NB} = \frac{f}{d} \frac{V^2}{2g} L_{NB} = \frac{64}{Re_3 d} \frac{V_3^2}{2g} L_{NB} = \frac{64}{670 (0,01 \text{ m})} \frac{(1,34 \text{ m/s})^2}{2g} 2 \text{ m} = 1,75 \text{ m}$$

$$E_B = h = 0,3 \text{ m}$$

$$H_{P1} = E_{NB}^{\text{CONTINU}} + E_B - E_{A1} = 1,75 \text{ m} + 0,3 \text{ m} - 0,02 \text{ m} = 2,03 \text{ m}$$

$$H_{P2} = E_{NB}^{\text{CONTINU}} + E_B - E_{A2} = 1,75 \text{ m} + 0,3 \text{ m} - 0,08 \text{ m} = 1,97 \text{ m} \quad \Rightarrow H_{P1} \approx H_{P2}$$

$$P_1 = \gamma Q_1 H_{P1} = 10800 \text{ N/m}^3 \cdot 0,035 \cdot 10^{-3} \text{ m}^3/\text{s} \cdot 2,03 \text{ m} = 0,77 \text{ W}$$

$$P_2 = \gamma Q_2 H_{P2} = 10800 \text{ N/m}^3 \cdot 2 \cdot 0,035 \cdot 10^{-3} \text{ m}^3/\text{s} \cdot 1,97 \text{ m} = 1,49 \text{ W}$$