

PR Project-1

– Report –

submitted by

Group 18 - M.Navyasri,P.Sruti,Y.Vishnu sreya
S20180020222, S20180020233, S20180020262

November 1, 2020

1 Introduction

The main objective of this project is to perform classification on Given data

Qns-1 : Non-linear transformation is used to convert multi-dimensional feature data into one-dimensional data using a suitable distance metric so that we can use a simple linear regression model to fit the data

Qns-2 : In Direct non-linear classification, we can fit multi-dimensional data into a classification model without even changing the data into one-dimensional data

2 problem Description

2.1 Qns1

Given the following parameters we had to generate a 2D Data set consisting of 2 classes

For class 1 : given co-variance matrix = $\begin{bmatrix} 15 & 0 \\ 0 & 1 \end{bmatrix}$

For class 2 : given co-variance matrix = $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

We have to transform the data into 1D feature data and build a suitable model to predict the classes of data.

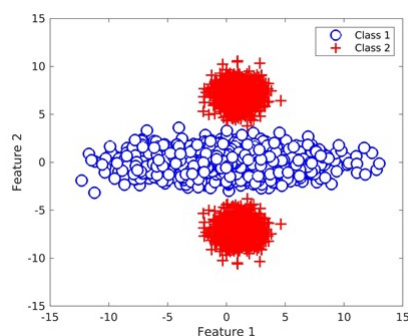
2.2 Qns2

Given the following parameters we had to generate a 2D Data set consisting of 2 classes

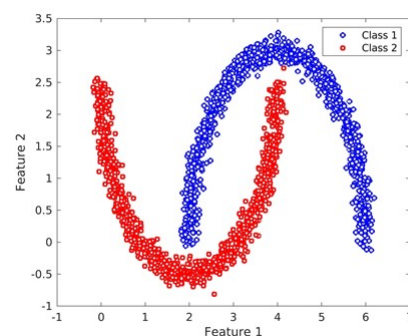
For class 1 : co-variance matrix = 0.1 ,mean vector = $[h1 + acost, bsint]^T$

For class 2 : mean vector = $[h2 + acost, k bsint]^T$ and co-variance vector = 0.1

The data is fitted in linear discriminant, Quadratic discriminant, SVM with Gaussian kernel, SVM with polynomial kernel , KNN classifier



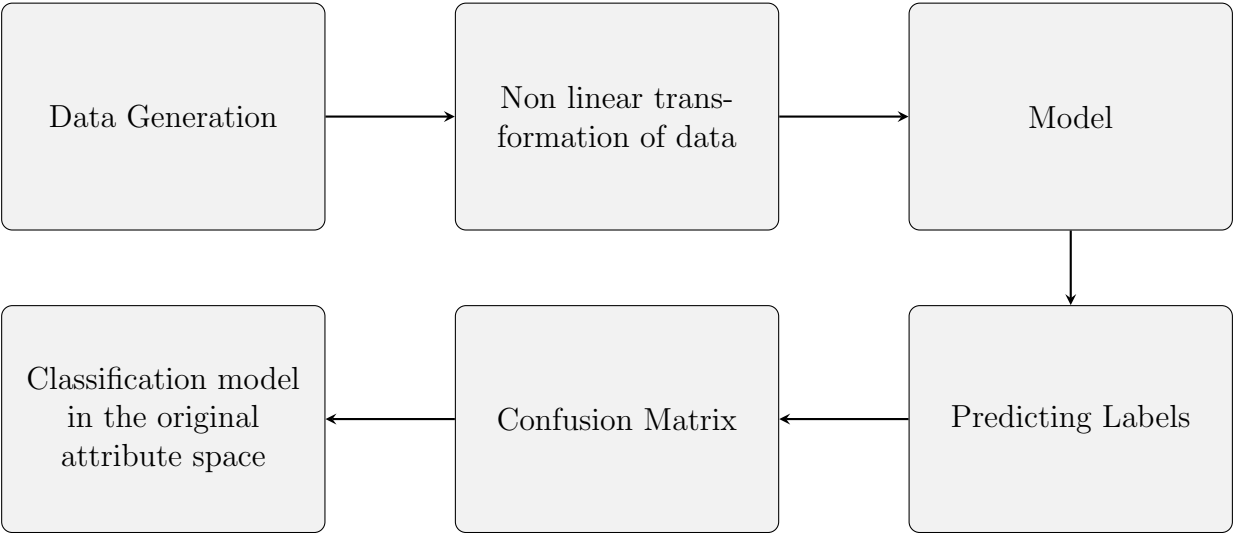
Divider Patterns - Question-1.



