

$$v_B, v_C$$

$$N_B, N_C$$

liscio \Rightarrow solo forze cons.

$$E_m = \text{cost}$$

$$E_{m, \text{in}} = \frac{1}{2} m v_0^2$$

$$E_{m, P} = E_{K, P} + E_{\text{pot}, P} = \frac{1}{2} m v^2 + m g z$$

$$z = R - R \cos \theta = R (1 - \cos \theta)$$

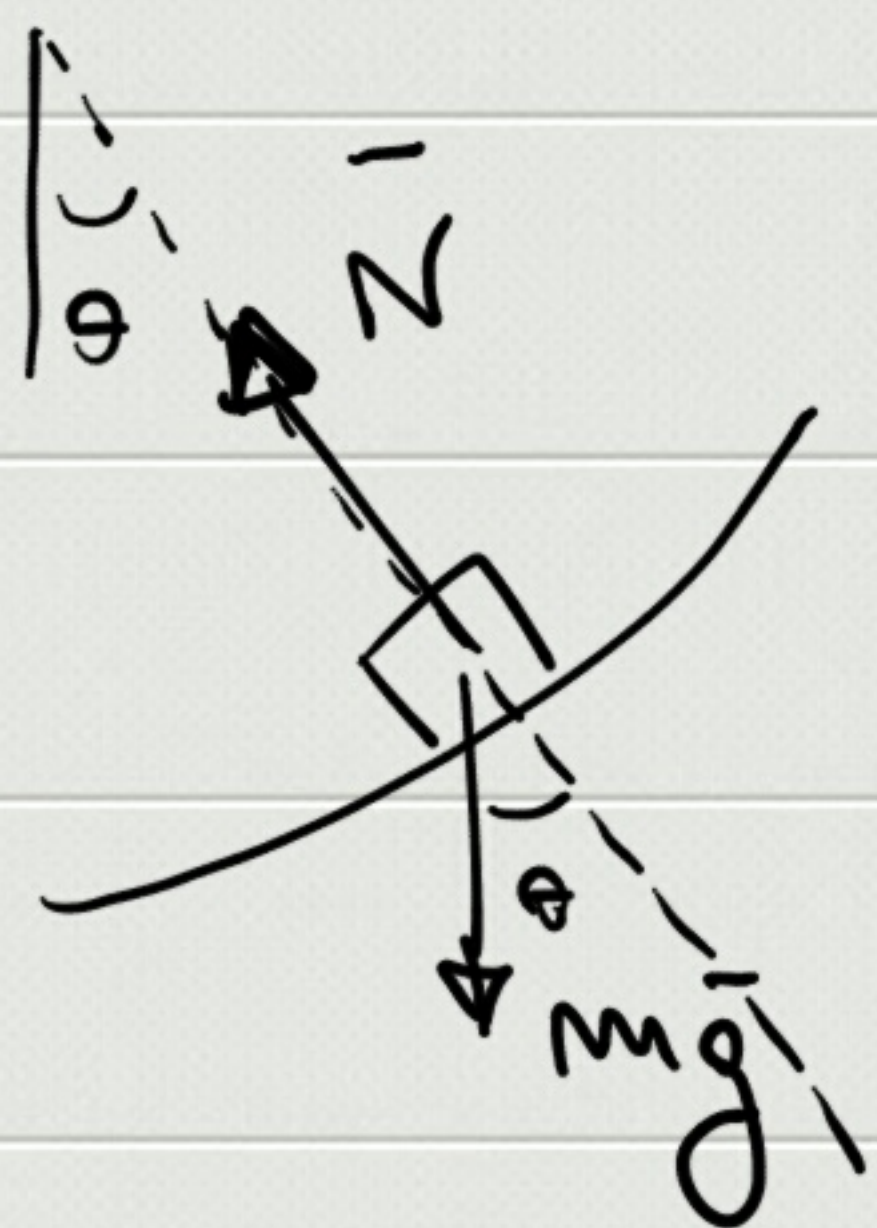
$$E_{m, P} = \frac{1}{2} m v^2(\theta) + m g R (1 - \cos \theta)$$

