Problem A. Oops, It's Yesterday Twice More

Input file: standard input
Output file: standard output

Time limit: 1 second Memory limit: 256 megabytes

After the great success in 2018, 2019, and 2020, Nanjing University of Aeronautics and Astronautics (NUAA) will host the *International Collegiate Programming Contest* (ICPC) Nanjing regional for the fourth time.

Team **Power of Two** and team **Three Hold Two** won the champion for Tsinghua University in 2018 and 2019. In 2020, team **Inverted Cross** from Peking University won the champion. In 2021, there are around 700 teams including **the defending champion** participating in the contest. We are so excited to see who will win this year!

Although we can't gather in Nanjing this time due to the pandemic, we should still be grateful for the hard work done by all staff and volunteers for this contest. Thank you all for your great contribution to this contest!

In the 2018 contest, problem K, *Kangaroo Puzzle*, requires the contestants to construct an operation sequence for the game:

The puzzle is a grid with n rows and m columns $(1 \le n, m \le 20)$ and there are some (at least 2) kangaroos standing in the puzzle. The player's goal is to control them to get together. There are some walls in some cells and the kangaroos cannot enter the cells with walls. The other cells are empty. The kangaroos can move from an empty cell to an adjacent empty cell in four directions: up, down, left, and right.

There is exactly one kangaroo in every empty cell in the beginning and the player can control the kangaroos by pressing the button U, D, L, R on the keyboard. The kangaroos will move simultaneously according to the button you press.

The contestant needs to construct an operating sequence of at most 5×10^4 steps consisting of U, D, L, R only to achieve the goal.

In the 2020 contest, problem A, Ah, It's Yesterday Once More, requires the contestants to construct an input map to hack the following code of the problem described before:

```
#include <bits/stdc++.h>
using namespace std;
string s = "UDLR";
int main()
{
    srand(time(NULL));
    for (int i = 1; i <= 50000; i++) putchar(s[rand() % 4]);
    return 0;
}</pre>
```

Now in the 2021 contest, Paimon prepares another version of the problem for you. You are given a grid with n rows and n columns ($2 \le n \le 500$). All cells are empty and there is one kangaroo standing in each cell.

Similarly, you can control the kangaroos by pressing the button U, D, L, R on the keyboard. The kangaroos will move simultaneously according to the button you press. Specifically, for any kangaroo located in the cell on the i-th row and the j-th column, indicated by (i, j):

1. Button U: it will move to (i-1,j) if i>1. Otherwise, it will stay in the same grid.

XXII Open Cup named after E.V. Pankratiev Stage 9: Grand Prix of Nanjing, Division 2, Sunday, December 12, 2021

- 2. Button D: it will move to (i+1,j) if i < n. Otherwise, it will stay in the same grid.
- 3. Button L: it will move to (i, j 1) if j > 1. Otherwise, it will stay in the same grid.
- 4. Button R: it will move to (i, j + 1) if j < n. Otherwise, it will stay in the same grid.

You need to construct an operating sequence consisting only of characters 'U', 'D', 'L', and 'R'. After applying it, you must make sure every kangaroo will gather at the specific cell (a,b). The length of the operating sequence cannot exceed 3(n-1).

Input

There is only one test case in each test file.

The first and only line of the input contains three integers n, a, b ($2 \le n \le 500$, $1 \le a, b \le n$) indicating the size of the grid and the target cell.

Output

Output a string consisting only of characters 'U', 'D', 'L' and 'R' in one line. And its length mustn't exceed 3(n-1). It can be proved that the answer always exists.

standard input	standard output
3 3 3	RRDD
4 3 2	DLDLDLUR

Problem C. Klee in Solitary Confinement

Input file: standard input
Output file: standard output

Time limit: 1 second Memory limit: 256 megabytes

Since the traveler comes, People in Monstadt suddenly raise great interest in computer programming and algorithms, including Klee, the Spark Knight of the Knights of Favonius.



Source: Genshin Impact Official

Being sent to solitary confinement by Jean again, Klee decides to spend time learning the famous Mo's algorithm, which can compute with a time complexity of $\mathcal{O}(n^{1.5})$ for some range query problem without modifications.