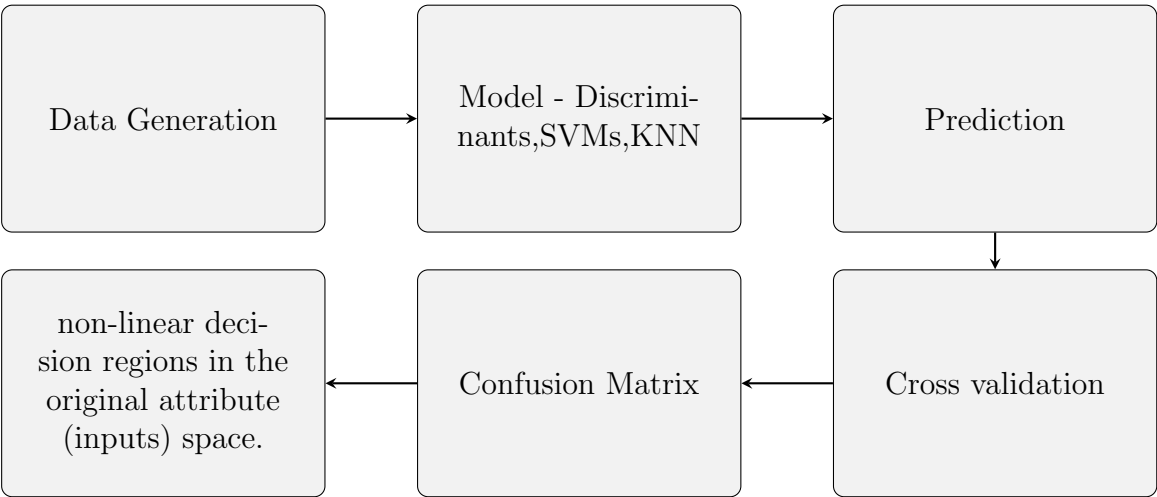
Interlocking Sinusoids - Question-2.

3 Methodology

3.1 Qns1

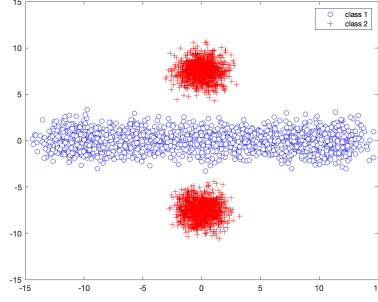


3.2 Qns2

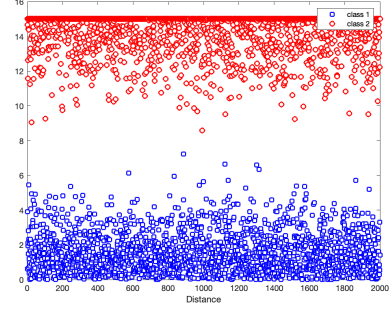


4 Implementation and Results

4.1 Qns1



Initial data generation.



data after non-linear transform

- The non linear transform is,

$$lx1 = \sum |x - [0, 7.5]| \quad (1)$$

$$lx2 = \sum |(x - [0, -7.5]| \quad (2)$$

$$lx = |lx2 - lx1| \quad (3)$$

$$ly1 = \sum |(y - [0, 7.5]| \quad (4)$$

$$ly2 = \sum |(y - [0, -7.5]| \quad (5)$$

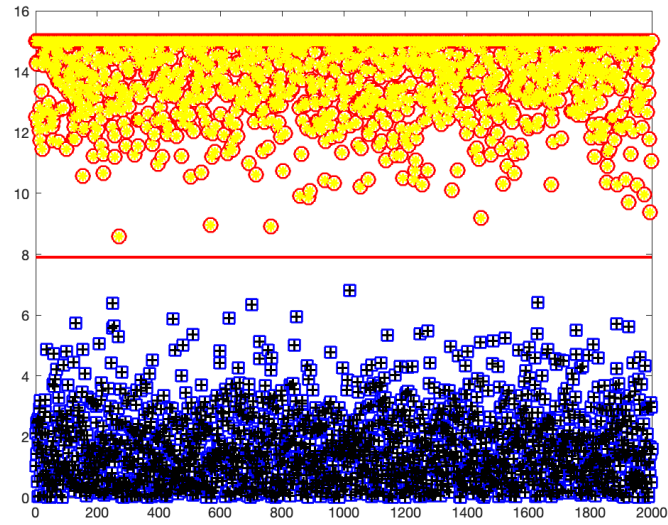
$$ly = |ly1 - ly2| \quad (6)$$

- Classes of the new transformed model are predicted using Least squares linear regression.

- Confusion Matrix and accuracy:

$$\begin{bmatrix} 1999 & 1 \\ 0 & 2000 \end{bmatrix}$$

accuracy=99.98

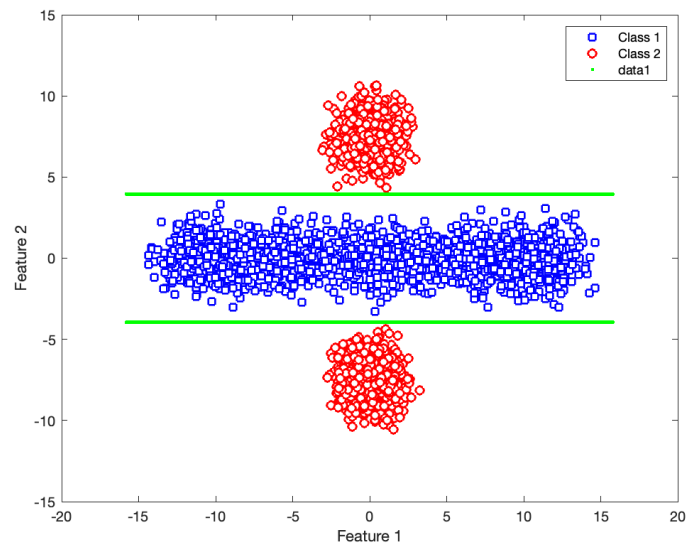


Predicted Classes.

