

Exercise 03 - Tail Recursion in Scheme

1. Create a .scm file named surname_e3.scm (e.g. tan_e3.scm).
2. For this exercise, you are tasked to implement **matrix multiplication** in Scheme using tail recursion.

Matrix Multiplication is an operation that accepts two matrices, A and B , where A is $n \times m$ and B is $m \times r$. The output of $A \times B$ is an $n \times r$ matrix C . Each element C_{ij} is given by $\sum_{k=0}^m A_{ik} \times B_{kj}$. That is, C_{ij} is the **dot product** of the i -th row of matrix A and the j -th column of matrix B .

An example is given as follows:

$$\begin{array}{|c|c|c|} \hline 1 & 2 & 3 \\ \hline 4 & 5 & 6 \\ \hline \end{array} \times \begin{array}{|c|c|c|c|} \hline 1 & 2 & 3 & 4 \\ \hline 8 & 7 & 6 & 5 \\ \hline 9 & 10 & 11 & 12 \\ \hline \end{array} = \begin{array}{|c|c|c|c|} \hline 44 & 46 & 48 & 50 \\ \hline 98 & 103 & 108 & 113 \\ \hline \end{array}$$

$A(n \times m)$

(2×3)

$B(m \times r)$

(3×4)

$C(n \times r)$

(2×4)

3. The requirements for this exercise are the following:
 - a. Implement a tail-recursive **dot product**.
 - b. Use the dot product to implement a tail-recursive **matrix multiplication**.