To check whether Klee has truly mastered the algorithm (or in fact making another bombs secretly), Jean gives her a problem of an integer sequence a_1, a_2, \dots, a_n along with some queries $[l_i, r_i]$ requiring her to find the mode number in the contiguous subsequence $a_{l_i}, a_{l_i+1}, \dots, a_{r_i}$. The mode number is the most common number (that is to say, the number which appears the maximum number of times) in the subsequence.

With the help of Mo's algorithm, Klee solves that problem without effort, but another problem comes into her mind. Given an integer sequence a_1, a_2, \dots, a_n of length n and an integer k, you can perform the following operation at most once: Choose two integers l and r such that $1 \le l \le r \le n$ and add k to every a_i where $l \le i \le r$. Note that it is OK not to perform this operation. Compute the maximum occurrence of the mode number of the whole sequence if you choose to perform (or not perform) the operation optimally.

Input

There is only one test case in each test file.

The first line of the input contains two integers n and k $(1 \le n \le 10^6, -10^6 \le k \le 10^6)$ indicating the length of the sequence and the additive number.

The second line of the input contains n integers a_1, a_2, \dots, a_n ($-10^6 \le a_i \le 10^6$) indicating the original sequence.

Output

Output one line containing one integer indicating the maximum occurrence of the mode number of the whole sequence after performing (or not performing) the operation.

Examples

standard input	standard output
5 2	5
2 2 4 4 4	
7 1	6
3 2 3 2 2 2 3	
7 1	5
2 3 2 3 2 3 3	
9 -100	3
-1 -2 1 2 -1 -2 1 -2 1	

Note

For the first sample test case, choose l=1 and r=2 and we'll result in the sequence $\{4,4,4,4,4\}$. The mode number is obviously 4 which appears 5 times.

For the second sample test case, choose l=4 and r=6 and we'll result in the sequence $\{3,2,3,3,3,3,3,3\}$. The mode number is 3 which appears 6 times.

For the fourth sample test case, choose not to perform the operation. The mode number is 1 and -2 which both appear 3 times.

Problem D. Paimon Sorting

Input file: standard input
Output file: standard output

Time limit: 1 second Memory limit: 256 megabytes

Paimon just invents a new sorting algorithm which looks much like $bubble\ sort$, with a few differences. It accepts a 1-indexed sequence A of length n and sorts it. Its pseudo-code is shown below.

Fun	ctions 1 The Sorting Algor	rithm
1: f	function $SORT(A)$	
2:	for $i \leftarrow 1$ to n do	$\triangleright n$ is the number of elements in A
3:	for $j \leftarrow 1$ to n do	
4:	if $a_i < a_j$ then	$\triangleright a_i$ is the <i>i</i> -th element in A
5:	Swap a_i and a_i	İj

If you don't believe this piece of algorithm can sort a sequence it will also be your task to prove it. Anyway here comes the question:

Given an integer sequence $A = a_1, a_2, \dots, a_n$ of length n, for each of its prefix A_k of length k (that is, for each $1 \le k \le n$, consider the subsequence $A_k = a_1, a_2, \dots, a_k$), count the number of swaps performed if we call $SORT(A_k)$.

Input

There are multiple test cases. The first line of the input contains an integer T indicating the number of test cases. For each test case:

The first line contains an integer n ($1 \le n \le 10^5$) indicating the length of the sequence.

The second line contains n integers a_1, a_2, \dots, a_n $(1 \le a_i \le n)$ indicating the given sequence.

It's guaranteed that the sum of n of all test cases will not exceed 10^6 .

Output

For each test case output one line containing n integers s_1, s_2, \dots, s_n separated by a space, where s_i is the number of swaps performed if we call $SORT(A_i)$.

standard input	standard output
3	0 2 3 5 7
5	0 2 4
2 3 2 1 5	0
3	
1 2 3	
1	
1	

Problem E. Paimon Segment Tree

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 256 megabytes

Paimon just learns the persistent segment tree and decides to practice immediately. Therefore, Lumine gives her an easy problem to start:

Given a sequence a_1, a_2, \dots, a_n of length n, Lumine will apply m modifications to the sequence. In the i-th modification, indicated by three integers l_i , r_i $(1 \le l_i \le r_i \le n)$ and x_i , Lumine will change a_k to $(a_k + x_i)$ for all $l_i \le k \le r_i$.