- Plotting in Original Feature Space

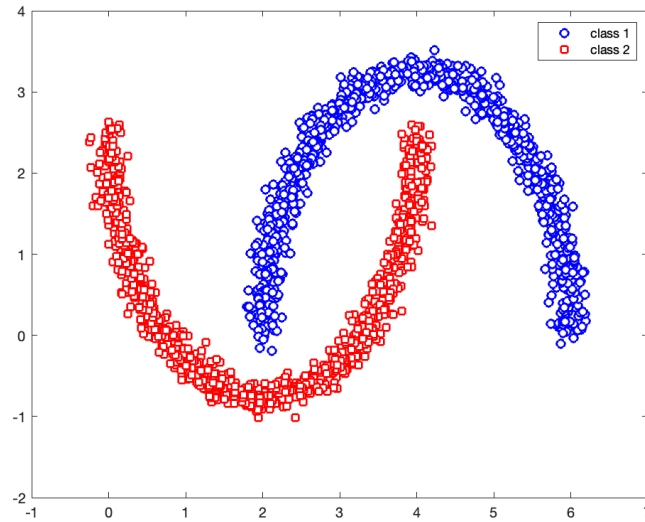
$$||z1| + |z2 - 7.5| - (|z1| + |z2 + 7.5|)| = thr \quad (7)$$

$$Z2 = +/- (thr/2) \quad (8)$$



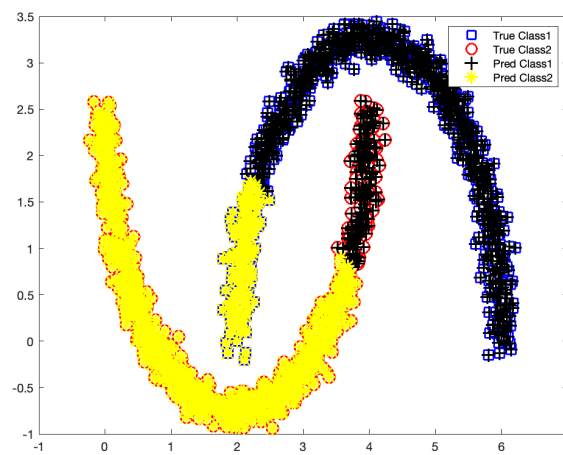
Predicted Classes.

4.2 Qns2

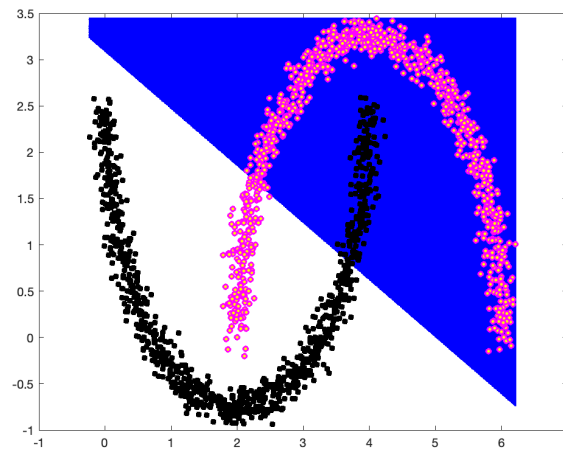


Initial data generation.

4.2.1 linear discriminant kernel

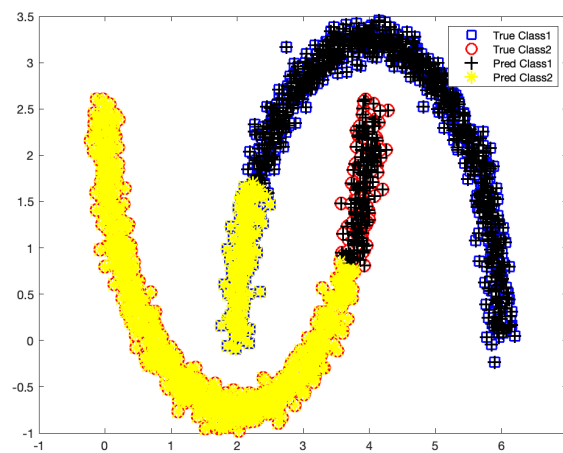


Predicted classes for Linear Discriminant.

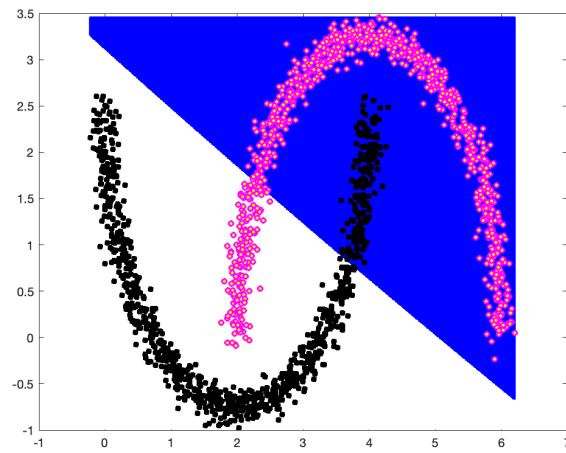


Non-linear Decision region.

