

# List 11: Marginal effects

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```
## Warning in find.package(package, lib.loc, verbose = verbose): there is no
## package called 'Ecdat'
```

```
## Warning in data(loanapp, SwissLabor, Mroz, package = c("wooldridge", "AER", :
## data set 'Mroz' not found
```

## 1 Marginal effects

### 1.1 for probit

Consider a probit-regression  $P(y = 1) = \Phi(x' \beta)$ , where  $x' \beta = \beta_0 + \beta_1 x_1 + \dots + \beta_k x_k$

Marginal effects  $\frac{\partial P(y=1)}{\partial x_j} = \phi(x' \beta) \beta_j$ , where  $\phi(z) = \frac{1}{\sqrt{2\pi}} \exp\{-z^2/2\}$

### 1.2 for logit

Consider a logit-regression  $P(y = 1) = \Lambda(x' \beta)$ , where  $x' \beta = \beta_0 + \beta_1 x_1 + \dots + \beta_k x_k$

Marginal effects  $\frac{\partial P(y=1)}{\partial x_j} = \lambda(x' \beta) \beta_j$ , where  $\lambda(z) = \frac{\exp(z)}{(1+\exp(z))^2}$

### 1.3 Average marginal effects

Usually we consider

- marginal effects at the mean of each regressor :
  - $\phi(\bar{x}' \beta) \beta_j$  for probit
  - $\lambda(\bar{x}' \beta) \beta_j$  for logit
- The average of the marginal effects at each observation:
  - $\overline{\phi(x' \beta) \beta_j}$  for probit
  - $\overline{\lambda(x' \beta) \beta_j}$  for logit

## 2 labour force equation

For the dataset TableF5-1 consider regression **LFP на WA, log(FAMINC), WE, KL6, K618, CIT, UN** of the following specifications:

- logit
- probit

The marginal effects at the mean of each regressor for logit model **Round the answer to 3 decimal places.**

|              | effect | error | t.value | p.value |
|--------------|--------|-------|---------|---------|
| (Intercept)  | -0.454 | 0.411 | -1.105  | 0.270   |
| WA           | -0.015 | 0.003 | -5.006  | 0.000   |
| log (FAMINC) | 0.083  | 0.042 | 1.982   | 0.048   |
| WE           | 0.044  | 0.010 | 4.450   | 0.000   |
| KL6          | -0.353 | 0.048 | -7.395  | 0.000   |
| K618         | -0.023 | 0.016 | -1.416  | 0.157   |
| CIT          | -0.052 | 0.043 | -1.219  | 0.223   |
| UN           | -0.004 | 0.006 | -0.675  | 0.500   |

The marginal effects at the mean of each regressor for probit model. **Round the answer to 3 decimal places.**

|              | effect | error | t.value | p.value |
|--------------|--------|-------|---------|---------|
| (Intercept)  | -0.434 | 0.399 | -1.089  | 0.277   |
| WA           | -0.015 | 0.003 | -5.066  | 0.000   |
| log (FAMINC) | 0.081  | 0.041 | 1.966   | 0.050   |
| WE           | 0.042  | 0.009 | 4.504   | 0.000   |
| KL6          | -0.340 | 0.044 | -7.663  | 0.000   |
| K618         | -0.022 | 0.016 | -1.402  | 0.161   |
| CIT          | -0.049 | 0.042 | -1.179  | 0.239   |
| UN           | -0.004 | 0.006 | -0.669  | 0.504   |

The average of the marginal effects at each observation for logit модели. **Round the answer to 3 decimal places.**

|              | effect | error | t.value | p.value |
|--------------|--------|-------|---------|---------|
| (Intercept)  | -0.395 | 0.358 | -1.105  | 0.270   |
| WA           | -0.013 | 0.003 | -5.006  | 0.000   |
| log (FAMINC) | 0.073  | 0.037 | 1.982   | 0.048   |
| WE           | 0.038  | 0.009 | 4.450   | 0.000   |
| KL6          | -0.307 | 0.042 | -7.395  | 0.000   |
| K618         | -0.020 | 0.014 | -1.416  | 0.157   |
| CIT          | -0.052 | 0.043 | -1.219  | 0.223   |
| UN           | -0.004 | 0.005 | -0.675  | 0.500   |

The average of the marginal effects at each observation for probit модели. **Round the answer to 3 decimal places.**

|              | effect | error | t.value | p.value |
|--------------|--------|-------|---------|---------|
| (Intercept)  | -0.388 | 0.357 | -1.089  | 0.277   |
| WA           | -0.013 | 0.003 | -5.066  | 0.000   |
| log (FAMINC) | 0.072  | 0.037 | 1.966   | 0.050   |
| WE           | 0.038  | 0.008 | 4.504   | 0.000   |
| KL6          | -0.304 | 0.040 | -7.663  | 0.000   |
| K618         | -0.020 | 0.014 | -1.402  | 0.161   |
| CIT          | -0.049 | 0.042 | -1.179  | 0.239   |
| UN           | -0.004 | 0.006 | -0.669  | 0.504   |

### 3 approve equation

For the dataset `loanapp` consider regression **approve** на **appinc/100**, **mortno**, **unem**, **dep**, **male** of the following specifications:

- logit
- probit

The marginal effects at the mean of each regressor for logit model **Round the answer to 3 decimal places.**

|               | effect | error | t.value | p.value |
|---------------|--------|-------|---------|---------|