$$= \frac{1}{2} m v_0^2$$

$$\Rightarrow v(\theta) = \sqrt{v_0^2 - 2 g R (1 - \cos \theta)}$$

$$v_B = v(\theta = \frac{\pi}{2}) = \sqrt{v_0^2 - 2 g R}$$

$$v_C = v(\theta = \pi) = \sqrt{v_0^2 - 4 g R}$$



$$\vec{N} + m\vec{g} = m\vec{a}$$

$$\vec{u}_N : N - mg \cos \theta = m a_N = m \frac{v^2}{R}$$

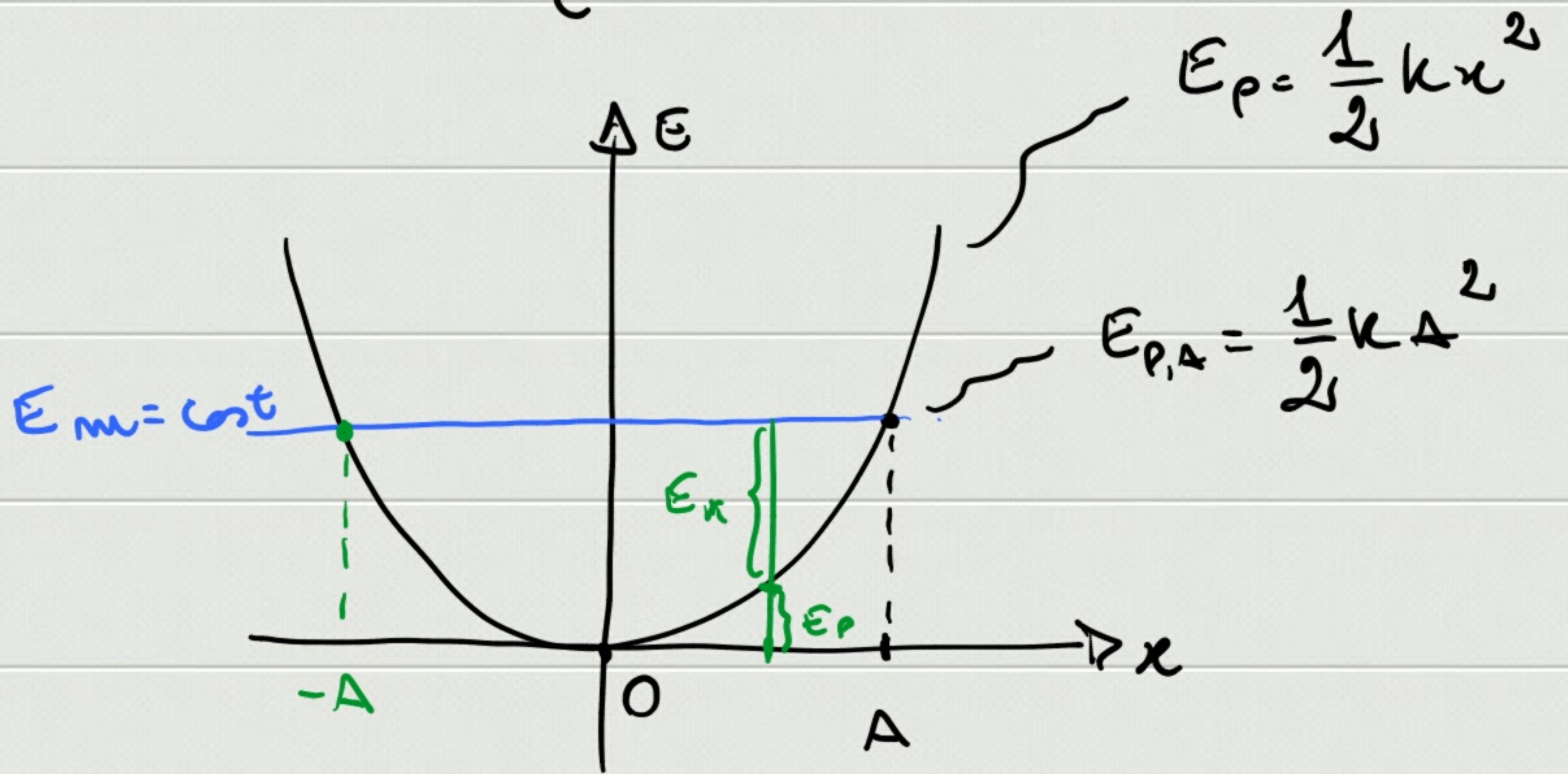
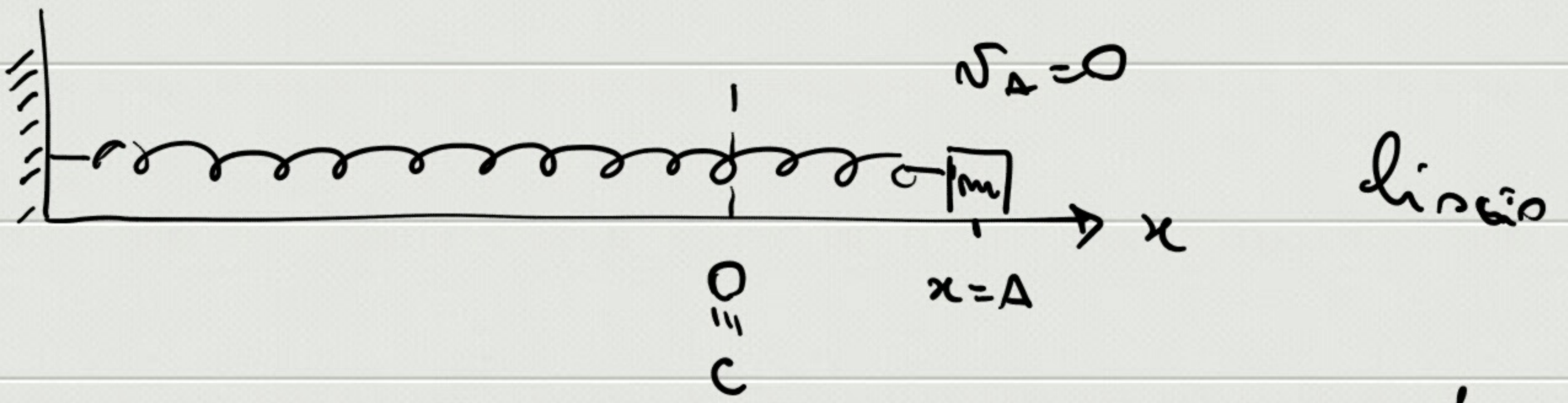
$$\Rightarrow N(\theta) = m \frac{v^2(\theta)}{R} + mg \cos \theta$$