4.2.2 Quadratic discriminant kernel

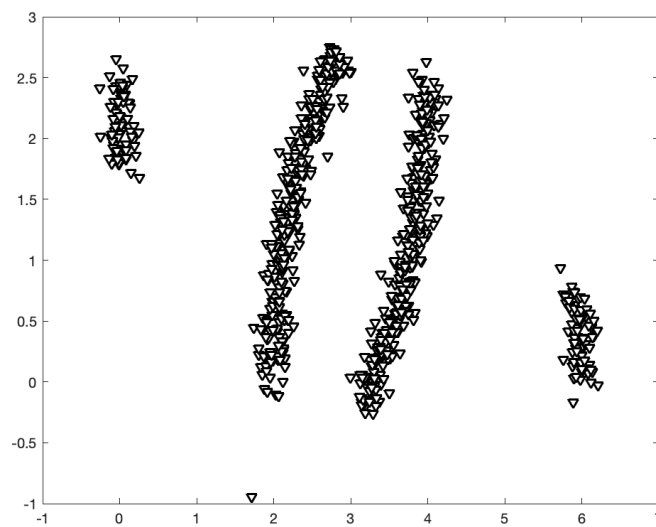


Predicted classes for Quadratic Discriminant kernel

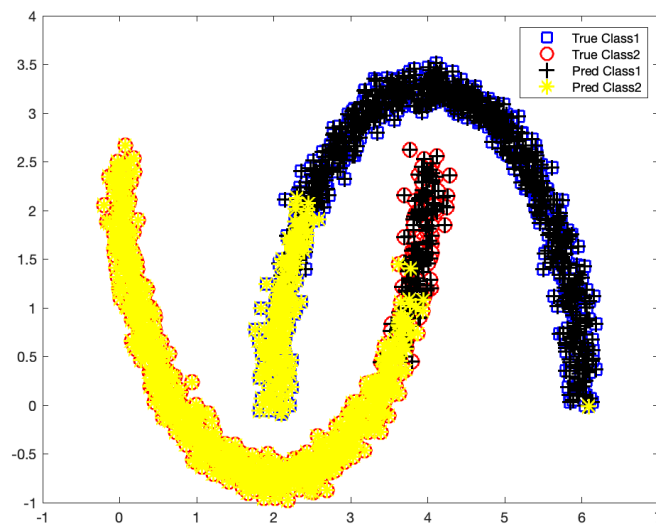


Non-linear decision region.

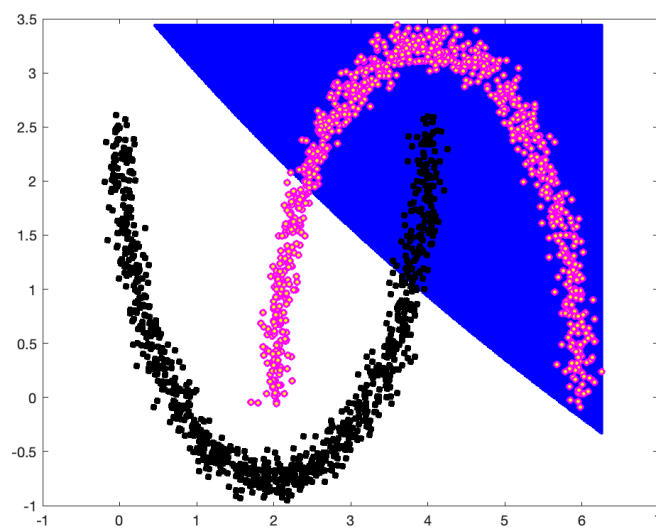
4.2.3 SVM with Polynomial (Quadratic) Kernel



support vectors for Quadratic kernel

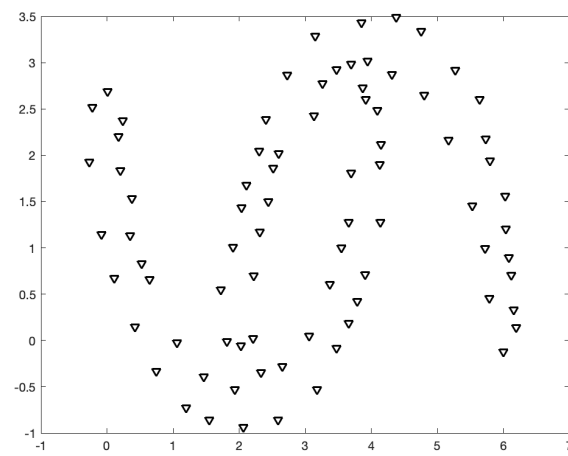


Predicted Classes for Quadratic kernel.

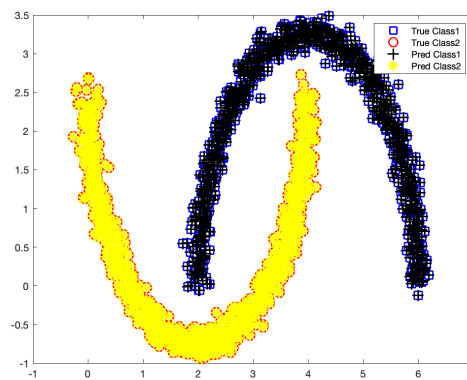


Non-linear Decision space.

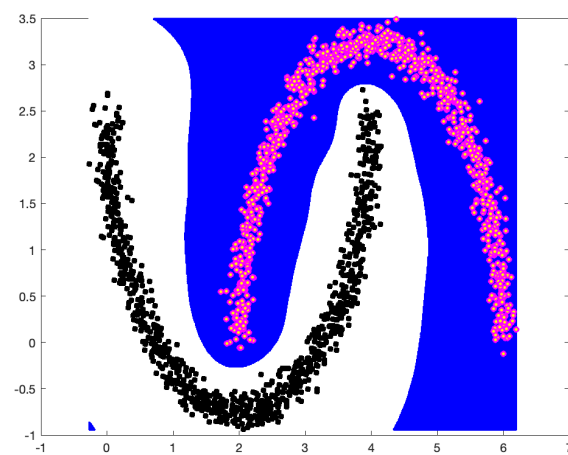
4.2.4 SVM with a Gaussian Kernel



support vectors for Gaussian(fine) kernel.