Let $a_{i,t}$ be the value of a_i just after the t-th operation. This way we can keep track of all historial versions of a_i . Note that $a_{i,t}$ might be the same as $a_{i,t-1}$ if it hasn't been modified in the t-th modification. For completeness we also define $a_{i,0}$ as the initial value of a_i .

After all modifications have been applied, Lumine will give Paimon q queries about the sum of squares among the historical values. The k-th query is indicated by four integers l_k , r_k , x_k and y_k and requires Paimon to calculate

$$\sum_{i=l_k}^{r_k} \sum_{j=x_k}^{y_k} a_{i,j}^2$$

Please help Paimon compute the result for all queries. As the answer might be very large, please output the answer modulo $10^9 + 7$.

Input

There is only one test case in each test file.

The first line of the input contains three integers n, m and q ($1 \le n, m, q \le 5 \times 10^4$) indicating the length of the sequence, the number of modifications and the number of queries.

The second line contains n integers a_1, a_2, \dots, a_n ($|a_i| < 10^9 + 7$) indicating the initial sequence.

For the following m lines, the i-th line contains three integers l_i , r_i and x_i $(1 \le l_i \le r_i \le n, |x_i| < 10^9 + 7)$ indicating the i-th modification.

For the following q lines, the i-th line contains four integers l_i , r_i , x_i and y_i ($1 \le l_i \le r_i \le n$, $0 \le x_i \le y_i \le m$) indicating the i-th query.

Output

For each query output one line containing one integer indicating the answer modulo $10^9 + 7$.

XXII Open Cup named after E.V. Pankratiev Stage 9: Grand Prix of Nanjing, Division 2, Sunday, December 12, 2021

standard input	standard output
3 1 1	1
8 1 6	
2 3 2	
2 2 0 0	
4 3 3	180
2 3 2 2	825
1 1 6	8
1 3 3	
1 3 6	
2 2 2 3	
1 4 1 3	
4 4 2 3	

Problem G. Paimon's Tree

Input file: standard input
Output file: standard output

Time limit: 4 seconds
Memory limit: 256 megabytes

Paimon has found a tree with (n + 1) initially white vertices in her left pocket and decides to play with it. A tree with (n + 1) nodes is an undirected connected graph with n edges.

Paimon will give you an integer sequence a_1, a_2, \dots, a_n of length n. We first need to select a vertex in the tree and paint it black. Then we perform the following operation n times.

During the *i*-th operation, we select a white vertex x_i which is directly connected with a black vertex y_i by an edge, set the weight of that edge to a_i and also paint x_i in black. After these n operations we get a tree whose edges are all weighted.

What's the maximum length of the diameter of the weighted tree if we select the vertices optimally? The diameter of a weighted tree is the longest simple path in that tree. The length of a simple path is the sum of the weights of all edges in that path.

Input

There are multiple test cases. The first line of the input contains an integer T ($1 \le T \le 5 \times 10^3$) indicating the number of test cases. For each test case:

The first line contains an integer n ($1 \le n \le 150$) indicating the length of the sequence.

The second line contains n integers a_1, a_2, \dots, a_n $(1 \le a_i \le 10^9)$ indicating the sequence.

For the following n lines, the i-th line contains two integers u_i and v_i $(1 \le u_i, v_i \le n+1)$ indicating that there is an edge connecting vertex u_i and v_i in the tree.

It's guaranteed that there is at most 10 test cases satisfying n > 20.

Output

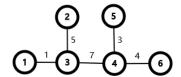
For each test case output one line containing one integer indicating the maximum length of the diameter of the tree.

Example

standard input	standard output
2	16
5	100000000
1 7 3 5 4	
1 3	
2 3	
3 4	
4 5	
4 6	
1	
100000000	
1 2	

Note

For the first sample test case, we select the vertices in the order of 1, 3, 4, 5, 2, 6, resulting in the weighted tree of the following image. It's obvious that the longest simple path is of length 16.



Problem H. Crystalfly

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 256 megabytes

Paimon is catching crystalflies on a tree, which are a special kind of butterflies in Teyvat. A tree is a connected graph consisting of n vertices and (n-1) undirected edges.



