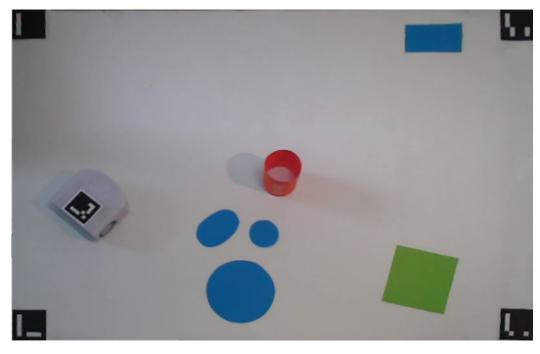
# Basics of mobile robotics



Thymio project

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### Our project: Arena



- A0 White sheet
- Goal : shape of different color than global obstacles
- Global obstacles: any colors, any shapes
- Local obstacles: small shapes, any color
- 5 ArUco markers : corners and thymio

### Computer Vision - Initialization

1) First image



2) After Warm Up

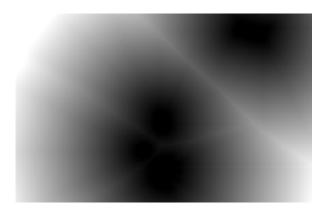


3) After perspective correction

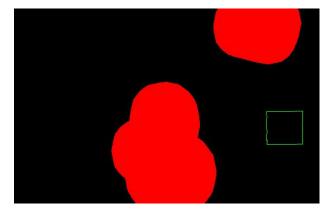


### Goal Detection and Obstacles Expansion

- Global obstacles and goal found with color thresholds
- Small blobs removed
- Contours extracted and expanded by the thymio radius for the obstacles



Distance map to obstacles for expansion



Final image for plotting and A\*

### Kalman Filter

Motion Equations: (Runge Kutta 2 for better precision)

$$\begin{pmatrix} x(t + \Delta t) = x(t) + v \cdot \cos(\theta + \frac{\omega \cdot \Delta t}{2}) \Delta t \\ y(t + \Delta t) = y(t) + v \cdot \sin(\theta + \frac{\omega \cdot \Delta t}{2}) \Delta t \\ \theta(t + \Delta t) = \theta(t) + \omega \cdot \Delta t \end{pmatrix}$$

$$\omega = \frac{v_L - v_R}{L} \quad v = \frac{v_L + v_R}{2}$$



1. Prediction: 
$$x_t = g(u_t, x_{t-1})$$
 and  $\Sigma_t = G_t \Sigma_{t-1} G_t^ op + Q_t$ 

2. Update: 
$$K_t = \Sigma_t H_t^{ op} \left( H_t \Sigma_t H_t^{ op} + R_t \right)^{-1}$$
,  $x_t = x_t + K_t \left( z_t - h(x_t) \right)$  and  $\Sigma_t = (I - K_t H_t) \Sigma_t$ 

With: 
$$Q = Gu, t \cdot Q_{control} \cdot Gu, t^{\top}$$

Q= diag(var(left motor speed),var(right motor speed))

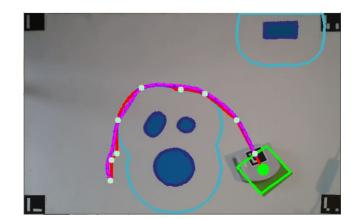
R=diag(var(x\_cam),var(y\_cam),var(theta\_cam))

Both covariance measured, not even tuned!

### Path Planning

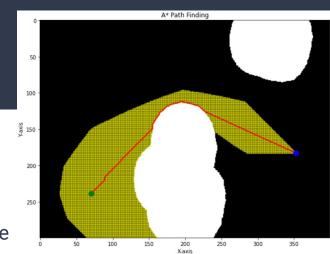
#### A\* path search:

- Complete, will always give a solution
- image is a grid so straightforward implementation
- processing time/precision trade off easily tuned with grid size
- 8 neighbors, L2 norms
- Problem: not optimal because robot is not constraint to 45 degree angles



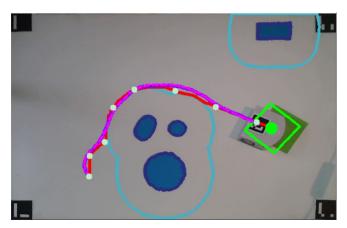
#### Key points:

- + Easier movement
- Shortcuts paths
- Rotation
- Max interval

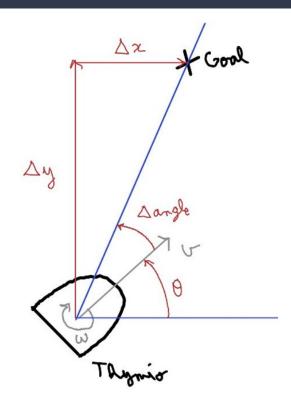


### Motion control: Following the path

Controller: proportional to ∆angle



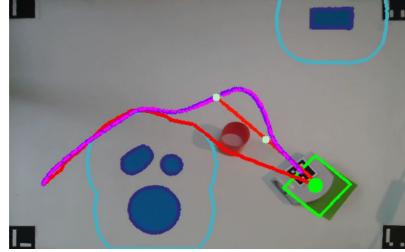
```
v = SPEED  # Translational velocity PWM
omega = k_alpha*(delta_angle) # Rotational velocity [rad/s]
# Calculate motor speed
v_ml = (v+omega*L_AXIS) #PWM
v_mr = (v-omega*L_AXIS) #PWM
```



### Motion control: Local avoidance

Braitenberg logic : speed corrections are added proportionally to proximity sensors values

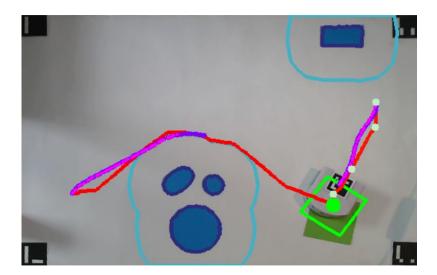
```
def avoid_obstacle(prox_values): # Prox values go from left to right
    braitenberg = [-2/300, -10/300, 25/300, 11/300, 3/300] # Tuned parameters
    v_mr, v_ml = SPEED, SPEED
    for i in range (len(prox_values)) :
        v_ml -= braitenberg[i] * prox_values[i]
        v_mr += braitenberg[i] * prox_values[i]
    return v_ml, v_mr
```



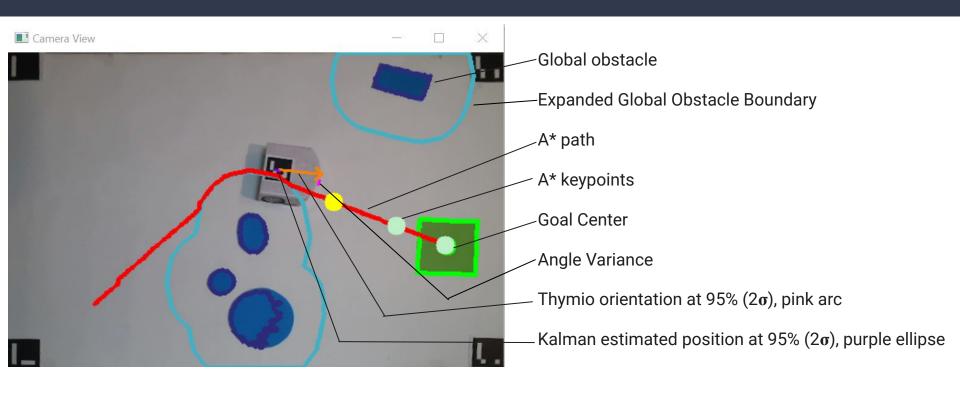
## Kidnapping: using proximity ground sensors

- If sensors value under a certain threshold -> not on the white ground anymore
  - -> we stop the motors and stop the localisation

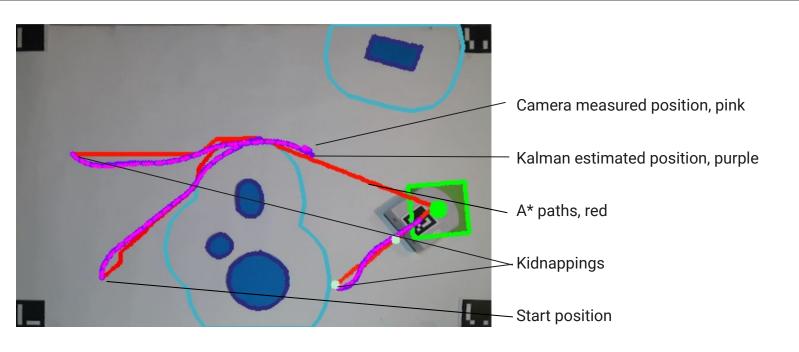
Once back on the ground : update position and find new path



# Path Tracking



## Path History (with kidnapping)



### Computer Vision - ArUco Markers

- The 4 corners of the arena are 4 Aruco markers with different ids. And there is one on the Thymio
- Aruco because robust to varying lighting conditions and precise
- With the corner's markers size in pixel and the real size in mm we get the factor pix/mm
- Thymio angle is found with the top and bottom edge