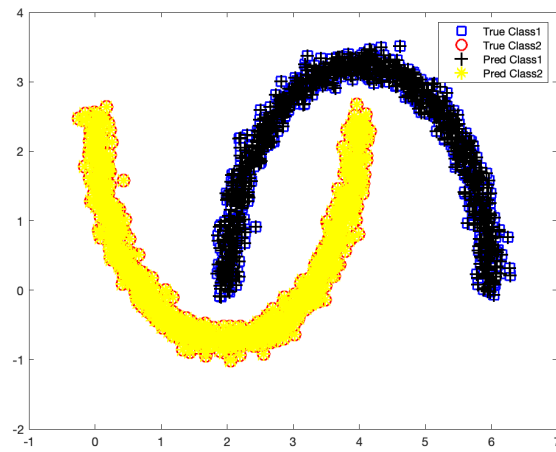


predicted classes for Gaussian(fine) kernel.

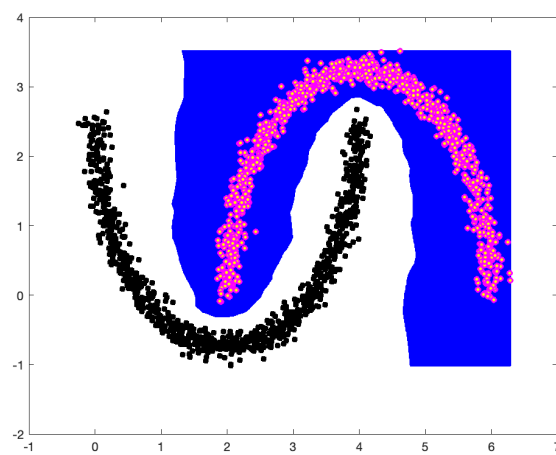


Non-Linear decision region.

4.2.5 K-nearest Neighbour kernel



Predicted classes for K-Nearest Neighbours.



Non-linear Decision Region.

5 Analysis

5.1 Qns2

Here is the Model accuracy analysis of the above 5 Models,

classification Model	Confusion Matrix	Accuracy(%)
Linear Discriminant	$\begin{bmatrix} 828 & 172 \\ 183 & 817 \end{bmatrix}$	82.25
Quadratic Discriminant	$\begin{bmatrix} 828 & 172 \\ 174 & 826 \end{bmatrix}$	82.7
SVM-Gaussian(fine)	$\begin{bmatrix} 1000 & 0 \\ 0 & 1000 \end{bmatrix}$	100
SVM-Quadratic	$\begin{bmatrix} 819 & 181 \\ 185 & 815 \end{bmatrix}$	81.7
K-Nearest neighbours	$\begin{bmatrix} 1000 & 0 \\ 0 & 1000 \end{bmatrix}$	100

From the above table we can observe that SVM with Gaussian kernel and K-Nearest neighbours gives you the best accuracy of 100 that is model classifies the data into 2 classes with 100percent accuracy

If we keep the best model for data with given parameters, the order would be like

1. SVM-Gaussian - 100
2. K-Nearest neighbours - 100
3. Quadratic discriminant - 82.7
4. Linear discriminant - 82.25
5. SVM-Quadratic - 81.7

6 MATLAB CODES

6.1 Qns 1

6.1.1 Data Generation

```

1 clear;
2 clc;
3 close all;
4 N = 2000;
5 h = 0;k = 0;a=12;b = 0;r = 2.5;
6 th = (1:N)*2*pi/N;
7 th = th(:);
8 xunit = h + a*cos(th);
9 yunit = k + b*sin(th);
10 plot(xunit,yunit);
11 figure;
12 %class 1
13 %mu1 is [h+a*cos(th),k+b*sin(th)]
14 sigma1 = [15 0;0 1];
15 x = [randn(N,1)+h+a*cos(th),randn(N,1)+k+b*sin(th)];
16 plot(x(:,1),x(:,2),'bo','MarkerFaceColor','w');
17 hold on;
18 %class 2
19 %mu2 is [0,+/-7.5]
20 sigma2 = [1 0;0 1];
21 y1 = [0 + randn(N/2,1),7.5 + randn(N/2,1)];
22 y2 = [0 + randn(N/2,1),-7.5 + randn(N/2,1)];
23 y = [y1;y2];
24 plot(y(:,1),y(:,2),'r+','MarkerFaceColor','w');
25 legend('class 1','class 2');
26 %nonlinear transformation
27 lx1 = (sum(abs(x-[0,7.5]))');
28 lx2 = (sum(abs(x-[0,-7.5]))');
29 lx = abs(lx2 - lx1);
30 ly1 = (sum(abs(y-[0,7.5]))');
31 ly2 = (sum(abs(y-[0,-7.5]))');

```

```

32 ly = abs(ly1 - ly2);
33 figure;
34 plot(lx, 'bs', 'LineWidth', 1.5, 'MarkerFaceColor', 'W');
35 hold on;
36 plot(ly, 'ro', 'LineWidth', 1.5, 'MarkerFaceColor', 'W');
37 hold on;
38 xlabel('Distance');
39 legend('class 1', 'class 2');

