

$$v = |\vec{v}| \neq \text{cost} \quad \Rightarrow \quad a_T = \frac{dv}{dt} \neq 0$$

$$\vec{a} = \vec{a}_T + \vec{a}_N$$

$$\Rightarrow a = \sqrt{a_T^2 + a_N^2}$$

Moto circolare uniformemente accelerato:

$$\boxed{a_T = \text{cost}}$$

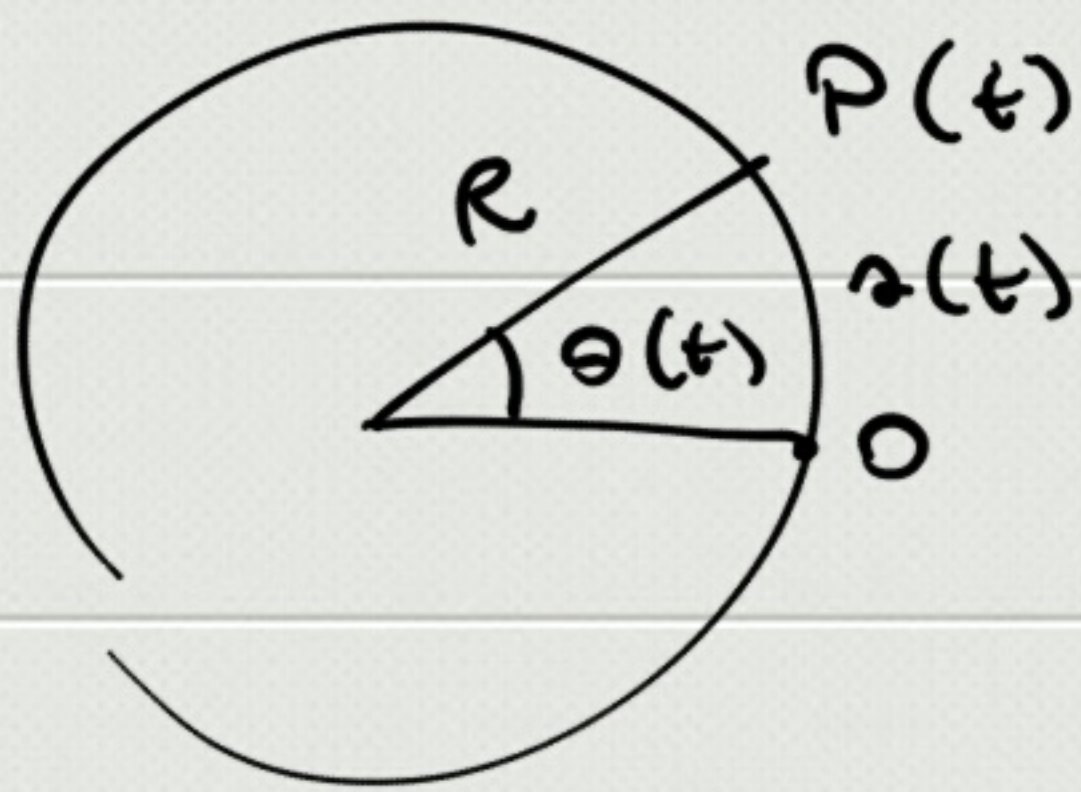
$$a_T = \frac{dv}{dt} = \frac{d^2s}{dt^2}$$

$$\Rightarrow \int_{v_0}^{v(t)} dv = \int_0^t a_T dt \quad \Rightarrow \quad v(t) = v_0 + \int_0^t a_T dt =$$

$$= v_0 + a_T t$$

$$a_T = \text{cost}$$

$$\int ds = \int v dt \quad \Rightarrow \quad s(t) = s_0 + v_0 t + \frac{1}{2} a_T t^2$$



$$\omega(t) = \frac{d\theta}{dt}$$

accelerazione angolare $\boxed{\alpha(t) = \frac{d\omega}{dt}}$

$$\int_{\omega_0}^{\omega(t)} d\omega = \int_0^t \alpha(t) dt \Rightarrow \omega(t) = \omega_0 + \int_0^t \alpha(t) dt$$

(α=cost) $\quad \quad \quad = \omega_0 + \alpha t$

$$\omega = \frac{d\theta}{dt} \Rightarrow \int_{\theta_0}^{\theta(t)} d\theta = \int_0^t \omega(t) dt$$

\Rightarrow $\boxed{\theta(t) = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2}$