Pixiv ID: 93964680

There are initially a_i crystalflies on the *i*-th vertex. When Paimon reaches a vertex, she can catch all the remaining crystalflies on the vertex immediately. However, the crystalflies are timid. When Paimon reaches a vertex, all the crystalflies on the adjacent vertices will be disturbed. For the *i*-th vertex, if the crystalflies on the vertex are disturbed for the first time at the beginning of the t'-th second, they will disappear at the end of the $(t' + t_i)$ -th second.

At the beginning of the 0-th second, Paimon reaches vertex 1 and stays there before the beginning of the 1-st second. Then at the beginning of each following second, she can choose one of the two operations:

- Move to one of the adjacent vertices of her current vertex and stay there before the beginning of the next second (if the crystalflies in the destination will disappear at the end of that second she can still catch them).
- Stay still in her current vertex before the beginning of the next second.

Input

There are multiple test cases. The first line of the input contains an integer T indicating the number of test cases. For each test case:

The first line contains an integer n $(1 \le n \le 10^5)$ indicating the number of vertices.

The second line contains n integers a_1, a_2, \dots, a_n $(1 \le a_i \le 10^9)$ where a_i is the number of crystalflies on the i-th vertex.

The third line contains n integers t_1, t_2, \dots, t_n $(1 \le t_i \le 3)$ where t_i is the time before the crystalflies on the i-th vertex disappear after disturbed.

For the next (n-1) lines, the *i*-th line contains two integers u_i and v_i $(1 \le u_i, v_i \le n)$ indicating an edge connecting vertices u_i and v_i in the tree.

It's guaranteed that the sum of n of all the test cases will not exceed 10^6 .

Output

For each test case output one line containing one integer indicating the maximum number of crystalflies Paimon can catch.

Example

standard input	standard output
2	10101
5	10111
1 10 100 1000 10000	
1 2 1 1 1	
1 2	
1 3	
2 4	
2 5	
5	
1 10 100 1000 10000	
1 3 1 1 1	
1 2	
1 3	
2 4	
2 5	

Note

For the first sample test case, follow the strategy below.

- During the 0-th second
 - Paimon arrives at vertex 1;
 - Paimon catches 1 crystalfly;
 - Crystalflies in vertices 2 and 3 are disturbed.
- During the 1-st second
 - Paimon arrives at vertex 3;
 - Paimon catches 100 crystalflies.
- During the 2-nd second
 - Paimon arrives at vertex 1;
 - Crystalflies in vertex 2 disappears.
- During the 3-rd second
 - Paimon arrives at vertex 2;
 - Crystalflies in vertices 4 and 5 are disturbed.
- During the 4-th second
 - Paimon arrives at vertex 5;
 - Paimon catches 10000 crystalflies;
 - Crystalflies in vertex 4 disappears.

XXII Open Cup named after E.V. Pankratiev Stage 9: Grand Prix of Nanjing, Division 2, Sunday, December 12, 2021

For the second sample test case, the optimal strategy is the same with the first sample test case. Crystalflies in vertex 2 are scheduled to disappear at the end of the 3-rd (instead of the 2-nd) second, allowing Paimon to catch them.

Problem I. Cloud Retainer's Game

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 256 megabytes

Cloud Retainer, the builder of the Dwelling in the clouds above Qingyun Peak, is very interested in mechanics. Although there is more than one month away from the Lantern Rite Festival in Liyue, she has already started the design of a gaming event for it.



Cloud Retainer and the Traveler

The game is mainly about releasing pinballs to get a score as high as possible. It is played on the 2-dimensional plane with two horizontal straight lines y = 0 and y = H. Between the two lines, there are n tiny wooden boards and m coins, both can be regarded as single points. The i-th wooden board is located at (x_i, y_i) while the i-th coin is located at (x_i', y_i') .

A pinball is released from $(10^{-9}, 10^{-9})$ by the player. Let $\overrightarrow{v} = (v_x, v_y)$ be the velocity of the ball (that is to say, if the ball is currently located at (x, y) it will move to $(x + v_x \epsilon, y + v_y \epsilon)$ after ϵ seconds). Initially $\overrightarrow{v} = (1, 1)$.

When the ball hits a wooden board or one of the two horizontal straight lines, v_y will be negated (that is, v_y becomes $-v_y$) while v_x remains unchanged. If the ball hits a coin, the player's score is increased by 1 and the velocity of the ball remains unchanged.