```

6.1.2 Model Training and Predicting Labels

```

1 %model
2 Z1(1:2:2*N-1,:) = x;
3 Z1(2:2:2*N,:) = y;
4 TestTarg1(1:2:2*N-1) = 1;
5 TestTarg1(2:2:2*N) = -1;
6 vx = var(x);
7 vy = var(y);
8 T = TestTarg1;
9 %PhiZ1 = (sum(abs(Z1-[0,7.5])));
10 %PhiZ2 = (sum(abs(Z1-[0,-7.5])));
11 %PhiZ = abs(PhiZ1 - PhiZ2);
12 PhiZ = [lx;ly];
13 Xmat = [ones(size(Z1,1),1) PhiZ(:)];
14 W_ls = regress(T(:),Xmat);
15 Y_x = Xmat*W_ls;
16 thr = -W_ls(1)/W_ls(2);
17
18 %predicting labels
19 pred_labels = ones(size(T));
20 pred_labels(Y_x < 0) = 2;
21 T(T == -1) = 2;
22 figure;
23 plot(lx, 'bs', 'LineWidth', 1.5, 'MarkerSize', 10, '
    MarkerFaceColor', 'w');
24 hold on;

```

```

25 plot(ly, 'ro', 'LineWidth', 1.5, 'MarkerSize', 10, '
    MarkerFaceColor', 'w');
26 plot(PhiZ(pred_labels == 1), 'k+', 'LineWidth', 1.5, '
    MarkerFaceColor', 'w');
27 plot(PhiZ(pred_labels == 2), 'y*', 'LineWidth', 1.5, '
    MarkerFaceColor', 'w');
28 plot(thr*ones(N), 'r', 'LineWidth', 2);
29 hold off;
30
31 %Confusion matrix
32 ConfMat = confusionmat(T, pred_labels);
33 disp(ConfMat);
34 acc = sum(diag(ConfMat))/sum(sum(ConfMat));
35 disp(acc);

```

6.1.3 Plotting the decision boundaries in original attribute Space

```

1 % phiz1 = |z1-0| + |z2-7.5| , phiz2 = |z1-0| + |z2-(-7.5)|
2 % phiz = |phiz1 - phiz2| = ||z2 - 7.5| - |z2 + 7.5|| = thr
3 %by solving ||z2 - 7.5| - |z2 + 7.5|| = thr ,we get z2 = +/-
    thr/2
4 %so here z1 can be anything from the given equation since it
    is not there
5 %in the euation
6 mu = mean(Z1);
7 %z1vec = min(min([x(1,:), y(1,:)])) : 0.01 : max(max([x(1,:), y
    (1,:)]));
8 z1vec = -2*thr : 0.01 : 2*thr;
9 ix = 1;
10 for zx = 1:length(z1vec)
11     z1 = z1vec(zx);
12     z2 = thr/2;
13     model(ix,:) = [z1, z2];
14     ix = ix + 1;
15     z2 = -thr/2;
16     model(ix,:) = [z1, z2];
17     ix = ix+1;

```

```

18 end
19 figure;
20 plot(x(:,1),x(:,2),'bs',y(:,1),y(:,2),'ro','LineWidth',1.5,'
    MarkerFaceColor','w');
21 xlabel('Feature 1');
22 ylabel('Feature 2');
23 legend('Class 1','Class 2');
24 hold on;
25 plot(model(:,1),model(:,2),'g.','LineWidth',2);

```

6.2 Qns 2

6.2.1 Generating and plotting data

```

1 clear
2 clc
3 close all
4 N = 1000;
5 h1 = 4;k = 2.5;a=2;b = 3.25;h2 = 2;
6 th = (1:N)*pi/N;
7 th = th(:);
8 xunit = h1 + a*cos(th);
9 yunit = b*sin(th);
10 plot(xunit,yunit);
11 hold on;
12 xunit = h2 + a*cos(th);
13 yunit = k-b*sin(th);
14 plot(xunit,yunit);
15 figure;
16 %class 1
17 x = [0.1*randn(N,1)+h1+a*cos(th),0.1*randn(N,1)+b*sin(th)];
18 plot(x(:,1),x(:,2),'bo','LineWidth',1.5,'MarkerFaceColor','w
    ');
19 hold on;
20 %class 2
21 y = [0.1*randn(N,1)+h2+a*cos(th),0.1*randn(N,1)+k-b*sin(th)
    ];

```



```

22 plot(y(:,1),y(:,2), 'rs', 'LineWidth', 1.5, 'MarkerFaceColor', 'w
    ');
23 legend('class 1', 'class 2');
24
25 t1 = ones(N,1);
26 t2 = -ones(N,1);
27 T = [t1;t2];
28 rin=randperm(length(T));
29 T=T(rin);
30 one_vec = ones(2*N,1);
31 xmat1 = [x;y];
32 xmat = xmat1(rin,:);
33 X = xmat;
34
35 trainingData = [X T];
36
37 predictors = trainingData(:,1:end-1);
38 response = trainingData(:,end);