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α=cost

$$\alpha = \frac{d\omega}{dt} = \frac{d}{dt} \left(\frac{v}{R} \right) = \frac{1}{R} \frac{dv}{dt} = \frac{a_T}{R}$$

$$\Rightarrow \boxed{\alpha = \frac{a_T}{R}}$$

$$[\alpha] = \text{rad/s}^2$$

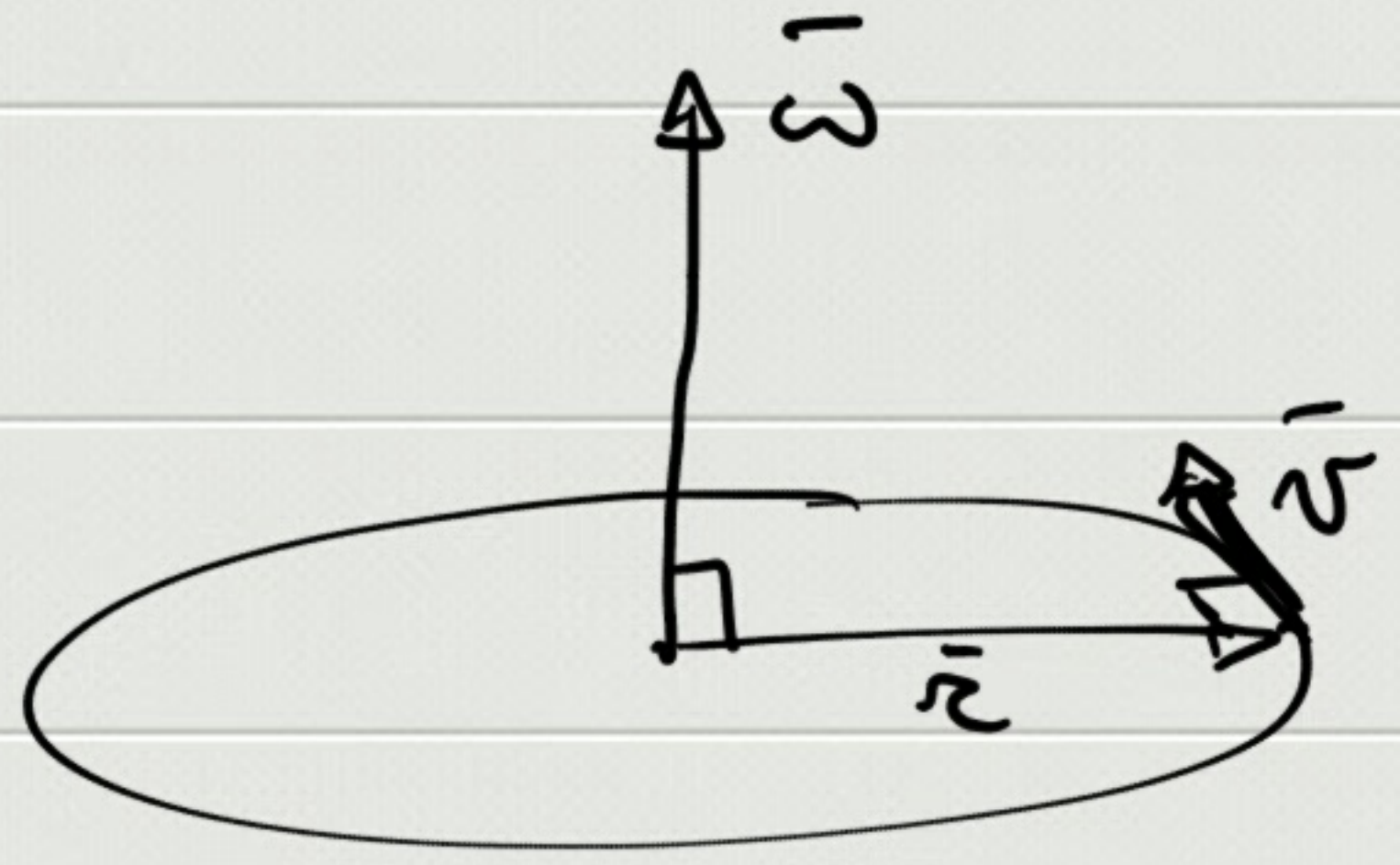
$$\alpha = \frac{d\omega}{dt} = \frac{d\omega}{d\theta} \frac{d\theta}{dt} = \omega \frac{d\omega}{d\theta}$$

$$\Rightarrow \int_{\omega_0}^{\omega(\theta)} \omega d\omega = \int_{\theta_0}^{\theta} \alpha d\theta \Rightarrow \frac{1}{2} \omega^2(\theta) - \frac{1}{2} \omega_0^2 = \int_{\theta_0}^{\theta} \alpha(\theta) d\theta$$

$$\Rightarrow \omega^2(\theta) = \omega_0^2 + 2 \int_{\theta_0}^{\theta} \alpha(\theta) d\theta$$

$$\alpha = \text{cont} \Rightarrow \boxed{\omega^2(\theta) = \omega_0^2 + 2\alpha(\theta - \theta_0)}$$