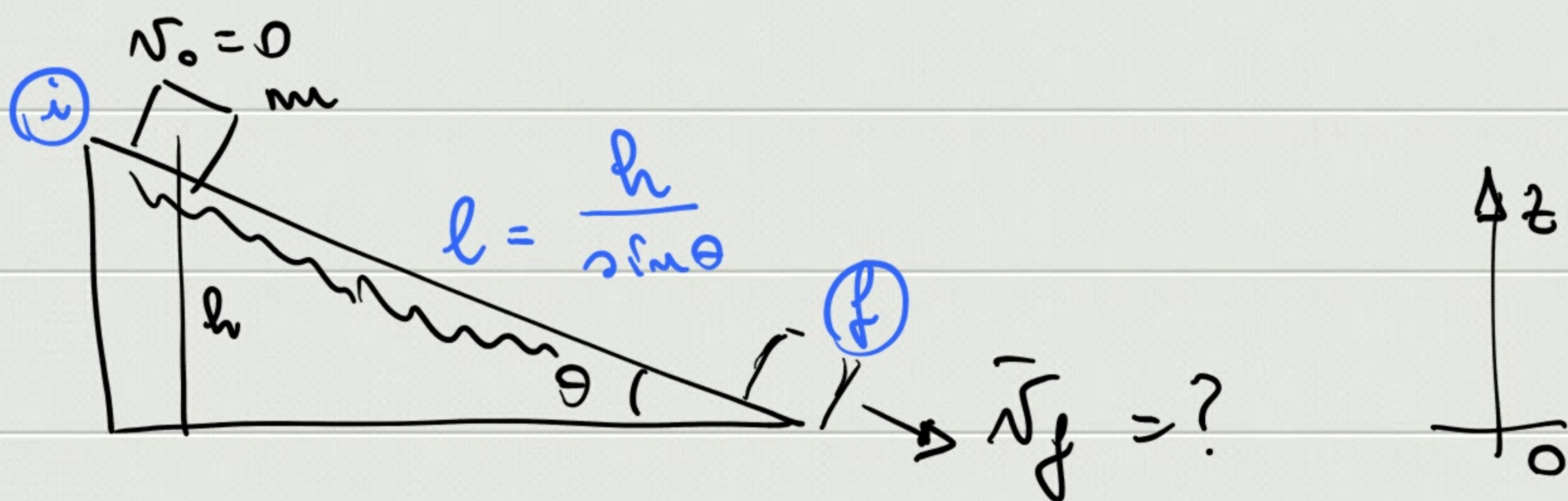
$$N_B = N\left(\theta = \frac{\pi}{2}\right) = \frac{mv^2}{R} (\nu_0^2 - 2gR)$$

$$N_C = N(\theta = \pi) = \frac{mv^2}{R} (\nu_0^2 - 4gR) - mg = m \left(\frac{\nu_0^2}{R} - 5g \right)$$

$$\nu_{0, \min} = ? \quad \Rightarrow N_C = 0$$

$$\Rightarrow \nu_{0, (\min)} = \sqrt{5gR}$$





force non cons. $\Rightarrow \boxed{W_{nc} = \Delta E_m}$

$$E_{m,f} = E_{k,f} + E_{p,f} = \frac{1}{2} m v_f^2$$

$$E_{m,i} = mgh$$

$$W_{m,c} = \int_i^f \vec{F}_{cd} d\vec{s} =$$

$$= \int_i^f (-\mu_d N \vec{u}_r) d\vec{s} = -\mu_d mg \cos \theta \int_i^f ds =$$

$$= -\mu_d mg \cos \theta \cdot l = -\mu_d mgh \cot \theta$$

$$-\mu_d mgh \cot \theta = \frac{1}{2} m v_f^2 - mgh$$

$$\Rightarrow v_f = \sqrt{2gh(1 - \mu_d \cot \theta)}$$