```

6.2.2 Linear Discriminant Model

```

1 inputTable = array2table(trainingData, 'VariableNames', {'
    column_1', 'column_2', 'column_3'});
2
3 predictorNames = {'column_1', 'column_2'};
4 predictors = inputTable(:, predictorNames);
5 response = inputTable.column_3;
6 isCategoricalPredictor = [false, false];
7 % Train a classifier
8 classificationDiscriminant = fitcdiscr(...
9     predictors, ...
10    response, ...
11    'DiscrimType', 'linear', ...
12    'Gamma', 0, ...
13    'FillCoeffs', 'off', ...
14    'ClassNames', [-1; 1]);
15

```

```

16 % Create the result struct with predict function
17 predictorExtractionFcn = @(x) array2table(x, 'VariableNames'
    , predictorNames);
18 discriminantPredictFcn = @(x) predict(
    classificationDiscriminant, x);
19 trainedClassifier.predictFcn = @(x) discriminantPredictFcn(
    predictorExtractionFcn(x));
20 % Add additional fields to the result struct
21 trainedClassifier.ClassificationDiscriminant =
    classificationDiscriminant;
22 %model
23 inputTable = array2table(trainingData, 'VariableNames', {'
    column_1', 'column_2', 'column_3'});
24
25 predictorNames = {'column_1', 'column_2'};
26 predictors = inputTable(:, predictorNames);
27 response = inputTable.column_3;
28 isCategoricalPredictor = [false, false];
29 % Perform cross-validation
30 partitionedModel = crossval(trainedClassifier.
    ClassificationDiscriminant, 'Kfold', 5);
31 % Compute validation predictions
32 [validationPredictions, validationScores] = kfoldPredict(
    partitionedModel);
33 % Compute validation accuracy
34 validationAccuracy = 1 - kfoldLoss(partitionedModel, '
    LossFun', 'ClassifError');

```

6.2.3 Quadratic Discriminant Model

```

1 inputTable = array2table(trainingData, 'VariableNames', {'
    column_1', 'column_2', 'column_3'});
2
3 predictorNames = {'column_1', 'column_2'};
4 predictors = inputTable(:, predictorNames);
5 response = inputTable.column_3;
6 isCategoricalPredictor = [false, false];

```

```

7
8 % Train a classifier
9 % This code specifies all the classifier options and trains
   the classifier.
10 classificationDiscriminant = fitcdiscr(...
11     predictors , ...
12     response , ...
13     'DiscrimType' , 'quadratic' , ...
14     'FillCoeffs' , 'off' , ...
15     'ClassNames' , [-1; 1]);
16
17 % Create the result struct with predict function
18 predictorExtractionFcn = @(x) array2table(x, 'VariableNames'
   , predictorNames);
19 discriminantPredictFcn = @(x) predict(
   classificationDiscriminant , x);
20 trainedClassifier.predictFcn = @(x) discriminantPredictFcn(
   predictorExtractionFcn(x));
21
22 % Add additional fields to the result struct
23 trainedClassifier.ClassificationDiscriminant =
   classificationDiscriminant;
24 % Convert input to table
25 inputTable = array2table(trainingData , 'VariableNames' , {'
   column_1' , 'column_2' , 'column_3'});
26 predictorNames = {'column_1' , 'column_2'};
27 predictors = inputTable(:, predictorNames);
28 response = inputTable.column_3;
29 isCategoricalPredictor = [false , false];
30 % Perform cross-validation
31 partitionedModel = crossval(trainedClassifier.
   ClassificationDiscriminant , 'KFold' , 5);
32 % Compute validation predictions
33 [validationPredictions , validationScores] = kfoldPredict(
   partitionedModel);
34 % Compute validation accuracy

```

```

35 validationAccuracy = 1 - kfoldLoss(partitionedModel, '
    LossFun', 'ClassifError');

```

6.2.4 Support Vector Machines with Gaussian Kernel

```

1 %SVM with gaussian kernel
2 classificationSVM = fitcsvm(...
3     predictors, ...
4     response, ...
5     'KernelFunction', 'gaussian', ...
6     'PolynomialOrder', [], ...
7     'KernelScale', 0.35, ...
8     'BoxConstraint', 1, ...
9     'Standardize', true, ...
10    'ClassNames', [-1; 1]);
11
12 % Create the result struct with predict function
13 predictorExtractionFcn = @(x) array2table(x, 'VariableNames'
    , predictorNames);
14 svmPredictFcn = @(x) predict(classificationSVM, x);
15 trainedClassifier.predictFcn = @(x) svmPredictFcn(
    predictorExtractionFcn(x));
16
17 % Add additional fields to the result struct
18 trainedClassifier.ClassificationSVM = classificationSVM;
19
20 % model.
21 inputTable = array2table(trainingData, 'VariableNames', {'
    column_1', 'column_2', 'column_3'});
22
23 predictorNames = {'column_1', 'column_2'};
24 predictors = inputTable(:, predictorNames);
25 response = inputTable.column_3;
26 isCategoricalPredictor = [false, false];
27
28 % Perform cross-validation

```

```

29 partitionedModel = crossval(trainedClassifier.
    ClassificationSVM, 'KFold', 10);
30
31 % Compute validation predictions
32 [validationPredictions, validationScores] = kfoldPredict(
    partitionedModel);
33
34 % Compute validation accuracy
35 validationAccuracy = 1 - kfoldLoss(partitionedModel, '
    LossFun', 'ClassifError');