Input

There are multiple test cases. The first line of the input contains an integer T indicating the number of test cases. For each test case:

The first line contains one integer H $(2 \le H \le 10^9)$.

The second line contains one integer n ($1 \le n \le 10^5$) indicating the number of wooden boards.

For the following n lines, the i-th line contains two integers x_i and y_i $(1 \le x_i \le 10^9, 1 \le y_i < H)$ indicating a wooden board located at (x_i, y_i) .

The following line contains one integer m $(1 \le m \le 10^5)$ indicating the number of coins.

For the following m lines, the i-th line contains two integers x_i' and y_i' $(1 \le x_i' \le 10^9, 1 \le y_i' < H)$ indicating a coin located at (x_i', y_i') .

It's guaranteed that the given (n+m) points in the same test case will be distinct. It's also guaranteed that neither the sum of n nor the sum of m of all test cases will exceed 5×10^5 .

Output

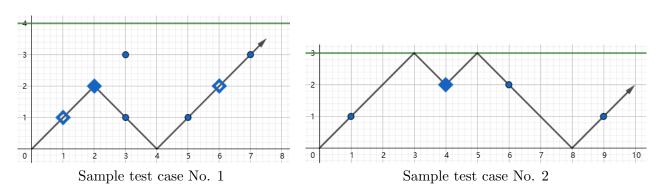
For each test case output one line containing one integer indicating the maximum score the player can get after removing some (or not removing any) wooden boards.

Example

standard input	standard output
2	3
4	3
3	
1 1	
2 2	
6 2	
4	
3 1	
3 3	
5 1	
7 3	
3	
1	
4 2	
3	
1 1	
6 2	
9 1	

Note

The two sample test cases are shown below. Solid diamonds represent the remaining wooden boards, while hollow diamonds represent the removed wooden boards and round dots represent the coins.



Problem J. Xingqiu's Joke

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 256 megabytes

Once again, Xingqiu hides Chongyun's ice cream into a box with a strange lock. Liyue's summer has been always very hot and Chongyun suffers more because of his excessive yang (positive) energy, so he needs that ice cream desperately.



Pixiv ID: 86787400

There are two integers a and b on the lock. Chongyun can perform the following three types of operations any number of times:

- Minus 1 from both a and b;
- Plus 1 to both a and b;
- Divide both a and b by one of their common **prime** factor (that is to say, divide them by a **prime** g where a and b are both divisible by g).

The box will be unlocked if either a or b or both become 1. To help Chongyun gets the ice cream back as quickly as possible, please tell him the minimum number of operations needed to unlock the box.

Input

There are multiple test cases. The first line of the input contains an integer T ($1 \le T \le 300$) indicating the number of test cases. For each test case:

The first and only line contains two integers a and b $(1 \le a, b \le 10^9, a \ne b)$.

Output

For each test case output one line containing one integer indicating the minimum number of operations to make a or b or both equal 1.

Example

standard input	standard output
5	2
4 7	7
9 8	5
32 84	4
11 35	0
2 1	

Note

For the first sample test case, the optimal way is $(4,7) \rightarrow (3,6) \rightarrow (1,2)$.

For the second sample test case, the optimal way is to apply the first type of operation 7 times.

For the third sample test case, the optimal way is $(32,84) \rightarrow (16,42) \rightarrow (15,41) \rightarrow (14,40) \rightarrow (13,39) \rightarrow (1,3)$.

For the fourth sample test case, the optimal way is $(11,35) \rightarrow (12,36) \rightarrow (6,18) \rightarrow (2,6) \rightarrow (1,3)$.

Problem M. Windblume Festival

Input file: standard input
Output file: standard output

Time limit: 3 seconds Memory limit: 256 megabytes

The Windblume Festival in Mondstadt is coming! People are preparing windblumes for Barbatos and for those they love and adore. The Windblume Festival is also an opportunity to improve the relationships people have.



Source: Genshin Impact Official

During the festival, a famous game will be played every year, invented by Jean, the Acting Grand Master of the Knights of Favonius. In the game, n players numbered from 1 to n stand in a circle, each holding an integer with them. Each turn, one player will be removed. The game will end when there is only one player left.