| (Intercept)   | 0.210  | 0.019 | 10.915  | 0.000   |
| I(appinc/100) | -0.011 | 0.007 | -1.583  | 0.114   |
| mortno        | 0.077  | 0.014 | 5.451   | 0.000   |
| unem          | -0.007 | 0.003 | -2.260  | 0.024   |
| dep           | -0.011 | 0.006 | -1.741  | 0.082   |
| male          | 0.019  | 0.020 | 0.945   | 0.345   |

The marginal effects at the mean of each regressor for probit model. **Round the answer to 3 decimal places.**

|               | effect | error | t.value | p.value |
|---------------|--------|-------|---------|---------|
| (Intercept)   | 0.237  | 0.020 | 12.009  | 0.000   |
| I(appinc/100) | -0.011 | 0.008 | -1.468  | 0.142   |
| mortno        | 0.077  | 0.014 | 5.415   | 0.000   |
| unem          | -0.007 | 0.003 | -2.272  | 0.023   |
| dep           | -0.011 | 0.007 | -1.650  | 0.099   |
| male          | 0.019  | 0.020 | 0.953   | 0.341   |

The average of the marginal effects at each observation for logit модели. **Round the answer to 3 decimal places.**

|               | effect | error | t.value | p.value |
|---------------|--------|-------|---------|---------|
| (Intercept)   | 0.217  | 0.020 | 10.915  | 0.000   |
| I(appinc/100) | -0.011 | 0.007 | -1.583  | 0.114   |
| mortno        | 0.077  | 0.014 | 5.451   | 0.000   |
| unem          | -0.007 | 0.003 | -2.260  | 0.024   |
| dep           | -0.011 | 0.006 | -1.741  | 0.082   |
| male          | 0.019  | 0.020 | 0.945   | 0.345   |

The average of the marginal effects at each observation for probit модели. **Round the answer to 3 decimal places.**

|               | effect | error | t.value | p.value |
|---------------|--------|-------|---------|---------|
| (Intercept)   | 0.239  | 0.020 | 12.009  | 0.000   |
| I(appinc/100) | -0.011 | 0.008 | -1.468  | 0.142   |
| mortno        | 0.077  | 0.014 | 5.415   | 0.000   |
| unem          | -0.007 | 0.003 | -2.272  | 0.023   |
| dep           | -0.011 | 0.007 | -1.650  | 0.099   |
| male          | 0.019  | 0.020 | 0.953   | 0.341   |

### 4 swiss labour force equation

For the dataset `SwissLabour` consider regression **participation** на **income**, **age**, **age^2**, **youngkids**, **oldkids** of the following specification:

- logit
- probit

The marginal effects at the mean of each regressor for logit model **Round the answer to 3 decimal places.**

| effect | error | t.value | p.value |
|--------|-------|---------|---------|
|--------|-------|---------|---------|

|             |        |       |        |       |
|-------------|--------|-------|--------|-------|
| (Intercept) | 2.083  | 0.576 | 3.617  | 0.000 |
| income      | -0.330 | 0.053 | -6.249 | 0.000 |
| age         | 0.965  | 0.165 | 5.849  | 0.000 |
| I (age^2)   | -0.136 | 0.020 | -6.633 | 0.000 |
| youngkids   | -0.264 | 0.041 | -6.458 | 0.000 |
| oldkids     | -0.062 | 0.020 | -3.052 | 0.002 |

The marginal effects at the mean of each regressor for probit model. **Round the answer to 3 decimal places.**

|             | effect | error | t.value | p.value |
|-------------|--------|-------|---------|---------|
| (Intercept) | 2.000  | 0.547 | 3.657   | 0.000   |
| income      | -0.318 | 0.050 | -6.419  | 0.000   |
| age         | 0.934  | 0.157 | 5.961   | 0.000   |
| I (age^2)   | -0.131 | 0.019 | -6.794  | 0.000   |
| youngkids   | -0.253 | 0.039 | -6.567  | 0.000   |
| oldkids     | -0.060 | 0.020 | -3.048  | 0.002   |

The average of the marginal effects at each observation for logit модели. **Round the answer to 3 decimal places.**

|             | effect | error | t.value | p.value |
|-------------|--------|-------|---------|---------|
| (Intercept) | 1.762  | 0.487 | 3.617   | 0.000   |
| income      | -0.279 | 0.045 | -6.249  | 0.000   |
| age         | 0.817  | 0.140 | 5.849   | 0.000   |
| I (age^2)   | -0.115 | 0.017 | -6.633  | 0.000   |
| youngkids   | -0.224 | 0.035 | -6.458  | 0.000   |
| oldkids     | -0.053 | 0.017 | -3.052  | 0.002   |

The average of the marginal effects at each observation for probit модели. **Round the answer to 3 decimal places.**

|             | effect | error | t.value | p.value |
|-------------|--------|-------|---------|---------|
| (Intercept) | 1.745  | 0.477 | 3.657   | 0.000   |
| income      | -0.278 | 0.043 | -6.419  | 0.000   |
| age         | 0.815  | 0.137 | 5.961   | 0.000   |
| I (age^2)   | -0.115 | 0.017 | -6.794  | 0.000   |
| youngkids   | -0.221 | 0.034 | -6.567  | 0.000   |
| oldkids     | -0.053 | 0.017 | -3.048  | 0.002   |