```

6.2.5 SVM with Polynomial Kernel

```

1 %SVM with polynomial kernal of degree 1
2 classificationSVM = fitsvm(...
3     predictors, ...
4     response, ...
5     'KernelFunction', 'linear', ...
6     'PolynomialOrder', [], ...
7     'KernelScale', 'auto', ...
8     'BoxConstraint', 1, ...
9     'Standardize', true, ...
10    'ClassNames', [-1; 1]);
11
12 % Create the result struct with predict function
13 predictorExtractionFcn = @(x) array2table(x, 'VariableNames'
    , predictorNames);
14 svmPredictFcn = @(x) predict(classificationSVM, x);
15 trainedClassifier.predictFcn = @(x) svmPredictFcn(
    predictorExtractionFcn(x));
16
17 % Add additional fields to the result struct
18 trainedClassifier.ClassificationSVM = classificationSVM;
19
20 % model.
21 inputTable = array2table(trainingData, 'VariableNames', {'
    column_1', 'column_2', 'column_3'});

```

```

22
23 predictorNames = {'column_1', 'column_2'};
24 predictors = inputTable(:, predictorNames);
25 response = inputTable.column_3;
26 isCategoricalPredictor = [false, false];
27
28 % Perform cross-validation
29 partitionedModel = crossval(trainedClassifier.
    ClassificationSVM, 'KFold', 10);
30
31 % Compute validation predictions
32 [validationPredictions, validationScores] = kfoldPredict(
    partitionedModel);
33
34 % Compute validation accuracy
35 validationAccuracy = 1 - kfoldLoss(partitionedModel, '
    LossFun', 'ClassifError');

```

6.2.6 K-Nearest Neighbours

```

1 %Fine KNN
2 classificationKNN = fitcknn(...
3     predictors, ...
4     response, ...
5     'Distance', 'Euclidean', ...
6     'Exponent', [], ...
7     'NumNeighbors', 1, ...
8     'DistanceWeight', 'Equal', ...
9     'Standardize', true, ...
10    'ClassNames', [-1; 1]);
11
12 % Create the result struct with predict function
13 predictorExtractionFcn = @(x) array2table(x, 'VariableNames'
    , predictorNames);
14 knnPredictFcn = @(x) predict(classificationKNN, x);
15 trainedClassifier.predictFcn = @(x) knnPredictFcn(
    predictorExtractionFcn(x));

```

```

16 % Add additional fields to the result struct
17 trainedClassifier.ClassificationKNN = classificationKNN;
18 %model
19 inputTable = array2table(trainingData, 'VariableNames', {'
    column_1', 'column_2', 'column_3'});
20
21 predictorNames = {'column_1', 'column_2'};
22 predictors = inputTable(:, predictorNames);
23 response = inputTable.column_3;
24 isCategoricalPredictor = [false, false];
25
26 % Perform cross-validation
27 partitionedModel = crossval(trainedClassifier.
    ClassificationKNN, 'KFold', 10);
28
29 % Compute validation predictions
30 [validationPredictions, validationScores] = kfoldPredict(
    partitionedModel);
31
32 % Compute validation accuracy
33 validationAccuracy = 1 - kfoldLoss(partitionedModel, '
    LossFun', 'ClassifError');

```

6.2.7 Confusion Matrix and Accuracy

```

1 pred_labels(pred_labels == -1) = 2;
2 TestTarg = T;
3 TestTarg(T == -1) = 2;
4 %ConfMat = ConfusionMatrix2(pred_labels, TestTarg, 2);
5 ConfMat = confusionmat(TestTarg, pred_labels);
6 disp(ConfMat);
7 acc = sum(diag(ConfMat))/sum(sum(ConfMat));
8 disp(acc);

```

6.2.8 support vectors plotting for SVM

```

1 figure;

```

```

2 plot(x(:,1),x(:,2),'bs','linewidth',1.5,'MarkerSize',10,'
   MarkerFaceColor','w');
3 hold on;
4 plot(y(:,1),y(:,2),'ro','linewidth',1.5,'MarkerSize',10,'
   MarkerFaceColor','w');
5
6 SVInx = trainedClassifier.ClassificationSVM.IsSupportVector;
7 %%
8
9 plot(X(SVInx == 1,1),X(SVInx == 1,2),'kv','linewidth',1.5,'
   MarkerFaceColor','w');

```

6.2.9 Decision region plotting for SVM, KNN, and Discriminant models

```

1 x1range = min(min([x(:,1),y(:,1)])):.01:max(max([x(:,1),y
   (:,1)]));
2 x2range = min(min([x(:,2),y(:,2)])):.01:max(max([x(:,2),y
   (:,2)]));
3 [xx1, xx2] = meshgrid(x1range,x2range);
4 XGrid = [xx1(:) xx2(:)];
5 predictedspecies = predict(trainedClassifier.
   ClassificationKNN,XGrid);
6 %in case of discriminant models,
7 %predict(trainedClassifier.ClassificationDiscriminant,XGrid)
   ;
8 %in case of SVM models,
9 %predict(trainedClassifier.ClassificationSvm,XGrid);
10 figure;
11 gscatter(xx1(:),xx2(:),predictedspecies,'wbr');
12 hold on;
13 plot(x(:,1),x(:,2),'mo','linewidth',1.5,'MarkerSize',4,'
   MarkerFaceColor','y');
14 hold on;
15 plot(y(:,1),y(:,2),'ks','linewidth',1.5,'MarkerSize',4,'
   MarkerFaceColor','k');
16 hold off;
17 legend off;

```


You can find all codes and output images [HERE](#)