For each turn, let k be the number of players remaining and a_i be the integer player i holds. Two adjacent players, x and $(x \mod k + 1)$ are selected and player $(x \mod k + 1)$ is removed from the game. Player x's integer will then change from a_x to $(a_x - a_{x \mod k + 1})$. Player y in this turn will become player (y - 1) in the next turn for all $x < y \le k$, though the integer they hold will not change.

Jean wants to know the maximum possible integer held by the last remaining player in the game by selecting the players in each round optimally.

Input

There are multiple test cases. The first line of the input contains one integer T indicating the number of test cases. For each test case:

The first line contains one integer n $(1 \le n \le 10^6)$ indicating the initial number of players.

The next line contains n integers a_i ($-10^9 \le a_i \le 10^9$) where a_i is the integer held by player i at the beginning.

It is guaranteed that the sum of n of all test cases will not exceed 10^6 .

Output

For each test case output one line containing one integer indicating the maximum possible integer.

Example

standard input	standard output
5	10
4	713
1 -3 2 -4	746
11	779
91 66 73 71 32 83 72 79 84 33 93	0
12	
91 66 73 71 32 83 72 79 84 33 33 93	
13	
91 66 73 71 32 83 72 79 84 33 33 33 93	
1	
0	

Note

For the first sample test case follow the strategy shown below, where the underlined integers are the integers held by the players selected in each turn.

$$\{\underline{1}, -3, 2, \underline{-4}\} \text{ (select } x=4) \to \{-3, 2, -5\} \text{ (select } x=2) \to \{-3, 7\} \text{ (select } x=2) \to \{10\}.$$

Problem N. Another Last Digit

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 256 mebibytes

Given positive integer N. Find the last digit of the product of first N integers of type $2^{2_i^p} + 1$, where p_i is *i*-th prime number.

Input

The first line of the input contains one integer N ($1 \le N \le 10^{18}$).

Output

Print one decimal digit — the answer to the problem.

standard input	standard output
1	5

Problem O. Byteland Names

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 256 mebibytes

In ancient Byteland language, the words are composed from lowercase Latin letters. As the names are used the words with following properties: let the word consists of n letters. Then exists $1 \le x < n$, such as all substrings of the length x are equal.

In the list of names found by archeologists, the names are ordered by its length, and names of the same length are ordered lexicographically. Your task is to find the length of the k-th name in the word and print its **last** letter.

Input

The input contains one integer k $(1 \le k \le 10^{18})$ — the number of the name in the list.

Output

Print the integer — the length of the k-th name, then print the space and one character — the last letter of that name.

standard input	standard output
1	2 a
2021	79 s

Problem P. Dense Polynomials

Input file: standard input
Output file: standard output

Time limit: 2 seconds Memory limit: 256 mebibytes

We will consider the polinomial of n-th degree with integer coefficients

$$x^{n} + a_{1} \cdot x^{n-1} + \ldots + a_{n-1} \cdot x + a_{n}$$

dense, if this polynomial have exactly n pairwise distinct **integer non-zero** roots, and absolute value $|a_n|$ is minimal possible.

Your task is to find the maximal and minimal value of a_1 in the dense polynomial.

Input

The input contains one integer n $(1 \le n \le 10^{18})$ — the degree of the polynomial.

Output

Print two pairwise distinct integer — the minimal and the maximal value of a_1 in that polynomial.

standard input	standard output
1	-1 1

Problem Q. Emptycoin

Input file: standard input
Output file: standard output

Time limit: 2 seconds
Memory limit: 256 mebibytes

To estimate the stability of new cryptocurrencty Emptycoin, the analysts are using the data on the houry change of the price d_i of the Emptycoin. There are n observations.

Consider as the *stability distance* the length of the maximum continuous segment, such as sum of d_i on that segment is zero, i.e the maximum integer k such as exists the index j: $\sum_{i=0}^{k-1} d_{j+i} = 0$. If the sum is non-zero for all k and j, then the stability distance is considered to be equal to zero.

Given the data, calculate the stability distance.

Input

First line of the input contains one integer n – the number of the observations $(1 \le n \le 2 \cdot 10^5)$. i-th of the following n lines contains one integer d_i $(-10^9 \le d_i \le 10^9)$ — i-th change of the price.

Output

Print one integer — the stability distance.

standard input	standard output
5	4
28 -11	
-11	
11	
0	
0	
4	0
1	
2	
3	
4	