$$v = \omega R$$



$$\vec{v} = \vec{\omega} \times \vec{r}$$

$$\vec{\alpha} = \frac{d\vec{\omega}}{dt}$$

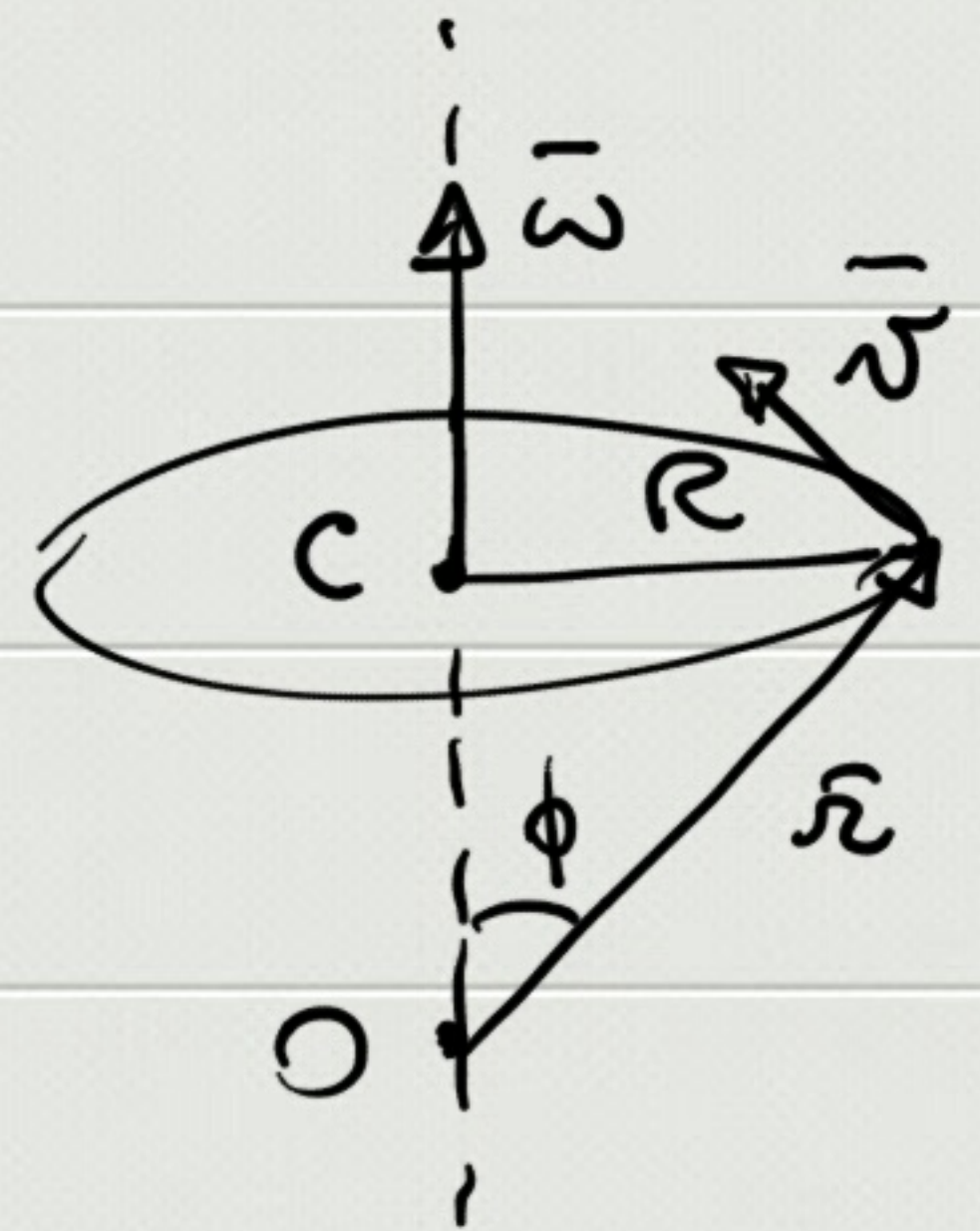
$$\vec{\alpha} \parallel \vec{\omega}$$

$$|\vec{\alpha}| = \left| \frac{d\vec{\omega}}{dt} \right|$$

$$\vec{v} = \vec{\omega} \times \vec{r} \Rightarrow \vec{a} = \frac{d\vec{v}}{dt} = \frac{d}{dt} (\vec{\omega} \times \vec{r}) =$$

$$= \frac{d\vec{\omega}}{dt} \times \vec{r} + \vec{\omega} \times \frac{d\vec{r}}{dt} = \boxed{\vec{\alpha} \times \vec{r} + \vec{\omega} \times \vec{v} = \vec{a}_\tau + \vec{a}_N}$$

$$\vec{a}_\tau = \vec{\alpha} \times \vec{r} \quad \vec{a}_N = \vec{\omega} \times \vec{v}$$



$$\vec{v} = \vec{\omega} \times \vec{r}$$

$$v = \omega r \sin \phi = \omega R$$